# CS315: DATABASE SYSTEMS NORMALIZATION THEORY

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- Normalization theory answers in the formal manner

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- Delete anomaly
  - Deleting a course may delete all the corresponding students

# **Lossless Decomposition**

- Must preserve losslessness of the corresponding join
- Lossy decomposition

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•		roll	name	batch	
Suppose		1	AB	2011	is decomposed into
		2	AB	2012	is decomposed into
		3	CD	2014	
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+		f atia.				

Try to preserve functional dependencies

# **Functional Dependencies**

- Functional dependencies (FDs) are constraints derived from the meaning of and relationships among attributes
- A set of attributes X functionally determines Y, denoted by  $X \to Y$ , if the value of X determines a *unique* value of Y
  - roll → name
- For any two tuples  $t_1$  and  $t_2$  in any *legal* instance of r(R), if  $t_1.X = t_2.X$  then  $t_1.Y = t_2.Y$
- A FD  $X \to Y$  is trivial if it is satisfied for all instances of a relation
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- A candidate key functionally determines all attributes
- Functional dependencies and keys define normal forms for relations
- Normal forms are formal measures of how "good" a database design is

# Armstrong's Axioms

- Given a set of FDs, additional FDs can be inferred using Armstrong's inference rules or Armstrong's axioms
  - **1** Reflexive: If  $Y \subseteq X$ , then  $X \to Y$
  - 2 Augmentation: If  $X \to Y$ , then  $X, Z \to Y, Z$
  - **3** Transitive: If  $X \to Y$  and  $Y \to Z$ , then  $X \to Z$

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- These rules are
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- Other inferred rules
  - **1** Decomposition: If  $X \to Y, Z$ , then  $X \to Y$  and  $X \to Z$
  - **1** Union: If  $X \to Y$  and  $X \to Z$ , then  $X \to Y, Z$
  - **1** Pseudotransitivity: If  $X \to Y$  and  $W, Y \to Z$ , then  $W, X \to Z$

- Closure of a set F of FDs is the set F<sup>+</sup> of all FDs that can be inferred from F
- Closure of a set of attributes X with respect to F is the set X<sup>+</sup> of all attributes that are functionally determined by X using F<sup>+</sup>

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- F and G are equivalent if  $F^+ = G^+$
- F and G are equivalent if F covers G and G covers F
- A set of FDs is minimal if
  - Every FD in F has only a single attribute in RHS
  - Any  $G \subset F$  is not equivalent to F
  - Any  $F (X \rightarrow A) \cup (Y \rightarrow A)$  where  $Y \subset X$  is not equivalent to F
- Every set of FD has at least one equivalent minimal set

#### Normal Forms

- The process of decomposing relations into smaller relations that conform to certain norms is called normalization
- Keys and FDs of a relation determine which normal form a relation is in
- Different normal forms
  - 1NF: based on attributes only
  - 2NF, 3NF, BCNF: based on keys and FDs
  - 4NF: based on keys and multi-valued dependencies (MVDs)
  - 5NF or PJNF: based on keys and join dependencies
  - DKNF: based on all constraints

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		(-)	-

-	<u>ld</u>	Name	Phone
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	1	Α	4
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Nested relations should be decomposed

-			Cours	е	-
	Roll	Name	Courseld	Title	-
	1	Α	1	30	should be broken into
	1	Α	2	20	Should be broken into
	2	В	2	25	
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  - Example: roll
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  - Example: (roll, courseid) → (grade)
- It is a partial functional dependency otherwise
  - (roll, gender) → (name)

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  - Example: (roll, courseid) → (grade)
- It is a partial functional dependency otherwise
  - (roll, gender) → (name)
- A FD X → Y is a transitive functional dependency if it can be derived from two FDs X → Z and Z → Y
  - Example: (roll) → (title) since (roll) → (courseid) and (courseid) → (title) hold
- It is non-transitive otherwise
  - Example: (roll) → (name)

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- Consider (<u>Id</u>, <u>ProjId</u>, Hrs, Name, ProjName) with FDs: (Id, ProjId) → (<u>Hrs</u>); (Id) → (Name); (ProjId) → (ProjName)

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  - (Id, Name) with FD: (Id) → (Name)
  - (Projld, ProjName) with FD: (Projld) → (ProjName)

- A relation is in 3NF if
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- Alternatively, for every FD  $X \rightarrow Y$ , either
  - It is trivial, or
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- $L = (\underline{Id}, Dist, Lot, Area, Price, Rate)$  with FDs:
  - (Id) → (Dist, Lot, Area, Price, Rate)
  - (Dist, Lot) → (Id, Area, Price, Rate)
  - (Dist) → (Rate)
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- $L_1 = (\underline{Id}, Dist, Lot, Area, Price)$  with FDs:
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- L<sub>2</sub> is in 2NF and in 3NF

# Example (contd.)

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- L<sub>1</sub> is in 2NF but not 3NF because (Price) depends on (Id) through (Area)
- $L_{11} = (\underline{Id}, Dist, Lot, Area)$  with FDs:
  - (Id) → (Dist, Lot, Area)
  - (Dist, Lot) → (Id, Area)
- $L_{12} = (\underline{\text{Area}}, \text{Price}) \text{ with FD}$ :
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  - (Dist, Lot)  $\rightarrow$  (Id, Area, Price)
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- $L_{11} = (\underline{Id}, Dist, Lot, Area)$  with FDs:
  - (Id) → (Dist, Lot, Area)
  - (Dist, Lot) → (Id, Area)
- $L_{12} = (\underline{\text{Area}}, \text{Price}) \text{ with FD}$ :
  - (Area)  $\rightarrow$  (Price)
- L<sub>11</sub> and L<sub>12</sub> are in 3NF

- A relation is in BCNF
  - If  $X \to Y$  is a non-trivial FD, then X is a superkey of R
- Alternatively, for every FD  $X \rightarrow Y$ , either
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  (Id) → (Dist, Lot, Area); (Dist, Lot) → (Id, Area); (Area) → (Dist)
- It is not in BCNF since (Area) is not a superkey although (Area) → (Dist) holds
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  - If  $X \to Y$  is a non-trivial FD, then X is a superkey of R
- Alternatively, for every FD  $X \rightarrow Y$ , either
  - It is trivial, or
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- BCNF can lose FDs
- Every BCNF relation is in 3NF
- Good design ensures that every relation is at least in 3NF (if not BCNF)
- Consider ( $\underline{\sf Id}$ , Dist, Lot, Area) with FDs: (Id)  $\rightarrow$  (Dist, Lot, Area); (Dist, Lot)  $\rightarrow$  (Id, Area); (Area)  $\rightarrow$  (Dist)
- It is not in BCNF since (Area) is not a superkey although (Area) → (Dist) holds
- After BCNF normalization,
  - (<u>Id</u>, Lot, Area) with FD: (Id) → (Dist, Lot, Area)
  - (Dist, Area) with FD: (Area) → (Dist)
  - Loses (Dist, Lot) → (Id, Area)

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- Remedy
  - BCNF: Decompose and set up a relation for each nonkey attribute with attributes functionally dependent on it

- BCNF decomposition is not always possible
- (town, state, dist) with FDs: (town, state) → (dist); (dist) → (state)

town	state	dist
iit	up	east
iit	wb	mdp
prayag	up	east
prayag	wb	dinaj
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- According to rule, decomposed into (state, <u>dist</u>) and (<u>town</u>, <u>state</u>)
- However, the decomposition is not lossless
- Also, (town, state) and (town, dist) is lossy
- Only (town, dist) and (state, dist) is lossless
- Losslessness must be preserved

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  - Inserting a new teacher for db requires two tuples
- Better design if (course, teacher) and (course, book)

#### Multi-valued dependency (MVD)

- A multi-valued dependency (MVD) X woheadrightarrow Y holds for a relation schema R if for all *legal* relations r(R), if for a pair of tuples  $t_1$  and  $t_2$ ,  $t_1.X = t_2.X$ , then there exists another pair of tuples  $t_3$  and  $t_4$ 
  - $t_1.X = t_2.X = t_3.X = t_4.X$
  - $t_3.Y = t_1.Y$
  - $t_3.R Y X = t_2.R Y X$
  - $t_4.Y = t_2.Y$
  - $t_4.R Y X = t_1.R Y X$

	Χ	Υ	R - Y - X
$t_1$	а	b	С
$t_2$	а	d	е
t <sub>2</sub> t <sub>3</sub>	a a a a	b	е
$t_4$	а	d	С

- Example: (course) → (teacher) in (course, teacher, book)
  - If (db, ab, fdb) and (db, sg, dbm) exist, then (db, ab, dbm) and (db, sg, fdb) must exist
  - Otherwise, ab has something to do with fdb

•  $X \rightarrow Y$  implies  $X \rightarrow R - Y - X$ 

- $X \rightarrow Y$  implies  $X \rightarrow R Y X$
- R = (X, Y, Z)
- X → Y, and by symmetry, X → Z
- Then, decomposition into (X, Y) and (X, Z) will be lossless
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- Closure of a set of MVDs is the set of all MVDs that can be inferred using the following rules

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- Decompose R with X → Y into (X,Y) and (X,R-Y-X)
- Good design ensures that every relation is in 3NF or BCNF

# Join dependency (JD)

- General way of decomposing a relation into multi-way joins
- A join dependency (JD)  $(R_1, ..., R_n)$  holds for a relation schema R if for all *legal* relations r(R),  $\bowtie_{i=1}^n (\Pi_{R_i}(r)) = r$
- A JD is trivial if one of R<sub>i</sub> is R itself

Salesman	Brand	Product
J	Α	V
J	Α	В
W	R	Р
W	R	V
W	R	В
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- Suppose, the following rule holds: If S sells products of brand B and if S sells product type P, then S must sell product type P of brand B (assuming B makes P)
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- A MVD is a special case of JD with n = 2

# Fifth normal form (5NF) or Project-Join normal form (PJNF)

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- Consider that J starts selling brand R's products
- Insertion anomaly since multiple tuples need to be inserted
- Better design if broken into three relations (B,P), (S,B), and (P,S)

Brand	Product			Product	Salesman
Α	V	Salesman	Brand	V	J
Α	В	J	Α	В	J
R	Р	W	R	Р	W
R	V	W	Α	V	W
R	В		ı	В	W

Now, insertion requires only one tuple (J, R) in (Salesman, Brand)

# Domain-Key normal form (DKNF)

- A relation schema is in domain-key normal form (DKNF) if all constraints and relations that should hold can be enforced simply by domain constraints and key constraints
- Ideal normal form
- Mostly theoretical
- Once a relation is in DKNF, there is no anomaly and FDs and MVDs need not be checked any more