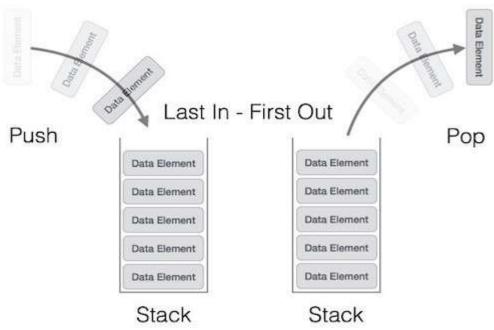
29-08-2020

Stacks

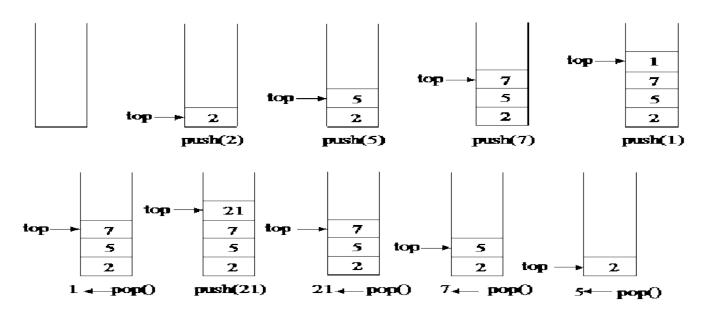
Stacks

- Stack is a linear data structure which follows a particular order in which the operations are performed.
- The order may be LIFO(Last In First Out) or FILO(First In Last Out).



Operation on Stacks

- Push operation-The insertion of an element into stack
- Pop operation Deletion of an element from the stack
- In stack we always keep track of the last element present in the list with a pointer called top.



Array Implementation of Stack

top Index of element at the top of stack

Stack is empty → top is -1

Push operation

top is increased by 1

New element is placed at index top

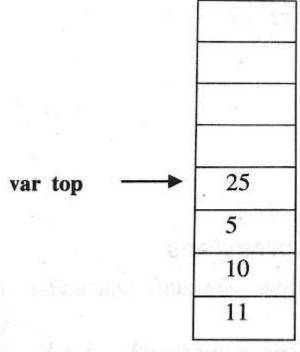
Pop operation

Element at index top is taken out

top is decreased by 1

Array Implementation of Stack

- Push element one by one onto stack from 0th position to n-1 th position.
- Variable top, which keeps the position of the top element in the array
- If there is no element in the stack, value of top will be -1



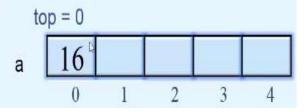
stack[]

PUSH Operation on Stack

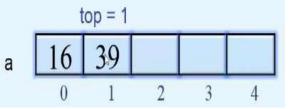
Empty stack



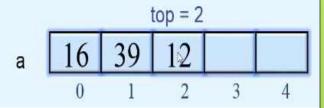
Push 16



Push 39



Push 12



Push 10

Push 47

Algorithm for PUSH Operation

- Check Stack Full condition
 If(top==MAX-1)
 Then print stack is full or overflow
- 2) Otherwise increase the top value by 1 top=top+1
- 3) Input the value
- Assign the item at top position stack_arr[top]=pushed_item

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Try writing the code for Push Operation function

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PUSH Operation

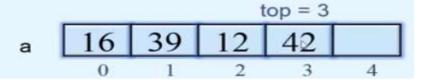
POP Operation on Stack

Empty stack

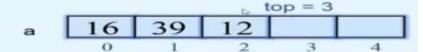
Stack Underflow condition

If(top== -1)

Push 42



Pop



Popped item = 42

Pop



Algorithm for POP Operation

- Check Stack Underflow condition
 If(top== -1)
 Then print stack is underflow
- Otherwise, delete the top position element Popped_item=stack_arr[top]
- 3) Decrease the position of top top=top-1
- 4) Print the popped_item

POP Operation

Try writing the code for Pop Operation function

Try writing the code for Display Operation function

29-08-2020

Display fn

```
display()
        int i;
        if(top == -1)
                 printf("Stack is empty\n");
        else
                 printf("Stack elements:\n");
                 for(i = top; i >= 0; i--)
                          printf("%d\n", stack_arr[i] );
}/*End of display()*/
```

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- An operation on certain abstract data types, specifically sequential collections such as stacks and queues,
 - which returns the value of the top ("front") of the collection
 - o without removing the element from the collection.
 - It thus returns the same value as operations such as "pop" or "dequeue", but does not modify the data.

- The name "peek" is similar to the basic "push" and "pop" operations on a stack,
 - but the name for this operation varies depending on data type and language.
- Peek is generally considered an inessential operation,
 - compared with the more basic operations of adding and removing data, and
 - as such is not included in the basic definition of these data types.

- Sequential types for which peek is often implemented include:
 - Stack
 - Queue
 - Priority queue (such as a heap)
 - Double-ended queue (deque)
 - Double-ended priority queue (DEPQ)

- Single-ended types, such as stack,
 - generally only admit a single peek, at the end that is modified.
- Double-ended types, such as deques,
 - o admit two peeks, one at each end.
- Names for peek vary.
 - "Peek" or "top" are common for stacks,
 - while for queues "front" is common.
 - Dequeues have varied names, often "front" and "back" or "first" and "last".
 - The name "peak" is also occasionally found

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Linked List Representation of Stack

Linked List Representation of Stack

- The info field of the node holds the elements of the stack
- Link fields hold pointers to the neighbouring element in the stack
- The start pointer behaves as the TOP pointer variable of the stack
- Null pointer of the last node in the linked list signals the bottom of the stack

Linked List Representation of Stack

```
struct node
{
    int info;
    struct node *link;
} *top=NULL;
```

Push Operation

- Inserting a node into the front or start of the list. i.e. at the top of the stack
- Stack after Before Push Operation,



Linked List Representation of Stack

Beginning of linked list top of the stack

top Point to first node of the list

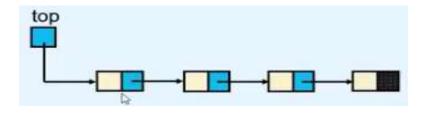
Stack is empty → top is NULL

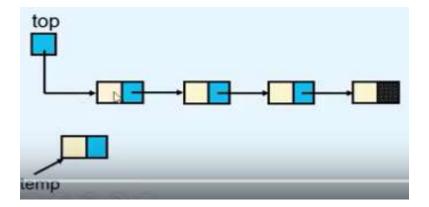
Push operation

Node is inserted in the beginning of the list

Pop operation

First node of the list is deleted





tmp = (struct node
*)malloc(sizeof(struct node));

```
temp->link=top;
temp;
```

Push Operation

```
push()
{
    struct node *tmp;
    int pushed_item;
    tmp = (struct node *)malloc(sizeof(struct node));
    printf("Input the new value to be pushed on the stack : ");
    scanf("%d",&pushed_item);
    tmp->info=pushed_item;
    tmp->link=top;
    top=tmp;
}/*End of push()*/
```

Pop Operation

- Deleting a node pointed to by start pointer of the list.
 i.e. at the top of the stack
- Stack after Before Pop Operation

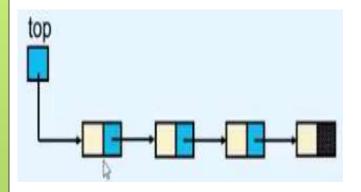


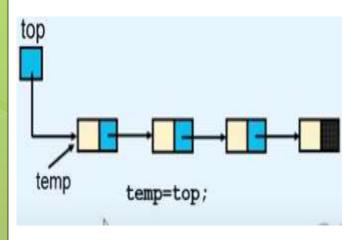
Stack after Pop Operation, element at top deleted

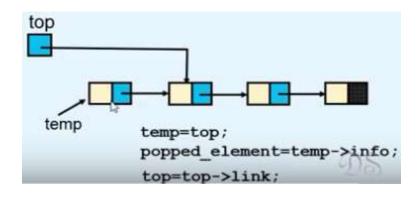
Top

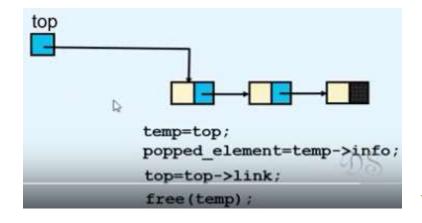


Bottom of Stack









POP Operation

Display Operation

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Application of Stack

Application of Stack –Reversal of a String

- Push each character of the string on the stack.
- When whole string is pushed on the stack
- Pop the characters from the stack to get the reversed string

Application of Stack –Reversal of a String

Try Writing the Code snippet for it......

Application of Stack –Polish Notation

- Polish notation (PN), also known as
 - normal Polish notation (NPN)
 - Łukasiewicz notation
 - Warsaw notation,
 - Polish prefix notation or
 - o simply prefix notation,

Application of Stack –Polish Notation

- Is a mathematical notation in which operators precede their operands,
- The description "Polish" refers to the nationality of logician Jan Łukasiewicz who invented Polish notation in 1924.

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Application of Stack –Reverse Polish Notation

- The more common infix notation, in which operators are placed between operands,
- Reverse Polish notation (RPN), in which operators follow their operands.

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 The term Polish notation is sometimes taken (as the opposite of infix notation) to also include reverse Polish notation.

Expression Representation

- An expression is defined as a number of operands or data items combined using several operators.
- 3 popular methods for representation:
 - Infix Notation
 - Prefix Notation
 - Postfix Notation

Infix Notation

- Used in General Mathematics
- Operator is written in between the operands
- Eg- a+b, x+y*z
- Called infix because of the position of the operator in expression.

Evaluation-

- Evaluated left to right but operator precedence must be taken into consideration
- Not used inside computer, due to additional complexity of handling of precedence

Prefix Notation

- Operator is written before the operands
- Also called Polish Notation
- Eg- +ab, +x*yz

Postfix Notation

- Operator is written after the operands
- Also called Reverse Polish or Suffix Notation
- Eg-ab+, xyz*+

Polish Notation

- Prefix and Postfix are free from any precedence
- Computers use postfix form

Notation Conversion

- Scan the expression from left to right
- o Operator Precedence-
 - Paranthesis evaluated first
 - After that evaluation is on the basis of operator precedence
 - Logical Not
 - Exponential Operator
 - Multiplication/division/modulus
 - Addition/Subtraction
 - Left shift, Right Shift
 - Relational
 - Logical And
 - Logical Or

Operator Precedence Table

Description	Operator	Associativity
Function expression	0	Left to Right
Array Expression	[]	Left to Right
Structure operator	-300	Left to Right
Structure operator		Left to Right
Unary minus	17-21	Right to left
Increment/Decrement	++	Right to Left
One's compliment	-	Right to left
Negation		Right to Left
Address of	eSc.	Right to left
Value of address	•	Right to left
Type cast	(type)	Right to left
Size in bytes	sizeof	Right to left
Multiplication	•	Left to right
Division	1	Left to right
Modulus	%	Left to right
Addition	+	Left to right
Subtraction	-	Left to right
Left shift	<<	Left to right
Right shift	3-3-	Left to right
Less than	-:-	Left to right
Less than or equal to	+Case	Left to right
Greater than	3=	Left to right
Greater than or equal to		Left to right
Equal to	==	Left to right
Not equal to	!=	Left to right
Description	Operator	Associativity
Bitwise AND	&c	Left to right
Bitwise exclusive OR	^	Left to right
Birwise inclusive OR	1	Left to right
Logical AND	x x	Left to right
Logical OR	11	Left to right
Conditional	7 :	Right to left
Assignment	100	Right to left
	*- /- %	Right to left
		Right to left
	Comment Description	Right to left
		Right to left
Comma	100	Right to left

Manual Conversion -Infix to Postfix

- A+B * C Given infix form
- Left to right scan, Brackets fist then Operator Precedence
- A + <u>B C *</u>
- Convert the multiplication

• A B C * +

Convert the addition

Manual Conversion -Infix to Postfix

Manual Conversion -Infix to Postfix

- A+[(B+C)+(D+E)*F]/G
- Left to right scan, Brackets first then Operator Precedence
- A + [(BC +) + (D + E) * F]/G
- A+[(<u>BC+</u>)+(<u>DE+</u>)*F]/G
- $A + [(BC +) + (DE +)F^*]/G$
- A+[(BC+)(DE+)F*+]/G
- A+[(BC+)(DE+)F*+]G/
- A[(BC+)(DE+)F*+]G/+
- O ABC+DE+F*+G/+

Manual Conversion -Infix to Postfix

- 1) A + B + C + D
- (A + B) / (C D)
- 3) (A + B) * C (D E) * (F + G)
- 4) ((A+B) C*(D/E)) + F
- 5) ((A + B) * (C- D) + E) / (F + G)

Manual Conversion -Infix to Postfix

1)
$$A + B + C + D = A B + C + D +$$

$$=AB++C+D$$

$$=AB+C++D$$

$$=AB+C+D+$$

Manual Conversion -Infix to Postfix

- 1) A + B + C + D = A B + C + D +
- 2) (A + B) / (C D) = A B + C D /

Manual Conversion -Infix to Postfix

- 1) A + B + C + D = A B + C + D +
- 2) (A + B) / (C D) = A B + C D /
- (A + B) * C (D E) * (F + G)=AB+C*DE-FG+*-

Manual Conversion -Infix to Postfix

- 1) A + B + C + D = A B + C + D +
- 2) (A + B) / (C D) = A B + C D /
- 3) (A + B) * C (D E) * (F + G) = AB + C*DE FG + * -
- 4) ((A+B) C * (D/E)) + F=A B + C D E / * F +

Manual Conversion -Infix to Postfix

- 1) A + B + C + D = A B + C + D +
- 2) (A + B) / (C D) = A B + C D /
- 3) (A + B) * C (D E) * (F + G) = AB + C*DE FG + * -
- 4) ((A+B) C*(D/E)) + F=AB+CDE/*-F+
- 5) ((A + B) * (C- D) + E) / (F + G) = A B + C D * E + F G + /

Manual Conversion -Infix to Prefix

- \circ A/B $^$ C+D
- Left to right scan, Brackets fist then Operator Precedence
- A/^BC+D
- <u>/A^BC</u>+D
- +/A^BCD

Manual Conversion -Infix to Prefix

- $(P*Q^R+S)$
- (A-B/C)*(D*E-F)
- 3) (A*B+(C/D))-F
- 4) $A+B*C-(D/E^F)*G*H$
- $(A+B)*C/D+E^{G}$

Manual Conversion -Infix to Prefix

1)
$$(P*Q^R+S)=+*P^QRS$$

Manual Conversion - Infix to Prefix

- $(P*Q^R+S)=+*P^QRS$
- 2) (A-B/C)*(D*E-F)=*(-A/BC)(-*DEF)

Manual Conversion - Infix to Prefix

- 1) $(P*Q^R+S)=+*P^QRS$
- 2) (A-B/C)*(D*E-F)=*(-A/BC)(-*DEF)
- 3) (A*B+(C/D))-F=-+*AB/CDF

Manual Conversion - Infix to Prefix

- $(P*Q^R+S)=+*P^QRS$
- 2) (A-B/C)*(D*E-F)=*(-A/BC)(-*DEF)
- 3) (A*B+(C/D))-F=-+*AB/CDF
- 4) $A+B*C-(D/E^F)*G*H$

$$=A+*BC-(/D^F)*G*H$$

Convert the following expressions from Infix to Prefix;

- $(P*Q^R+S)=+*P^QRS$
- 2) (A-B/C)*(D*E-F)=*(-A/BC)(-*DEF)
- 3) (A*B+(C/D))-F=-+*AB/CDF
- 4) $A+B*C-(D/E^F)*G*H$
 - $=A+*BC-(/D^{F})*G*H$
 - =A+*BC-*/D^EFG*H
 - =A+*BC-**/D^EFGH
 - =+A*BC-**/D^EFGH
 - =-+A*BC**/D ^EFGH
- $(A+B)*C/D+E^F/G$
 - $=+AB*C/D+E^F/G$
 - =+AB*C/D+^EF/G
 - =*+ABC/D+ $^{\wedge}$ EF/G
 - =<u>/*+ABCD</u>+^EF/G
 - =/*+ABCD+/^EFG
 - =+/*+ABCD/^EFG

Algorithm for Infix to Postiix using stack

Step 1-Put the opening bracket '(' on the start of the expression and add the closing bracket ')' at the end of the input expression 'P'

Step 2-Scan the Expression P from left to right and repeat steps 3 to 6 for each element of P until the stack is empty

Step 3-If an operand is encountered, add it to the output expression 'Q'

Step 4-If a left bracket is encountered push it onto the stack

Algorithm for Infix to Postilix using stac

Step 5-If an operator is encountered then

5a) Repatedly pop from the stack and add to the output expression Q, each operator which has the same or higher priority compared to the operator just scanned.

5b) then Add the operator to the stack

Step 6-Ifa right bracket ')' is encountered then repeatedly pop from the stack and add to the output expression Q until a left bracket is encountered. Pop the left bracket also

Infix to Postfix Conversion using stack

Eg-
$$P=(A+B)*C$$

 $P=((A+B)*C)$

Scan	Stack	Expression Q
((
(((
Α	((Α
+	((+	Α
В	((+	AB
)	(AB+
*	(*	AB+
С	(*	AB+C
)	NULL	AB+C*

Infix to Postfix Conversion using stack

Convert P=(a & b | |c| | ! (e > f))

Notation Conversion

- Scan the expression from left to right
- o Operator Precedence-
 - Paranthesis evaluated first
 - After that evaluation is on the basis of operator precedence
 - Logical Not
 - Exponential Operator
 - Multiplication/division/modulus
 - Addition/Subtraction
 - Left shift, Right Shift
 - Relational
 - Logical And
 - Logical Or

Infix to Postfix Conversion using state Convert P=(a && b | | c | | ! (e > f))

Scan	Stack	Expression Q
((
а	(а
&&	(&&	а
b	(&&	ab
	(ab&&
С	(ab&&c
	(ab&&c
!	(!	ab&&c
((!(ab&&c
е	(!(ab&&c e
>	(!(>	ab&&c e
f	(!(>	ab&&c ef
)	(!	ab&&c ef>
)	NULL	ab&&c ef>!

Infix to Postfix Conversion using stack

Convert $P=(A+(B*C-(D/E^F)*G*H))$

Infix to Postfix Conversion using stack

Convert $P=(A+(B*C-(D/E^F)*G*H))$

Scan	Stack	Expression Q
((
A	(Α
+	(+	Α
((+(AB
В	(+(AB
*	(+(*	AB
С	(+(*	ABC
-	(+(-	ABC*
((+(-(ABC*
D	(+(-(ABC*D
/	(+(-(/	ABC*D
Е	(+(-(/	ABC*DE
٨	(+(-(/^	ABC*DE
F	(+(-(/^	ABC*DEF
)	(+(-	ABC*DEF^/
*	(+(-*	ABC*DEF^/
G	(+(-*	ABC*DEF^/G
*	(+(-*	ABC*DEF^/G*
Н	(+(-*	ABC*DEF^/G*H
)	(+	ABC*DEF^/G*H*-
	null	rofineshierster phawan Chachra

Convert $P=(A+(B*C-(D/E^F)*G*H))$

Scan	Słack	Expression Q
((
Α	(Α
+	(+	A
((+(AB
В	(+(AB
•	(+(*	AB
C	(+(~	ABC
-	(+(-	ABC*
((+(-(ABC*
D	(+(-(ABC*D
/	(+(-(/	ABC*D
E	(+(-(/	ABC*DE
^	(+(-(/^	ABC*DE
F	(+(-(/^	ABC*DEF
)	(+(-	ABC*DEF^/
•	(+(-∞	ABC*DEF^/
G	(+(-*	ABC*DEF^/G
•	(+(-*	ABC*DEF^/G*
Н	(+(-*	ABC*DEF^/G*H
)	(+	ABC*DEF^/G*H*-
)	null	ABC*DEF^/G*H*-+

Infix to Postfix Conversion using stock

Convert (P/(Q-R)*S+T))

Infix to Postfix Conversion using stack

Convert (P/(Q-R)*S+T))

$$(P/(Q-R)*S+T)$$

Symbol	Stack	Expression
((_
P	(P
1	(/	P
((/(P
Q	(/(PQ
-	(/(-	PQ
R	(/(-	PQR
)	(/	PQR-
*	(*	PQR-/
S	(*	PQR-/S
+	(+	PQR-/S*
T	(+	PQR-/S*T
	null	PQR-/S*T+

Manual Evaluation of a Prefix notation

- Lets take an eg: +5*32
- Find an operator from left to right having 2 operands after it
- Multiplication of 3 and 2 is carried out
- Expression becomes +56
- Now + has two operands so evaluated
- Exp=11

Manual Evaluation of a Postfix notation

- Lets take an eg: 532*+
- Find first operator from left to right having
 2 operands before it
- perform the operation
- Multiplication of 3 and 2 is carried out
- Expression becomes 56+
- Now + is evaluated
- Exp=11

Step 1-Scan the Expression P from left to right and repeat steps 2 and 3 for each element of 'P' until the last element

Step 2- If an operand is encountered, push it on the stack

1st operand say 'a' is pushed

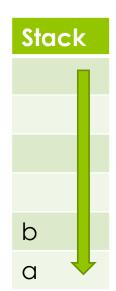
2nd operand say 'b' is pushed

Step 3-If an operator is encountered then
3a) Remove the top two elements of stack and perform

a operator b

(where b is the top element and a is the next element to top element)

3b)Push the result onto the stack



$$P=3+9*+$$

$$P = +9* +$$

Evaluate 5+3=8

Push 8

Evaluate

Push 72

Evaluate 6+72=78

$$Ans=78$$

Stack

Stack

6

Stack

5

6

Stack

3

5

6

Stack

8

6

Stack

9

8

6

Stack

72

6

Evaluate the following expression-

- 1) 432*+5-
- 2) 532*+4-5+
- 3) 53+82-*
- 4) Evaluate 562+*(12)4/taking 12 as a single number

Evaluate 432*+5-

Postfix
$$\to$$
 a b c * + d - Let, a = 4, b = 3, c = 2, d = 5
Postfix \to 4 3 2 * + 5 -

Operator/Operand	Action	Stack 4	
4	Push		
3	Push	4, 3	
2	Push	4, 3, 2	
*	Pop (2, 3) and 3*2 = 6 then Push 6	4, 6	
+	Pop (6, 4) and 4+6 = 10 then Push 10	10	
5	Push	10, 5	
雨	Pop (5, 10) and 10-5 = 5 then Push 5	5	

Example

Evaluate the postfix expression

5 3 2 * + 4 - 5 +

(a) Input so far (shaded): 5 3 2 * + 4 - 5 +

(d) input so far (shaded):



5 3 2 * + 4 - 5 +



(e) Input so far (shaded):

(b) Input so far (shaded):



(g) Input so far (shaded): 5 3 2 * + 4 - 5 +



(h) Input so far (shaded): 5 3 2 * + 4 - 5 +



(c) Input so far (shaded):



(f) Input so far (shaded):



(i) Input so far (shaded): 5 3 2 * + 4 - 5 +



The result of the computation is

Evaluate 562+*(12)4/taking 12 as a single number

www.unacademy

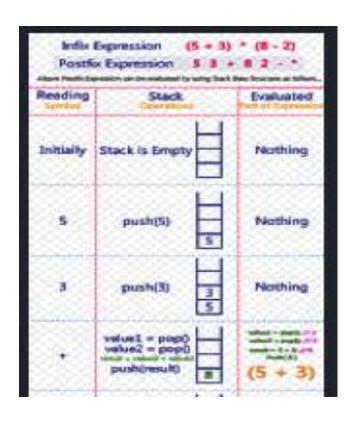
562+ = 124/-

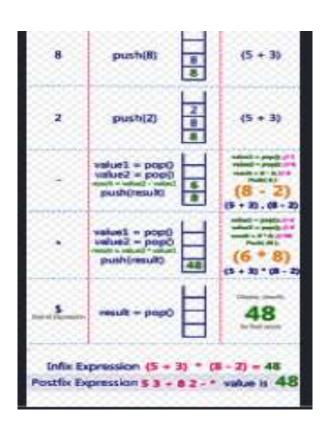
Step		Input Symbol/Element	Stack	Intermediate Calculations Output
1	5	Push	5	
2	6	Push	5,6	
3	2	Push	5, 6, 2	
3 4 5	+	Pop 2 elements and evaluate	5	6 + 2 = 8
5		Push result 8	5, 8	
6	*	Pop 2 elements and evaluate	# empty	5 x 8 = 40
6 7 8		Push result 40	40	
8	12	Push	40,12	
9	4	Push	40, 12, 4	
10	1	Pop 2 elements and evaluate	40	12/4=3
11		Push result 3	40, 3	DAMEST SES
12	2	Pop 2 elements and evaluate	# empty	40 - 3 = 37
13		Push result 37	37	450 - 250 x
14		No more elements		37

Courtesy:https://unacademy.com/lesson/evaluation-of-a-postfix-expression-in-tabular-form/8Z5PDFL5

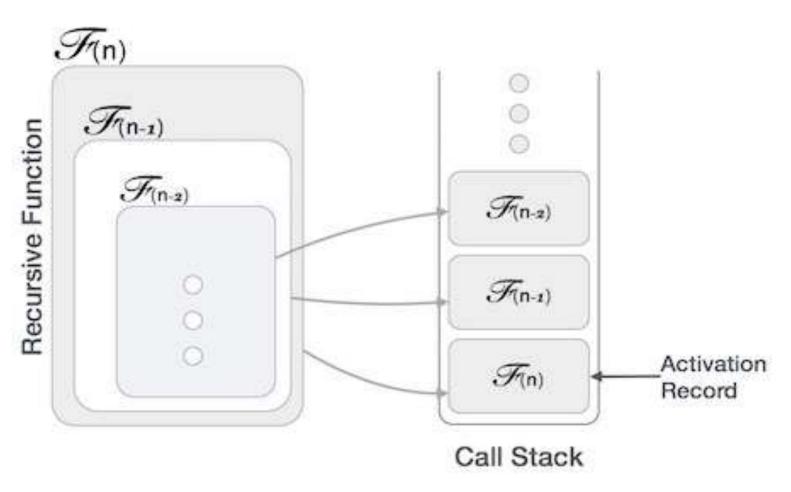
Prof. Shweta Dhawan Chachra

Postfix Expression 5 3 + 8 2 - *

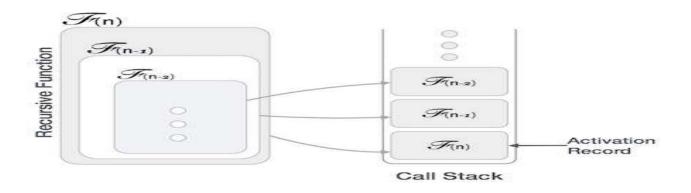




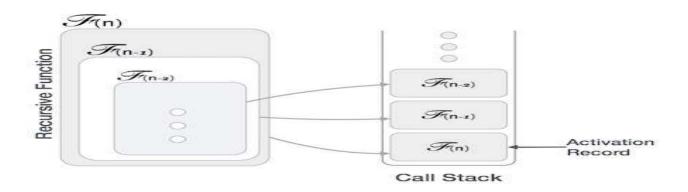
Courtesy:http://btechsmartclass.com/data_structures/postfix-evaluation.html



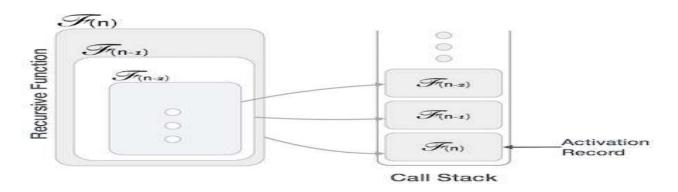
- Many programming languages implement recursion by means of stacks.
- A function (caller) calls another function (callee) or itself as callee,
 - The caller function transfers execution control to the callee.
 - This transfer process may also involve some data to be passed from the caller to the callee.



- The caller function has
 - to suspend its execution temporarily and
 - resume later
 - when the execution control returns from the callee function.



- Here, the caller function needs to start exactly from the point of execution where it puts itself on hold.
 - It also needs the exact same data values it was working on.
 - So, an activation record (or stack frame) is created for the caller function.
 - Activation record keeps the information about
 - local variables,
 - formal parameters,
 - return address and
 - all information passed to the caller function.

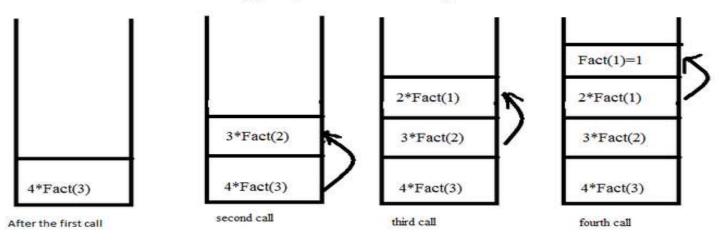


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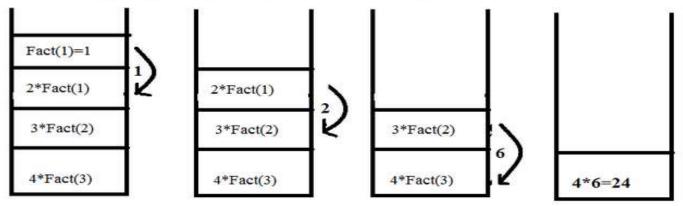
Application of Stack –Recursion

A recursive function to find the factorial of a positive whole number

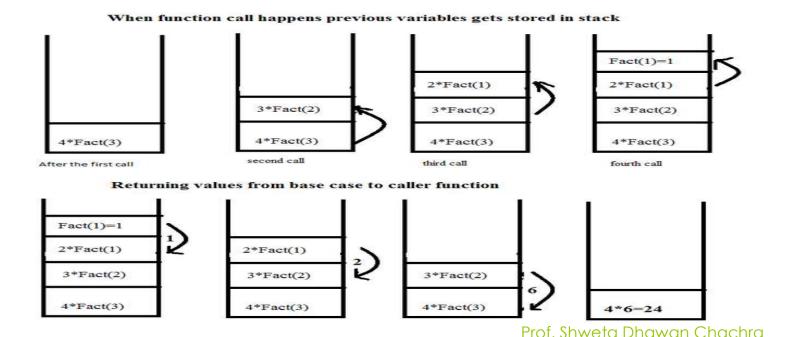
When function call happens previous variables gets stored in stack



Returning values from base case to caller function



- Functions calls are 'stacked' one on top of the other,
- This is called the call stack (or execution stack)
- The call stack operates on a "Last In, First Out" basis. An item is "pushed" onto a stack on function call, and an item is "popped" off the stack when removed from it (when that function returns a value).



Time Complexity

- o In iterations,
 - we take number of iterations to count the time complexity.
- o In recursion,
 - assuming everything is constant,
 - count the number of times a recursive call is being made.

Space Complexity

- Space complexity is counted as
 - what amount of extra space is required for a module to execute.
- In iterations,
 - the compiler hardly requires any extra space.
 - The compiler keeps updating the values of variables used in the iterations.

Time Complexity

- A call made to a function is O(1),
 - hence the (n) number of times a recursive call is made
 - makes the recursive function O(n).

Space Complexity

- o In recursion,
 - the system needs to store activation record each time a recursive call is made.
 - Thus, space complexity of recursive function
 - may go higher than that of a function with iteration.