

# CS315: DATABASE SYSTEMS QUERY PROCESSING

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Mon 12:00-13:15, Tue 9:00-10:15

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- For  $s$  seeks and  $b$  block transfers, simply estimated as  $s \times t_s + b \times t_b$
- Ignores CPU time and buffer management issues

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- **LINEAR SEARCH**
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- Cost for a relation containing  $b$  blocks
  - 1 seek
  - $b$  transfers
- If equality on key, then  $b/2$  transfers on average

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  - Scan from beginning till matching record



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- Negation of comparison is just another comparison

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- When it does not, **external sorting** algorithms are used
- **EXTERNAL MERGESORT** or **EXTERNAL SORT-MERGE** is the most used

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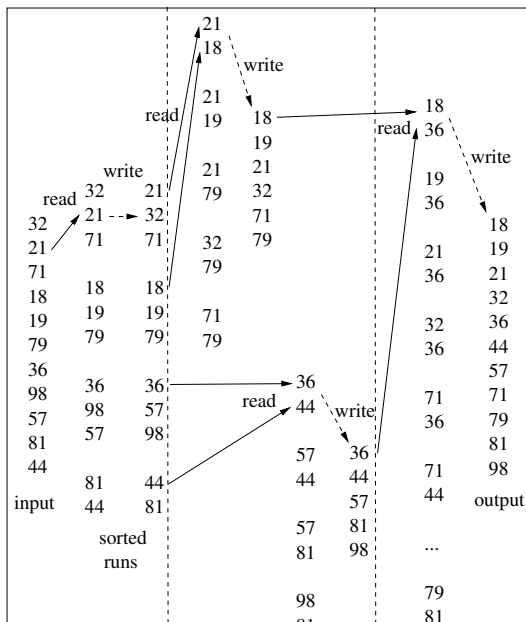
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  - Read in first block of  $m - 1$  runs
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- Continue with  $(m - 1)$ -way merge till the number of sorted runs is *less than  $m$*
- The last  $(m - 1)$ -way merge sorts the relation

# Example



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- Hence, total number of block transfers is  $2b(r + 1)$

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- Therefore, total number of seeks is  $2n + 2br$

- Different join algorithms
  - NESTED-LOOP JOIN
  - BLOCK NESTED-LOOP JOIN
  - INDEXED NESTED-LOOP JOIN
  - MERGE JOIN
  - HASH JOIN
- Choice depends on cost estimates

# Nested-Loop Join

- Applicable for any kind of join
- For each record  $t_r \in r$  and for each record  $t_s \in s$ , if  $t_r \bowtie t_s$  satisfies the join condition, add it to result
- **Outer relation**  $r$ : outer loop; **inner relation**  $s$ : inner loop

# Block Nested-Loop Join

- Applicable for any kind of join
- Block version of the nested-loop algorithm
- For each block  $l_r \in r$  and for each block  $l_s \in s$ , test if every record  $t_r \in l_r$  and  $t_s \in l_s$  satisfies the join condition; if so, add to the result



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- Number of runs is

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- $r$  requires 8 seeks and 200 transfers
- Total is 16 seeks and 2200 transfers

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- Total is 8 seeks and 2000 transfers
- $r$  requires 8 seeks and 200 transfers
- Total is 16 seeks and 2200 transfers
- If  $s$  made outer, 20 seeks and 2250 transfers

# Indexed Nested-Loop Join

- Indexed version of the block nested-loop algorithm
- Applicable when inner relation has an index on the joining attribute
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- Most effective when the join condition is equality

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- Generally, all levels of B+-tree are held in memory except the last
  - Then, cost of index search falls to  $c_s = c_t = 1$



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- Join step is similar to merge step in mergesort
- If relations are not sorted, secondary index on attributes can be used
- **HYBRID MERGE JOIN** algorithm merges sorted records in one relation with B+-tree leaves of other relation

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- Number of passes is  $p = \lfloor \log_m b_s \rfloor$

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- Available memory is  $m = 4$  blocks
  - Partitioning produces  $120/4 = 30$  and then  $30/4 = 8$  and then  $8/4 = 2$  blocks
  - Thus, 3 passes are required

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- Therefore, total number of transfers is  $3(b_r + b_s) + 4n$
- Assume memory buffer of  $m$  blocks
- Partitioning requires  $\lceil b_i/m \rceil$  seeks for reading and  $\lceil (b_i + n)/m \rceil$  seeks for writing
- Reading  $n$  partitions during matching requires  $n$  seeks per relation
- Therefore, total number of seeks is
$$\left\lceil \frac{b_r}{m} \right\rceil + \left\lceil \frac{b_s}{m} \right\rceil + \left\lceil \frac{b_r+n}{m} \right\rceil + \left\lceil \frac{b_s+n}{m} \right\rceil + 2n$$

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 $215 + 265 = 480$
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- Total is 124 seeks and 1410 transfers

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- Set operations
  - If relations are sorted, scan in order
  - Build hash index on one relation; test records from other relation
- Aggregation with grouping
  - Use hashing to organize into groups; then apply aggregation
- Duplicate detection and elimination
  - Use hashing or sorting