Machine Learning

Important points and calculations

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Disclaimer

- Please use LMS notes for introduction and theory about each alogorithm
- This notes is mainly to cover important points discussed in class

Naïve Bayes

| Outlook | Temperature | Humidity | Wind | Play Tennis |
|----------|-------------|----------|--------|-------------|
| Sunny | Hot | High | Weak | No |
| Sunny | Hot | High | Strong | No |
| Overcast | Hot | High | Weak | Yes |
| Rain | Mild | High | Weak | Yes |
| Rain | Cool | Normal | Weak | Yes |
| Rain | Cool | Normal | Strong | No |
| Overcast | Cool | Normal | Strong | Yes |
| Sunny | Mild | High | Weak | No |
| Sunny | Cool | Normal | Weak | Yes |
| Rain | Mild | Normal | Weak | Yes |
| Sunny | Mild | Normal | Strong | Yes |
| Overcast | Mild | High | Strong | Yes |
| Overcast | Hot | Normal | Weak | Yes |
| Rain | Mild | High | Strong | No |

Frequency Tables

| Outlook | Play=Yes | Play=No | Temperature | Play=Yes | Play=No |
|----------|----------|---------|-------------|----------|---------|
| Sunny | 2/9 | 3/5 | Hot | 2/9 | 2/5 |
| Overcast | 4/9 | 0/5 | Mild | 4/9 | 2/5 |
| Rain | 3/9 | 2/5 | Cool | 3/9 | 1/5 |

| Humidity | Play=Yes | Play=No |
|----------|----------|---------|
| High | 3/9 | 4/5 |
| Normal | 6/9 | 1/5 |

| Wind | Play=Yes | Play=No |
|--------|----------|---------|
| Strong | 3/9 | 3/5 |
| Weak | 6/9 | 2/5 |

Predictions

Given a new instance, predict its label

X = (Outlook=Sunny, Temperature=Cool, Humidity=High, Wind=Strong)

P(Outlook=Sunny | Play=Yes) = (2 + 1) / (9 + 3) = 0.25 P(Outlook=Sunny | Play=No) = (3 + 1) / (5 + 3) = 0.5 P(Temperature=Cool | Play=Yes) = (3 + 1) / (9 + 3) = 0.25 P(Temperature=Cool | Play=No) = (1 + 1) / (5 + 3) = 0.25 P(Humidity=High | Play=No) = (4 + 1) / (5 + 2) = 0.71 P(Humidity=High | Play=Yes) = (3 + 1) / (9 + 2) = 0.36 P(Wind=Strong | Play=No) = (3 + 1) / (5 + 2) = 0.57 P(Wind=Strong | Play=Yes) = (3 + 1) / (9 + 2) = 0.36 P(Play=No) = (3 + 1) / (5 + 2) = 0.57

P(Play=Yes) = 9 / 14 = 0.64

 $P(Yes \mid X) = [P(Sunny \mid Yes) P(Cool \mid Yes) P(High \mid Yes) P(Strong \mid Yes)] P(Play=Yes) = 0.0068 P(Yes \mid X) = [P(Sunny \mid No) P(Cool \mid No) P(High \mid No) P(Strong \mid No)] P(Play=No) = 0.0177$

Given the fact $P(Yes \mid X) < P(No \mid X)$. We label X to No

K Nearest Neighbor

| X1 | X2 | Y |
|----|----|------|
| 7 | 7 | Bad |
| 7 | 4 | Bad |
| 3 | 4 | Good |
| 1 | 4 | Good |

Predict Y if X1=3, X2=7; K= 3

K Nearest Neighbor

| X1 | X2 | Euclidian Distance | Neighbor | Υ |
|-----------|----|---------------------------------|----------|------|
| 7 | 7 | $Sqrt((7-3)^2 + (7-7)^2) = 4$ | 3 | Bad |
| 7 | 4 | $Sqrt((7-3)^2 + (4-7)^2) = 5$ | 4 | Bad |
| 3 | 4 | $Sqrt((3-3)^2 + (4-7)^2) = 3$ | 1 | Good |
| 1 | 4 | $Sqrt((1-3)^2 + (4-7)^2) = 3.6$ | 2 | Good |

Among the first 3 Neighbors, 2 samples are Good and 1 sample is Bad; Prediction is Good

| X1 | X2 | Euclidian Distance | Neighbor | Υ |
|----------------|----------------|---------------------------------|----------------|------------------|
| <mark>7</mark> | <mark>7</mark> | $Sqrt((7-3)^2 + (7-7)^2) = 4$ | <mark>3</mark> | <mark>Bad</mark> |
| 7 | 4 | $Sqrt((7-3)^2 + (4-7)^2) = 5$ | 4 | Bad |
| 3 | <mark>4</mark> | $Sqrt((3-3)^2 + (4-7)^2) = 3$ | <mark>1</mark> | Good |
| 1 | <mark>4</mark> | $Sqrt((1-3)^2 + (4-7)^2) = 3.6$ | 2 | Good |

Random Forest

- Each tree is grown fully to reduce bias; Due to this variance will be high
- To reduce variance, multiple such trees are grown
- For each tree, 60% of samples are randomly selected
- While randomly selecting samples, each sample is given equal weight
- For each tree, Sqrt(No. of cols) are randomly selected
- Prediction is based on polling of predictions from all trees

Adaboost

- In Random Forest, each sample is given equal weight while sampling
- In Adaboost, while building first decision tree, each sample is given equal weight
- While building second decision tree, for each sample new weights are calculated
- Samples which are misclassified in first decision tree are given higher weights in second decision tree

Sample Data

| Outlook | Temperature | Humidity | Wind | Target Original | Target New |
|----------|-------------|----------|--------|-----------------|------------|
| Sunny | Hot | High | Weak | No | -1 |
| Sunny | Hot | High | Strong | No | -1 |
| Overcast | Hot | High | Weak | Yes | 1 |
| Rain | Mild | High | Weak | Yes | 1 |
| Rain | Cool | Normal | Weak | Yes | 1 |
| Rain | Cool | Normal | Strong | No | -1 |
| Overcast | Cool | Normal | Strong | Yes | 1 |
| Sunny | Mild | High | Weak | No | -1 |
| Sunny | Cool | Normal | Weak | Yes | 1 |

First Tree Prediction on Training Data

| Sample Weight | Actual | Predicted | Correct Prediction? |
|------------------|--------|-----------|---------------------|
| 1/N = 1 / 9 | -1 | 1 | Wrong |
| 1/9 | -1 | -1 | Correct |
| 1/9 | 1 | -1 | Wrong |
| 1/9 | 1 | 1 | Correct |
| 1/9 | 1 | 1 | Correct |
| 1/9 | -1 | 1 | Wrong |
| 1/9 | 1 | 1 | Correct |
| 1/9 | -1 | -1 | Correct |
| 1/9 | 1 | 1 | Correct |

Error Rate

Error Rate = Wrong / Total Predictions

Error Rate = 3 / 9 = 0.33

Classifier's weight

$$\alpha_t = \frac{1}{2} ln \left(\frac{1 - \epsilon_t}{\epsilon_t} \right)$$

$$(1 / 2) * np.log((1-0.33) / 0.33)$$

0.3540925289622428

Samples new weight

$$D_{t+1}(i) = \frac{D_t(i)\exp(-\alpha_t y_i h_t(x_i))}{Z_t}$$

- Y_i = Actual value of ith sample
- $H_t(x_i)$ = Prediction value of i^{th} sample
- Alpha_t = Classifiers weight

| Sample Weight (D ₁) | Actu al | Predict ed | Correct Prediction? | Sample Weight (D ₂) (numerator) |
|------------------------------------|------------|---------------|---------------------|---|
| 1/N = 1 / 9 | -1 | 1 | Wrong | $(1/9) \exp(-0.35*(-1)*(1)) = 0.15$ |
| 1/9 | -1 | -1 | Correct | $(1/9) \exp(-0.35*(-1)*(-1)) = 0.07$ |
| 1/9 | 1 | -1 | Wrong | $(1/9) \exp(-0.35*(1)*(-1)) = 0.15$ |
| 1/9 | 1 | 1 | Correct | $(1/9) \exp(-0.35*(1)*(1)) = 0.07$ |
| 1/9 | 1 | 1 | Correct | |
| 1/9 | -1 | 1 | Wrong | |
| 1/9 | 1 | 1 | Correct | |
| 1/9 | -1 | -1 | Correct | |
| 1/9 | 1 | 1 | Correct | |

- Samples which are misclassified given weight as 0.15
- Samples which are correctly classified given weight as 0.07
- Samples which are misclassified are given more weight
- Zt is nothing but summation of all new weights
- Mainly used to make values add up to 1
- Second decision tree gives more weights to misclassified samples

Weighted Polling

$$H(x) = sign\left(\sum_{t=1}^{T} \alpha_t h_t(x)\right)$$

- While polling prediction from each tree is added together along with classifier weight
- It is called as weighted polling
- If sum comes out to be positive, final prediction is +1
- If sum comes out to be negative, final prediction is -1