

9/10
good

1. Consider a single-channel DIMM card with a 128-bit channel. The channel has two ranks. The DIMM card uses x8 chips and each chip has sixteen banks. If each bank has 8192 rows and 1024 columns, what is the total capacity of the DIMM card in bits? (2 points)

$$\Rightarrow \text{Total capacity} = 2^9 \times 2^{23} \text{ bits}$$
$$= \underline{\underline{2^{32} \text{ bits}}}$$
$$(7,8), (11,2), (11,11), (19,2), (19,5)$$

2

3. Write down the two's complement binary representation of the decimal integer -79 assuming that twelve bits are used for the representation. (2 points)

$$79 = 1001111$$

$$2\text{'s complement of } (-x) = (2^n - 1) - x + 1$$

$$79 \text{ (12 bit representation)} = 000001001111$$

$$\Rightarrow -79 \text{ (in 2's complement)} = 111110110000 + 1$$

$$= 111110110001$$

Rough

$$64 = 1000000$$

$$15 = 1111$$

$$79 = 1001111$$

$$64 + 15 = 79$$

4. Write down the binary representation of the decimal fraction 14.6875 in normalized scientific notation. (4 points)

$$14.6875_{10} = 1110_2 + 0.6875_{10}$$

$$0.6875_{10} = 1.375_{10} \times 2^{-1} = 2.75_{10} \times 2^{-2}$$

$$= 5.5_{10} \times 2^{-3}$$

$$= 11_{10} \times 2^{-4}$$

$$= 1011_2 \times 2^{-4}$$

$$\Rightarrow 14.6875_{10} = 1110 + 1011 \times 2^{-4}$$

$$= 1110 + 0.1011$$

$$= 1110.1011$$

$$14.6875_{10} = 1.1101011 \times 2^3$$

Rough

$$14 = 1110$$

$$0.6 = \frac{6}{10} = \frac{3}{5}$$

$$\frac{0.5 + 0.1}{0.1} \times 10^{-1}$$

$$6875_2$$

$$1.3750$$

$$1.375 \times 2^{-1}$$

$$2.75_2 \times 2^{-2}$$

$$5.5_2$$

$$11_2$$

$$1011$$

$$101.1 \times 2^{-3}$$

$$10.11$$

$$1.011$$

2/10

CS220: Computer Organization Quiz#3

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General instructions: In all the questions, you will assume 32-bit big-endian MIPS ISA.

1. Consider translating the following for loop into MIPS. Assume that i and N allocated in registers \$t0 and \$t1, respectively.

for (i=0; i<N; i++) { loop body }

The skeleton of the MIPS translation is shown below. The bne instruction starts at address 0x00603000. What is the minimum possible address of the first instruction of the loop situated at the label start? Express your answer in hexadecimal. (2 points)

```

...
start: ...
      loop body
      ...
      slt $t2, $t0, $t1
      bne $t2, $0, start

```

bne has 16 bit immediate and it is ~~sign extended~~. and it is sign extended.
so, 0x8000 will be 0xbbbb8000
~~which is most~~

adding 0x00603000 to 0xbbbb8000

So, minimum ^{possible} address of first instruction
is 0x005fb000

```

0x00603000
0xbbbb8000
-----
0x005fb000

```

2. Consider the following MIPS instruction sequence. What is the final hexadecimal value in \$t0? (2 points)

```

lui $t0, 0x62
addi $t0, $t0, 0xaabc
sra $t0, $t0, 0x4

```

0x61aabc is stored
in \$t0 finally.

after lui → {0062, 0000}

+ 1111 aabc

after addi → 0061aabc

after sra → 00061aabc ✓

2

Rough 0101

```

0110 0010
1111 1111
0110 0001
0060 3000
bbbb - -
00 1044
00 11
00000001
0000
8000
603000
bbbb0000

```


3. Consider the following MIPS instruction sequence. Assume that initially \$t0 contains 0x10000000 and \$t1 contains 0x10000004. Initially, the word stored at address 0x10000000 is 0x12fe43ba and the word stored at address 0x10000004 is 0xab34ef21. What is the final hexadecimal value of the word stored at address 0x10000004? (3 points)

lb \$t0, 1(\$t0)
sh \$t0, 0(\$t1)

addr 0x10000000 → 0x12fe43ba → 32bit

lb \$t0, 1(\$t0) stores 0xfe in \$t0.

sh \$t0, 0(\$t1) stores 0x00fe (16bits) in address 0x10000004

So, word at address 0x10000004 is

0x00feef21

4. Consider translating the following C statement where the value of label is 0x0 and label1 is 2^{28} instructions away. This information is available at the time of compilation of the statement. Show the MIPS translation of this C statement using minimum number of instructions. (3 points)

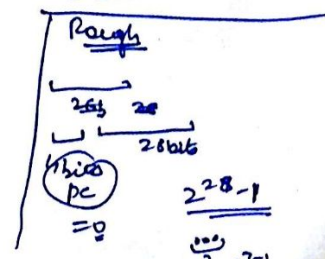
label: goto label1

~~label: goto labelx~~
~~labelx: goto label1~~
~~label1:~~

0x0 label: j labelx
labelx: j labely
labely: j labelz
labelz: j label1
label1

2²⁶ instructions
2²⁶ instructions
2²⁶ instructions
2²⁶ instructions

∴ j has 26 bit target, i.e. max ~~2²⁸~~ 2²⁸ bytes can be traversed
[∵ lower 2bits are 0 i.e. < 2]
but each instruction is 4 bytes ⇒ 2²⁶ instructions can be traversed.
Moreover 4 MSB of PC are 0 in all instruction addresses



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CS220: Computer Organization Quiz#4

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1. Suppose Booth's algorithm is used in a multiplication where the multiplicand and the multiplier are represented in two's complement and their respective values are 0xabcdef01 and 0xcdcf01ab. Count the number of addition and subtraction operations. (1+1 points)

~~Multiplier~~ → ~~Both multiplier and multiplicand are in two's complement, so we first convert them to their true absolute values.~~

Multiplier → ' 110011011101111 0000 0001 1010 1011

~~Convert to~~

No. of addition = No. of times transition from 1 to 0. (lower to higher)

= 8

No. of subtraction = No. of transition from 0 to 1 (lower to higher)

= 7

Rough

8 → 1000
9 → 1001
a → 1010
b → 1011
c → 1100
d → 1101
e → 1110
f → 1111

2. Consider a program that has 15% load/store instructions, 25% conditional branch instructions, 10% other types of control transfer instructions, and 50% arithmetic and logic instructions. The program is executed on a processor with average CPI of load/store 10, of conditional branch 4, of other types of control transfer instructions 3, and of arithmetic and logic instructions 2. Rank these four categories of instructions from most important to least important for optimizing the overall performance of the program. Assume that the clock frequency of the processor which the program runs on is kept constant during the optimization process. (2 points)

Arithmetic & Logic instructions

Conditional Branch Instructions

Load/Store Instructions

Control Transfer.

0.5

∴ Using Andahl's law, optimization of part of program that is most common is best.

3. Suppose the variables x, y, z are of signed type of length 32 bits and we would like to compute $z = x - y$. If x is $0xffff0abc$, what is the range of permissible values of y so that no overflow occurs in the subtraction used to compute z ? Express the upper and lower bounds in hexadecimal of length 32 bits. (3 points)

$$x \rightarrow 0xffff0abc$$

Max value:

Let $y = 0x7fffff$, in this case overflow occurs.

But if there is at least one 1 in upper 16 bits of 2's complement of y , then overflow will not occur.

$\Rightarrow y = 0x7ffeff$ is upper bound.

Lower bound:

$0xffff$ is lower bound.

Rough

Handwritten rough work for question 3, showing binary representations and calculations for overflow.

4. Suppose 1001010 (in binary) is divided by 1001 (in binary). We would like to calculate the number of additions and subtractions when using the restoring, non-performing restoring, and non-restoring algorithms. Fill out the six entries in the table below. (0.5×6 points)

Table 1. Count of additions and subtractions in division algorithms

Algorithm	Number of additions	Number of subtractions
Restoring	3	4
Non-performing restoring	0	4
Non-restoring	3	2

3

Rough

Handwritten rough work for question 4, showing binary division steps and counts for additions and subtractions.