

29-01-18

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ARTIFICIAL INTELLIGENCE

INT-404

* Characteristics of problem:—

6. What is the role of knowledge

knowledge is imp. only to constrain the search for Solution.

Ex: Playing chess

7. Does the task require interaction with the person?

Solitary:

Ex: Theorem Proving

Conversational:

Ex: Medical diagnosis

* Production System Characteristics:—

It is a good way to describe the operations that can be performed in a search for a solution to a problem.

class of production System

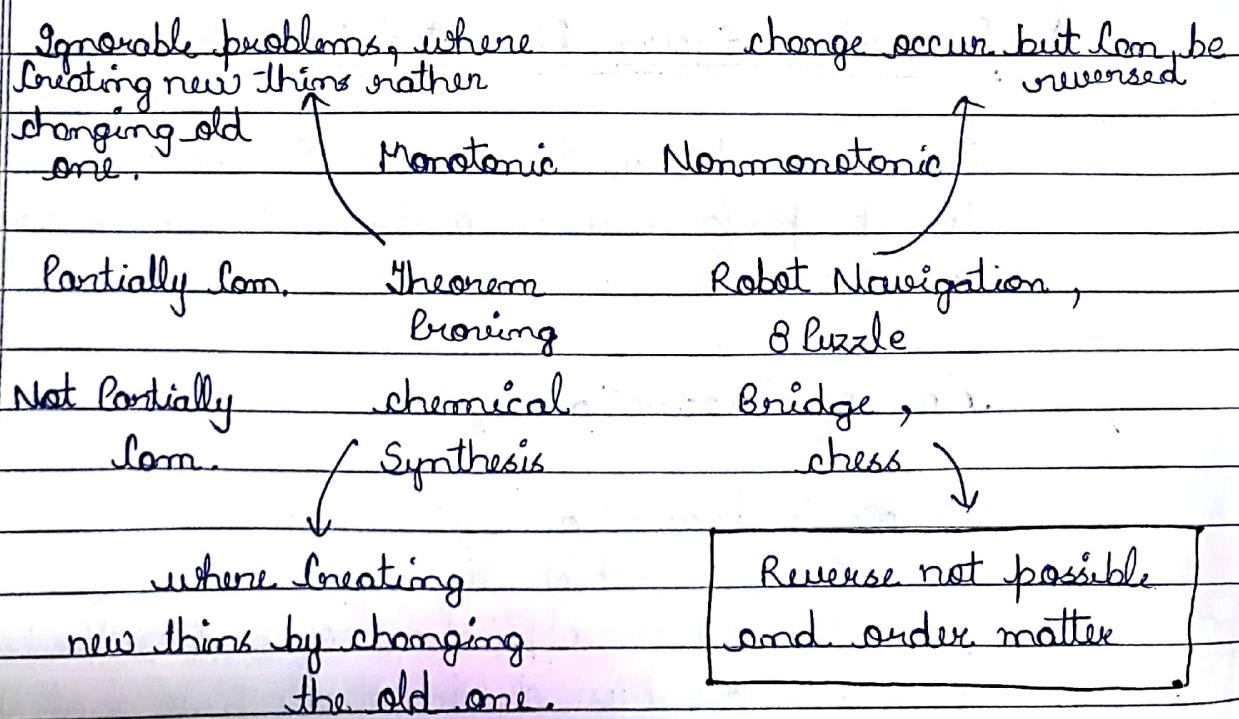
Monotonic production System

a system in which the application of one never prevents the later application of another rule that could also have been applied at the time that the first rule was selected. Ex: Theorem Proving.

- **Nonmonotonic Production System**
is one in which this one is not true.
- **Partially Commutative Production System**
is a system in with the property that if the application of particular sequence of rules transform state x into state y , then any permutation of those rules that is allowable also transform State x in to state y . (Ex: 8 puzzle problem.)
- **Commutative Production System**
is a productive system that is both monotonic and partially commutative.

* Relationship b/W problems and Production System:-

There is no relationship b/W kind of problem and productive system, in formal sense.



- State Space Search is the process of Searching through a State Space for a Solution by making explicit a Sufficient portion of an implicit state - Space graph to include a goal node.
 - Hence, initially $V = \{S\}$, where S is the Start node.
 - When S is expanded, its Successor are generated and those nodes are added to V and the associated arcs are added to E .
 - This process continues until a goal node is generated (include in V) and identified (by goal test)
- During Search, a node can be in one of the three Categories :-
 - Not generated yet (has not been made explicit yet)
 - OPEN : generated but not expanded.
 - CLOSED : expanded

A General Space State Search Algorithm

open := { } ; closed := { } ;

repeat

n := select(open) ; /* Select one node from open
if n is a goal
then exit with success ; /* delayed goal
testing */

expand(n)

/* generate all children of n
put these newly generated nodes in
open (check duplicates)
put in closed
n

until open = {} ;
exit with failure

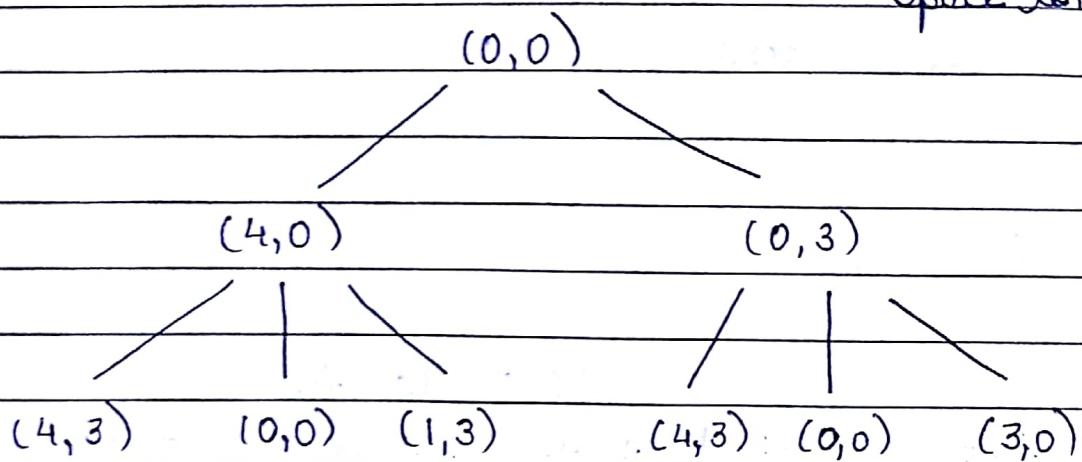
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* Breadth First Search :-

Water Jug Problem

→ Large amt. of
Space complexity



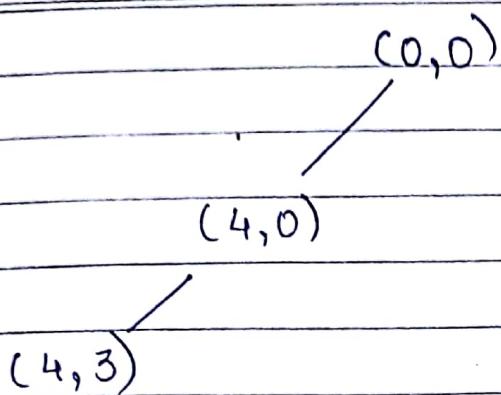
Two Levels of a breadth First Search Tree.

→ Time Complexity = $O(b^d)$
where b is branching factor
d is depth

* Depth First Search :-

Disadvantage :- Blind alley { Exploring single branch and there is possibility that we don't get the Answer there).

Example :- Water Jug Problem



Disadvantage :-

- May not terminate
- Not Complete
- does not guarantee us a Solution.

* Depth - First Iterative Deepening (DFID) :-

- BF and DF both have exponential Time Complexity $O(b^d)$
 BF is complete but have exponential Space Complexity.
 DF is Linear Space Complexity that is incomplete.
- DFID by Korf in 1985
 First do DFS to depth 0 (i.e. treat start node as having no successors), then, if no Solution found, do DFS to depth 1, etc.
 until Solution found do DFS with depth bound d

$$d = d + 1$$

Features :-

1. Complete
2. Optimal

* Bidirectional Search :-

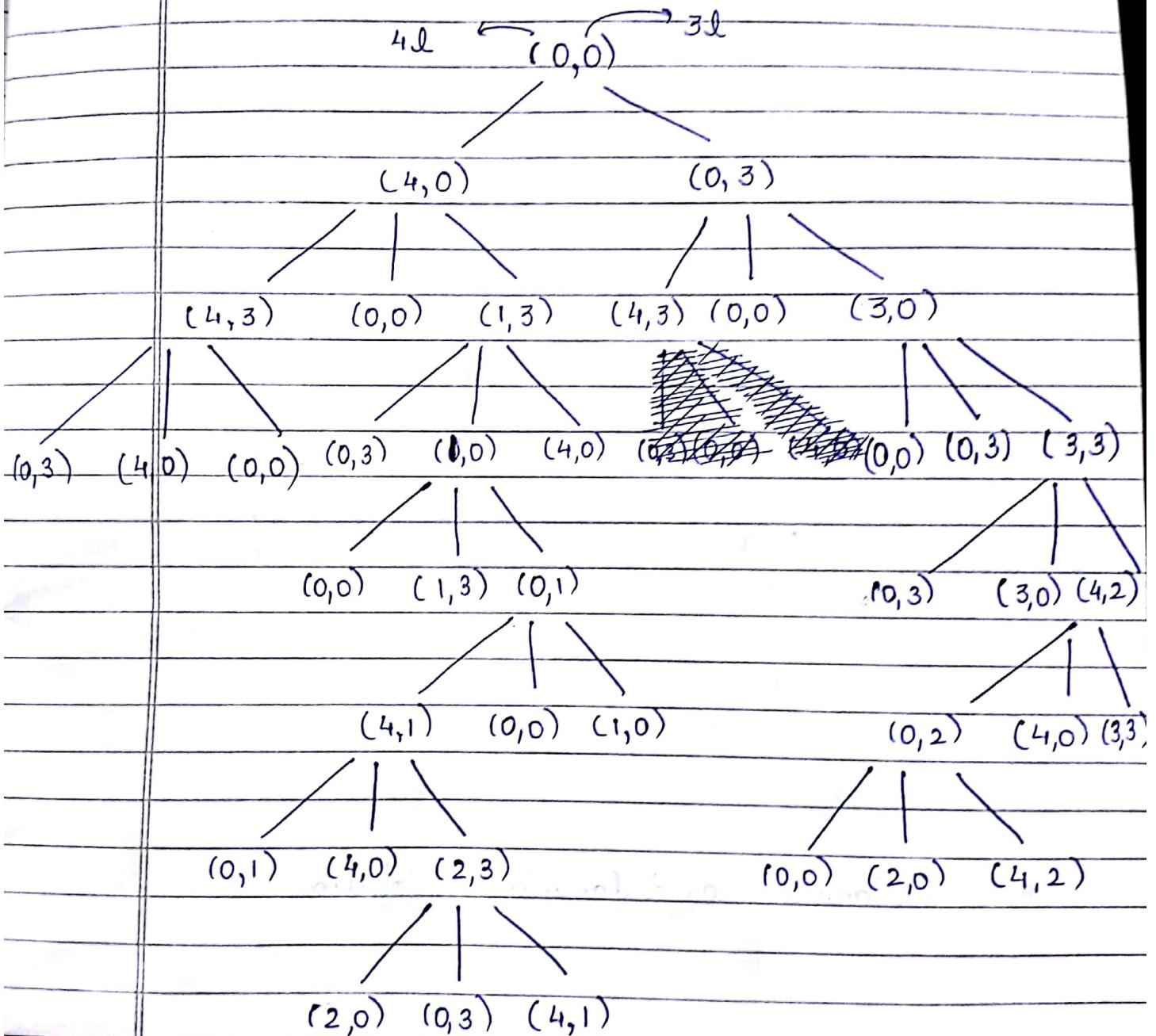
- graph search algorithm that finds a shortest path from initial vertex to a goal vertex in a directional graph.
- It runs two Simultaneous Searches : one[↑] from the initial state, and one backward from the goal, stopping when the two meet in the middle. ^{forward}

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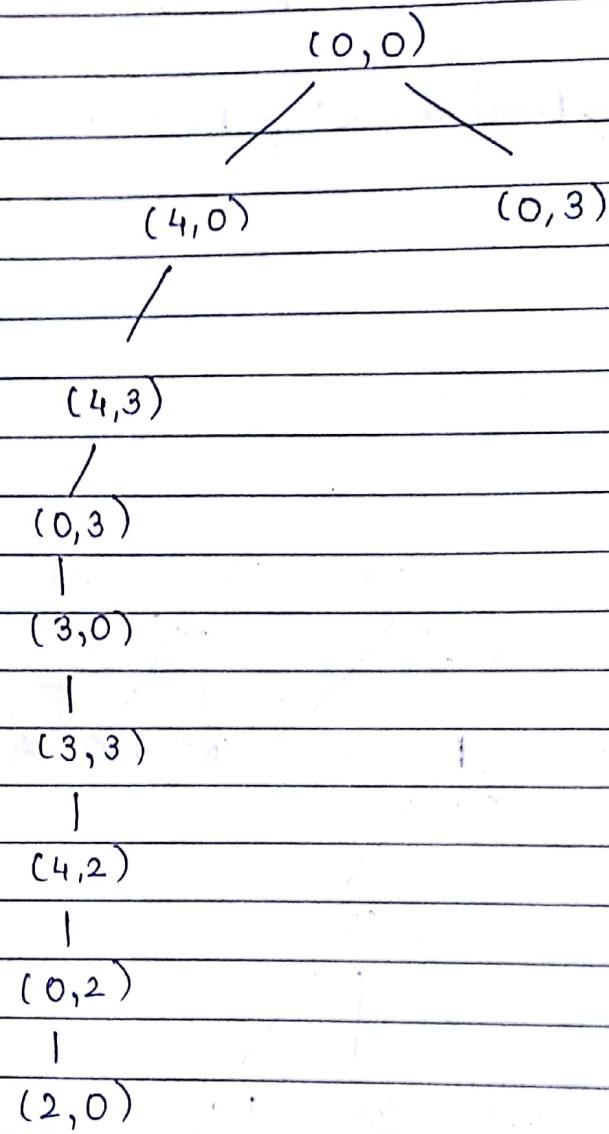
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★ Water Jug Problem using BFS :-



* Water Jug Problem using DFS :-



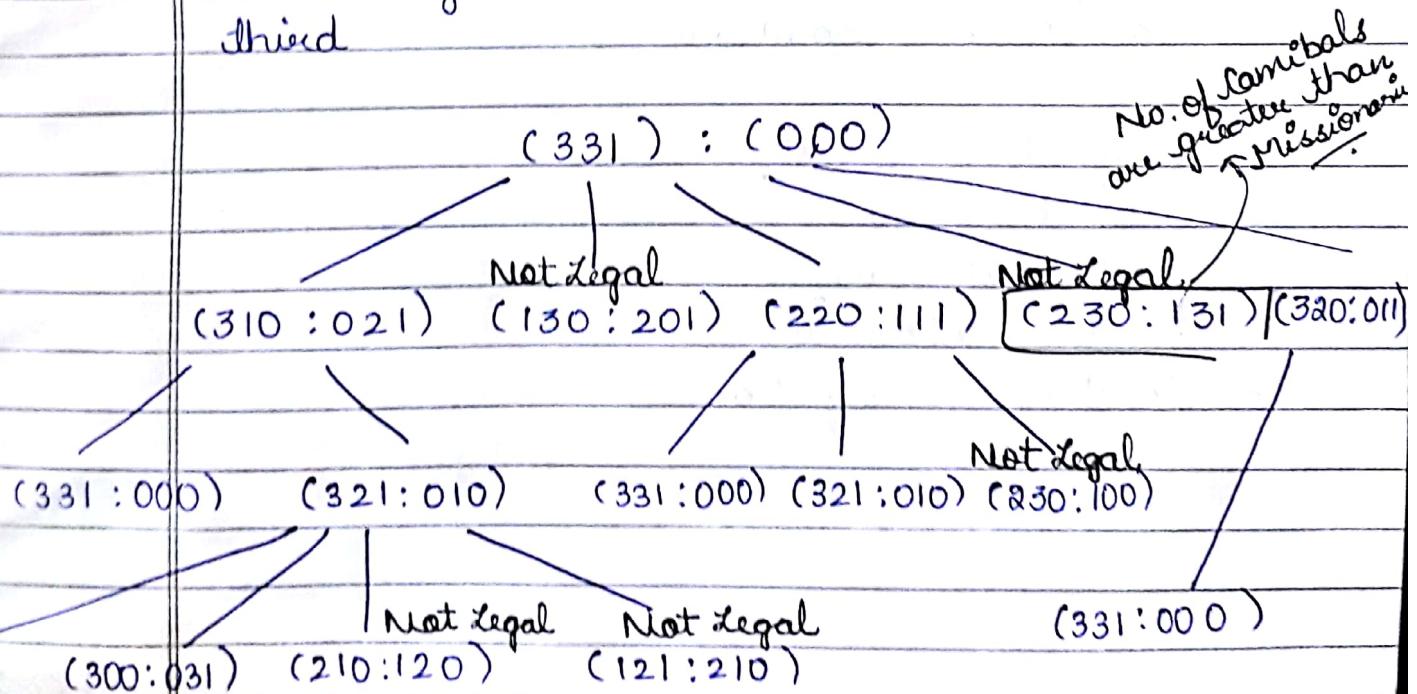
* Missionaries and Cannibals Solution :-

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0. 1 initial Setup MMMCCC B
1. Two Cannibals cross over MMMCC ~~BB~~ B CC
2. One comes back MMMCC B ~~BB~~ C
3. Two Cannibals go over again. MMM ~~BB~~ B CCC
4. One comes back MMMC B CC
5. Two missionaries cross MC B MMCC
6. A missionary & cannibal return MMCC B MC
7. Two missionaries cross CC B MMMC
8. A cannibal returns ~~crosses~~ CCC B MMM
9. ~~One cannibal~~ Two cannibal cross C B MMMCC
10. ~~Two cannibals cross~~ ~~one cannibal~~ One returns. CC B MMMC
11. And bring over the third B MMMCCC



Lecture

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* Heuristic Functions :-

- is a function that maps from problem state descriptions to measures of desirability, usually represented as numbers.
- Well designed Heuristic function play an important role in guiding a Search process towards a Solution
- For chess heuristic function should be high whereas in travelling Salesman it is Low.
- The purpose of Heuristic func. is to guide the Search process in profitable direction by Suggesting which path to follow first when more than one is available.
- Using good heuristics we can get good possible non optimal Solutions

1. Generate and Test
2. Hill Climbing
3. Best First Search
4. Problem reduction
5. Constraint Satisfaction

* Generate and Test :-

1. Generate a possible Solution
2. Test to See if this is actually a Solution by Comparing the chose point or the endpoint of the chosen path to the set of acceptable goal states.
3. If a Solution has been

→ Example :

1. Finding key of a 3 digit Lock.
 2. 8-Puzzle problem.
- Inefficient for problems with Large Space.
- Features of Generate & Test :-

1. Generate Solution randomly.
2. Exhaustive : Consider each case in depth.
3. Heuristic : not Consider paths that seem unlikely to lead a solution.
4. Plan

* Hill Climbing :-

- Hill climbing can be used to solve problems that have many solutions but where some solutions are better than others.

- It is often used when a good heuristic function is available for evaluating state but when no other useful knowledge is available.
- Example: In Travelling Salesman, straight line distance b/w two cities can be a heuristic measure of remaining distance.
- Test function + heuristic function = Hill climbing

* Simple Hill Climbing :-

The key difference b/w Simple Hill climbing and Hill climbing is

8-Puzzle Problem (using Simple Hill Climbing)

2	8	3		1	2	3	
1	6	4	→	8		4	
7		5		7	6	5	

Heuristic Value = 4 = 0

2	8	3		2		3	
1		4	→	1	8	4	
7	6	5		7	6	5	

= 3 = 3

	2	3		1	2	3
1	8	4	→	8	4	
7	6	5		7	6	5

= 2

= 1

1	2	3	
8		4	
7	6	5	

= 0

* Steepest-Ascent Hill Climbing :-

- Consider all the moves from current state.
- Selects the best one as the next state.
- Also known as Gradient Search.

$$h(n) = d(n) + w(n)$$

↓

0

↗ No. of files
misplaced

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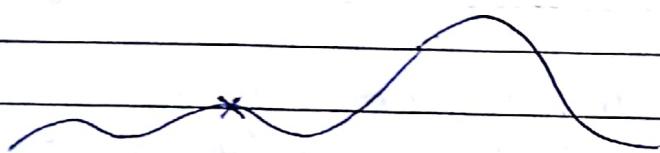
- It uses BFS.
- ~~no. of files~~

* Disadvantages of Hill Climbing :-

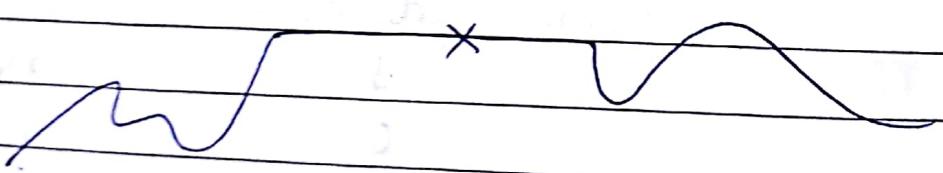
1. Local maximum : A state that is better than all of its neighbours, but not better than some other states far away.

2. Plateau : A flat area of Search Space in which all neighbouring states have the same value.
3. Ridge : Special kind of Local maximum. It is an area of Search Space that is higher than the surrounding area and itself has a slope on but cannot be traversed by Single move in any one direction. Means move in several direction in one.

- Local maximum



- Plateau



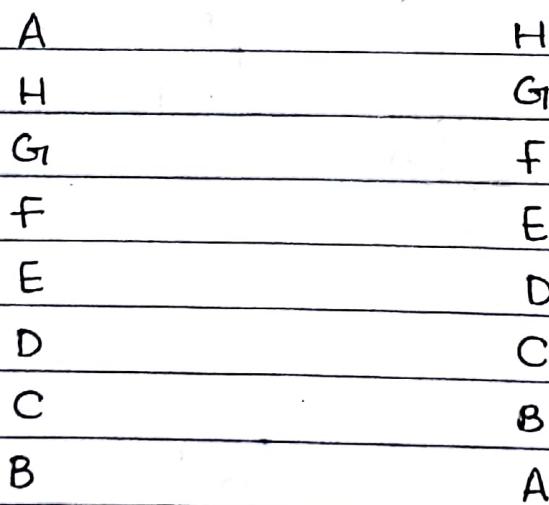
- Ridge



To Solve these 3 problems :

1. Backtrack to some earlier node and try going in a different direction. (good way in dealing with Local maxima)
2. Make a big jump to try to get in a new Section. (good way in dealing with plateaus)
3. Moving in several directions at once. (good strategy for dealing with ridges)

* A Hill Climbing Problem



Initial State

Goal State

Local : Add one pt. for every block that is resting on thing it is supposed to be resting on. Subtract one point from every block that is sitting on wrong thing.

-1	A	H	+1
+1	H	G	+1
+1	G	F	+1
+4 =	+1 F	E	+1 = +8
	+1 E	D	+1
	+1 D	C	+1
<i>As B was d to -1</i>	+1 C	B	+1
<i>Suppose on A</i>	-1 B	A	+1

Initial

Goal

H	+1
G	+1
F	+1
E	+1
D	+1
C	+1 +6
A	+1
B	-1

A
H
G
F
E
D
C
B

G
F
E
D
C
H
A
B

(a)

G
F
E
D
C
A
H
B

(c)

(b)

point

Global : Add one for every block in Current Support Structure, Subtract one point for every block in existing Support Structure.

-7	A
-6	H
= -28	G
-5	F
-4	E
-3	D
-2	C
-1	B
0	

Initial State

H	+7
G	+6
F	+5
E	+4
D	+3
C	+2
B	+1
A	0

Goal State

H	-6
G	-5
F	-4
E	-3
D	-2
C	-1
B	0

A							
H							
G							
F							
E							
D							
C	-1	H	C	-1			
B	0	A	B	0	A	H	B

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Lecture 1

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Artificial Intelligence★ Simulated Annealing :

- A variation of hill climbing in which at the beginning
- Probability of transition to higher energy state is given by function :

$$P = e^{-\Delta E/RT} \rightarrow \begin{matrix} \text{No. of Steps} \\ \text{downhill} \end{matrix}$$

where

 ΔE is the positive change in the Energy Level

T is Temperature

K is Boltzmann Constant

Suppose K = 1

$$P = e^{\Delta E/T}$$

Next State

$$\Delta E = h(\text{Current State}) - h(\text{N.S.})$$

Annealing Schedule : If the Temp. is lowered sufficiently slowly, then the goal will be obtained.

* BEST FIRST SEARCH :-

- OR Graph
 - A* Search
 - Agenda Search
- Combines the advantages of both DFS and BFS into a single method.
- Depth First Search : not all competing branches having to be expanded.
- Breadth First Search : not getting trapped on dead-end paths.
- ⇒ Combining the two is to follow a single path at a time, but switch paths whenever some competing path look more promising than the current one.
- General approach of At each step of BFS search process, we select the most promising of the nodes we have generated so far.
 - This is called OR-graph, since each of its branches represents an alternative problem solving path.

Water Jug Problem using BFS

$$h = (x_c - x_g + (y_c - y_g))$$

$$h = (x_c + y_c - 2)$$

$$h = (0 - 2 + 0 - 0) = -2$$

$$h = (4 + 0 - 2) = +2$$

$$+2 \quad (4, 0)$$

$$(0, 0) (-2)$$

$$+1 \quad h = (0 + 3 - 2) = +1$$

Wrong

$$1, 3$$

$$3 + 1 - 2$$

$$(3, 1)$$

$$(0, 0)$$

$$4 + 3 - 2 = +5$$

$$(4, 3)$$

$$3 + 0 - 2$$

$$= +1$$

$$(4, 3)$$

$$(4, 0)$$

$$(3, 0)$$

$$(0, 1)$$

$$(1, 3)$$

$$(0, 3)$$

$$(0, 0)$$

$$3 + 3 - 2$$

$$= +4$$

$$(0, 0)$$

$$(1, 0)$$

$$(0, 1)$$

$$1 + 0 - 2$$

$$= -1$$

$$4 + 1 - 2$$

$$= +3$$

Now, we

will expand
(4, 0) as its head
is more close
our goal.

$$(0, 0)$$

$$(0, 1)$$

$$1 + 3 - 2$$

$$= +2$$

$$(1, 0)$$

$$(0, 3)$$

$$(4, 0)$$

Best First Search Vs Hill Climbing

- In hill climbing, one move is selected and all the others are rejected. In BFS, one move is selected but
- OPEN : nodes that have been generated but have not examined. This is organized as Priority queue.
- CLOSED :

* A* SEARCH :-

Evaluation function : $f(n) = g(n) + h(n)$

- $g(n)$ the cost to reach the node.
- $h(n)$ estimated cost to get from node to the goal.
- $f(n)$ estimated total cost of path through n to goal.

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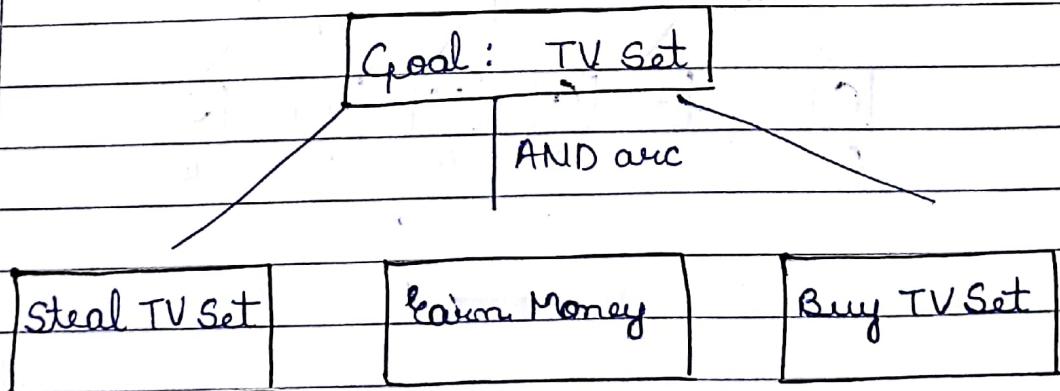
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* AND OR Graph:-

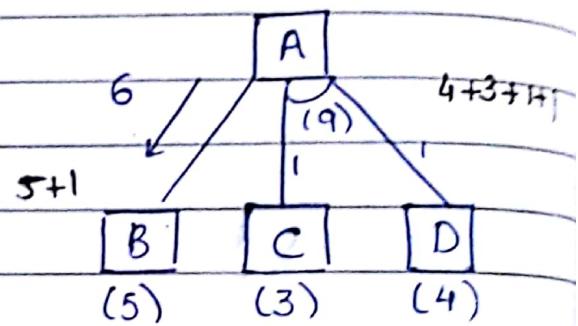
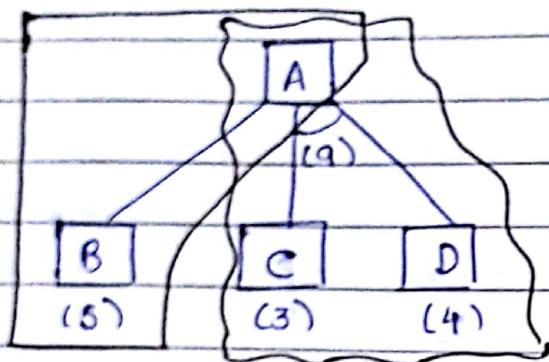
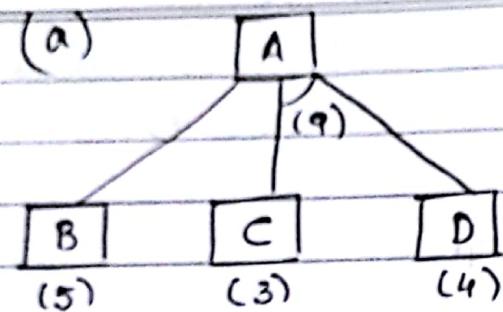
When a problem can be divided into a set of sub problems, where each sub problem can be solved separately and a combination of these will be a solution, AND-OR graphs or AND-OR trees are used for representing the solution.

The decomposition of the problem or problem reduction generates AND arcs. One AND arc may point to any number of successor node.

All these must be ~~solved~~ solved so that the arc will rise to many arcs, indicating several possible solutions. Hence the graph is known as AND-OR instead of AND.



Example: (a)

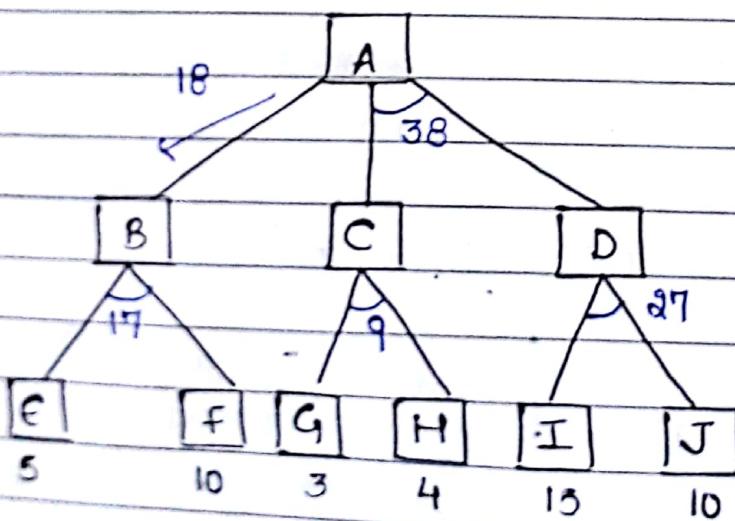


OR

AND

We will expand B
as it having 6.

(b)



* Constraint Satisfaction :-

- The goal is to discover some problem state that satisfies a given set of constraints. Ex: Puzzles, real world perceptual labeling problems, design tasks etc.
- Helps in reducing the amt. of search required as compared with a method that attempts to form partial solutions directly by choosing specific value for components of the eventual solutions.

(a)

$$\begin{array}{r}
 & & & ① \\
 & 1 & 0 & 9^4 & 1 & C^2 \\
 + & 1 & 0 & 9^4 & 1 & C^2 \\
 \hline
 & P & R & 0 & 1 & 0 & G^4
 \end{array}$$

$O = 1$
 $I = 5$
 $C = 2$
 $G = 4$
 $L = 9$
 $R = 8$

Given
So $P = 1$

- (i) No two letters can have same digits.
(ii) Should satisfy arithmetic operations.

(b)

$$\begin{array}{r}
 C_4 \quad C_3 \quad C_2 \quad C_1 \\
 S \quad E \quad N \quad D \\
 + \quad M \quad O \quad R \quad E \\
 \hline
 M \quad O \quad N \quad E \quad Y
 \end{array}$$

Assuming the carry
 C_1, C_2, C_3, C_4

Given
 $R = 8, 9$
 $M = 1$
 $S = 8, 9$
 $O = 0$
 $E = 2$
assumption

$C_2 + E + O = N$
 $C_2 + E = N$
 $C_1 + N + R = E$
 $C_1 + 3 + R = 12$
 $C_1 = 0$
 $C_1 = 1$
 $R = 9$
 $R = 8$

as E can't be equal to N

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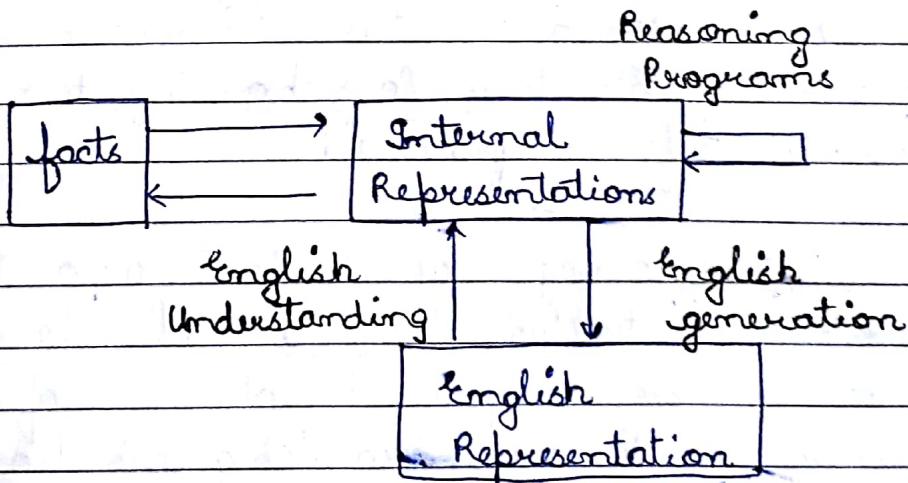
* Knowledge Representation : —

knowledge can be defined as body of facts and principles accumulated by human-kind or the act, fact or state of knowing.

knowledge can be of following types

1. Declarative (Statements)
2. Procedural (facts, rules, function)
3. Heuristic (rule of thumb/experience)

→ Mapping b/w facts and Representation



Facts : Truths in some relevant world. These are the things we want to represent.

1. Spot is a dog \rightarrow dog(Spot)
2. All dogs have tails $\rightarrow \forall x : \text{dog}(x) \rightarrow \text{has.tail}(x)$
3. Then using the deduction method of Logic, we may generate the new representation object : has.tail(Spot)
4. So we can, using backward mapping function :
Spot has a tail.

~~points~~ → A good System for the representation of knowledge should have following properties :-

1. Representational Adequacy : the ability to represent all of the kinds of knowledge that one needed in that domain.
2. Inferential Adequacy : The ability to manipulate the representational structures in such a way as to derive new structures corresponding to new knowledge inferred from old.
3. Inferential efficiency : ability to incorporate into knowledge structure the additional information that can be used to focus the attention of inference mechanism in the most promising direction.
4. Acquisitional efficiency : Acquiring new information easily using automatic methods wherever possible rather than reliance on human intervention.

4 types of knowledge representation :-

1. Simple Relational knowledge

Player	Height	Weight	Runs
dhoni	6 - 0	150	3000
Sachin	5 - 4	140	15000
Zahoor	6 - 2	160	1000

This even does not tell us who is heaviest player

2. Inheritable knowledge

- It is possible to enhance the basic representation with inference mechanism that operate on the structure of representation.
- The most useful form of inference is Property Inheritance, in which elements of specific classes inherit attributes and values from ~~one specific~~ one general classes in which they are included.

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$$\begin{array}{r}
 C_3 C_2 C_1 \\
 \text{TWO} \\
 + \text{TWO} \\
 \hline
 \text{FOUR}
 \end{array}$$

1. $f = 1$

2. $\theta \neq 0$ ~~as~~ as then R will also be zero. $\theta \neq 1$ as f is 1. $\theta = 2$ So R is 4.

3. $C_2 + 2T = 12$

 \downarrow

0 $T = 6$

4. Assume $\theta = 4$

3. $R = 8$

$C_2 + 2T = 14$

 \downarrow

0 $T = 7$

5. $C_1 + W + W = U$

 \downarrow

0 $W + W = U$

$W = 3 \rightarrow U = 6$

2.
 $\begin{array}{r} C_4 C_3 C_2 C_1 \\ \text{E A T} \\ + \text{T H A T} \\ \hline \text{A P P L E} \end{array}$

1. $A = 1$ as it is a carry.

2. $C_1 + A + A = L$

$C_1 + 1 + 1 = L$

$L = 2 + C_1$

$C_1 + 2 = L$

$3 = L$

3. $T = 9$

4. $T + T = E$

$9 + 9 = E$

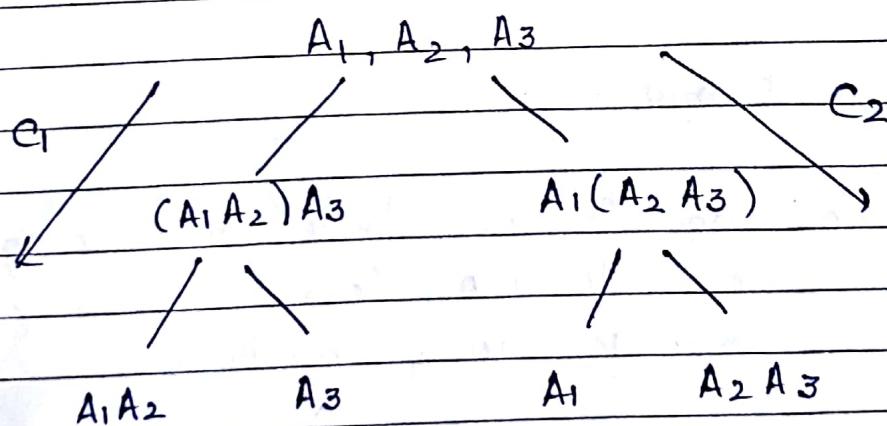
$18 = E \quad (C_1 = 1)$

$E = 8$

5. $P = 0$

6. $H = 2$

* AO :-



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Knowledge Representation

→ 4 Types of Knowledge Representation :-

3. Inferential knowledge

Sometimes all the power of traditional logic is necessary to describe the inferences that are needed. We can represent inferential knowledge about a domain using first order predicate logic.

1. Marcus was a man.

man(marcus)

2. Marcus was a Pompeian.

Pompeian(marcus)

4. Procedural knowledge

- This knowledge can be represented in programs in many ways. The most common way is simply as code for doing something.

- The machine uses the knowledge when it executes the code to perform a task.

10 Marks
Imp.

* Issues in Knowledge Representation :-

1. Important Attributes

- There are two attributes that are of very general significance, and we have already seen their use; instance and isa.
- Attributes are imp. bcos they support the property inheritance.

2. Relationship among Attributes

Properties as:

- Inverse
- Existence in an isa hierarchy
- Single - Valued Attributes

3. Choosing the Granularity of the Representation

It is necessary to answer the question "At what level of detail should the world be represented?" .

Another way this question is phrased is "What should be our primitives?" .

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* Issues in Knowledge Representation :-

4. Representing Set of Objects

It is imp. to be able to represent sets of objects for several reasons:

- There are some properties that are true of sets that are not true of the

Two ways to represent the object :

1. Extensional : List the members

2. Intensional : provide a rule that, when a particular object is evaluated return true or false depending the object is in the set or not.

Ex:

Extensional description of the set of our Sun's planets on which people live is {earth} and intensional description is :

$$\{x : \text{Sun-planet}(x) \wedge \text{human-inhabited}(x)\}$$

chapter - 5 PREDICATE Logic

* Propositional Logic & Predicate Logic :-

1. Socrate is a man

Man.Socrate (Propositional logic)

2. Plato is a man

Man.Plato (Propositional)

3. All men are mortal

Mortal.Man (Propositional)

1. Socrate is a Man \rightarrow Man(Socrate)

2. Plato is a Man \rightarrow Man(Plato)

3. All men are mortal \rightarrow Mortal (Socrate)

Predicate
Logic

Propositional

1. Represent using Variable.

2. New knowledge cannot be easily generated.

3. No Quantifiers

Predicate

1. Represent using classes and instance.

2. New knowledge is easily generated.

3. Quantifiers

$\forall \rightarrow$ for all

$\exists \rightarrow$ There exist

→ Some Simple facts in Propositional Logic :-

1. It is raining
RAINING

2. It is Sunny
SUNNY

3. It is Windy
WINDY

4. If it is raining, then it is not sunny.

RAINING \rightarrow \neg SUNNY

- $\wedge \rightarrow$ and
- $\vee \rightarrow$ or
- $\neg \rightarrow$ negation
- $\rightarrow \rightarrow$ implies

→ Predicate Logic :-

also called First order predicate logic or Simply First order Logic or Predicate Calculus or FOL.

It is more versatile than propositional. Counterpart for its added features.

→ Limitations of Propositional Logic :-

Socrates is a man

SOCRATE MAN

Plato is a man

PLATOMAN

Can't able to draw
Similarities b/w Socrates
and Plato.

Better representation:

MAN(SOCRATE)

MAN(PLATO)

All men are mortal

MORTAL MAN

fail to capture relationship
b/w any individual being
a man and that individual
being mortal.

$\forall x : \text{man}(x) \rightarrow \text{mortal}(x)$

Predicate Logic Example

1. Marcus is a man.
2. Marcus was a pompeian
3. All pompeians were romans.
4. Caesar was a ruler
5. All romans were either loyal ~~or~~ to Caesar or hated him.
6. Everyone is loyal to someone.
7. People only try to assassinate ruler they are not loyal to.
8. Marcus tried to assassinate Caesar.

1. $\text{Man}(\text{Marcus})$
2. $\text{Pompeian}(\text{Marcus})$
3. $\forall x: \text{pompeian}(x) \rightarrow \text{Romans}(x)$
4. $\text{Ruler}(\text{Caesar})$
5. $\forall x: \cancel{\text{Roman}(x)} \rightarrow \text{Loyal to}(\text{Caesar}, x)$
 $\vee \text{hated}(\text{Caesar}, x)$
6. $\forall x, \exists y: \rightarrow \text{Loyal to}(x, y)$
7. $\forall x: \forall y: \text{people}(x) \wedge \text{ruler}(y) \rightarrow \cancel{\text{try to assassinate}}(x, y) \wedge \neg \text{Loyal to}(x, y)$
- 8.

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1. All hounds howl at night.
2. Anyone who has any cats will not have any mice.
3. Light Sleepers do not have anything which howls at nights.
4. John has either a cat or a hound.
5. If John is a Light Sleeper then John does not have any mice.

1. $\forall x : \text{hound}(x) \rightarrow \text{howl}(x)$.
2. $\forall x \forall y : \text{have}(x, y) \wedge \text{cat}(y) \rightarrow \forall z (\neg(\text{have}(x, z) \wedge \text{mouse}(z)))$
3. $\forall x : \text{LightSleeper}(x) \rightarrow \neg \exists y (\text{have}(x, y) \wedge \text{howl}(y))$
4. $\exists x : \text{have}(\text{John}, x) \wedge \text{cat}(x) \vee \text{hound}(x)$
5. $\text{LightSleeper}(\text{John}) \rightarrow \neg \exists x (\text{have}(\text{John}, x) \wedge \text{mouse}(x))$

1. Anyone whom many loves is a football star.
2. Any student who does not pass does not play.
3. John is a student.
4. Any student who does not study does not pass.
5. Anyone who does not play is not a football star.
6. If John does not study then many does not love John.

1. $\forall x : \text{Loves}(\text{Mary}, x) \rightarrow \text{Football Star}(x)$.
2. $\forall x : \text{Student}(x) \wedge \neg \text{pass}(x) \rightarrow \neg \text{play}(x)$.
3. $\text{student}(\text{John})$.
4. $\forall x : \text{Student}(x) \wedge \neg \text{Study}(x) \rightarrow \neg \text{pass}(x)$.
5. $\forall x : \neg \text{play}(x) \rightarrow \neg \text{football Star}(x)$.
6. $\neg \text{Study}(\text{John}) \rightarrow \neg \text{Love}(\text{Mary}, \text{John})$.

1. Every child loves Santa.
2. Everyone who loves Santa loves Reindeer.
3. Rudolf is a reindeer and Rudolf has a red nose.
4. Anything which has a red nose is weird or clown.
5. No Reindeer is a clown.
6. Scrooge does not love anything which is weird.
7. Scrooge is not a child.

1. $\forall x : \text{child}(x) \rightarrow \text{Loves}(\text{Santa}, x)$
2. $\forall x : \text{Loves}(x, \text{Reindeer}) \rightarrow \forall y : \text{Reindeer}(y) \wedge \text{Loves}(x, y)$
3. $\text{Reindeer}(\text{Rudolf}) \wedge$
4. $\forall x : \text{has}(\text{red nose}) \rightarrow \text{Weird V clown}$
5. ~~$\text{childless}(\text{Scrooge})$~~
6. $\forall x : \text{Loves}(\text{Scrooge}, x) \rightarrow \text{Weird}$
7. $\neg \text{child}(\text{Scrooge})$

1. No mortal lives longer than 150 years.
2. All Romans died when volcano erupted in 1979 AD.

1. $\forall x : \text{Mortal}(x) \wedge \text{born}(x, t_1) \wedge \exists t_2 \forall t_1 \text{gt}((t_2 - t_1), 150) \rightarrow \text{dead}(x)$
2. $\forall x : \text{Roman}(x) \rightarrow \text{dead}(x, 1979)$
3. Alive means not dead.

$\forall x : \forall t : \text{alive}(x, t) \rightarrow \neg \text{dead}(x, t)$

[Lecture].

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* Clause Normal Form (CNF) :-

1. Eliminate \rightarrow , using: $a \rightarrow b = \neg a \vee b$
2. Reduce the scope of each \neg to a single term using:

- $\neg(\neg p) = p$
- de Morgan's Laws : $\neg(a \wedge b) = \neg a \vee \neg b$
 $\neg(a \vee b) = \neg a \wedge \neg b$
- $\neg \forall x : P(x) = \exists x : \neg P(x)$
- $\neg \exists x : P(x) = \forall x : \neg P(x)$

3. Standardize variables.
4. Move all quantifiers to the left of the formula without changing their relative order.
5. Eliminate existential quantifiers by inserting Skolem Fun.
6. Drop the prefix.
7. Convert the matrix into a conjunction of disjuncts, using associativity and distributivity.
8. Create separate clauses for each conjunct.
9. Standardize apart the variable in the set of clauses generated in Step 8, using the fact that

$$(\forall x : P(x) \wedge Q(x)) = \forall x : P(x) \wedge \forall x : Q(x)$$

$\forall x : \text{Student}(x) \wedge \text{pass}(x) \rightarrow \text{play}(x)$

Step 1: $\forall x : \neg \text{Student}(x) \wedge \neg \text{pass}(x) \vee \neg \text{play}(x)$

Step 2: $\forall x : \neg \text{Student}(x) \vee \neg (\neg \text{pass}(x) \vee \neg \text{play}(x))$

Step 3: $\forall x_1 : \neg \text{Student}(x_1) \vee \text{pass}(x_1) \vee \neg \text{play}(x_1)$

Step 5. Example:

$\exists y : \text{President}(y)$

will be converted to

$\text{President}(\text{s1})$

While

$\forall x : \exists y : \text{father-of}(y, x)$

will be converted to

$\forall x : \text{father-of}(\text{s2}(x), x))$

Lecture

86-02-18

Artificial Intelligence

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1. Marcus was a man.
2. Marcus was a Pompeean.
3. All Pompeeans were Romans.
4. All Romans were either loyal to Caesar or hated him.
5. Caesar was a ruler.
6. Everyone is loyal to someone.
7. People only try to assassinate ruler they are not loyal to.
8. Marcus tried to assassinate Caesar.

1. man (Marcus)

2. Pompeean (Marcus)

3. $\forall x : \text{Pompeean}(x) \rightarrow \text{Roman}(x)$

$\neg \text{Pompeean}(x_1) \vee \text{Roman}(x_1)$ } In CNF.

4. ruler (Caesar)

5. $\forall x : \text{Roman}(x) \rightarrow \text{Loyal.to}(\text{Caesar}, x) \vee \text{hate}(\text{Caesar}, x)$

$\forall x \rightarrow \text{Roman}(x) \vee \text{Loyal.to}(\text{Caesar}, x) \vee \text{hate}(\text{Caesar}, x)$

$\forall x_2 \rightarrow \text{Roman}(x_2) \vee \text{Loyal.to}(\text{Caesar}, x_2) \vee \text{hate}(\text{Caesar}, x_2)$
 $\neg \text{Roman}(x_2) \vee \text{Loyal.to}(\text{Caesar}, x_2) \vee \text{hate}(\text{Caesar}, x_2)$

6. $\forall x \exists y : \text{Loyal.to}(x, y)$

$\forall x_3 \exists y_1 : \text{Loyal.to}(x_3, y_1)$

$\forall x_3 : \text{Loyal.to}(x_3, f(x_3))$

7. $\forall x \forall y : \text{People}(x) \wedge \text{ruler}(x) \wedge \text{trytoassassinate}(x, y) \rightarrow \text{LoyalTo}(x, y)$

$\forall x \forall y : [\text{People}(x) \wedge \text{ruler}(x) \wedge \text{trytoassassinate}(x, y)] \rightarrow \text{LoyalTo}(x, y)$

$\forall x_4 \forall x_2 : \neg [\text{People}(x_4) \wedge \text{ruler}(x_4) \wedge \text{trytoassassinate}(x_4, y_2)] \vee \neg \text{LoyalTo}(x_4, y_2)$

$\rightarrow \neg \text{People}(x) \vee \neg \text{ruler}(x) \vee \neg \text{trytoassassinate}(x, y) \vee \neg \text{LoyalTo}(x, y)$

$\neg \text{People}(x_4) \vee \neg \text{ruler}(x_4) \vee \neg \text{trytoassassinate}(x_4, y_1)$

$\vee \neg \text{LoyalTo}(x_4, y_1)$.

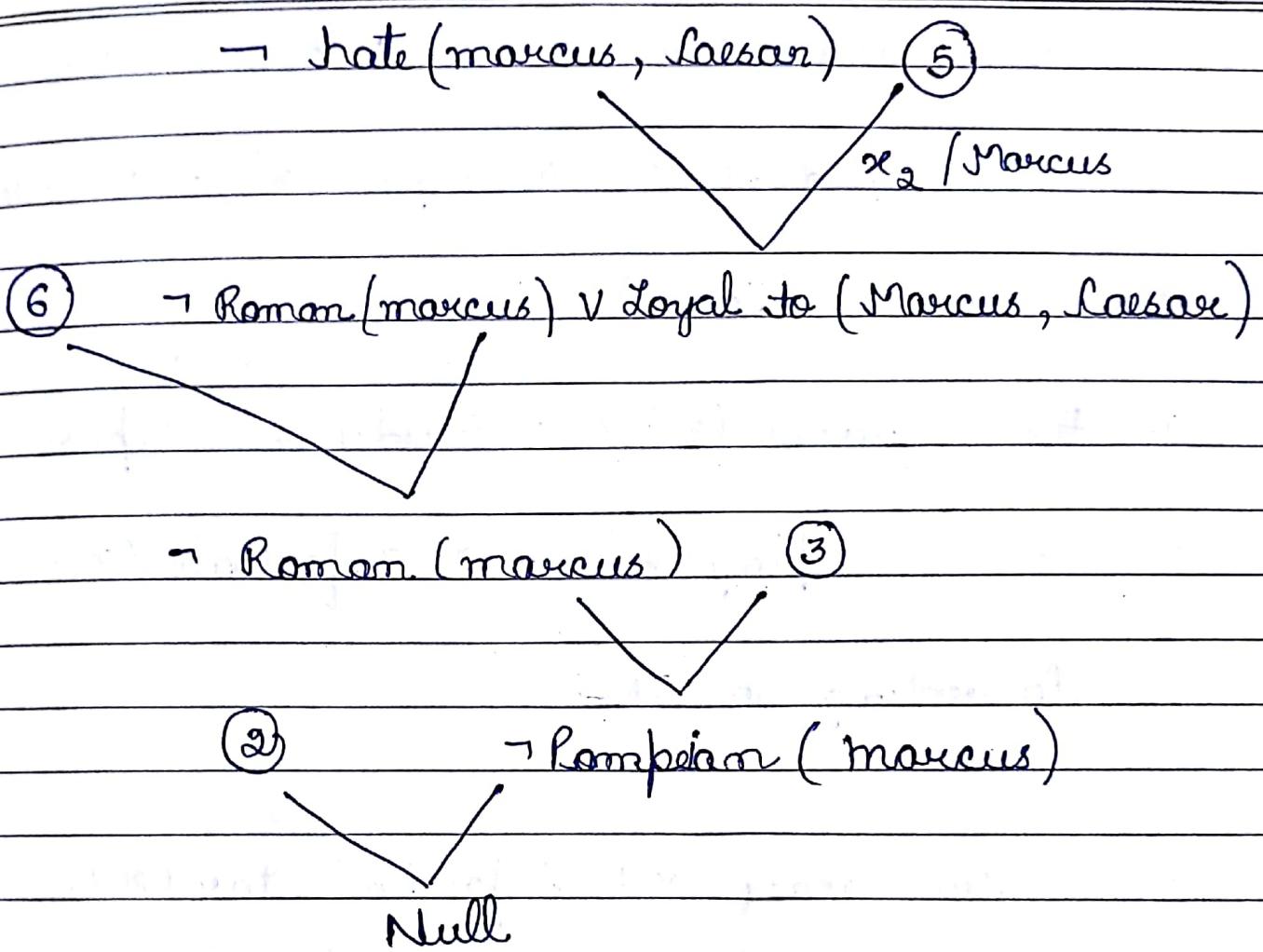
8. Trytoassassinate (Marcus, Caesar)

Prove: Marcus hate Caesar
 hate (Marcus, Caesar)

We will start by assuming the Contradiction part.

Resolution Proof

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- Q.
1. Anyone whom Mary loves is a football star.
 2. Any student who does not pass do not play.
 3. John is a student.
 4. Any student who does not study does not pass.
 5. Anyone who does not play is not a football star.
 6. If John does not study, then Mary does not love John.

Prove : If John does not study, then Mary does not love John.

Predicate Logic

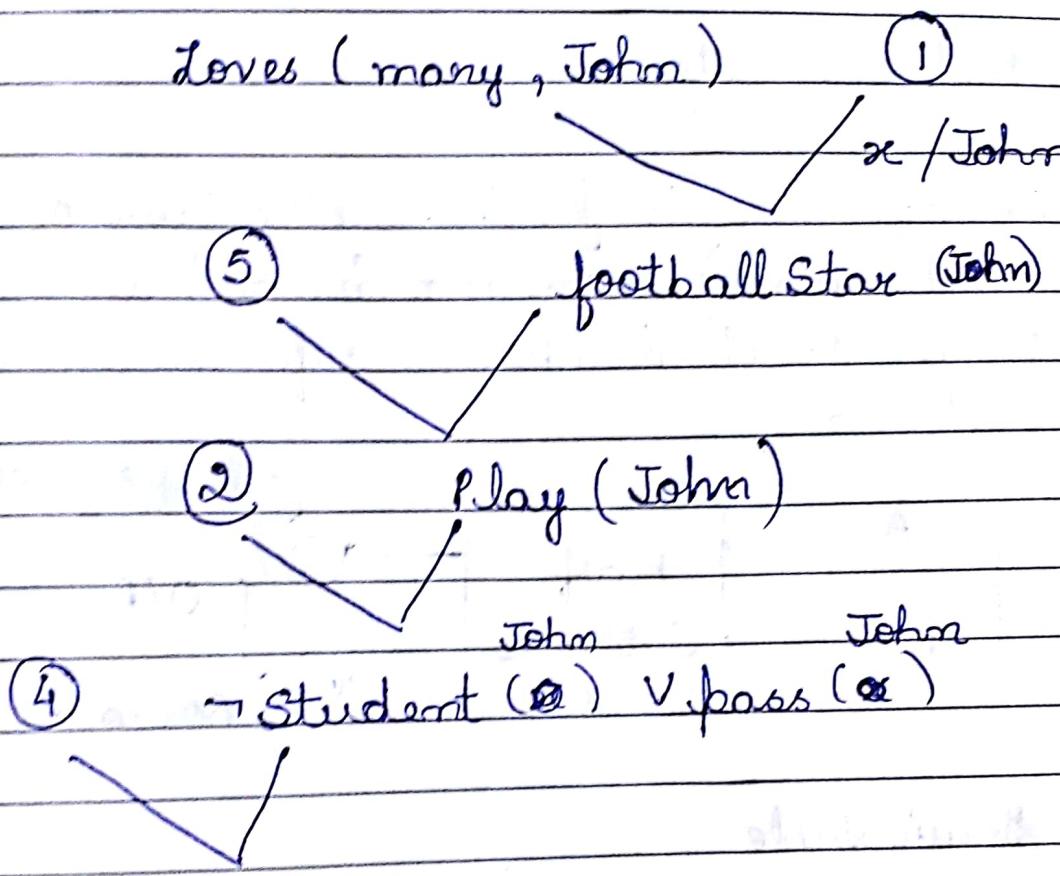
1. $\forall x : \text{Loves}(\text{Mary}, x) \rightarrow \text{FootballStar}(x)$.
2. $\forall x : \text{Student}(x) \wedge \neg \text{pass}(x) \rightarrow \neg \text{Play}(x)$
3. $\text{Student}(\text{John})$
4. $\forall x : \text{Student}(x) \wedge \neg \text{Study}(x) \wedge \neg \text{pass}(x)$
5. $\forall x : \neg \text{play}(x) \rightarrow \neg \text{football}(x)$

Converting to CNF.

1. $\neg \text{Love}(\text{Mary}, x) \vee \text{FootballStar}(x)$.
2. $\neg (\text{Student}(x) \wedge \neg \text{pass}(x)) \cancel{\vee} \neg \text{Play}(x)$
 $\neg \text{Student}(x) \vee \text{pass}(x) \vee \neg \text{Play}(x)$
3. $\text{Student}(\text{John})$
4. $\neg (\text{Student}(x) \wedge \neg \text{Study}(x)) \vee \neg \text{pass}(x)$
 $\neg \text{Student}(x) \vee \text{Study}(x) \vee \neg \text{pass}(x)$
5. $\neg (\neg \text{play}(x)) \vee \neg \text{footballStar}(x)$
 $\text{play}(x) \vee \neg \text{footballStar}(x)$

Resolution Proof

Broke: $\neg \text{Loves}(\text{mary}, \text{John})$



LectureArtificial Intelligence
INT-404

1. Anyone who rides a Harley is a rough character.
2. Every biker rides either Harley or bmw.
3. Anyone who rides a BMW is a yuppie.
4. Every yuppie is a Lawyer.
5. Mary is a nice girl and John is a biker.
6. Prove : If John is not a Lawyer then Mary does not date John.

Predicate Logic x, Harley

1. $\forall x : \text{rides}(\text{Harley}) \rightarrow \text{rough character}(x)$
2. $\forall x : \text{biker}(x) \rightarrow \text{rides}(x, \text{Harley}) \vee \text{rides}(x, \text{BMW})$
3. $\forall x : \text{rides}(\text{BMW}, x) \rightarrow \text{yuppie}(x)$.
4. $\forall x : \text{yuppie}(x) \rightarrow \text{Lawyer}(x)$
5. Any nice girl does not date anyone who is a rough character.
 $\forall x \forall y : \text{Nice girl}(x) \wedge \neg \text{date}(x, y) \rightarrow \text{RC}(y)$
OR
 $\forall x \forall y : \text{Nice girl}(x) \wedge \text{RC}(y) \rightarrow \neg \text{date}(x, y)$
6. $\text{Nice girl}(\text{Mary}) \wedge \text{biker}(\text{John})$
7. $\neg \text{Lawyer}(\text{John}) \rightarrow \neg \text{date}(\text{Mary}, \text{John})$

CNF Conversion

- $\neg \text{rides}(x, \text{harley}) \vee \text{rough_character}(x)$.
- $\neg \text{biker}(x_2) \vee \text{rides}(x_2, \text{harley}) \vee \text{rides}(x_2, \text{BMW})$
- $\neg \text{rides}(x_3, \text{BMW}) \vee \text{yuppie}(x_3)$.
- $\neg \text{yuppie}(x_4) \vee \text{Lawyer}(x_4)$.
- $\neg (\text{NC}(x_5) \wedge \text{RC}(y_1)) \vee \neg \text{date}(x_5, y_1)$

- $\neg \text{NC}(x_5) \vee \neg \text{RC}(y_1) \vee \neg \text{date}(x_5, y_1)$

- 6. $\text{Nice_girl}(\text{Mary}) \wedge \text{biker}(\text{John})$
- 7. $\neg (\neg \text{Lawyer}(\text{John})) \cancel{\vee} \neg \text{date}(\text{Mary}, \text{John})$
 $\text{Lawyer}(\text{John}) \cancel{\vee} \neg \text{date}(\text{Mary}, \text{John})$

Resolution Proof by forward Reasoning

- $\neg \text{NC}(\text{Mary}) \vee \neg \text{RC}(\text{John}) \vee \neg \text{date}(\text{Mary}, \text{John}) \quad (6)$
- ② $\neg \text{RC}(\text{John}) \vee \neg \text{date}(\text{Mary}, \text{John}) \wedge \text{biker}(\text{John})$

- $\neg \text{RC}(\text{John}) \vee \neg \text{date}(\text{Mary}, \text{John}) \vee \text{rides}(\text{John}, \text{harley})$
 $\vee \text{rides}(\text{John}, \text{BMW})$

- $\neg \text{RC}(\text{John}) \neg \text{date}(\text{M}, \text{J}) \vee \text{rides}$

chapter - 6

★ Representing Knowledge For Rules :-

→ Procedural V/S Declarative knowledge

Declarative knowledge is one in which knowledge is specified but the use to which that knowledge is to be put in, is not given.

Procedural knowledge is one in which the control information that is necessary to use the knowledge is considered to be embedded in the knowledge itself.

Declarative knowledge is defined as the factual information stored in memory and known to be static in nature.

Procedural is the knowledge of how to perform or how to operate.

→ Logic programming

is a programming language para

Artificial Intelligence
INT - 404

1. John likes all kinds of food.
2. Apples are food.
3. Chicken is food.
4. Anything anyone eats and is not killed by food.
5. Bill eats peanuts and is still alive.
6. Sue eats everything Bill eats.

Prove : John likes peanuts. Likes (John, Peanuts)

Predicate Logic

1. $\forall x : \text{food}(x) \rightarrow \text{Likes}(\text{John}, x)$
2. $\text{food}(\text{apple})$
3. $\text{food}(\text{chicken})$
4. $\forall x \forall y : \text{eats}(x, y) \wedge \neg \text{killed by } y \rightarrow \text{food}(y)$
5. $\text{eats}(\text{Bill}, \text{peanuts}) \wedge \text{alive}(\text{Bill})$
6. $\forall x : \text{eats}(\text{Bill}, x) \rightarrow \text{eats}(\text{Sue}, x)$

CNF Conversion

1. $\neg \text{food}(x) \vee \text{Likes}(\text{John}, x)$
2. $\neg \text{food}(\text{apple})$
3. $\text{food}(\text{chicken})$
4. $\neg [\text{eats}(x, y) \wedge \neg \text{killed}(x) \rightarrow \text{food}(y)]$
5. $\neg \text{eats}(x, y) \vee \text{killed}(x) \vee \text{food}(y)$
 $\quad \quad \quad \neg \text{not.alive}(x)$
6. $\neg \text{eats}(\text{Bill}, x) \vee \text{eats}(\text{Sue}, x)$

Resolution Proof

(1)

 $\neg \text{Likes}(\text{John}, \text{Peanuts})$
 $\cancel{x / \text{Peanuts}}$
 $\neg \text{food}(\text{Peanuts})$

(4)

 $\cancel{y / \text{Peanuts}}$

(5a)

 $\neg \text{eats}(x, \text{Peanuts}) \vee \text{killed}(x)$ Will backtrack
 $\neg \text{eats}(x, \text{Peanuts}) \vee \neg \text{not.alive}(x)$
 $\cancel{x / \text{Bill}}$
 $\neg \text{not.alive}(x)$

5(b)

 $\cancel{x / \text{Bill}}$

Null

1. Every child loves Santa.
2. Every who loves Santa loves Reindeer.
3. Randolph is a reindeer and Randolph has a red nose.
4. Anything which has a Red nose is weird or clown.
5. No Reindeer is a clown.
6. Scrooge does not love anything which is weird.

Prove: Scrooge is not a child.

1. $\forall x : \text{child}(x) \rightarrow \text{Loves}(x, \text{Santa})$
2. $\forall x : \text{Loves}(x, \text{Santa}) \rightarrow \forall y : \text{Reindeer}(y) \wedge \text{Loves}(x, y)$
3. ~~Reindeer(Randolph) \wedge has(Randolph, red nose)~~
4. ~~$\forall x : \text{Reindeer}(x) \rightarrow \text{weird}(x) \wedge \text{clown}(x)$~~
5. $\neg \exists x : \text{Reindeer}(x) \wedge \text{clown}(x)$
6. $\forall x : \neg \text{Loves}(\text{Scrooge}, x) \rightarrow \text{weird}(x)$
7. $\neg \text{Reindeer}(\text{Randolph}) \wedge \text{Reindeer}(\text{Red Nose})$
 $3(a)$ $3(b)$

1. $\neg \text{child}(x) \vee \text{Loves}(x, \text{Santa})$
2. $\neg \text{Loves}(x, \text{Santa}) \vee \text{Reindeer}(y) \wedge \text{Loves}(x, y)$
3. (a) $\text{Reindeer}(\text{Randolph})$
 (b) $\text{Reindeer}(\text{Red Nose})$
4. $\neg \text{Reindeer}(x) \rightarrow \text{weird}(x) \vee \text{clown}(x)$
5. $\forall x : \neg [\text{Reindeer}(x) \wedge \text{clown}(x)]$
 $\neg \text{Reindeer}(x) \vee \neg \text{clown}(x)$
6. $\forall x : \text{weird}(x) \rightarrow \neg \text{Love}(\text{Scrooge}, x)$
 $\neg \text{weird}(x) \vee \neg \text{Love}(\text{Scrooge}, x)$

Resolution Proof

① child (Scrooge)

✓ x/Scrooge

② loves (Scrooge, Santa)

36) ✓ ~Reindeer (y) ∨ Love (Scrooge, y)

Love (Scrooge,

Lecture

* Factors to decide whether to use Backward
or forward Reasoning :-

i. Are there more possible start states or goal
state? We ~~would~~ like to go from Smaller
Set of states to larger Set of states.

ii. In which direction is the branching factor
(the average number of nodes that can be
reached directly from a single node) greater?
We would like to proceed in the direction
with the lower

Contd...

* MATCHING :

1. Indexing :

Do a simple search through all the rules, comparing each one's precondition to the current state and extracting all the ones that match.

But this has two problems

→ In order to solve any

2. Matching with Variables :

The problem of selecting applicable rules is made more difficult when preconditions are not stated as exact descriptions of particular situations but

3. Complex and Approximate Matching :

An even more complex matching process is required if rules should be

4. Conflict Resolution :

- 1. Preferences based on rules that match.
- 2. Preferences based on objects that match.
- 3. Preferences based on actions that match.

5-03-18

→ UNIT - 1

chapter - 1

- AI
- Applications of AI.
- 4 Algos of Tic - Tac - Toe.

chapter - 2

- | | | |
|-----------------|---|--|
| Imp. | Problem characteristics | Control Strategies |
| | <ul style="list-style-type: none"> • Production System • State Space • State Space Search • Additional Problems | <ul style="list-style-type: none"> • Control Strategies |

→ UNIT - 2

Control Strategies

- BFS
- DFS
- Bidirectional Search

chapter - 3

- Heuristics
- Generate and Test
- Hill climbing Algos
- (i) Simple hill climbing
- (ii) Steepest Ascent HC

(iii) Simulated Annealing

- Best First Search

(i) OR- Algo

(ii) A* Algo

- Problem Reduction

(i) AND-OR Algo

(ii) AO*

- Constraint Satisfaction

- Bryparithmetic

→ UNIT - 3

chapter - 4

- Approaches to knowledge Representation

- Issues

- Properties of knowledge Representation

chapter - 5

- Diff. b/w Propositional Logic & Predicate Logic

Imp. • Resolution

(i) Predicate Conversion

(ii) CNF

(iii) Resolution

chapter - 6

- Procedural vs declarative knowledge

- Forward & Backward Reasoning

- Matching

- Conflict Resolution

3-03-18

Artificial Intelligence

INT - 404

* Symbolic Reasoning under uncertainty :-

explore techniques for solving problems with incomplete and uncertain models.

→ The ABC Murder Mystery

→ Non-monotonic Reasoning :-

in which the axioms and/or the rules of inference are extended to make it possible to reason with incomplete information.

→ Statistical Reasoning :-

in which representation is extended to allow some kind of numeric measure of certainty (other than true or false) to be associated with each statement.

→ Default Reasoning :-

- We use non-monotonic reasoning to perform,
- what is commonly called Default Reasoning.

• Two approaches are :

1. Non-monotonic Logic

2. Default Logic

• Two common kinds of Non-monotonic reasoning

that can be defined by these logics :-

1. Abduction

2. Inheritance

* Non-Monotonic Logic :-

→ It is one in which the language of FOL is augmented with a modal operator M, which can be read as "is consistent".

→ ~~$\forall x, y : \text{Related}(x, y) \wedge M \text{Getalong}(x, y) \rightarrow \text{WillDefend}(x, y)$~~

→ for all x and y, if x and y are related and if the fact that x gets along with y is consistent with everything else that is believed, then conclude that x will defend y.

* Default Logic :-

A : B

C

Tutorial

5-18

Artificial Intelligence
INT-404

C₄ C₃ C₂ C₁

1. B A S E

+ B A L L

—————
G A M E S

Assume C₁, C₂, C₃ and C₄ as carry

$$G = 1$$

$$A = \text{[redacted]} 4$$

$$A = 4$$

$$C_3 + B + B \neq A$$

$$B = 7$$

$$C_3 + 7 + 7 = 8$$

↙ ↘

$$1 \quad 0$$

$$C_2 + A + A = M$$

$$C_2 + 4 + 4 = M$$

$$C_2 + 8 = M$$

↙ ↘

$$1 \text{ or } 0$$

$$M = 8$$

or

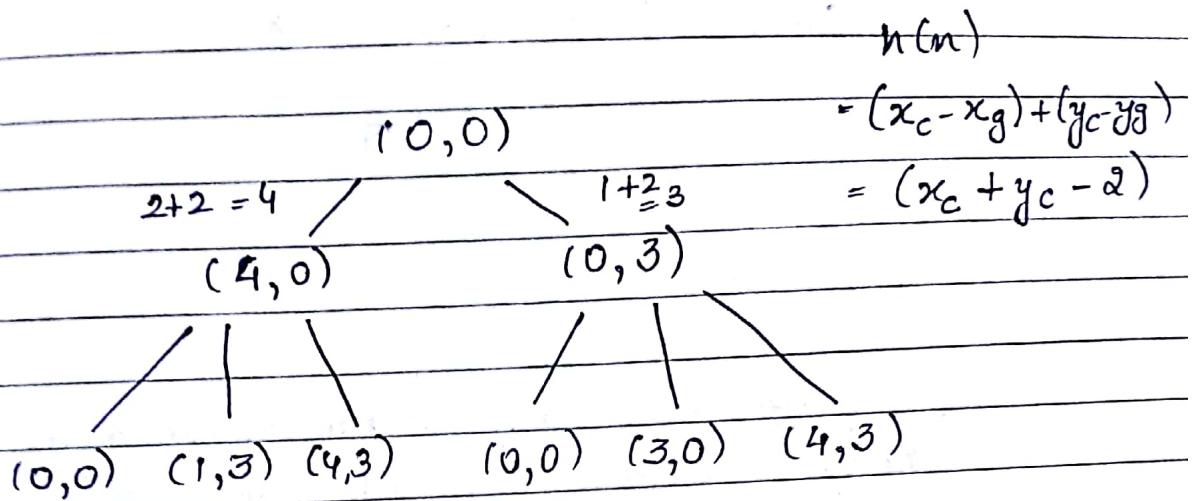
$$M = 9$$

$$S = 8$$

$$L = 5$$

$$E = 3$$

2. Water Jug Problem using A* Algorithm. choose any heuristic, any initial state, Goal state but consider the cost as 2 at every node.



3. Convert to PROLOG

$\forall x : \text{pet}(x) \wedge \text{Small}(x) \rightarrow \text{apartment}(x)$

$\text{apartment}(x) :- \text{pet}(x), \text{Small}(x)$

$\forall x : \text{Cat}(x) \vee \text{dog}(x) \rightarrow \text{pet}(x)$

$\text{pet}(x) :- \text{Cat}(x)$

$\text{pet}(x) :- \text{dog}(x)$

Rules

1. Variables are written with Capital Letter.

2. ' \wedge ' in if is converted to ','

3. ' \vee ' in if is converted to 2 parts.

4. ' \vee ', ' \wedge ' in then part \rightarrow Separate rules.

$\forall x : \text{poodle}(x) \rightarrow \text{dog}(x) \wedge \text{small}(x)$

$\text{dog}(x) :- \text{poodle}(x)$

$\text{small}(x) :- \text{poodle}(x)$

Lecture

→ Default Logic :-

for performing default based reasoning is
Reiter's Default Logic (DL) in which a new
class of inference rules is introduced. In this
approach,

$$\frac{A : B}{C}$$

→ Abduction :-

Standard logic performs deduction. Give 2
axioms.

→ $\forall x : A(x) \rightarrow B(x)$

→ $A(C)$

→ We conclude $B(C)$ using deduction.

→ $\forall x : \text{Mongrel}(x) \rightarrow \text{Spots}(x)$

9-03-18

Artificial Intelligence.

* Inheritance in Default Logic :-

Inheritance says that "An object inherits attributes values from all the classes which it is member unless doing so leads to contradiction, in which case a value from a more restricted class has precedence over a value from a broader class."

* Minimalist Reasoning :-

Two kinds of minimalist reasoning :

1. closed World Assumption (CWA)
2. Circumscription.

1. Closed World Assumption (CWA) :

This type of assumption is useful in application where most of the facts are true and it is, therefore, reasonable to assume that if a proposition cannot be proven, it is false.

2. Circumscription :

Two advantages over CWA :

- operates on whole formulas, not individual predicates.

- Allows some predicates to be marked as closed and others as open.
- It is not feasible to write all the exceptions.

→ AB Predicates

$\text{Adultmale}(x) : \neg \text{BaseballP}(x) \wedge \neg \text{Midget}(x) \wedge \neg \text{Jockey}(x) \wedge \text{height}(x, 5-10)$

$\text{height}(x, 5-10)$

$\forall x : \text{Adultmale}(x) \wedge \neg \text{AB}(x, \text{aspect}) \rightarrow \text{height}(x, 5-10)$

$\forall x : \text{Baseball player}(x) \rightarrow \text{AB}(x, \text{aspect 1})$

$\forall x : \text{Midget}(x) \rightarrow \text{AB}(x, \text{aspect 1})$

$\forall x : \text{Jockey}(x) \rightarrow \text{AB}(x, \text{aspect 1})$

★ Augmented Problem Solver :-

(Backward Rules Using UNLESS)

→ Implementation Issues :-

i. How to find out only those rules from non monotonic reasoning which are actually useful.

ii. How to update our knowledge base while solving our problem.

There can be possibility where we can draw different inference from same rule.

This is not computationally effective / or is difficult.

We will be solving the issues in 2 steps:-

1. Actual Problem Solver.

2. TMS → Truth Maintenance System.

→ require to do away with (2) issue

→ will help us to eliminate the 2nd issue.

Solutions

→ The Computational System to these problems are Separated into two parts :

1. Problem Solver that uses whatever mechanism it happens to draw Conclusion as necessary.

2. TMS whose Job is to do the book keeping required to provide a Solution to our 2nd problem.

Two mechanism of Problem Solving

1. Backward Reasoning
2. Forward Reasoning

1. Problem Solver.

Suspect (x) \leftarrow Beneficiary (x)
UNLESS Alibi (x)

Alibi (x) \leftarrow Somewhere Else (x)

Somewhere Else (x) \leftarrow Registered Hotel (x, y) and
FarAway (y)
UNLESS Forged Register (y)

Alibi (x) \leftarrow Defends (x, y)

UNLESS Lies (y)

Somewhere Else (x) \leftarrow PictureOf (x, y) and
Faraway (y)

Contradiction () \leftarrow TRUE

UNLESS $\exists x : \text{Suspect} (x)$

3-19

Artificial Intelligence

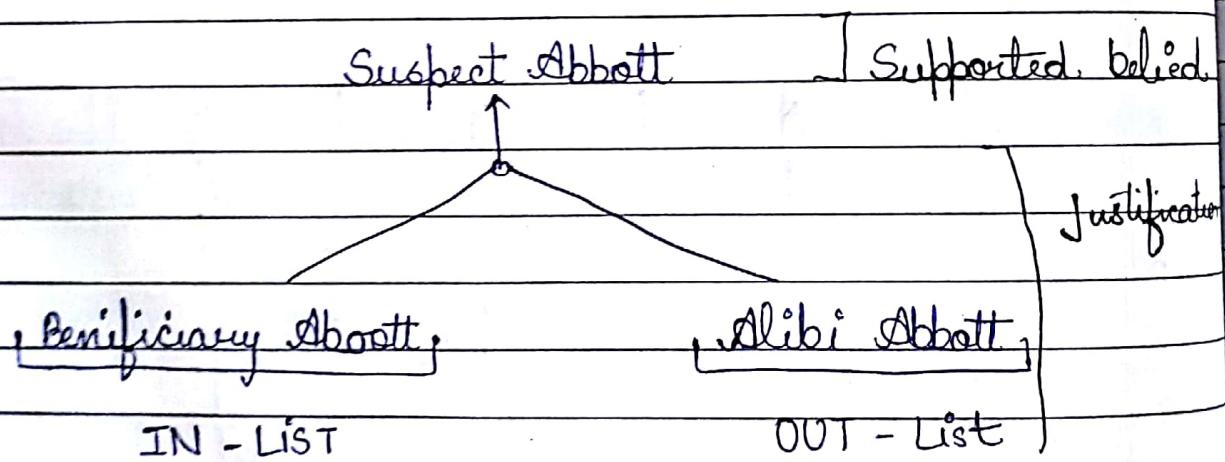
INT - 404

* ABC Murder Mystery :-

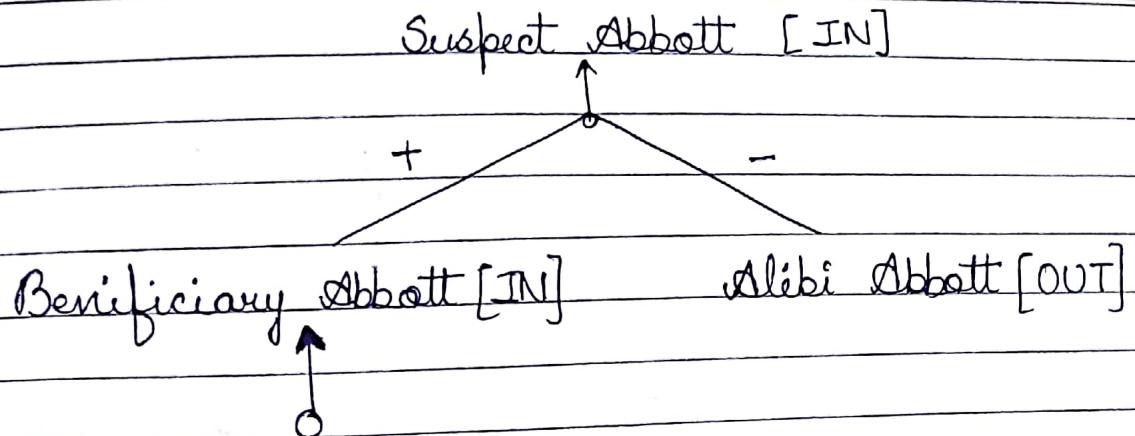
Various techniques for TMS

1. JTMS (Justification Based TMS)
2. ATMS (Assumption Based TMS)
- 3.

1. JTMS (Justification based TMS)

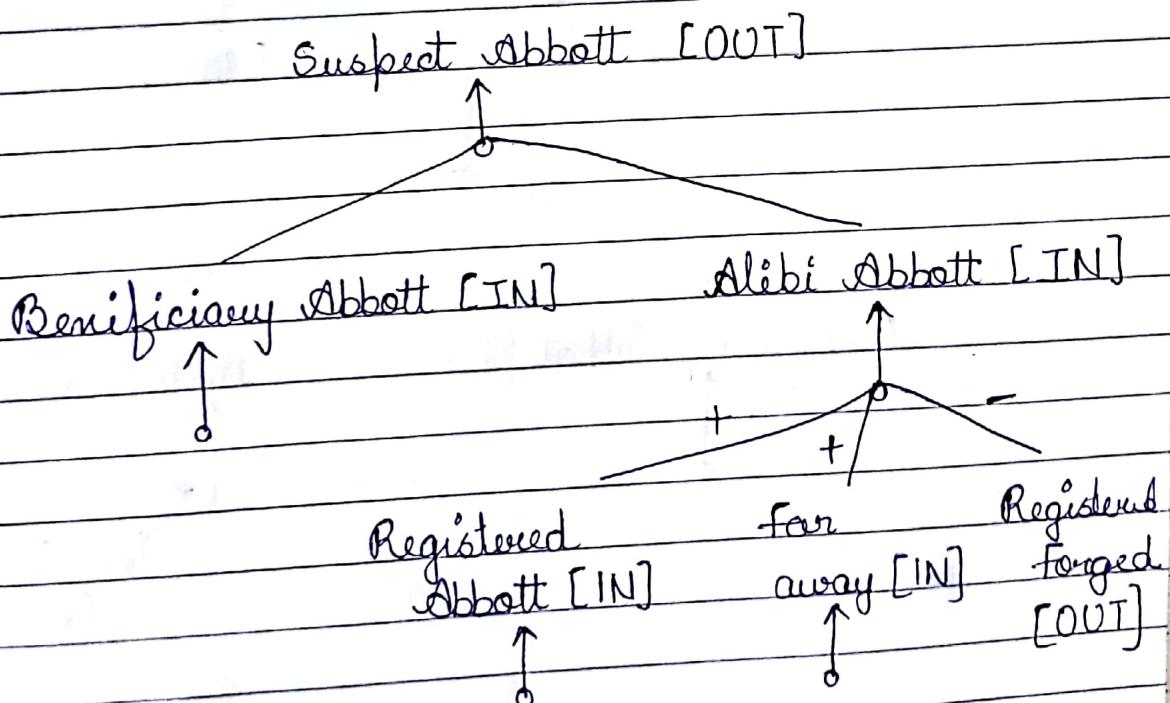


- A justification is Valid if every assertion in the IN-list is believed and none of those in the OUT-list is.
- A justification is Non-monotonic if its OUT-list is not empty, or, recursive, if any assertion in its IN-list has a Non-monotonic justification.

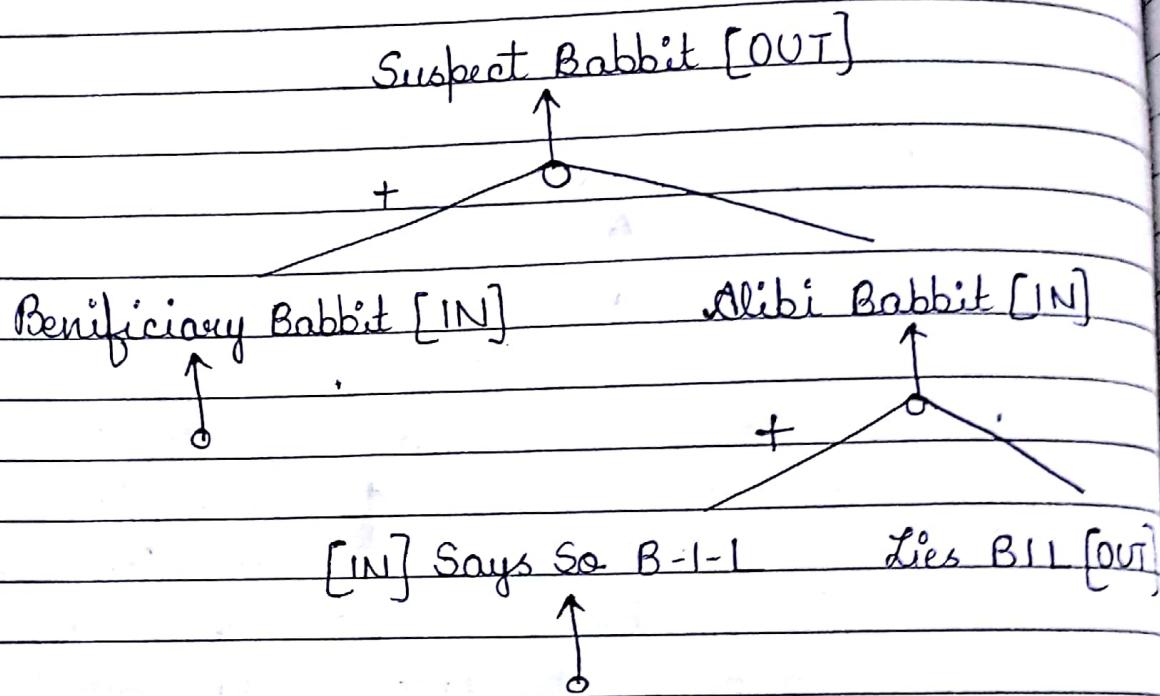


We are told that Abbott is a Beneficiary.
 We have no further justification for this fact
 So we must simply except it. For such facts
 we give a premise justification i.e. a
 justification with empty IN and OUT list.

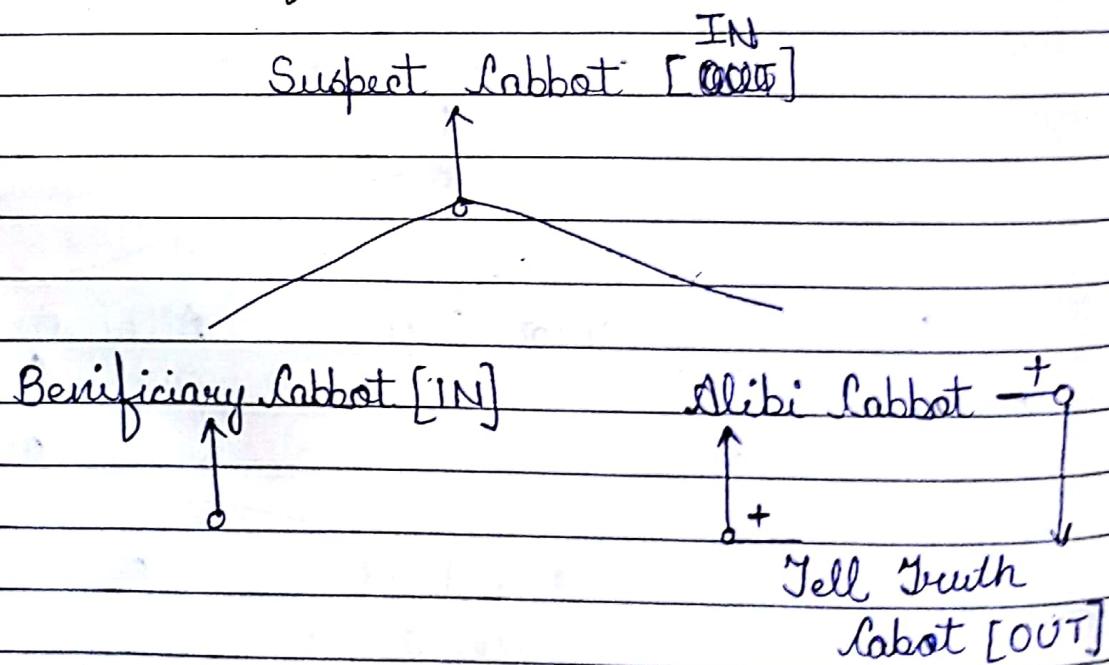
changed Labeling



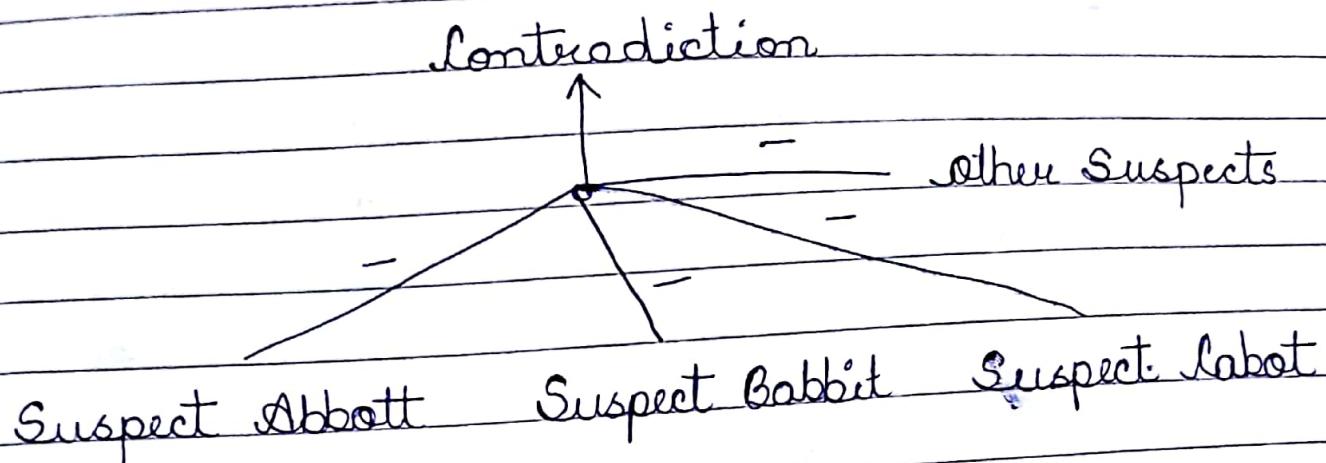
Babbit's Justification



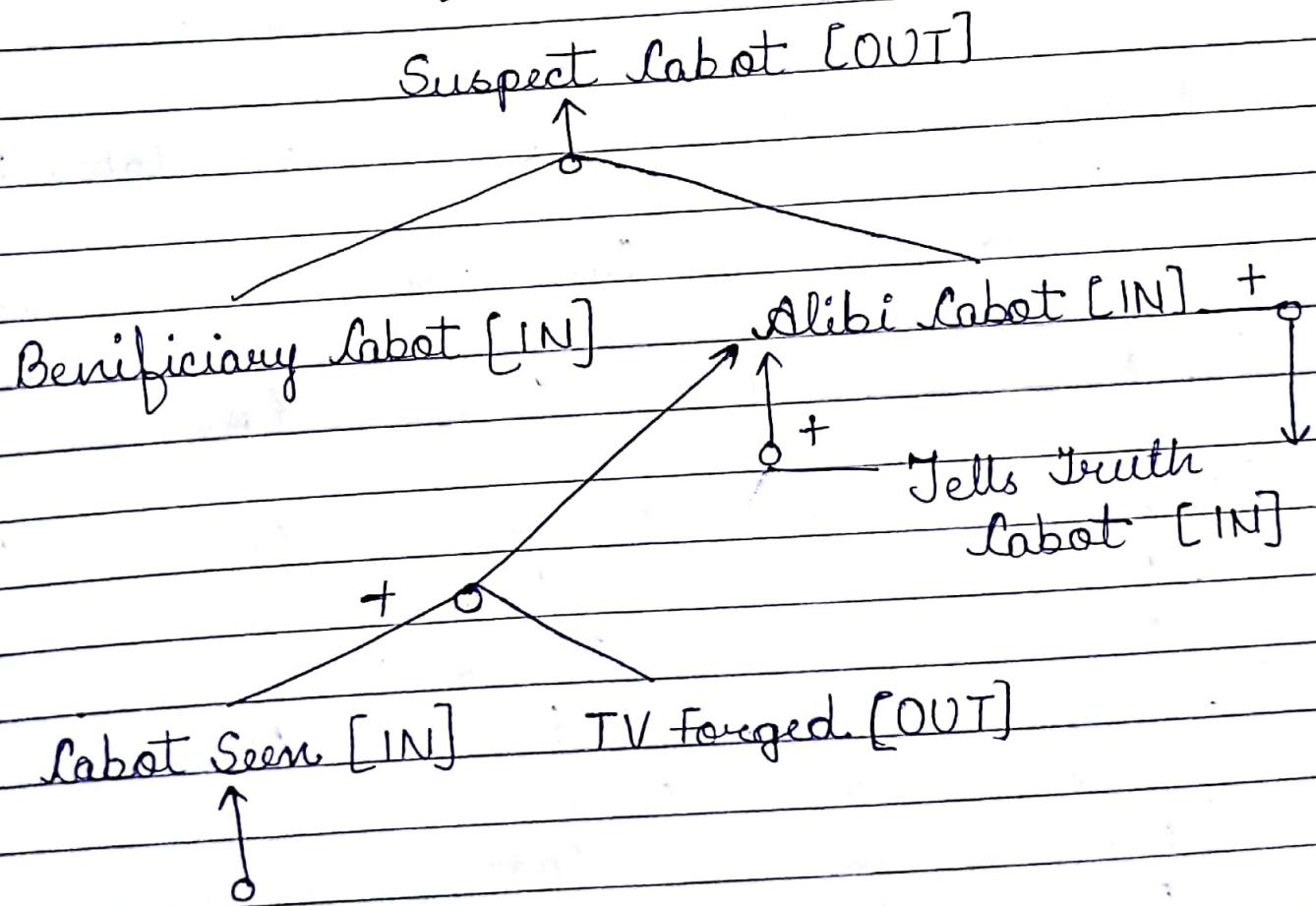
Cabbit's Justification



A Contradiction



A Second Justification



Lecture* ATMS (Assumption based TMS) :-

- A1 : Hotel register was forged
- A2 Hotel register was not forged
- A3 Babbit's brother - in - Law Lied.
- A4 Babbit's brother - in - Law did not Lie.
- A5 Cabot Lied.
- A6 Cabot did not Lie.
- A7 Abbott, Babbitt, Cabot are only Suspects.
- A8 Abbott, Babbitt, Cabot are not only Suspects.

* Nodes and their Justifications and Labels :-

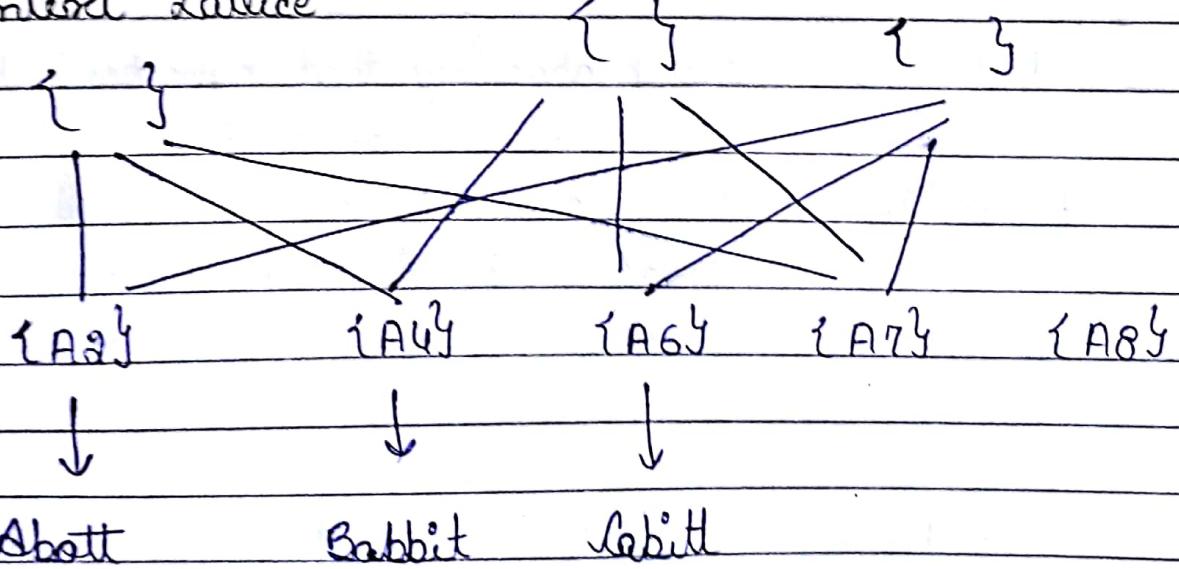
Nodes	Justifications	Labels
[1] Register was not forged.	{A2}	{A2}
[2] Abbott at Hotel	[1] → [2]	{A2}
[3] BIL didn't Lie	{4}	{A4}
[4] Babbit at BIL	[3] → [4]	{A4}
[5] Cabot didn't Lie	{6}	{A6}
[6] Cabot at Show	[5] → [6]	{A6}
[7] A, B, C. only Susp.	{A7}	{A7}
[8] Prime Susp A	[7] ∧ [13] ∧ [14] → [8]	{A7, A4, A6}
[9] Prime Sp. B	[7] ∧ [12] ∧ [14] → [9]	{A7, A2, A6}
[10] Prime Susp. C	[7] ∧ [19] ∧ [13] → [10]	{A7, A2, A4}
[110] A, B, C. not Sup.	{A8}	{A8}

[13]	Net prime Susp. A	$[2] \rightarrow [12]$	$\{A_2\}$	$\{A_2\} \{A_8\}$
		$[11] \rightarrow [12]$	$\{A_8\}$	
		$[9] \rightarrow [12]$	$\{A_7, A_2, A_6\}$	
		$[10] \rightarrow [12]$	$\{A_7, A_2, A_4\}$	

[13]	Net prime Susp. B	$[4] \rightarrow [13]$	$\{A_4\}$	$\{A_4\} \{A_8\}$
		$[11] \rightarrow [13]$	$\{A_8\}$	
		$[8] \rightarrow [13]$	$\{A_7, A_4, A_6\}$	
		$[10] \rightarrow [13]$	$\{A_7, A_4, A_2\}$	

[14]	Net prime Susp. C	$[6] \rightarrow [14]$	$\{A_6\}$	$\{A_6\} \{A_8\}$
		$[11] \rightarrow [14]$	$\{A_8\}$	
		$[8] \rightarrow [14]$	$\{A_7, A_4, A_6\}$	
		$[9] \rightarrow [14]$	$\{A_7, A_2, A_6\}$	

Context Lattice



26-03-18

chapter - 8
Artificial Intelligence
INT-404

* Statistical Reasoning :-

→ Bayes Theorem :-

Probability =

$$P(x) = \frac{\text{No. of favourable outcome}}{\text{Total outcome}}$$

The notion of Conditional probability : $P(H/E)$

Let

$P(H_i/E)$ = the probability that hypothesis H_i is true given evidence E .

$P(E/H_i)$ = the probability that we will observe evidence E that the hypothesis H_i is true.

$$P(H_i/E) = \frac{P(E/H_i) \cdot P(H_i)}{\sum P(H_i) \cdot P(E/H_i)}$$

Car, Bus, Train

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Ex:

$$P(C) = \frac{1}{3}$$

$$P(L/C) = 0.5$$

$$P(B) = \frac{1}{3}$$

$$P(L/B) = 0.2$$

$$P(T) = \frac{1}{3}$$

$$P(L/T) = 0.01$$

$$P(C/L) = P(C) \cdot P(L/C)$$

$$\frac{P(C)}{P(C) \cdot P(L/C) + P(B) \cdot P(L/B) + P(T) \cdot P(L/T)}$$

$$= \frac{(1/3) \cdot (0.5)}{ }$$

$$\frac{1}{3} \cdot (0.5) + \frac{1}{3} \cdot (0.2) + \frac{1}{3} \times (0.01)$$

$$= \frac{1/3 \times 5/10}{ }$$

$$\frac{1}{3} \times \frac{5}{10} + \frac{1}{3} \times \frac{2}{10} + \frac{1}{3} \times \frac{1}{100}$$

(b) $P(B) = 0$
 $P(T) = 0.9$
 $P(C) = \frac{10}{100} = 0.1$

$$P(L/C) = 0.5$$

 $P(L/B) = 0.2$
 $P(L/T) = 0.01$

→ Adding Certainty factors to Rules :-

Example of Mycin Rule :
→ Expert System.

Ex:

$A_1 \rightarrow$ it will rain

$A_2 \rightarrow$ it will not rain

$$P(A_1) = \frac{5}{365}$$

$$P(A_2) = \frac{360}{365}$$

$B \rightarrow$ Weatherman predicted the rain

$$P(B/A_1) = 90\%$$

$$P(B/A_2) = 10\%$$

$$P(A_1/B) = P(A_1) \cdot P(B/A_1)$$

$$P(A_1) \cdot P(B/A_1) + P(A_2) \cdot P(B/A_2)$$

$$= \left(\frac{5}{365} \times \frac{90}{100} \right)$$

$$\left(\frac{5}{365} \times \frac{90}{100} \right) + \left(\frac{360}{365} \times \frac{10}{100} \right)$$

$$= 0.111$$

Ans.

→ Measures of Belief :-

Uncertainty factor [-1 to +1]

$$1. CF(h, e) = MB(h, e) - MD(h, e)$$

$$2. MB[h, e, \wedge e_2] = MB[h, e_1] + MB[h, e_2] \cdot [1 - MB[h, e_1]]$$

$$MD[h, e, \wedge e_2] = MD[h, e_1] + MD[h, e_2] \cdot [1 - MD[h, e_1]]$$

$$CF(h, e, \wedge e_2) = MB[h, e, \wedge e_2] - MD[h, e, \wedge e_2]$$

$$3. MB[h, \wedge h_2, e] = \min [MB(h_1, e), MB(h_2, e)]$$

$$MD[h, \wedge h_2, e] = \min [MD(h_1, e), MD(h_2, e)]$$

$$4. MB[h, V h_2, e] = \max [MB(h_1, e), MB(h_2, e)]$$

$$MD[h, V h_2, e] = \max [MD(h_1, e), MD(h_2, e)]$$

$h \rightarrow$ hypothesis

$e \rightarrow$ evidence

$MB \rightarrow$ Measure of Belief

$MD \rightarrow$ Measure of Disbelief

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Artificial Intelligence INT-404

Ans. 1 $MB(h, e_1) = 0.3$

$\leqslant MD(h, e_1) = 0$

$CF(h, e_1) = 0.3$

$MB(h, e_2) = 0.2$

$$MB(h, e_1 \wedge e_2) = MB(h, e_1) + MB(h, e_2) [1 - MB(h, e_1)]$$

$$= 0.3 + 0.2 (1 - 0.3)$$

$$= 0.3 + 0.2 \times 0.7$$

$$= 0.3 + 0.14$$

$$= 0.44$$

$$MD(h, e_1 \wedge e_2) = MD(h, e_1) + MD(h, e_2) [1 - MD(h, e_1)]$$

$$= 0 + 0 [1 - 0]$$

$$= 0$$

$$CF(h, e_1 \wedge e_2) = MB(h, e_1 \wedge e_2) - MD(h, e_1 \wedge e_2)$$

$$= 0.44 - 0$$

$$= 0.44 \quad \underline{\text{Ans.}}$$

Ans. 2 $MB(h, e_1) = 0.5$

$\leqslant MB(h, e_2) = 0.2$

$MB(h, e_3) = 0.6$

Find $CF(h, e_1 \wedge e_2 \wedge e_3)$

$$MB(h, e_1 \wedge e_2) = MB(h, e_1) + MB(h, e_2)[1 - MB(h, e_1)]$$

$$= 0.5 + 0.2[1 - 0.5]$$

$$= 0.6$$

$$MB(h, (e_1 \wedge e_2) \wedge e_3) = MB(h, e_1 \wedge e_2) + MB(h, e_3)[1 - MB(h, e_1 \wedge e_2)]$$

$$= 0.6 + 0.6(1 - 0.6)$$

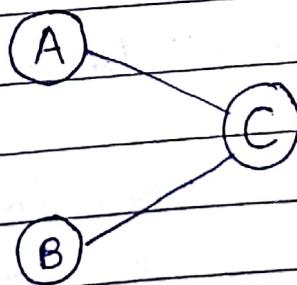
$$= 0.6 + 0.6 \times 0.4$$

$$= 0.6 + 0.24$$

$$= 0.84$$

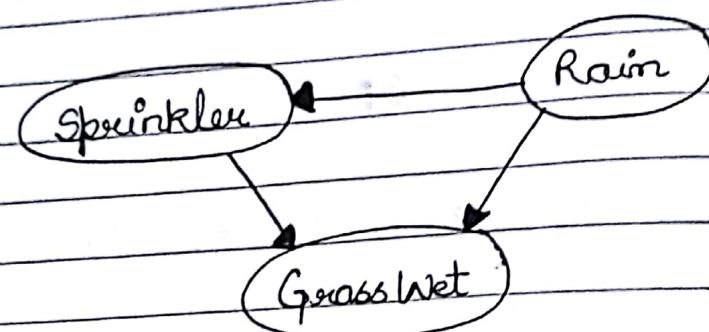
$$CF(h, e_1 \wedge e_2 \wedge e_3) = MB(h, e_1 \wedge e_2 \wedge e_3) - MD(h, e_1 \wedge e_2 \wedge e_3)$$

* Combining Two Pieces of Evidence :-

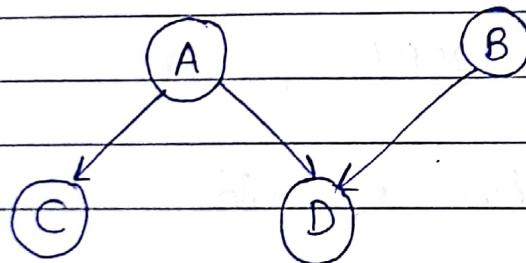


* Bayesian Network :-

Ex:-



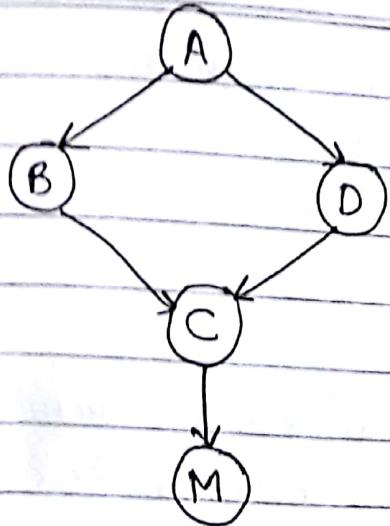
The Bayesian network is an acyclic directed graph where nodes of the graph represent evidence or hypothesis and arc connecting two nodes represents dependence between them.



- If nodes having no parent called unconditional node like A, B.
- If nodes having parent called conditional.
- Node with no children called hypothesis and with children
- Joint Probability for above example:

$$P(G, S, R) = P(G/S, R) * P(R) * P(S/R)$$

Ex:



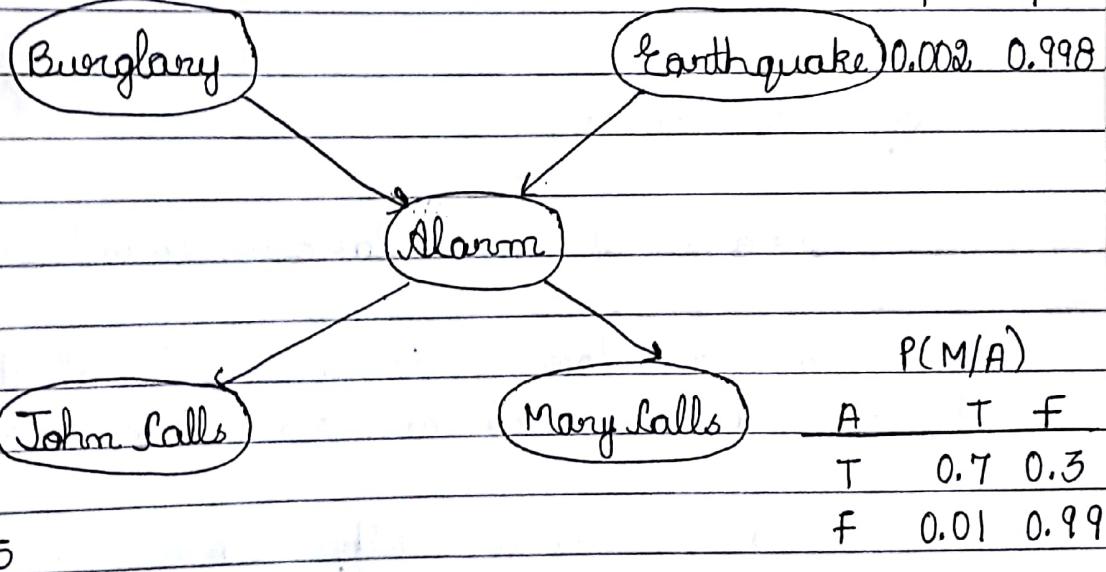
$$P(A, B, C, D, M) = P(A) * P(B|A) * P(D|A) * P(C|B, D)$$

$P(B)$	T	F
0.001	0.999	

$$* P(M|C)$$

T	F

Ex:

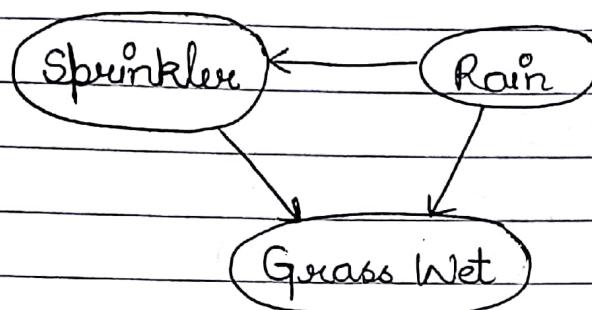


$$P(J, M, A, B, E) = P(J|A) * P(M|A) * P(A|B, E) * P(B) * P(E)$$

$$P(A=T | J=T, M=F, B=T) = \sum_{E=T, F} P(A=T, J=T, M=F, B=T)$$

$$\sum_{(A, E)=T, F} P(J=T, M=F, B=T)$$

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INT-404Ques.
=

		Sprinkler		Rain		
		Rain	T	F	T	F
	T	0.4	0.6			0.2
	F	0.01	0.99			0.8

		Grass Wet			
		Sprinkler	Rain	T	F
	F	F	F	0.0	1.0
	F	F	T	0.8	0.2
	T	F	F	0.9	0.1
	T	T	T	0.99	0.01

I. $P(G, S, R) = P(R) * P(S|R) * P(G|S, R)$

Joint probability
Case 1 : $P(G=T, S=T, R=F)$

$$P(G=T, S=T, R=F) = P(R=F) * P(S=T|R=F) *$$

$$P(G=T | S=T, R=F)$$

$$= 0.8 * 0.4 * 0.9 \\ = 0.288 \quad \underline{\text{Ans.}}$$

Case 2: $P(G = T)$

$$\begin{aligned} & P(G = T, S = T, R = T) \\ & P(G = T, S = T, R = F) \\ & P(G = T, S = F, R = T) \\ & P(G = T, S = F, R = F) \end{aligned}$$

$$\begin{aligned} P(G = T, S = T, R = T) &= P(R = T) * P(S = T | R = T) * P(G = T | S = T, R = T) \\ &= 0.2 * 0.01 * 0.99 \\ &= 0.00198 \end{aligned}$$

$$\begin{aligned} P(G = T, S = F, R = T) &= P(R = T) * P(S = F | R = T) * P(G = T | S = F, R = T) \\ &= 0.2 * 0.99 * 0.8 \\ &= 0.1584 \end{aligned}$$

$$\begin{aligned} P(G = T, S = F, R = F) &= P(R = F) * P(S = F | R = F) * P(G = T | S = F, R = F) \\ &= 0.8 * 0.6 * 0.0 \\ &= 0 \end{aligned}$$

$$P(G = T) = 0.00198 + 0.288 + 0.1584 + 0$$

$$= 0.44838 \quad \underline{\text{Ans.}}$$

II Conditional Probability

$$P(R/G) = \frac{\sum_{S=T,F} P(R, G)}{\sum_{S,R} P(G)}$$

$$= P(G=T, R=T, S=T) + P(G=T, R=T, S=F) \\ P(G=T, R=T, S=T) + P(G=T, R=T, S=F) \\ + (P(G=T, R=F, S=T) + P(G=T, R=F, S=F))$$

$$= 0.00198 + 0.158$$

$$0.00198 + 0.158 + 0.288 + 0$$

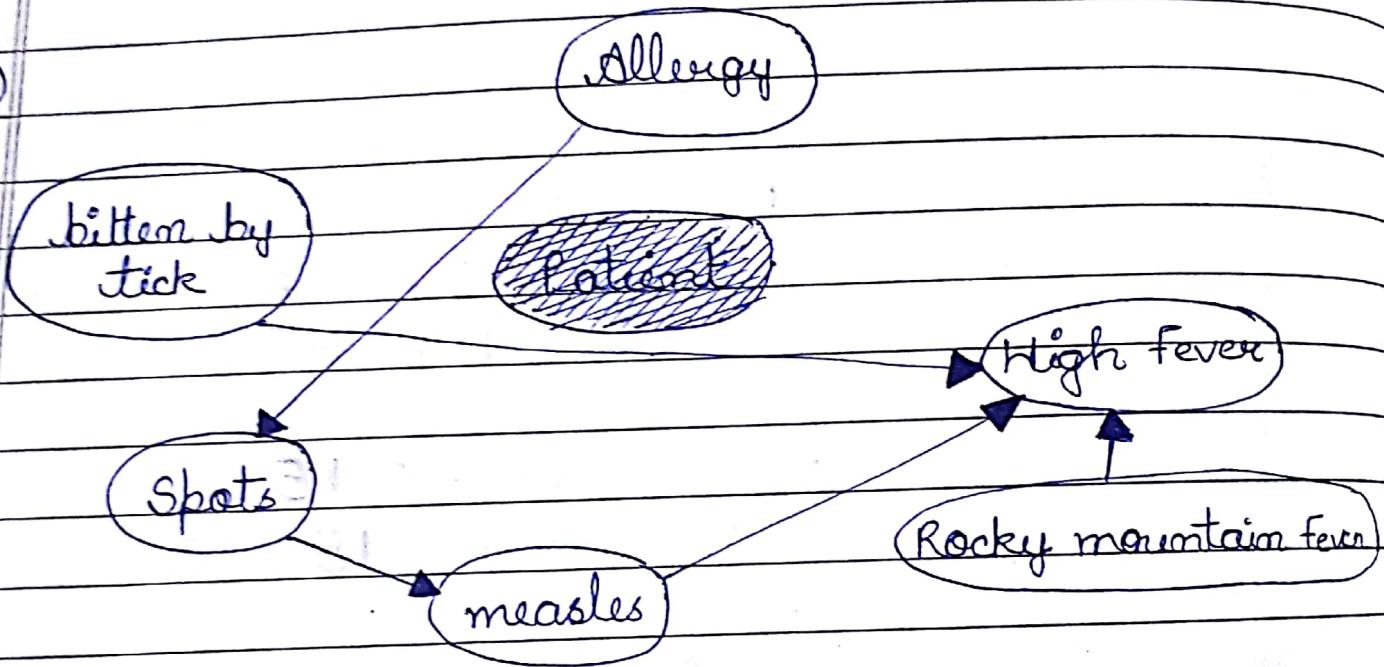
$$= 0.357 \text{ Ans.}$$

Ques 1. Consider the following set :

1. Patient has Spots.
2. Patient has measles.
3. Patient has high Fever.
4. Patient has rocky mountain spotted fever.
5. Patient has previously been detected against measles.
6. Patient was recently bitten by a tick.
7. Patient has an Allergy.

- Ques a) Create a network that defines the causal connections among these nodes.
- Ques b) make it a bayesian network by constructing the necessary Conditional Probability matrix.

(a)



(b)

Ques 2.

= Suppose we have following rule R1 if (P_1 and P_2 and P_3) or (P_4 and not P_5) then

$$C_1 (0.7) \quad C_2 (0.5)$$

$$CF(P_1) = 0.8$$

$$CF(P_2) = 0.7$$

$$(P_3) = 0.6$$

$$(P_4) = 0.9$$

$$(P_5) = -0.5$$

What are the certainty factors associated with conditions C_1 and C_2 after using rule R1.

(P_1 and P_2 and P_3)

$$CF = \min(P_1 \text{ and } P_2 \text{ and } P_3)$$

$$CF = \min(0.8, 0.7, 0.6)$$

$$CF = 0.6$$

(P_4 and P_5)

$$CF = \min(0.9, \neg P_5)$$

$$= \min(0.9, 0.5)$$

$$= 0.5$$

$$CF = 0.6 \text{ or } 0.5$$

$$CF = \max(0.6, 0.5)$$

$$CF(R1) = 0.6$$

$$CF_{C_1} R_1 = 0.6 \times 0.7 = 0.42$$

$$CF_{C_2} R_1 = 0.6 \times 0.5 = 0.3$$

Lecture

* Dempster-Shafer Theory :-

Dempster-Shafer Theory considers the set of propositions and assigns to each of them an interval in which degree of belief must lie.

[Belief, Plausibility]

Belief denoted as Bel measures the strength of the evidence in favour of a set of propositions. It ranges from 0 (no evidence) to 1 (definite certainty).

Plausibility (Pl) is $\text{Pl}(s) = 1 - \text{Bel}(\neg s)$

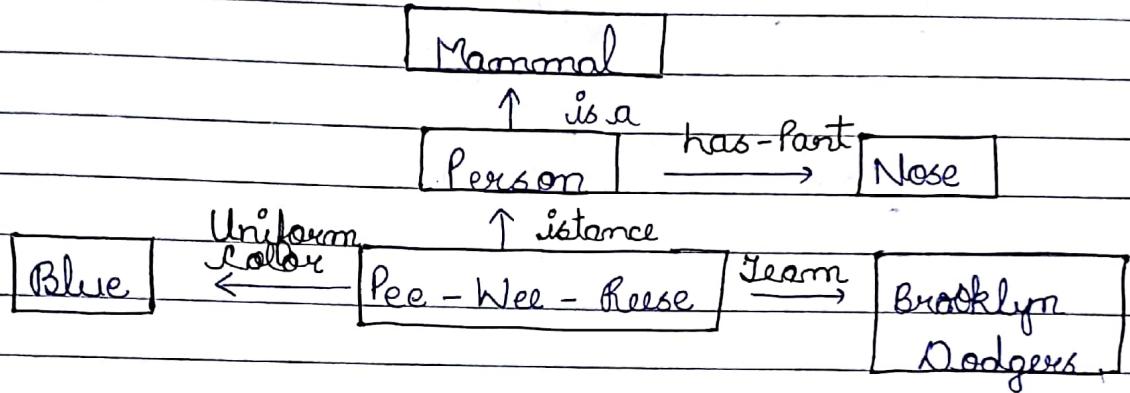
It also ranges from 0 to 1 and measures the extent to which evidence in favour of (not) s , leaves room for belief in s .

9-05-18

Artificial Intelligence

UNIT - 5

* SEMANTIC NETWORKS :-



→ Representing Non-Binary Predicates :-

- Unary Predicates can be rewritten as binary one.

man (Marcus)

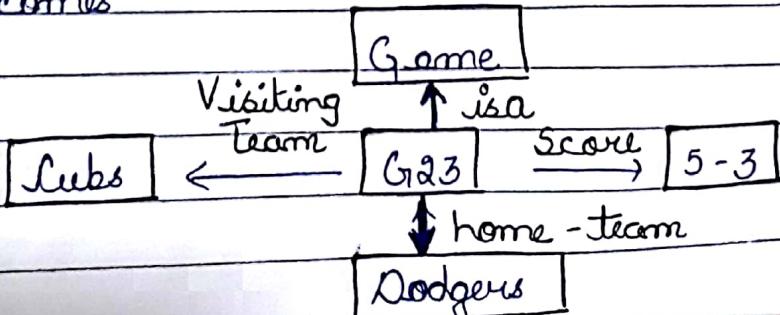
Could be rewritten as

instance (Marcus, Man)

- N-Place Predicates

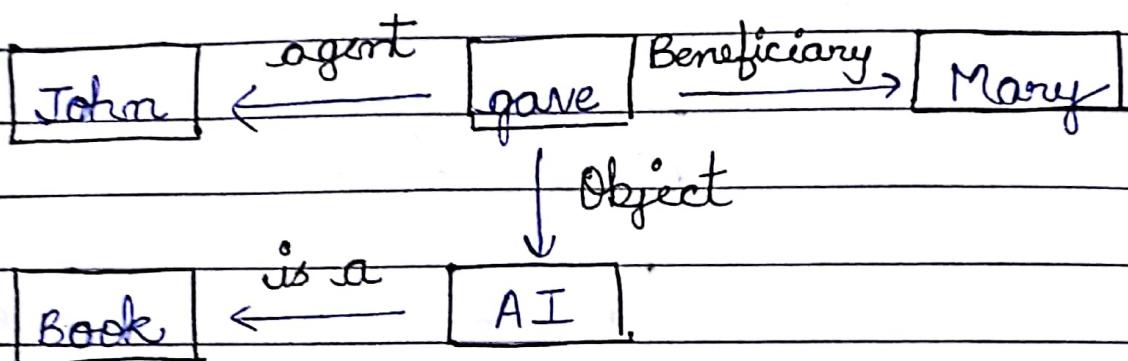
Score (Cubs, Dodgers, 5-3)

becomes



→ A Semantic Net representing a Sentence :-

- John gave the book to Mary.



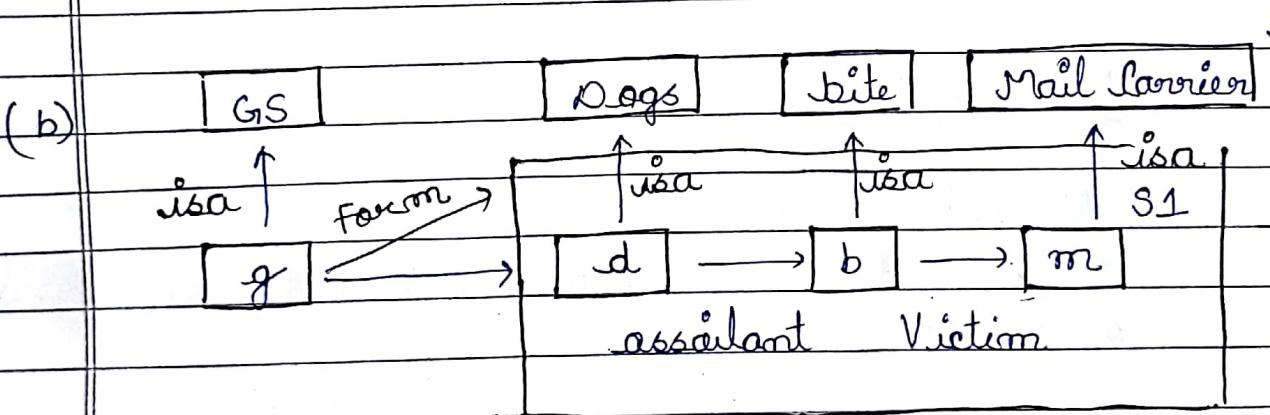
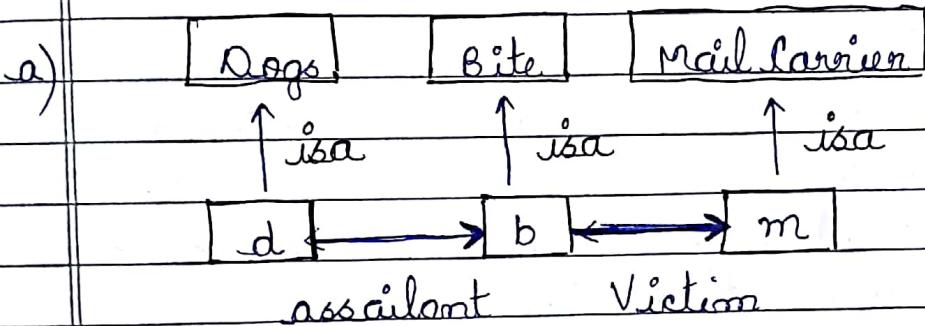
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Artificial Intelligence

* Partitioned Semantic Nets :-

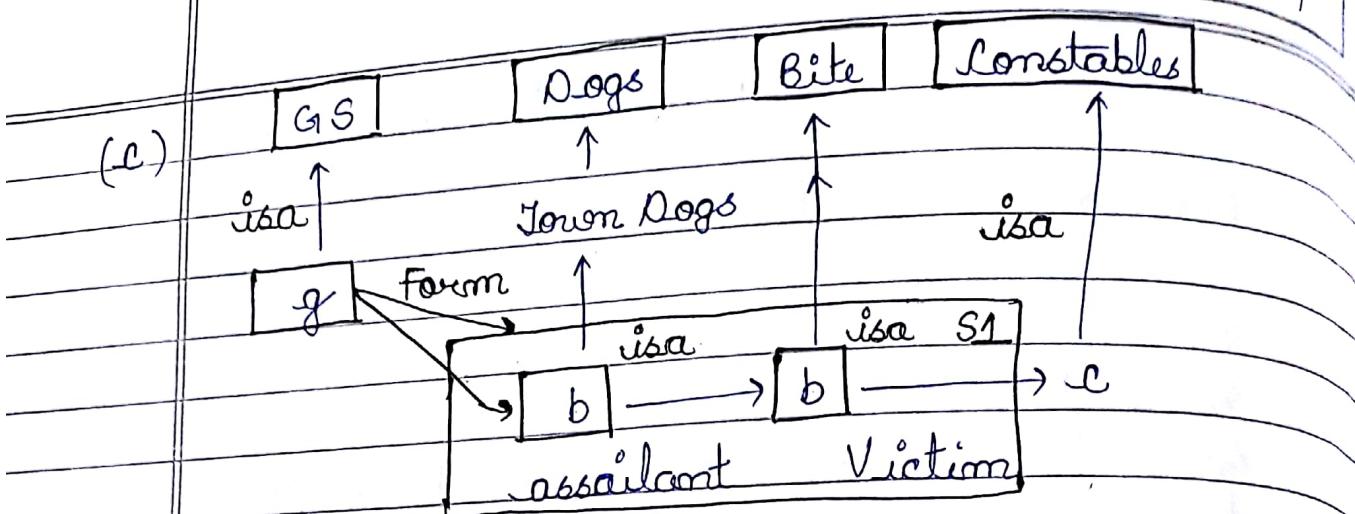
- (a) The dog bit the mail carrier.
- b) Every dog has bitten a mail carrier.
- c) Every dog in town has bitten the constables.
- d) Every dog has bitten every mail carrier.



GA → General Statement.

SA → Space Corresponding to Whole Event.

S1 → Space Corresponding to own event.



* FRAMES :-

- represents an entity as a set of slots and associated values.
- The concept of a frame is defined by a collection of slots. Each slot describes a particular attribute or operation of a frame.

frame System

- Attributes about the set itself.
- * → Attributes that are to be inherited by each element of the set.

Regular class :-

Those classes whose elements are individual entities.

Meta class :-

Those classes whose elements are themselves classes.

Regular class : $\{E_1, E_2, E_3\} \rightarrow$ instance

Meta class : $\{C_1, C_2, C_3\} \rightarrow$ is-a

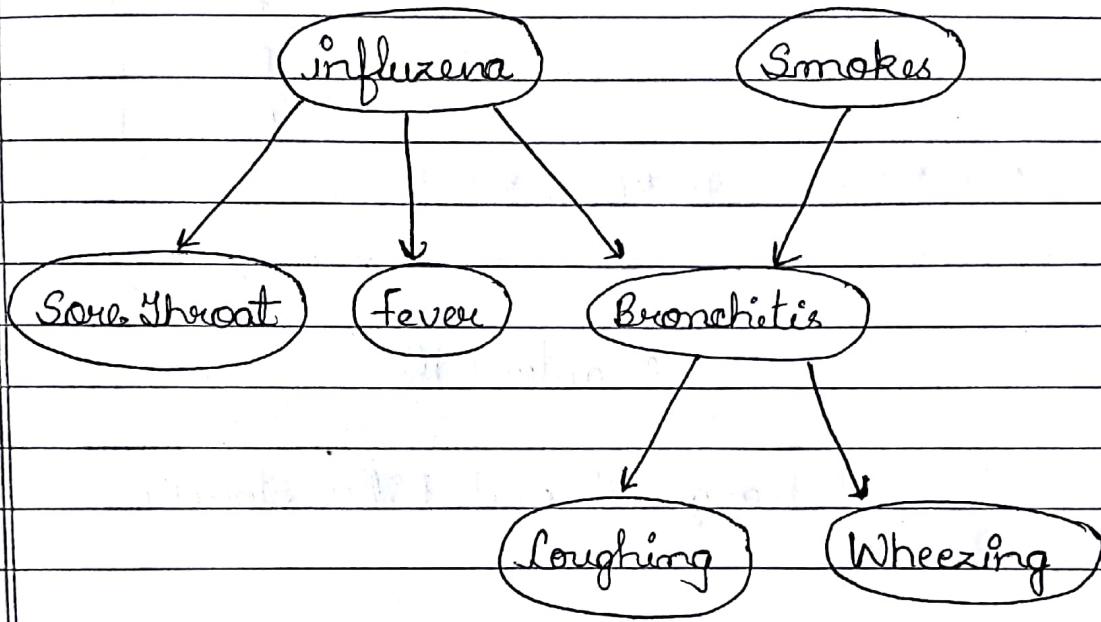
Tangled Hierarchy :-

To support flexible representations of knowledge about the world. It is necessary to allow the hierarchy to be an arbitrary directed acyclic graph. Hierarchies that are not trees are called Tangled Hierarchies.

12-04-18

Artificial Intelligence
INT-404

Ques: Find the Probability of Wheezing, given that influenza is true, fever is true, bronchitis is true, Sore throat is false.



$$\begin{aligned}
 P(W, C, B, S, ST, F, I) &= P(C|B) * P(W|B) * P(B|I, S) \\
 &\quad * P(F|I) * P(ST|I) * \\
 &\quad P(S) * P(I)
 \end{aligned}$$

$$\begin{aligned}
 P(W = T | I = T, F = T, B = T, ST = F) &= \sum_{C, S \in \{T, F\}} P(W = T, I = T, F = T, B = T, ST = F) \\
 &\quad \sum_{(C, S, W) \in \{(T, F)\}} P(I = T, F = T, B = T, ST = F)
 \end{aligned}$$

$$P(St/I) = 0.3, P(\neg St/I) = (1 - 0.3) \\ = 0.7$$

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$$P(I=T, F=T, B=T, St=F, C=T, S=T, W=T)$$

C	S	W
T	T	T
T	T	F
T	F	T
T	F	F
F	T	T
F	T	F
F	F	T
F	F	F

$$= P(C=T/B=T) * P(W=T/B=T)$$

$$* P(B=T/I=T, S=T) *$$

$$P(F=T/I=T) * P(St=F/I=T)$$

$$* P(S=T) * P(I=T)$$

$$= 0.8 * 0.6 * 0.99 * 0.9 * 0.7$$

Chapter = 10

Strong Slot and Filler Structure

Strong Slot & Filler Structure

Conceptual Dependency Script

→ The Probability of getting the answers from Strong Slot (CD and Script) are more as compared to Weak slot & Filler Structure.

* Conceptual Dependency : -

is a theory to represent a kind of knowledge about event that is usually contained in Natural Language Sentence.

A Simple Conceptual Dependency Representation

"I gave the man a book"

CD Primitive Actions

1. ATRANS : Transfer of an abstract relationship
ex: give
2. PTRANS : Transfer of the physical location of object
ex: go
3. PROPEL : Application of physical force to an object
ex: Push
4. MOVE : Movement of a body part by its owner.
ex: Kick
5. GRASP : Grasping of an object by an Actor
ex: clutch
6. INGEST : Ingestion of an object by an animal
ex: eat
7. EXPEL : Expulsion of something from body
ex: cry

8. MTRANS : Transfer of mental information.
Ex: Tell
9. MBUILD : Building new info. out of old.
Ex: Decide
10. SPEAK : Production of Sounds
Ex: Say
11. ATTEND : Focusing of a sense toward a

CD Primitive Conceptual Categories

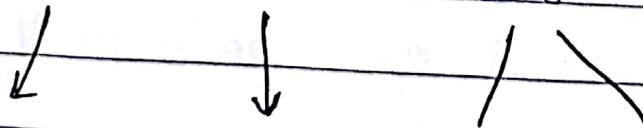
ACTs Actions

PPs Objects (picture producers)

AAs Modifiers of actions (action aiders)

PA s Modifiers of PP s (picture aiders)

Nice John Ran



PA
(telling)
PP
ACTs , AA

Something about
PP.)

The Dependencies of CD

1. \leftrightarrow used to represent the relation b/w Object & Action.

John ran

John \xleftrightarrow{P} PTRANS

2. \longleftrightarrow used to represent is a relation.
i.e b/w class - class
class - instance

John is a doctor

John \longleftrightarrow doctor

3. $\overset{PP}{\uparrow}$ used to represent relation b/w PA and PP.

Nice boy

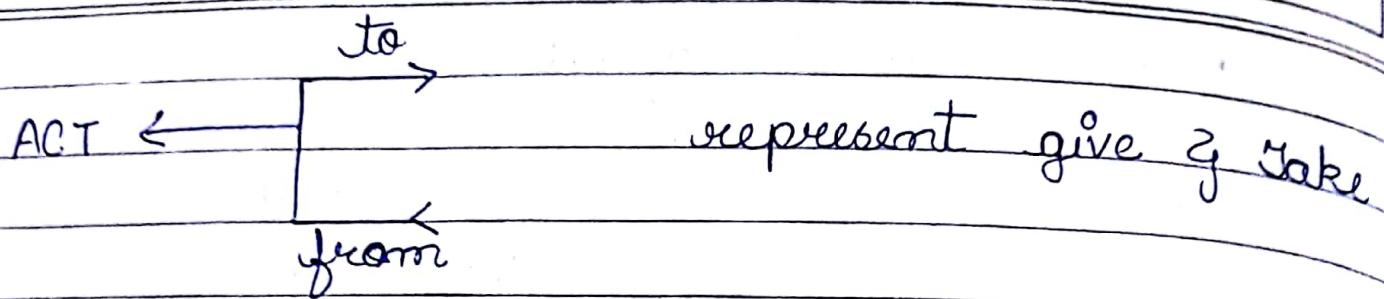
boy
 \uparrow
Nice

4. $\overset{PP}{\uparrow}$ used to represent Some possession

John's Dog

Dog
 \uparrow
John

5.



John took the book
from Mary

ATRANS

John

Mary

CD Dependencies Tense

p

Past

f

Future

t

Transition

ts

Start Transition

tf

Finished transition

K

Continuing

?

Interrogative

/

Negative

nil

Present

delta

Timeless

c

Conditional

The Dependencies of CD :-

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p

1. John man

John \longleftrightarrow PTRANS

2. John is tall

John \longleftrightarrow height ($>$ average)

3. John is a doctor

John \longleftrightarrow Doctor

4. A nice boy

boy
↑
Nice

5. John's Dog

Dog
↑ Poss- by
John

6. John pushed the
Cart.

John \longleftrightarrow PROPEL \leftarrow Cart

7. John took the book
from Mary

John \longleftrightarrow ATRANS \leftarrow John
↑ o \leftarrow Mary
book

8. John ate ice cream
with a spoon

John \longleftrightarrow INGEST \leftarrow John
↑ o \uparrow MOVE
ice cream. \uparrow o
Spoon

* SCRIPT :-

Entry Conditions : Conditions that must, in general, be satisfied before the events described in the Script can occur.

Result conditions : that will, in general, be true after the events described in the Script have occurred.

Props : Slots representing Objects that are involved in the events described in the Script.

Roles : Slots representing people who are involved in the events described in the Script.

Track : The specific variation on a more general pattern that is represented by this particular Script.

Scenes : The actual Sequences of events that occur. The events are represented in conceptual dependency formalism.

Ques. What are Various Components of Script?

→ Entry Conditions, Result Conditions, Props, Track, Scenes.

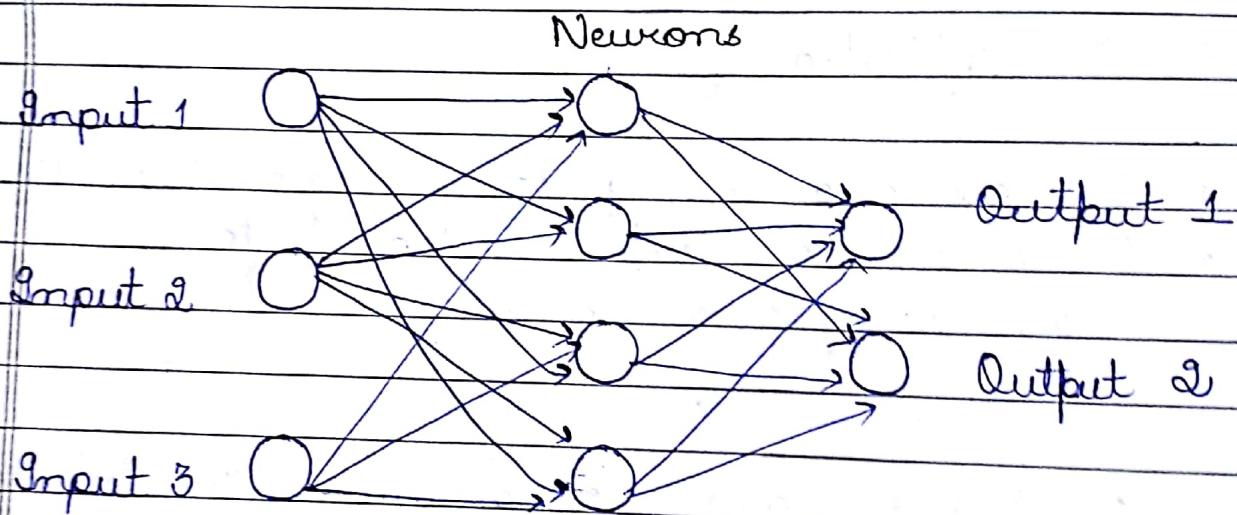
Ques. Construct a Script on Restaurants, Theatre.

CD Primitive Actions

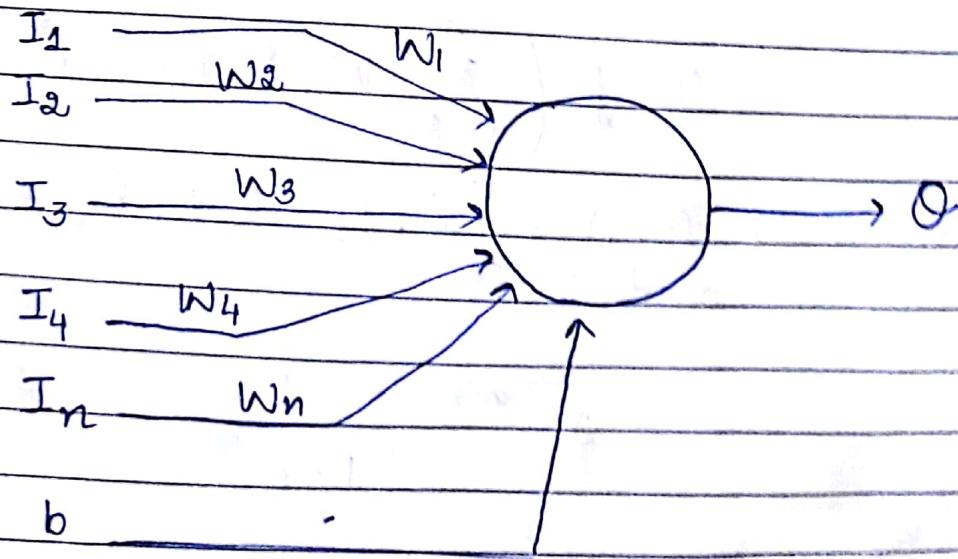
1. ATRANS → Give, Take, Purchase
2. PTRANS → go, walk, fly
3. PROPEL → Push, Pull, Throw
4. MOVE → Kick, Hit, Throw, Punch
5. GRASP → catch, clutch
6. INGEST → eat, drink, Smoke, breathe
7. MTRANS → Yell, Speak, Sing, read, Remember
8. MBUILD → decide, describe, imagine,
Consider, Answer.
9. EXPEL → Weep, Cry, Sweat
10. SPEAK → Say, Yell, Sing
11. ATTEND → Listen, Watch, See, Look

Artificial Intelligence
TNT-404Artificial Neural Network
UNIT - 6★ ANNs - How They Operate :-

→ ANN represent a highly connected networks of neurons - the basic processing unit.



Structure of an Artificial Neuron :-



→ The neuron consists of no. of inputs. The info. is given as inputs via input connections,

→ b = bias O = Output
 w = Weight

→ The Processing of the Neuron :-

$$O = f \left(\sum_{i=1}^n w_i * I_i + b \right)$$

→ The Activation function :-

- The activation fun" performs several imp. tasks.
- One of the most imp. Function is to non-linearity of an equation.

Ques. Calculate the output for a neuron. The inputs are $(0.10, 0.90, 0.05)$ and the corresponding weights are $(2, 5, 2)$. Bias is given to be 1. The activation fun" is Logistic. Also draw the neuron architecture

$$O = f \left(\sum_{i=1}^n w_i * I_i + b \right)$$

where $I_1 = 0.1, w_1 = 2, I_2 = 0.9, w_2 = 5, I_3 = 0.05, w_3 = 2$ and $b = 1$

$$f(x) = \frac{1}{1 - e^{-x}}$$

$$= f(w_1 * I_1 + w_2 * I_2 + w_3 * I_3)$$

$$= f(2 * 0.1 + 5 * 0.9 + 2 * 0.05)$$

$$= f(0.2 + 4.5 + 0.1)$$

$$= 1.008 \quad \underline{\text{Ans.}}$$

* Training :-

Two Techq. for Feeding Training

1. Supervised Learning

In this kind, both the I/P and O/P are well determined and supplied to the training algo.

Hence whenever an I/P is applied, we can calculate the error. We try to adjust the weights in such a way that this error is reduced.

2. Unsupervised Learning

In this type, the target O/P's are unknown. The I/P are applied, and the system is adjusted.

GENETIC ALGORITHM

A genetic algorithm is a search heuristic that is inspired by Charles Darwin's theory of natural evolution. This algorithm reflects the process of natural selection where the fittest individuals are selected for reproduction in order to produce offspring of the next generation.

04-18

Artificial Intelligence

INT - 404

UNIT - 5

Position SN
Script

UNIT - 6

ANN
GA
NLP

Game Playing

→ MIN MAX
→ α, β

* Genetic Algorithm :-

1. Five Phases of Genetic Algorithm

1. Initial Population
 2. Fitness Function → How fit an individual is.
 3. Selection → To Select the fittest individual.
 4. Crossover
 5. Mutation
- Termination

→ Applications of GA :-

1. Clustering
2. ~~Image Processing~~
3. Data Analysis
4. Telecommunication

→ Steps of Genetic Algorithm :-

1. Initialization / Initial Population

The entire range of possible Solution (Search Space) is Selected.

2. Apply the Fitness Function on the Generation and Select two pair of individual based on fitness score.

if (Max fitness > threshold Value)
return Current generation.

3. While (max fitness < threshold)

- a.) Perform Crossover
- b.) Perform Mutation
- c.) update fitness
- d.) Compare

4. Termination

(NLP) Natural Language Processing

NLP Problems can be divided into two parts :-

1. Processing Written Text.
2. Processing Spoken Language.

→ Steps in NLP :-

1. Morphological Analysis

it means whenever we are writing a Sentence, it will extract meaningful words from that Sentence.

2. Syntactic Analysis

after categorizing the words, it will perform Syntactic Analysis. Build a ~~tree~~ structure description of Sentence based.

3. Semantic Analysis

4. Discourse Integration

5. Pragmatic Analysis

It refers to intended meaning of Sentences used in different contexts. The context affects the interpretation of the Sentence.

In Min Max, we have to compare every node which is drawback and to solve this we use Alpha Beta Pruning.

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* Min Max Algorithm :-

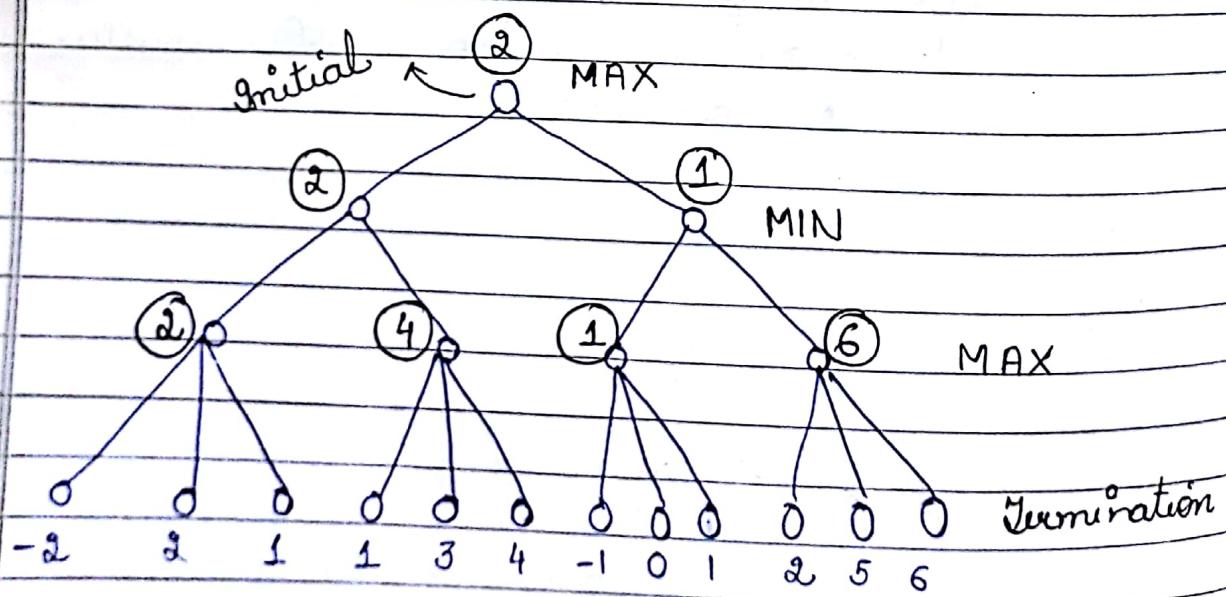
A game can be formally defined as a kind of search problem with the following components :

- The initial state
- A set of operators
- A terminal test
- A Utility function (also called payoff function)

2 Players

1st Player - MAX → will select the max utility value - to win

2nd Player - MIN → will select the min utility value



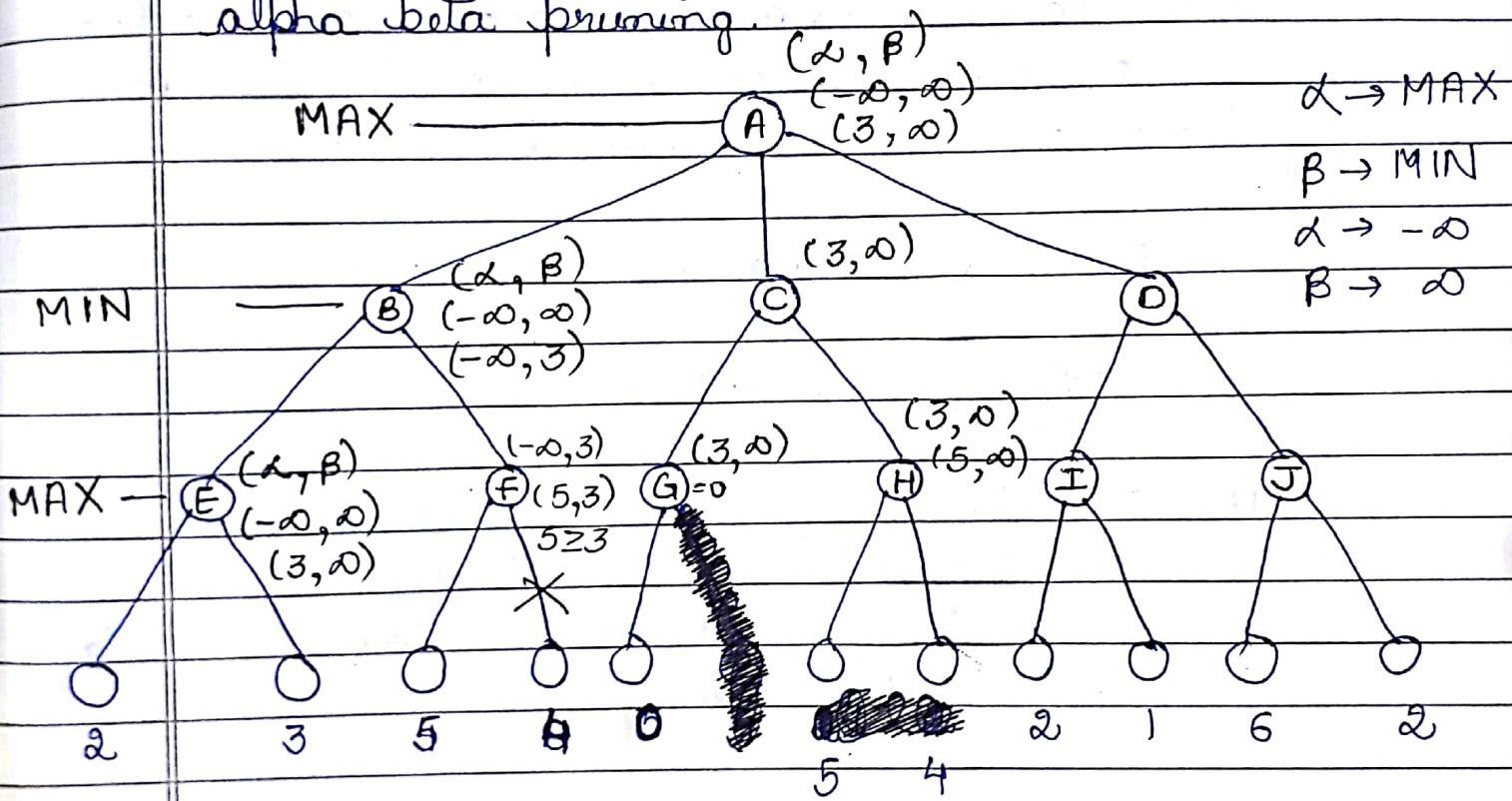
$$\text{Max} = -\infty$$

$$\text{Min} = +\infty$$

* ALPHA BETA Pruning :-

Follows DFS approach.

The process of eliminating a branch of the Search tree from consideration without examining it is called Pruning the Search Tree. The particular techq. we will examine is called alpha beta pruning.



Values will always transferred from Top to Bottom

$$\alpha \geq \beta$$

If its true, will Prun the next node.