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### ASSIGNMENT-3

CLASSMATE

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Q1.

A computer while calculating correlation between two variables  $X$  and  $Y$  from 25 pairs of observations obtained the following results:  $n=25$ ,  $\sum X=125$ ,  $\sum X^2=650$ ,  $\sum Y=100$ ,  $\sum Y^2=460$ ,  $\sum XY=508$ . If was, however, later discovered at the time of checking that he had copied down two pairs as  $(x, y) = (16, 14)$ ,  $(8, 6)$  while the correct values were  $(x, y) = (8, 12)$ ,  $(6, 8)$ , obtain the correct value of correlation co-efficient.

Ans.

$$\sum x_i = 125 - 16 + 8 + 6 = 125$$

$$\sum y_i = 100 - 14 - 6 + 12 + 8 = 100$$

$$\sum x_i^2 = 650 - 16^2 + 8^2 + 6^2 = 650$$

$$\sum y_i^2 = 460 - 14^2 + 6^2 + 12^2 + 8^2 = 436$$

$$\sum x_i y_i = 508 - 16 \times 14 - 8 \times 6 + 8 \times 12 + 6 \times 8 = 520$$

$$r = \frac{n \sum xy - \sum x \sum y}{\sqrt{n \sum x^2 - (\sum x)^2} \sqrt{n \sum y^2 - (\sum y)^2}}$$

$$= \frac{25 \times 520 - 125 \times 100}{\sqrt{25 \times 650 - (125)^2} \sqrt{25 \times 436 - (100)^2}}$$

$$= \frac{13000 - 12500}{\sqrt{625} \sqrt{900}} = \frac{500}{25 \times 30} = \frac{2}{3}$$

$$r = 0.667$$



Q2. Samples of size 10 and 14 were taken from two populations with SD 3.5 and 5.2. The sample means were found to be 20.3 and 18.6. Test whether the means of the two populations are the same at 5% level.

Ans.  $H_0: \mu_1 = \mu_2$  i.e. the means of the two populations are the same.

$$H_1: \mu_1 \neq \mu_2$$

$$\text{Given } \bar{x}_1 = 20.3, \bar{x}_2 = 18.6, n_1 = 10, n_2 = 14, \\ s_1 = 3.5, s_2 = 5.2$$

$$s^2 = \frac{n_1 s_1^2 + n_2 s_2^2}{n_1 + n_2 - 2} = \frac{10(3.5)^2 + 14(5.2)^2}{10 + 14 - 2}$$

$$t = \frac{\bar{x}_1 - \bar{x}_2}{s} = \frac{20.3 - 18.6}{s} = 0.8604$$

$$s \left( \frac{1}{n_1} + \frac{1}{n_2} \right) = \left[ \frac{1}{10} + \frac{1}{14} \right] \\ = 4.772$$

The value of  $t$  at 5% level for 22 d.f. is  $t_{0.05} = 2.0739$

Since  $t = 0.8604 < t_{0.05}$  the hypothesis is accepted, i.e., there is no significant diff. between their means.



Q3. Compute the rank correlation co-efficient for the following data:

| Ser.no. | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
|---------|----|----|----|----|----|----|----|----|----|
| X:      | 10 | 15 | 12 | 17 | 13 | 16 | 24 | 14 | 22 |
| Y:      | 30 | 42 | 45 | 46 | 32 | 34 | 40 | 35 | 39 |

| Ans. | X  | Y  | $R_I$ | $R_{II}$ | $D = R_I - R_{II}$ | $D^2$             |
|------|----|----|-------|----------|--------------------|-------------------|
|      | 10 | 30 | 1     | 1        | 0                  | 0                 |
|      | 15 | 42 | 5     | 7        | -2                 | 4                 |
|      | 12 | 45 | 2     | 8        | -6                 | 36                |
|      | 17 | 46 | 7     | 9        | -2                 | 4                 |
|      | 13 | 32 | 3     | 2        | 1                  | 1                 |
|      | 16 | 34 | 6     | 3        | 3                  | 9                 |
|      | 24 | 40 | 9     | 6        | 3                  | 9                 |
|      | 14 | 35 | 4     | 4        | 0                  | 0                 |
|      | 22 | 39 | 8     | 5        | 3                  | 9                 |
|      |    |    |       |          |                    | $\Sigma D^2 = 72$ |

$$r \Rightarrow \frac{1 - \frac{\Sigma D^2}{n(n^2 - 1)}}$$

$$\Rightarrow 1 - \frac{6 \times 72}{9(9^2 - 1)}$$

$$\Rightarrow 1 - \frac{6 \times 72}{9(81 - 1)}$$

$$\Rightarrow 1 - \frac{432}{720}$$

$$\Rightarrow \frac{288}{720} = 0.4$$

$$\text{Ans. } \boxed{r = 0.4}$$



Q.4. 12 entries in a painting competition were ranked by two judges, judge I: 5, 2, 3, 4, 1, 6, 8, 7, 10, 9, 12, 11 and by judge II: 4, 5, 2, 1, 6, 7, 10, 9, 11, 12, 3, 8. Calculate Spearman's rank correlation coefficient.

| Ans. | $R_x$ | $R_y$ | $d = R_x - R_y$ | $d^2$            |
|------|-------|-------|-----------------|------------------|
|      | 5     | 4     | 1               | 1                |
|      | 2     | 5     | -3              | 9                |
|      | 3     | 2     | 1               | 1                |
|      | 4     | 1     | 3               | 9                |
|      | 1     | 6     | -5              | 25               |
|      | 6     | 7     | -1              | 1                |
|      | 8     | 10    | -2              | 4                |
|      | 7     | 9     | -2              | 4                |
|      | 10    | 11    | -1              | 1                |
|      | 9     | 12    | -3              | 9                |
|      | 12    | 3     | 9               | 81               |
|      | 11    | 8     | 3               | 9                |
|      |       |       |                 | $\sum d^2 = 154$ |

$$r = 1 - \frac{6 \cdot \sum d^2}{n(n^2 - 1)}$$

$$\Rightarrow 1 - \frac{6 \times 154}{12(12^2 - 1)} \Rightarrow 1 - \frac{6 \times 154}{12 \cdot (144 - 1)}$$

$$\Rightarrow 1 - \frac{924}{1716} \Rightarrow 1 - 0.5385$$

$$\Rightarrow 0.4615$$

$$r = 0.4615$$



Q5. A die is thrown 276 times and the results of these throws are given below.

|                     |    |    |    |    |    |    |
|---------------------|----|----|----|----|----|----|
| No. appeared on die | 1  | 2  | 3  | 4  | 5  | 6  |
| Frequency           | 40 | 32 | 29 | 59 | 57 | 59 |

|                 |    |     |     |     |     |     |
|-----------------|----|-----|-----|-----|-----|-----|
| Frequency $O_i$ | 40 | 32  | 29  | 59  | 57  | 59  |
| $E_i$           | 46 | 46  | 46  | 46  | 46  | 46  |
| $(O_i - E_i)$   | -6 | -14 | -17 | 13  | 11  | 13  |
| $(O_i - E_i)^2$ | 36 | 196 | 289 | 169 | 121 | 169 |

$$\frac{(O_i - E_i)^2}{E_i} \Rightarrow \frac{36}{46} \quad \frac{196}{46} \quad \frac{289}{46} \quad \frac{169}{46} \quad \frac{121}{46} \quad \frac{169}{46}$$

$$\chi^2 = \left( \frac{[O_i - E_i]^2}{E_i} \right)$$

$$\chi^2 = \frac{36}{46} + \frac{196}{46} + \frac{289}{46} + \frac{169}{46} + \frac{121}{46} + \frac{169}{46}$$

$$= \frac{36 + 196 + 289 + 169 + 121 + 169}{46}$$

$$= 21.30$$

Ans.