AE 234 Course Project

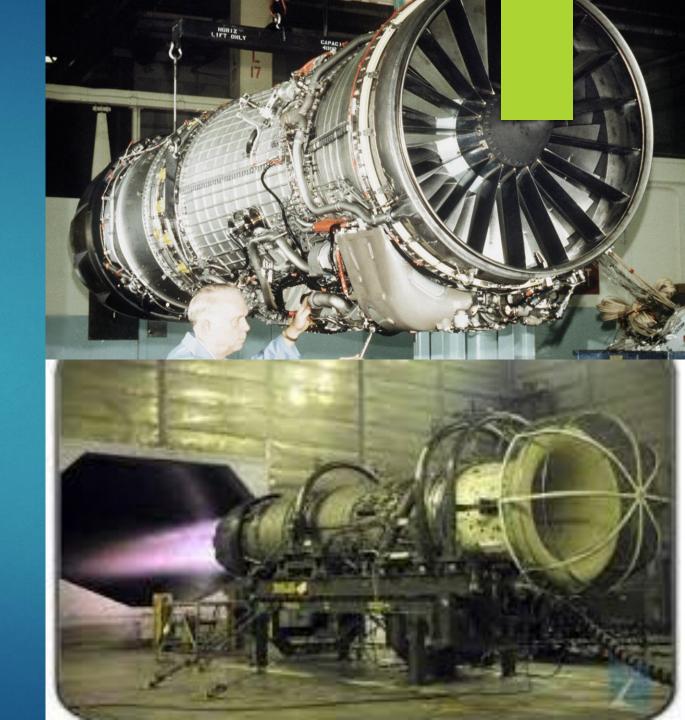
Group - 10

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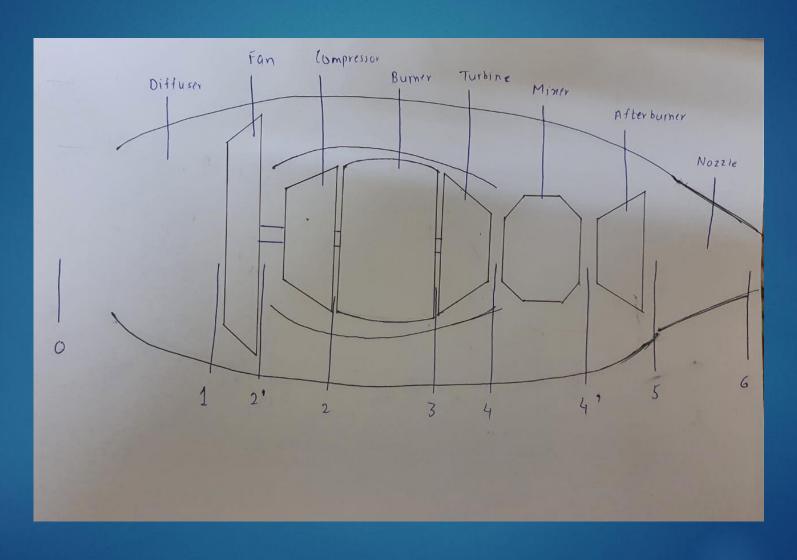
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Objective

Cycle analysis of GEF – 101 turbofan engine:
Detailed analysis of each of the component in the engine to obtain Thrust and TSFC



Engine schematic



Engine Parameters

- ▶ Design Point Mach Number(M_0) = 1.25
- Altitude(h) = 15.2 KM
- Intake: $\eta_d = 0.94$
- Fan: $\pi_f = 2.3$, $\eta_f = 0.8$
- Compressor : $\pi_c = 11.65$, $\eta_f = 0.87$
- Burner: $\eta_b=0.97$, $\dot{Q}_R=47.2\,MJ/Kg$, $\dot{m}_f=0.7\,kg/s$; $C_{p1}(Pre\ Combustor)=1005J/Kg$ $C_{p2}(Post\ Combustor)=1090\,J/KgK$
- Turbine : $\eta_t = 0.89$
- Afterburner: $\dot{m}_{ab}=2~kg/s$, $\eta_{ab}=0.97$, $C_{p3}(Post~afterburner)=1098$ J/KKg
- Nozzle : NPR = 4.98, η_n = 0.94

Diffuser

Known parameters are:

$$\eta_{\rm d} = 0.94$$
 $M_0 = 1.25$

$$P_o = 12 \text{ kPa}$$

We know the relations for diffuser as;

$$\tau_{\rm r} = \frac{T_{\rm to}}{T_{\rm o}} = (1 + \frac{\gamma - 1}{2} M_0^2)$$

$$P_{t1} = (1 + \eta_d \frac{\gamma - 1}{2} M_0^2)^{\frac{\gamma}{\gamma - 1}}$$

► Hence,
$$T_{to} = T_{t1} = 284.35 \text{ K}$$
 ; $P_{t1} = 29.66 \text{ kPa}$

Fan

• Bypass ratio =
$$\alpha = \frac{\dot{m}_{bypass}}{\dot{m}_{core}} = 2$$

$$\eta_f = \frac{h_{t_2/s} - h_{t_1}}{h_{t_2/s} - h_{t_1}} = \frac{\pi_f^{\frac{\gamma - 1}{\gamma}} - 1}{\tau_f - 1}$$

$$\pi_f = \frac{P_{t2}}{P_{t1}} = 2.3$$

$$\eta_f = 0.8$$

$$\tau_f = \frac{T_{t2}}{T_{t1}} = 1.335$$

$$T_{t2}$$
, = 379.85 K ; P_{t2} , = 68.23 kPa

Compressor

$$\pi_c = \frac{P_{t2}}{P_{t1}} = 11.65$$

$$T_{2s} = \pi_c^{\frac{\gamma-1}{\gamma}}$$

$$\eta_c = \frac{h_{t2s} - h_1}{h_{t2} - h_1} = \frac{\frac{h_{t2s}}{h_1} - 1}{\frac{h_{t2}}{h_1} - 1} = \frac{\pi_c^{\frac{\gamma}{\gamma - 1}} - 1}{\tau_c - 1}$$

$$\eta_c = 0.87$$

$$\tau_c = 2.17$$

$$T_{t2} = 823.85 K$$
; $P_{t2} = 345.66 \text{ kPa}$

Burner

Using energy conservation in burner as follows;

- We know; $\eta_b = 0.97$, $\dot{Q}_R = 47.2 \, MJ/Kg$, $\dot{m}_f = 0.7 \, kg/s$
- $(\dot{m}_c + \dot{m}_{f,c})C_{p2}T_{t3} \dot{m}_{f,c}C_{p1}T_{t2} = \eta_b \dot{Q}_R \dot{m}_{f,c}$
- Hence from the equation we get;
- $T_{t3} = 1540 \text{ K}$

Turbine

$$T_{4s} = \pi_t^{\frac{\gamma-1}{\gamma}}$$

$$\eta_t = \frac{h_{t3} - h_{t4}}{h_{t3} - h_{4s}} = \frac{1 - \tau_t}{1 - \pi_t}$$

$$\eta_t = 0.89$$

- From Power balance of turbine, compressor and fan;
- $T_{t4} = 956 \, \text{K}$
- $\tau_t = 0.619$
- $\pi_t = \frac{P_{t4}}{P_{t3}} = 0.142$
- $P_{t4} = 48.94 \text{ kPa}$

Mixer

For bypass flow;

- $\dot{m}_{bypass} = 74.73 \text{ Kg/s}$
- $T_{bypass} = T_{t2}$, = 379.85 K
- $C_{P,bypass} = C_{P1} = 1005 \text{ J/KgK}$

For core flow;

- $\dot{m}_{core} = 37.37 \text{ Kg/s}$
- $T_{core} = T_{t4} = 956 \text{ K}$
- $C_{P,core} = C_{P2} = 1090 \text{ J/KgK}$

From energy conservation;

$$(\dot{m}_{core} + \dot{m}_{f,c})(T_{t4} - T_{t4}) C_{P2} = \dot{m}_{bypass}C_{P1}(T_{t4}, - T_{t2}) \Longrightarrow T_{t4}, = 588 \text{ K}$$

After Burner

- Using energy conservation in burner as follows;
- ▶ We know;
- $\dot{m}_{ab} = 2 kg/s$, $\eta_{ab} = 0.97$,
- $C_{p3}(Post\ afterburner) = 1098J/KKg, \gamma(post) = 1.3$
- Using energy balance;
- $(\dot{m}_o + \dot{m}_{ab} + \dot{m}_{f,c})C_{p3}T_{t5} m_{ab}C_{p2}T_{t4} = \eta_{ab}\dot{Q}_R\dot{m}_{ab}$
- Hence from the equation we get;
- $T_{t5} = 1310 \text{ K}$

Nozzle

Known parameters are:

$$\eta_n = 0.94$$

NPR =
$$\frac{P_{t6}}{P_6} = 4.98$$

$$P_6 = P_0 = 12 \text{ kPa}$$

We know the relations for diffuser as ;

$$\eta_n = \frac{NPR^{\frac{\gamma-1}{\gamma}} - \pi_n^{\frac{1-\gamma}{\gamma}}}{NPR^{\frac{\gamma-1}{\gamma}} - 1}$$

$$\pi_n = \frac{P_{t6}}{P_{t5}} = 1.87$$

$$\frac{P_{t6}}{P_6} = \left(1 + \frac{\gamma - 1}{2} M_e^2\right)^{\frac{\gamma}{\gamma - 1}}, \frac{T_{t6}}{T_6} = \left(1 + \frac{\gamma - 1}{2} M_e^2\right)$$

• Hence,
$$T_6 = 327 \text{ K}$$
 ; $M_e = 4.49$

Performance parameters

$$V_e = M_e \sqrt{\gamma R T_e} = 1570.75 \text{ m/s}$$

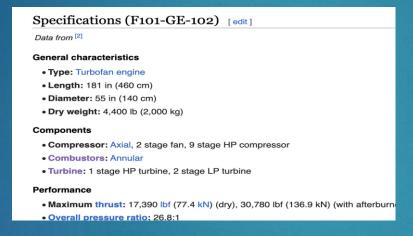
$$V_o = M_o \sqrt{\gamma R T_o} = 368.80 \text{ m/s}$$

► Thrust(T) =
$$V_e(\dot{m}_0 + \dot{m}_{f,c} + \dot{m}_{ab}) - \dot{m}_0 V_o = 137 \text{ kN}$$

> TSFC =
$$\frac{\dot{m}_f + \dot{m}_{f,ab}}{T}$$
 = 68.13 kg/kNh

References

- AIAA PAPER No 75-1308(GE F101 Structure) : https://arc.aiaa.org/doi/pdf/10.2514/6.1975-1308
- ► F-101 engine combustion system: https://apps.dtic.mil/sti/pdfs/ADA077860.pdf
- Wikipedia:



- Calculation work:
 https://docs.google.com/spreadsheets/d/11Xztg6qBeyn3groeU3Viptlt19k7H3TK5i3rz7fXL6c/edit?usp=sharing
- Some of the parameters are assumed due to lack of data

THANK YOU!