



# Computer Vision

**CSC-455**

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# Today's Lecture

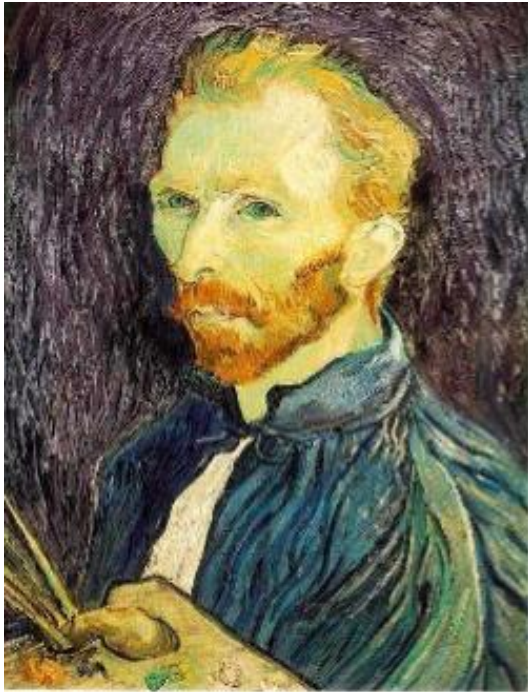


# Image representation

- Pixels: great for spatial resolution, poor access to frequency
- Fourier transform: great for frequency, not for spatial info
- Pyramids/filter banks: balance between spatial and frequency information

# Better image downsampling

Apply a smoothing filter first, then throw away half the rows and columns



1/2

Gaussian filter  
delete even rows  
delete even columns



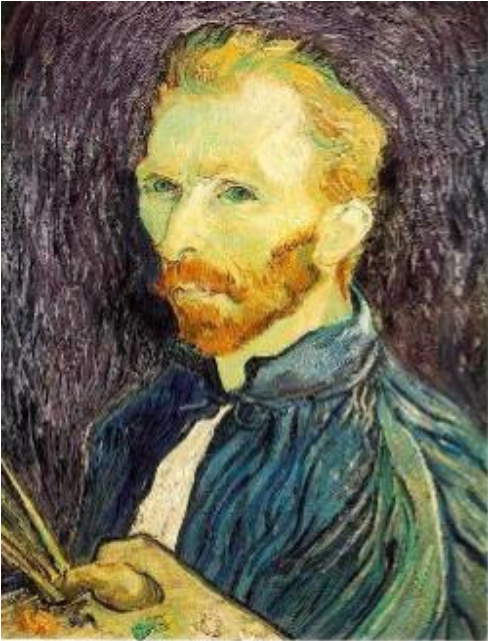
1/4

Gaussian filter  
delete even rows  
delete even columns

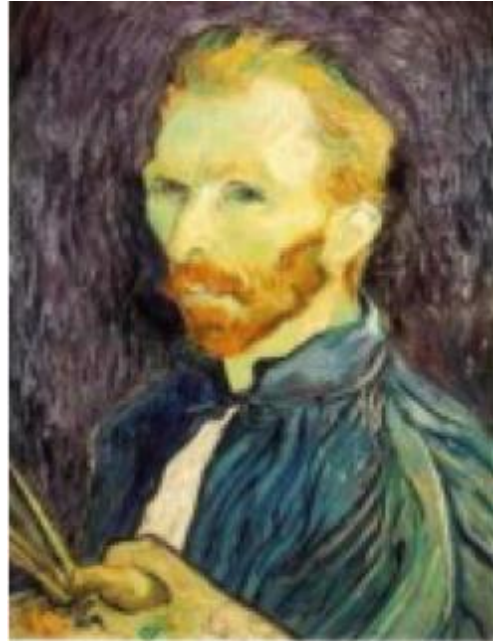


1/8

# Better image downsampling



1/2



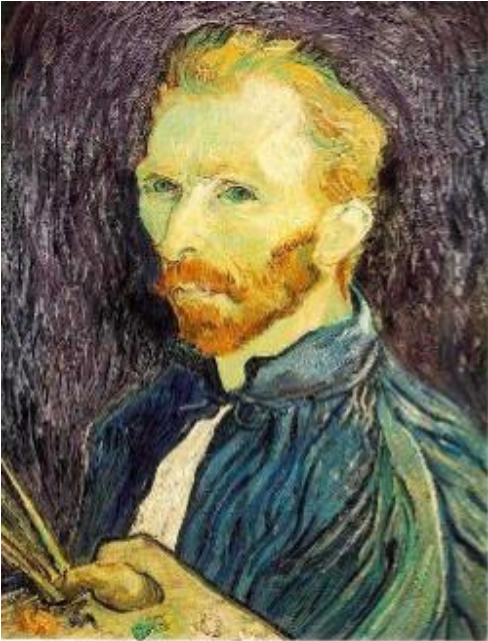
1/4 (2x zoom)



1/8 (4x zoom)



# Naïve image downsampling



1/2



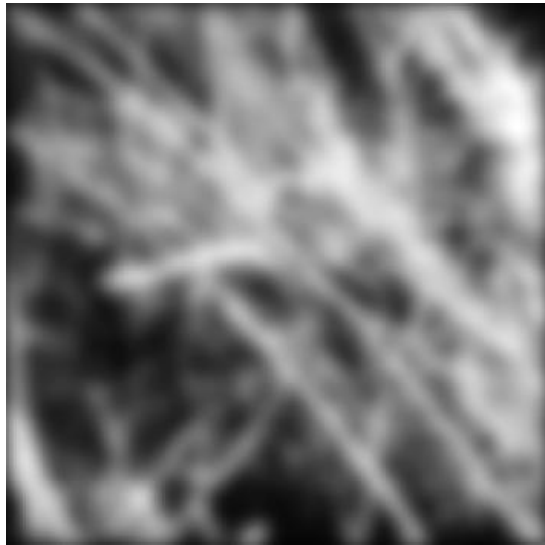
1/4 (2x zoom)



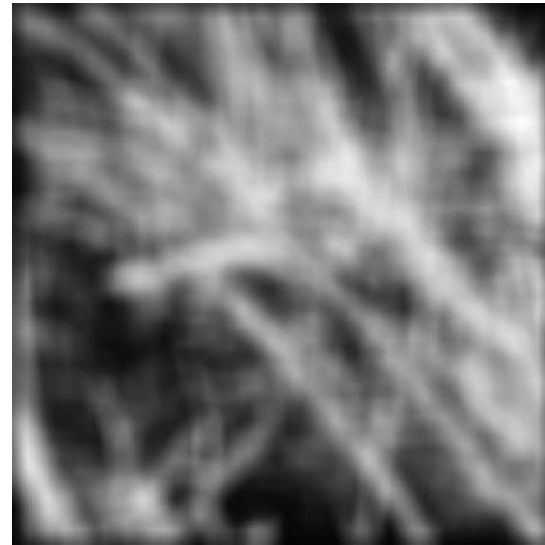
1/8 (4x zoom)

# Revisiting blurring

Why does the Gaussian give a nice smooth image, but the square filter give edgy artifacts?



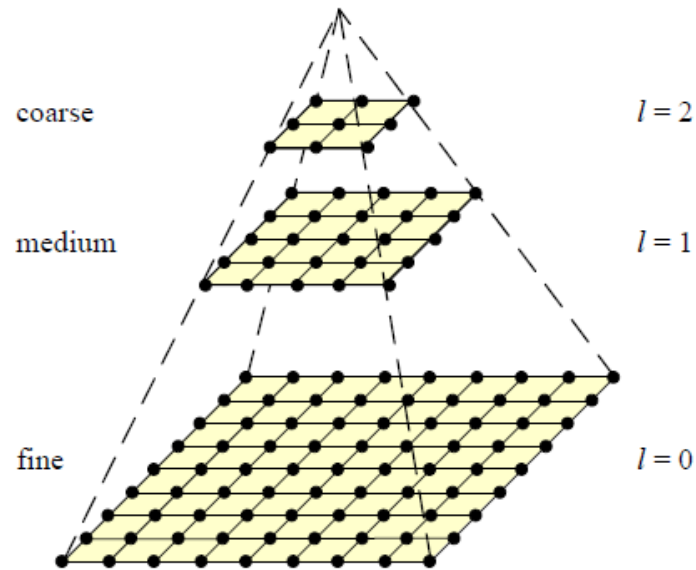
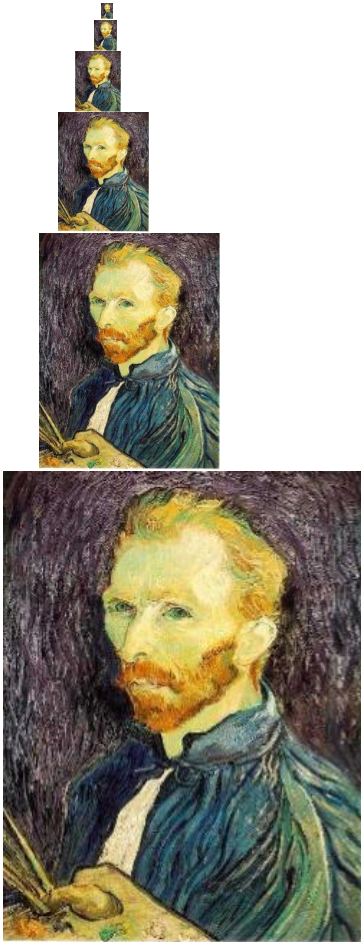
Gaussian  
filter



Box  
filter



# Gaussian image pyramid



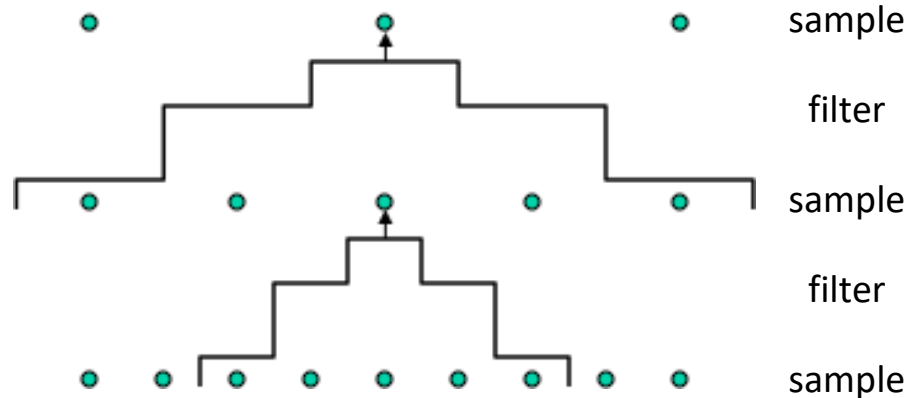
The name of this sequence of subsampled images



# Constructing a Gaussian pyramid

## Algorithm

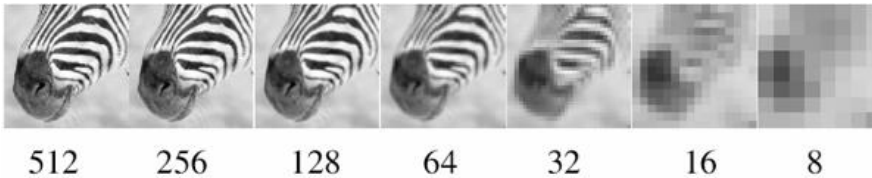
```
repeat:  
    filter  
    subsample  
until min resolution  
reached
```



Question: How much bigger than the original image is the whole pyramid?

Answer: Just  $\frac{4}{3}$  times the size of the original image! (How did I come up with this number?)

# Some properties of the Gaussian pyramid



What happens to the details of the image?

- They get smoothed out as we move to higher levels.

What is preserved at the higher levels?

- Mostly large uniform regions in the original image.

How would you reconstruct the original image from the image at the upper level?

- That's not possible.



# Blurring is lossy



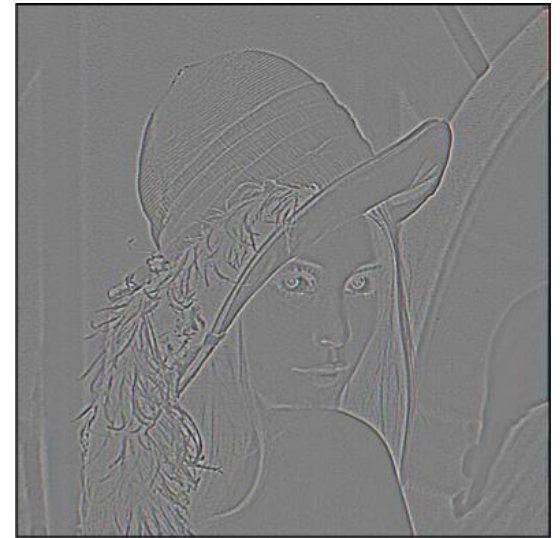
level 0

-



level 1 (before downsampling)

=



residual

What does the residual look like?

# Blurring is lossy



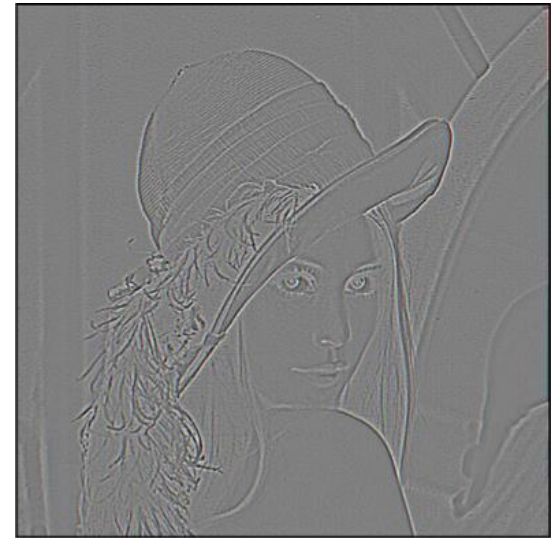
level 0

-



level 1 (before downsampling)

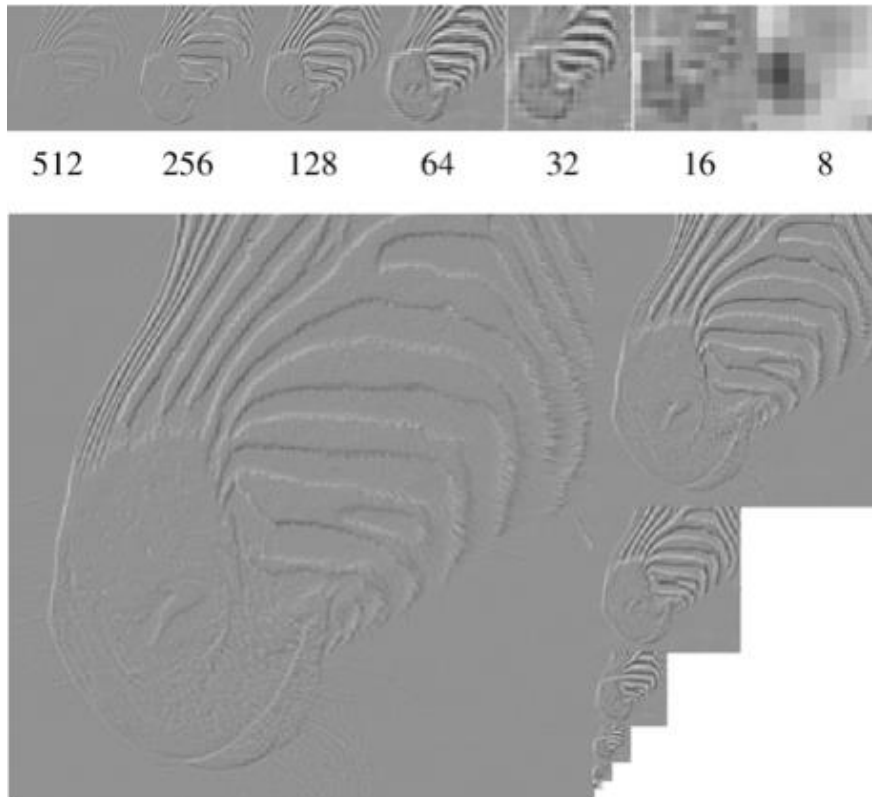
=



residual

Can we make a pyramid that is lossless?

# Laplacian image pyramid



At each level, retain the residuals instead of the blurred images themselves.

Can we reconstruct the original image using the pyramid?

- Yes we can!



What do we need to store to be able to reconstruct the original image?



# Let's start by looking at just one level



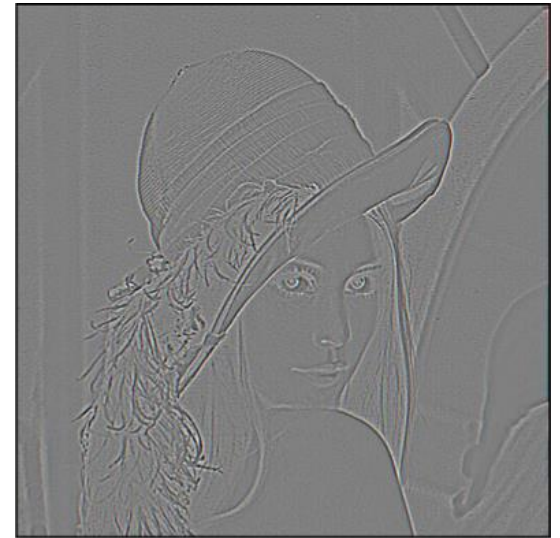
level 0

=



level 1 (upsampled)

+

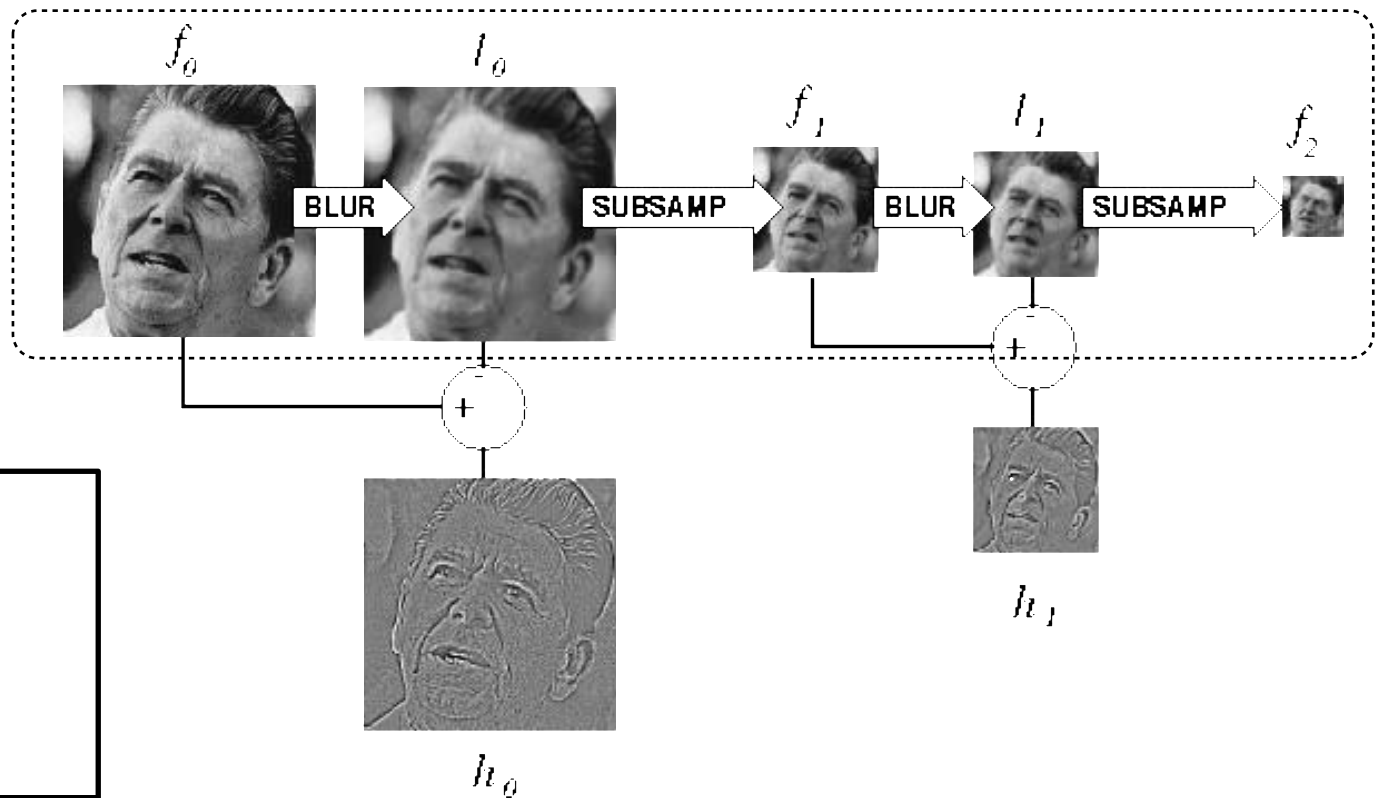


residual

Does this mean we need to store both residuals and the blurred copies of the original?

# Constructing a Laplacian pyramid

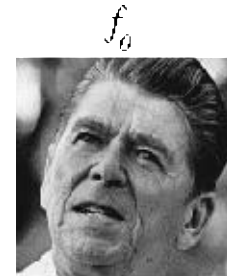
It's a Gaussian pyramid.



## Algorithm

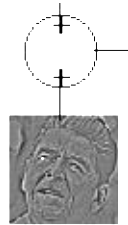
```
repeat:
  filter
  compute residual
  subsample
until min resolution
reached
```

# What do we need to construct the original image?



# What do we need to construct the original image?

(2) smallest  
image

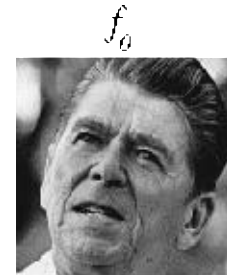


$h_1$

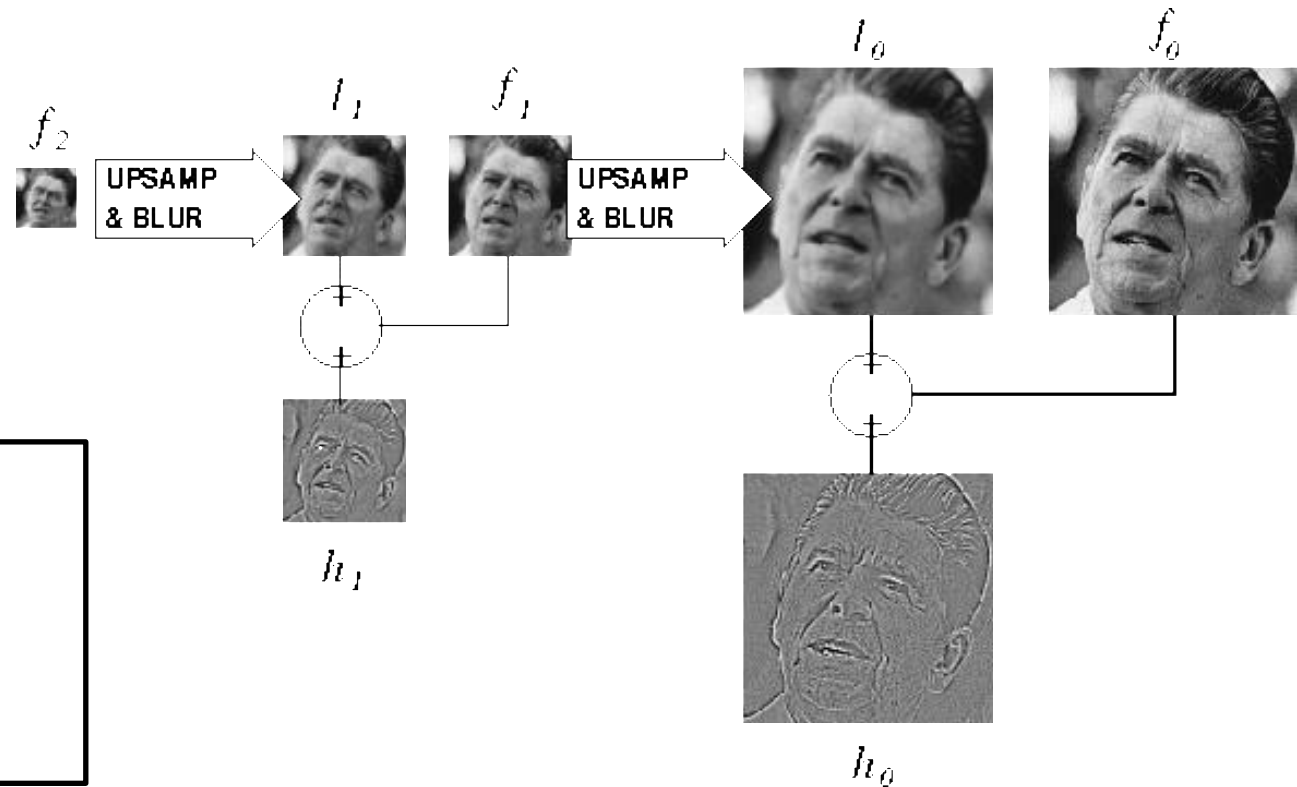
(1) residuals



$h_0$



# Reconstructing the original image



## Algorithm

```
repeat:  
    upsample  
    sum with residual  
until orig resolution  
reached
```

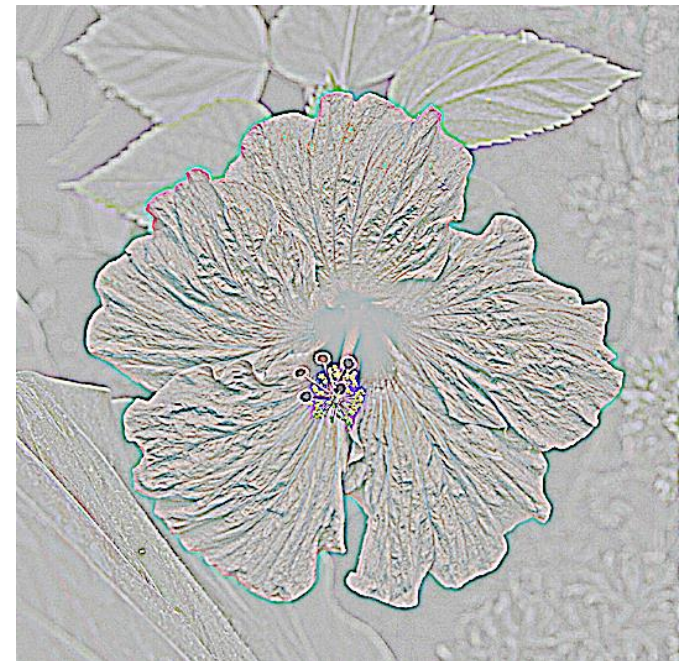
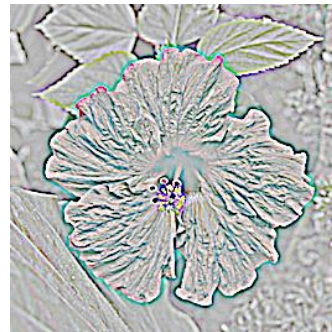


# Gaussian vs Laplacian Pyramid

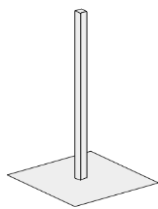
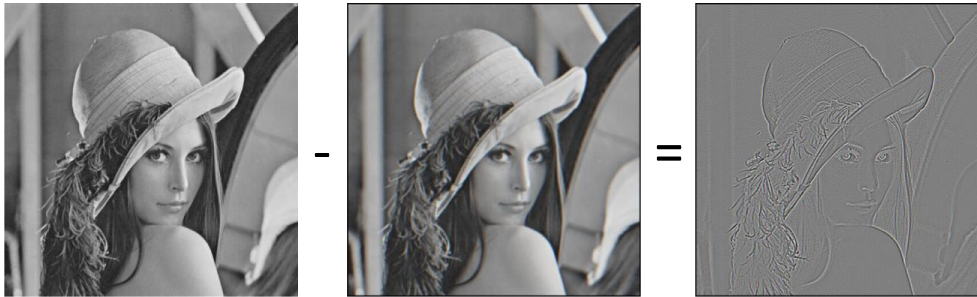


Shown in opposite  
order for space.

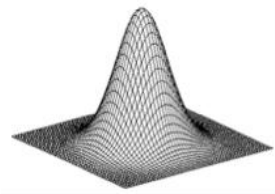
Which one takes  
more space to store?



# Why is it called a Laplacian pyramid?



unit



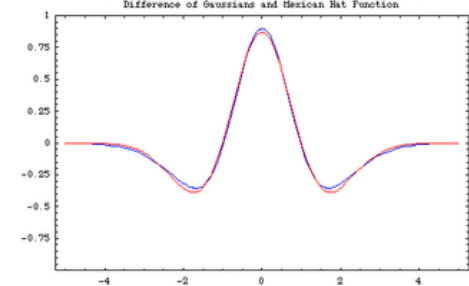
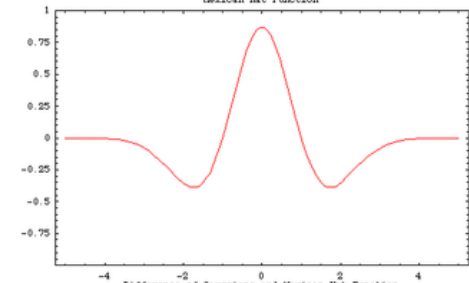
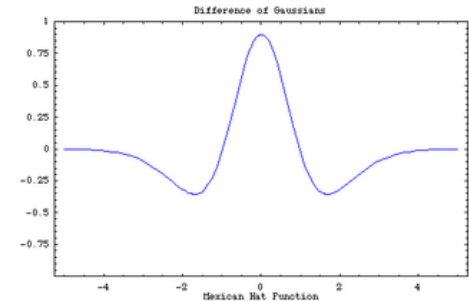
Gaussian

$\approx$



Laplacian

Difference of Gaussians approximates the Laplacian





# Still used extensively



# Still used extensively



foreground details enhanced, background details reduced



input image



user-provided mask



# What are image pyramids used for?

image compression



multi-scale  
texture mapping

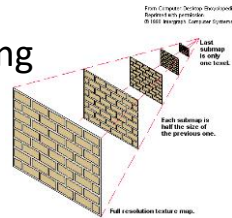
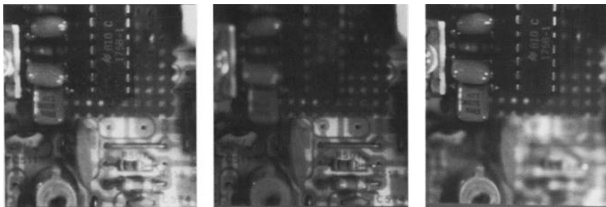


image blending



focal stack compositing



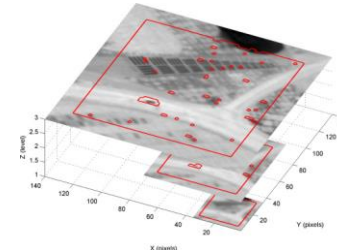
denoising



multi-scale detection



multi-scale registration





# References

- ◆ Some Slide material has been taken from Dr M. Usman Akram Computer Vision Lectures
- ◆ CSCI 1430: Introduction to Computer Vision by [James Tompkin](#)
- ◆ Statistical Pattern Recognition: A Review – A.K Jain et al., PAMI (22) 2000
- ◆ Pattern Recognition and Analysis Course – A.K. Jain, MSU
- ◆ *Pattern Classification*” by Duda et al., John Wiley & Sons.
- ◆ Digital Image Processing”, Rafael C. Gonzalez & Richard E. Woods, Addison-Wesley, 2002
- ◆ Machine Vision: Automated Visual Inspection and Robot Vision”, David Vernon, Prentice Hall, 1991
- ◆ [www.eu.aibo.com/](http://www.eu.aibo.com/)
- ◆ Advances in Human Computer Interaction, Shane Pinder, InTech, Austria, October 2008
- ◆ Computer Vision A modern Approach by Frosyth
- ◆ <http://www.cs.cmu.edu/~16385/s18/>