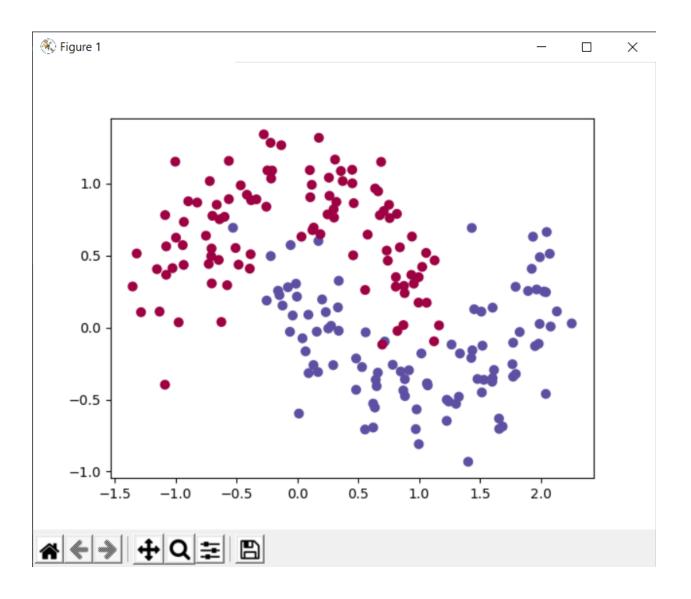
<u>ELEC 576 / COMP 576 – Fall 2021 Assignment 1</u>

<u>Task - 1:</u>

a. **Dataset:** three_layer_neuralnetwork.py



b. Activation Function:

C

Tanh function

```
\tanh = 1 - e^{-2x} / 1 + e^{-2x} \det(x) / dx = 2e^{-2x} / 1 + e^{-2x} + ((1-e)^{2x} - 2x e^{-2x}) / (1 + e^{-2x})^{2x} = 4e^{-2x} / (1 + e^{-2x})^{2x} 2 = 1 - \tanh^{2}(x)
```

Sigmoid function

```
dsig(x)/dx = e^{-x}/(1+e^{-x})^{-2} = sig(x)(1 - sig(x))
```

ReLU function

The derivative of x is, 1 for x > 0 and 0 for x = 0.

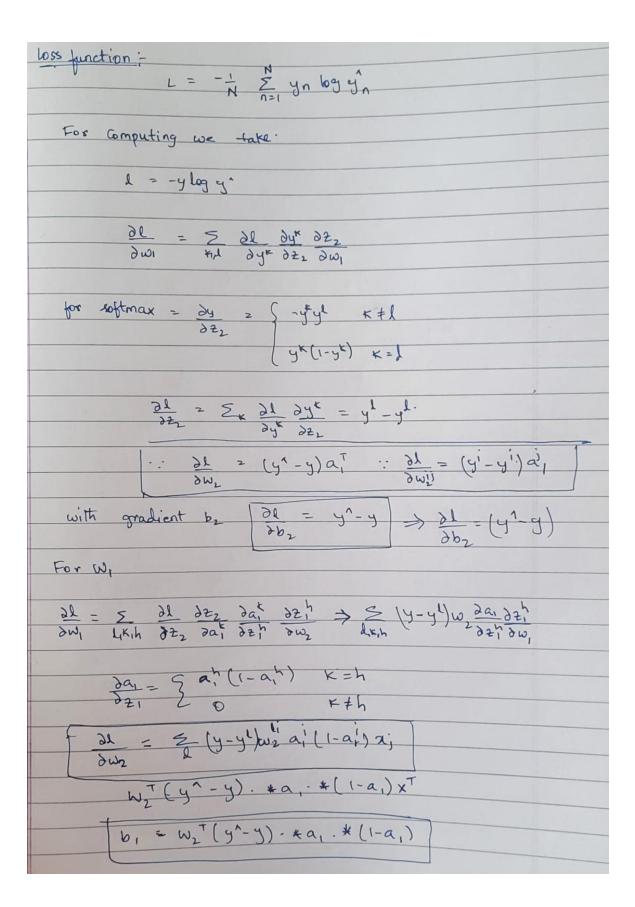
d. Build a Neural Network:

Feed forward:

Calculate_loss:

e. Backward Pass - Backward Propagation

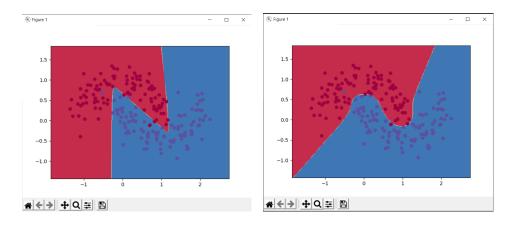
1. Derivation:

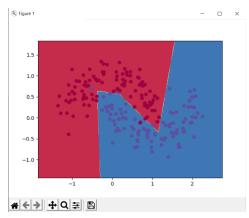


2. <u>Implementation:</u>

f. Time to have fun - Training

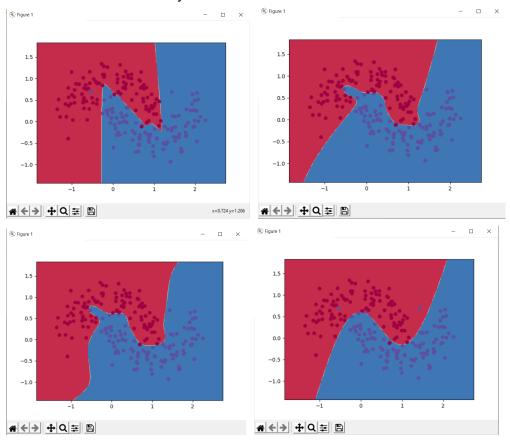
1. Plots for Tanh, sigmoid, relu:





Here we can observe that the sigmoid function has a better fitting than other Tanh and relu functions.

2. Tanh for different hidden layers:



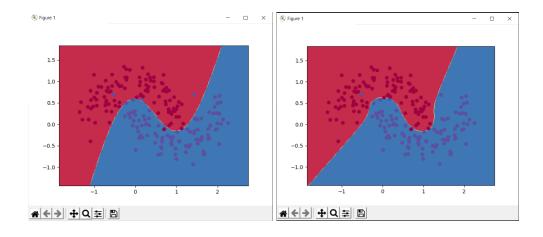
The above 3 figures are plots of Tanh activation function for hidden layers = 5, 10, 20, 6.

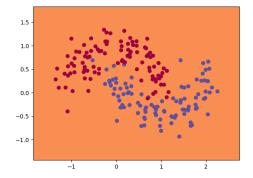
We can observe that for hidden layers = 6 the plot is smooth and fits perfectly, while others are under fitted or overfitted.

g. Deep Neural Network:

```
Layer Class:
import numpy as np
from configs import configration
config = configration()
class Layer():
  def __init__(self, layer_id, actFun):
     self.actFun = actFun
     self.layer_id = layer_id
  def feedforward(self, input_, W, b):
    if self.layer id < config.nn layers - 1:
       self.z = np.matmul(input_, W) + b
       self.a = self.actFun(self.z)
    if self.layer_id == config.nn_layers - 1:
       self.z = np.matmul(input, W) + b
       exp\_scores = np.exp(self.z)
       self.a = exp_scores / np.sum(exp_scores, axis=1, keepdims=True)
    return self.a
  def backprop(self, input_, num_examples, delta):
       dW = 1/num_examples * np.dot(np.transpose(input_),delta)
       db = 1/num_examples * np.sum(delta, axis = 0, keepdims = True)
       return dW, db
```

Neuralnetwork Class:

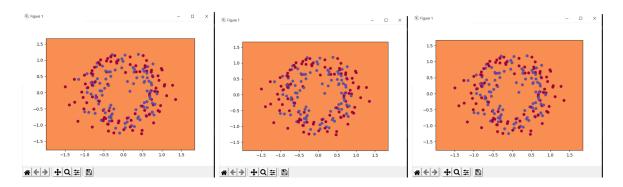




This is for the Make_moons dataset .

Here we can observe that while the tanh and sigmoid act_fun are fine but the relu function is filled with an orange background, this is due to vanishing gradients and strong regularization.

- This is for make_circles dataset



As we can observe for all act_fun i.e. tanh, sigmoid and relu, due to densely packed and nodes being over each other nodes the gradients are vanishing and are very strongly regularized therefore the orange background.

Task - 2: Deep Convolutional Networks with MNIST

- a. Build and train Networks:
 - Functions:
 - 1. Weight function:

```
def weight_variable(shape, initializer=None):

///
Initialize weights
    :param shape: shape of weights, e.g. [w, h ,Cin, Cout] where
    w: width of the filters
    h: height of the filters
    Cin: the number of the channels of the filters
    Cout: the number of filters
    :return: a tensor variable for weights with initial values

///

# IMPLEMENT YOUR WEIGHT_VARIABLE HERE
    initial = tf.truncated_normal(shape, stddev=0.1)

• W = tf.Variable(initial)

return W
```

2. Bias function:

```
def bias_variable(shape, initializer=None):

Initialize biases

:param shape: shape of biases, e.g. [Cout] where

Cout: the number of filters

:return: a tensor variable for biases with initial values

"""

# IMPLEMENT YOUR BIAS_VARIABLE HERE

initial = tf.constant(0.1, shape=shape)

b = tf.Variable(initial)

return b
```

3. Conv2d function:

4. Max_pool_2x2:

Build your network:

```
# first convolutional layer
       W_{conv1} = weight_{variable}([5, 5, 1, 32])
       b conv1 = bias variable([32])
       h conv1 = tf.nn.relu(conv2d(x_image, W_conv1) + b_conv1)
       h_pool1 = max_pool_2x2(h_conv1)
       # second convolutional layer
       W_{conv2} = weight_{variable}([5, 5, 32, 64])
       b_conv2 = bias_variable([64])
       h conv2 = tf.nn.relu(conv2d(h pool1, W conv2) + b conv2)
       h_{pool2} = max_{pool}_{2x2}(h_{conv2})
       # densely connected layer
       W_{fc1} = weight_variable([7 * 7 * 64, 1024])
       b fc1 = bias variable([1024])
       h_pool2_flat = tf.reshape(h_pool2, [-1, 7 * 7 * 64])
       h_fc1 = tf.nn.relu(tf.matmul(h_pool2_flat, W_fc1) + b_fc1)
       # dropout
       keep prob = tf.placeholder(tf.float32)
       h fc1 drop = tf.nn.dropout(h fc1, keep prob)
       # softmax
       W fc2 = weight_variable([1024, 10])
       b_fc2 = bias_variable([10])
       y_conv = tf.matmul(h_fc1_drop, W_fc2) + b_fc2
```

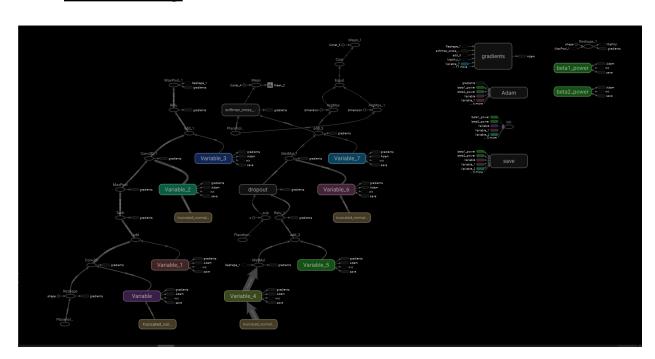
Set up Training:

• Run Training:

```
step 0, training accuracy 0.08
step 100, training accuracy 0.04
step 200, training accuracy 0.34
step 300, training accuracy 0.22
step 400, training accuracy 0.64
step 500, training accuracy 0.22
step 600, training accuracy 0.4
step 700, training accuracy 0.62
step 800, training accuracy 0.6
step 900, training accuracy 0.6
step 1000, training accuracy 0.64
step 1100, training accuracy 0.66
step 1200, training accuracy 0.72
step 1300, training accuracy 0.72
step 1400, training accuracy 0.72
step 1500, training accuracy 0.74
step 1600, training accuracy 0.7
step 1700, training accuracy 0.84
step 1800, training accuracy 0.82
step 1900, training accuracy 0.78
step 2000, training accuracy 0.7
step 2100, training accuracy 0.82
step 2200, training accuracy 0.84
step 2300, training accuracy 0.74
step 2400, training accuracy 0.84
step 2500, training accuracy 0.86
step 2600, training accuracy 0.76
step 2700, training accuracy 0.78
step 2800, training accuracy 0.7
step 2900, training accuracy 0.82
step 3000, training accuracy 0.72
step 3100, training accuracy 0.86
step 3200, training accuracy 0.78
```

```
step 3300, training accuracy 0.92
step 3400, training accuracy 0.78
step 3500, training accuracy 0.84
step 3600, training accuracy 0.8
step 3700, training accuracy 0.86
step 3800, training accuracy 0.86
step 3900, training accuracy 0.82
step 4000, training accuracy 0.86
step 4100, training accuracy 0.8
step 4200, training accuracy 0.86
step 4300, training accuracy 0.9
step 4400, training accuracy 0.82
step 4500, training accuracy 0.86
step 4600, training accuracy 0.82
step 4700, training accuracy 0.86
step 4800, training accuracy 0.88
step 4900, training accuracy 0.88
step 5000, training accuracy 0.92
step 5100, training accuracy 0.94
step 5200, training accuracy 0.94
step 5300, training accuracy 0.92
step 5400, training accuracy 0.88
test accuracy 0.8886
The training takes 383.276304 seconds to finish
```

Visualise Training:



b. More on Visualizing:

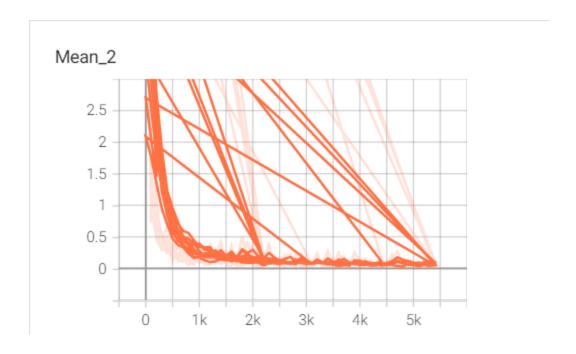
By using 'tensorboard --logdir=./results/' we will get the scalar, histogram and graphs for all the summaries we plot for.

```
with tf.name_scope('summaries'):
    mean = tf.reduce_mean(var)
    tf.summary.scalar('mean', mean)
    with tf.name_scope('stddev'):
        stddev = tf.sqrt(tf.reduce_mean(tf.square(var - mean)))
    tf.summary.scalar('stddev', stddev)
    tf.summary.scalar('max', tf.reduce_max(var))
    tf.summary.scalar('min', tf.reduce_min(var))
    tf.summary.histogram('histogram', var)
```

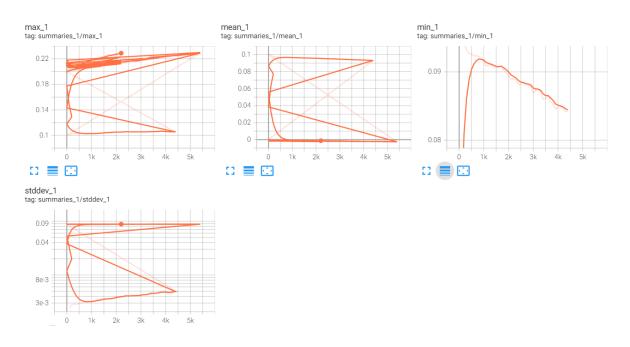
```
variable_summaries(W_conv1)
variable_summaries(W_conv2)
variable_summaries(W_fc1)
variable_summaries(W_fc2)
variable_summaries(b_fc2)
variable_summaries(b_fc1)
variable_summaries(b_conv2)
variable_summaries(b_conv1)
variable_summaries(conv2d(h_pool1, W_conv2) + b_conv2)
variable_summaries(conv2d(x_image, W_conv1) + b_conv1)
variable_summaries(tf.matmul(h_pool2_flat, W_fc1) + b_fc1)
variable_summaries(h_conv1)
variable_summaries(h_conv2)
variable_summaries(h_fc1)
variable_summaries(h_pool1)
variable_summaries(h_pool2)
```

The above are the summaries for all the convolution layers, softmax, dropout and densely packed layers.

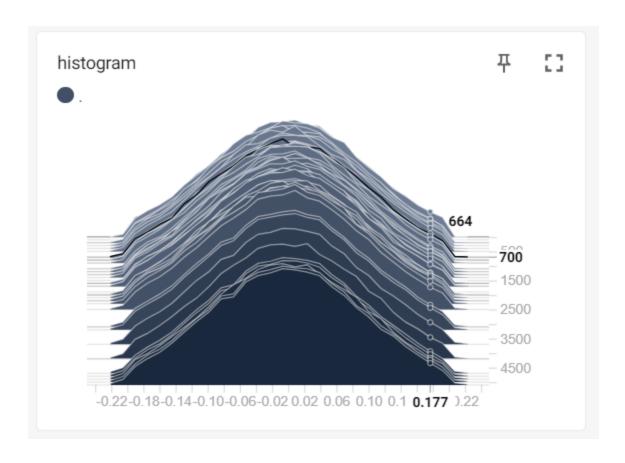
The loss path is given below.



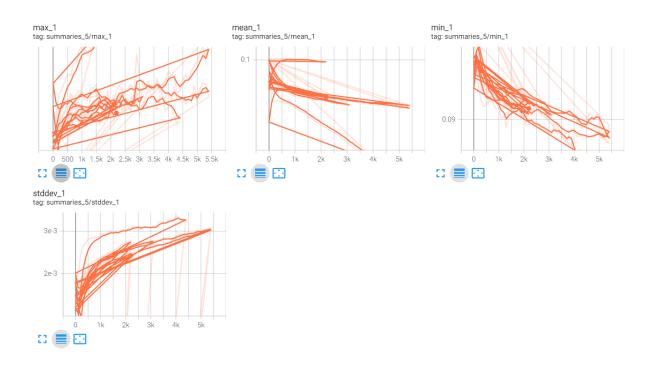
For weight W_conv1:



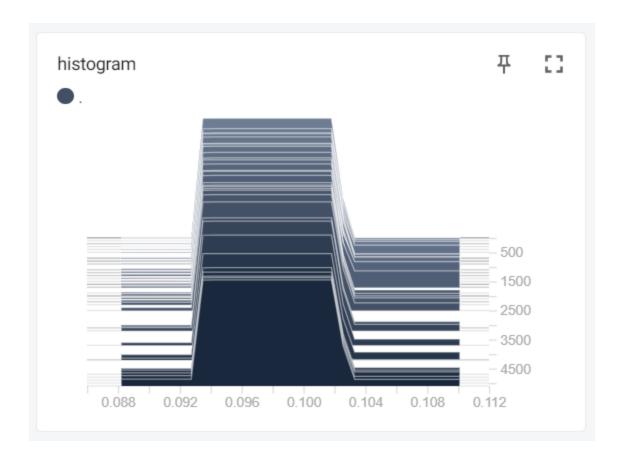
Histogram of weight:



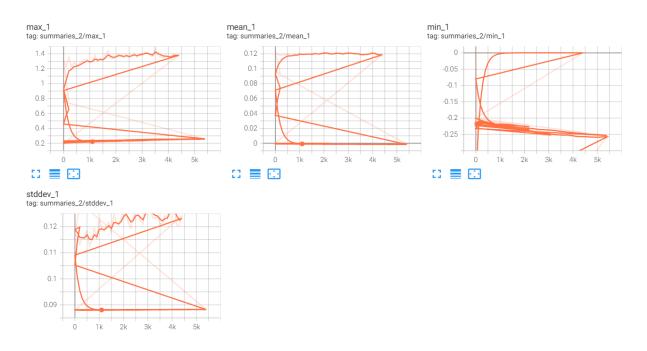
For Bias b_fc1:

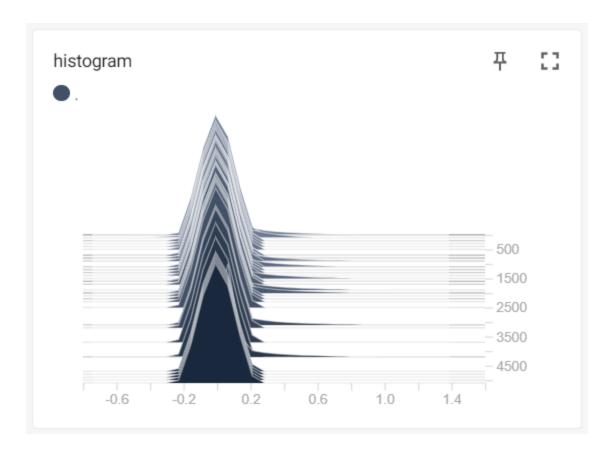


Histogram for Bias:

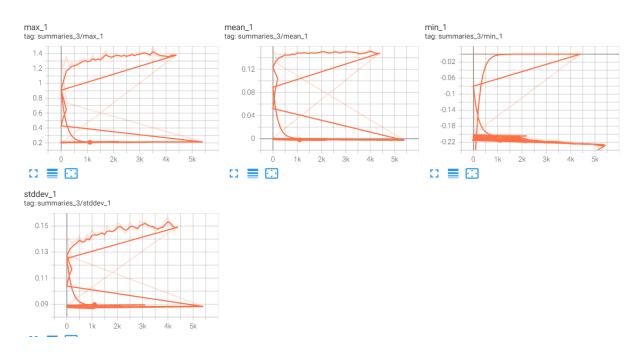


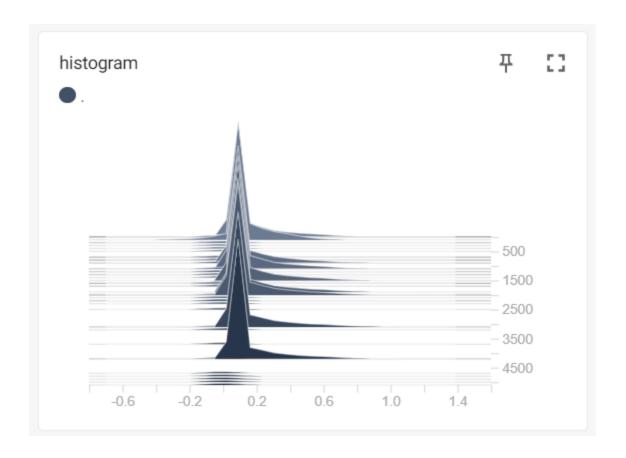
For W_conv2:



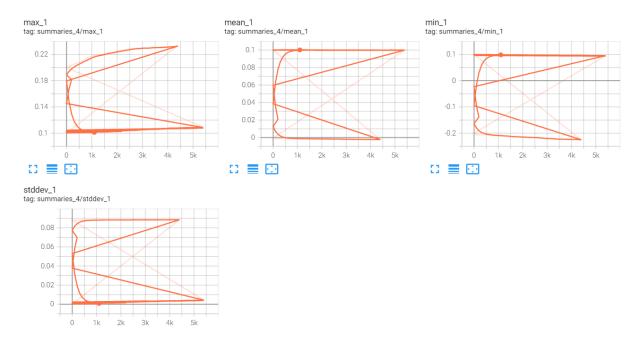


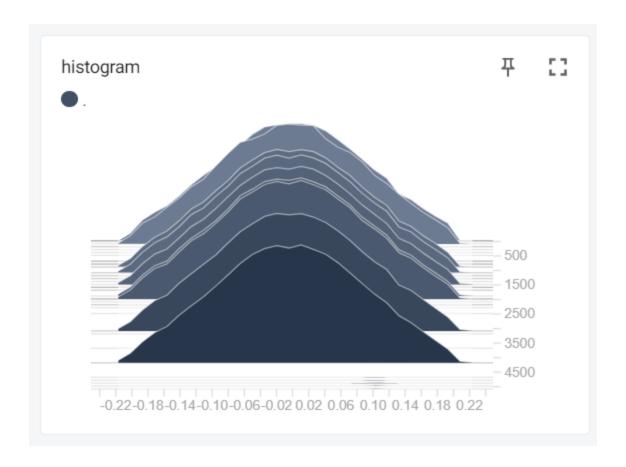
For W_fc1:



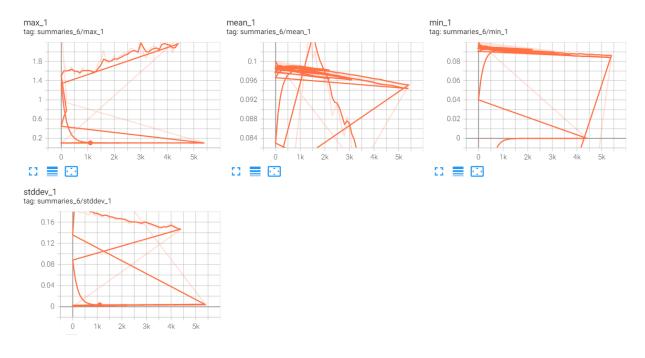


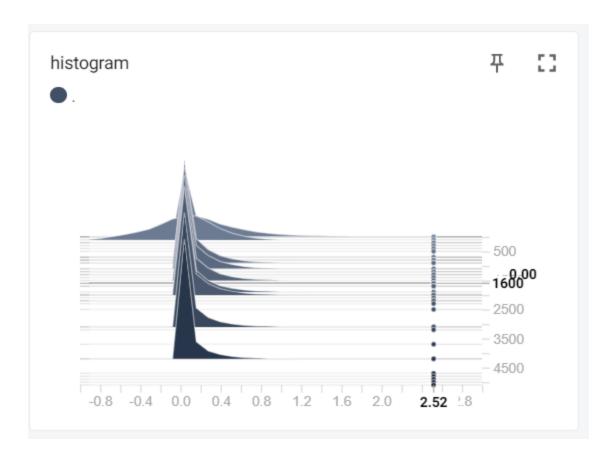
For W_fc2:





For b_fc2:

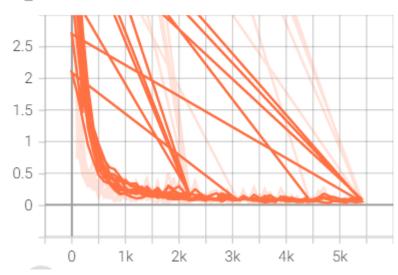




Like the following above images we will get plots of summaries for all the variables we get.

The final training loss for all test cases:





c. Time for more fun:

For Adam optimiser:

- step 100, training accuracy 0.82
- step 200, training accuracy 0.92
- step 300, training accuracy 0.94
- step 400, training accuracy 0.94
- step 500, training accuracy 0.96
- step 600, training accuracy 0.98
- step 700, training accuracy 0.94
- step 800, training accuracy 0.96
- step 900, training accuracy 0.92
- step 1000, training accuracy 0.96
- step 1100, training accuracy 1
- step 1200, training accuracy 0.96
- step 1300, training accuracy 0.9
- step 1400, training accuracy 0.98
- step 1500, training accuracy 1
- step 1600, training accuracy 0.96
- step 1700, training accuracy 0.98
- step 1800, training accuracy 0.98
- step 1900, training accuracy 1
- step 2000, training accuracy 0.96
- step 2100, training accuracy 0.98
- step 2200, training accuracy 0.98
- step 2300, training accuracy 1
- step 2400, training accuracy 0.96
- step 2500, training accuracy 0.96
- step 2600, training accuracy 0.98
- step 2700, training accuracy 0.94
- step 2800, training accuracy 0.98
- step 2900, training accuracy 0.98
- step 3000, training accuracy 0.98
- step 3100, training accuracy 0.98
- step 3200, training accuracy 0.94
- step 3300, training accuracy 0.96
- step 3400, training accuracy 0.98
- step 3500, training accuracy 0.98
- step 3600, training accuracy 1
- step 3700, training accuracy 0.98
- step 3800, training accuracy 1
- step 3900, training accuracy 1
- step 4000, training accuracy 1
- step 4100, training accuracy 1
- step 4200, training accuracy 0.94
- step 4300, training accuracy 1

step 4400, training accuracy 0.98 step 4500, training accuracy 0.98 step 4600, training accuracy 1 step 4700, training accuracy 1 step 4800, training accuracy 1 step 4900, training accuracy 0.98 step 5000, training accuracy 0.98 step 5100, training accuracy 1 step 5200, training accuracy 1 step 5300, training accuracy 1 step 5400, training accuracy 1 step 5400, training accuracy 1 test accuracy 0.9889

For Gradient Optimiser:

step 0, training accuracy 0.08 step 100, training accuracy 0.04 step 200, training accuracy 0.34 step 300, training accuracy 0.22 step 400, training accuracy 0.64 step 500, training accuracy 0.22 step 600, training accuracy 0.4 step 700, training accuracy 0.62 step 800, training accuracy 0.6 step 900, training accuracy 0.6 step 1000, training accuracy 0.64 step 1100, training accuracy 0.66 step 1200, training accuracy 0.72 step 1300, training accuracy 0.72 step 1400, training accuracy 0.72 step 1500, training accuracy 0.74 step 1600, training accuracy 0.7 step 1700, training accuracy 0.84 step 1800, training accuracy 0.82 step 1900, training accuracy 0.78 step 2000, training accuracy 0.7 step 2100, training accuracy 0.82

step 2200, training accuracy 0.84 step 2300, training accuracy 0.74 step 2400, training accuracy 0.84 step 2500, training accuracy 0.86 step 2600, training accuracy 0.76 step 2700, training accuracy 0.78 step 2800, training accuracy 0.7 step 2900, training accuracy 0.82

step 3000, training accuracy 0.72 step 3100, training accuracy 0.86 step 3200, training accuracy 0.78 step 3300, training accuracy 0.92 step 3400, training accuracy 0.78 step 3500, training accuracy 0.84 step 3600, training accuracy 0.8 step 3700, training accuracy 0.86 step 3800, training accuracy 0.86 step 3900, training accuracy 0.82 step 4000, training accuracy 0.86 step 4100, training accuracy 0.8 step 4200, training accuracy 0.86 step 4300, training accuracy 0.9 step 4400, training accuracy 0.82 step 4500, training accuracy 0.86 step 4600, training accuracy 0.82 step 4700, training accuracy 0.86 step 4800, training accuracy 0.88 step 4900, training accuracy 0.88 step 5000, training accuracy 0.92 step 5100, training accuracy 0.94 step 5200, training accuracy 0.94 step 5300, training accuracy 0.92 step 5400, training accuracy 0.88 test accuracy 0.8886

For Tanh:

step 0, training accuracy 0.06 step 100, training accuracy 0.4 step 200, training accuracy 0.7 step 300, training accuracy 0.86 step 400, training accuracy 0.84 step 500, training accuracy 0.94 step 600, training accuracy 0.94 step 700, training accuracy 0.98 step 800, training accuracy 0.94 step 900, training accuracy 0.96 step 1000, training accuracy 0.96 step 1100, training accuracy 0.9 step 1200, training accuracy 0.98 step 1300, training accuracy 0.98 step 1400, training accuracy 0.94 step 1500, training accuracy 0.98

```
step 1600, training accuracy 0.96
step 1700, training accuracy 0.98
step 1800, training accuracy 0.94
step 1900, training accuracy 0.98
step 2000, training accuracy 1
step 2100, training accuracy 0.94
step 2200, training accuracy 0.96
step 2300, training accuracy 1
step 2400, training accuracy 0.96
step 2500, training accuracy 0.92
step 2600, training accuracy 0.96
step 2700, training accuracy 1
step 2800, training accuracy 0.98
step 2900, training accuracy 1
step 3000, training accuracy 0.96
step 3100, training accuracy 1
step 3200, training accuracy 0.98
step 3300, training accuracy 0.98
step 3400, training accuracy 0.96
step 3500, training accuracy 0.96
step 3600, training accuracy 1
step 3700, training accuracy 0.98
step 3800, training accuracy 1
step 3900, training accuracy 0.98
step 4000, training accuracy 0.98
step 4100, training accuracy 0.98
step 4200, training accuracy 1
step 4300, training accuracy 0.96
step 4400, training accuracy 1
step 4500, training accuracy 1
step 4600, training accuracy 0.98
step 4700, training accuracy 1
step 4800, training accuracy 1
step 4900, training accuracy 1
step 5000, training accuracy 0.98
step 5100, training accuracy 0.98
step 5200, training accuracy 0.96
step 5300, training accuracy 1
step 5400, training accuracy 0.98
test accuracy 0.9846
```

From the above results we can observe that Tanh nonlinearity, and Adam optimiser have higher test accuracy than gradient optimiser and relu.

The below is the test accuracy plot: for Gradient optimiser, Tanh and xavier initilizer.

