Empirical Finance: A Review

For Personal Reference

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HERE WE GO!

Empirical finance is an absolutely fascinating field, with some of the most cutting-edge methodologies and the most exploratory techniques. Although it is not my speciality, I am always interested in this literature. During my pre-doc research fellowship at London Business School, I have had the previlege to study in the course *Financial Economics II: Empirical Finance*. The course instructor Dr. Svetlana Bryzgalova is absolutely one of the most brilliant scholars I have encountered. Thanks to her, I have got to understand this liturature more systematically. In this (personal) review, I summarize the most influential and inspirational works in this field and organize them by different topics. The structure of this review resembles the structure of Dr. Bryzgalova's course, while adjusted according to my personal research interest. I intend to review classic works and discuss some potential directions of future study regarding my personal interest in Behavioral Economics, Game Theory and Network.

Since this review is tailored according to my own research interest and experience, I will not only summarize the theoretical perspectives of the studies, present their findings and discuss how they fit into the literature, but document my replication attempts and pseudo codes as well. All the codes related to this review can be found on my Github page.

I thank Dr. Svetlana Bryzgalova for her valuable intuitions and impressive knowledge of the empirical finance literature. Building this review is truly a memorable journey for me. I would love to share this review and all the related materials to anyone that finds them useful. And unavoidably, I would make some typos and other minor mistakes (hopefully not big ones). So I'd really appreciate any correction. If you find any mistakes, please either set up a branch on Github or send the mistakes to this email address saizhang.econ@gmail.com, BIG thanks in advance!

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CHAPTER 1

TIME-SERIES PREDICTABILITY

Contents

Every investor knows that trading in financial markets is to play games with time itself. Daily trades determine asset prices at every date and hence influence the random distribution of future prices as well as the initial level of prices. One would need "much more careful attention to the process by which both expected payoffs and required rates of return determine asset prices"[1].

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[1]See Campbell (2017, p. 121)

In this chapter, I first, following Campbell (2017, Chapter 5), summarize models mapping cash flows and discount rates into prices using present value relations in Section 1.1. Then I discuss the early evidence for mean reversion in returns in Section 1.2. In Section 1.3, I examine the excess volatility puzzle in the predictability debate. To accomodate the stylized facts of time-series predictability, Section 1.4 presents two of the most influential approaches to decompose prices. In Section 1.5, I selectively summarize some researches from the so-called "Prediction Zoo", which satirically describes the floods of price predictors. Finally, I discuss the issues and extensions of time-series predictability in Section 1.6.

1.1   Concepts and models

In this section, I follow Campbell (2017, Chapter 5) and discuss some of the conceptual building blocks for the strand of time-series empirical finance literature.

1.1.1   Market Efficiency

An intuitive way of explaining *market efficiency* is that efficient markets are competitive and allow no easy ways to make economic profit. A more useful and testable definition was given by Malkiel (1989, p. 127):

> The market is said to be efficient with respect to some information set ϕ, if security prices would be unaffected by revealing that information to all participants.

Some event studies that measure market responses to news announcements can be interpreted as tests of market efficiency regarding the announced information, but in general, this definition is not easy to test. On the other hand, Malkiel (1989) gives a more testable alternative:

> Efficiency with respect to an information set ϕ implies that it is impossible to make economic profits by trading on the basis of ϕ.

This is the idea behind an enormous literature in empirical asset pricing: if an economic model defines the equilibrium return as $\Theta_{i,t}$, then the null hypothesis is

$$R_{i,t+1} = \Theta_{i,t} + U_{i,t+1} \tag{1.1}$$

where $U_{i,t+1}$ is a FAIR game regarding the information set at t, or $\mathbb{E}(U_{i,t+1}|\phi_t) = 0$. Notice that market efficiency is equivalent to rational expectations, one must text a model of expected returns as well when testing market efficiency. After defining a model of expected returns, the variables to be included in the information set must be specified. Malkiel and Fama (1970) define three forms of efficient market hypothesis and the corresponding information sets:

   - the *weak form*: past returns

- the *semi-strong form*: publicly available information such as stock splits, dividends, or earnings
- the *strong form*: information available to some market participants, but NOT necessarily to all participants.

In the time-series literature, the simplest economic model is constant return: $\Theta_{i,t} = \Theta$. In Section 1.2, I summarize the early literature focusing on this model.

Market efficiency has been widely tested and debated, now the most accepted view of market efficiency hypothesis is that it is a useful benchmark but does not hold perfectly. The debates between long-term versus short-term efficiency, micro versus macro efficiency are still and will continue to be heated. Some noticable alternative hypotheses are:

$\leftarrow$ this could be tested by using measureable actions (trades or portfolio holdings) of the potentially better informed agents

- *High-frequency noise*: market prices are contaminated by short-term noise, which can be caused by measurement errors or illiquidity (bid-ask bounce).
- *Inperfect information processing*: the market reacts sluggishly to information after its releasing
- *Persistent mispricing*: market prices deviate substantially from efficient levels in a LONG time
- *Disposition effect*: individual investors are more willing to sell winning stocks then losing stocks, see Shefrin and Statman (1985) for details.

1.1.2 Model: autocorrelation of returns

The most basic time-series test of market efficiency is to test "whether past deviations of returns from model-implied expected returns predict future return deviations" (See Campbell, 2017, p. 124). The leading approach to do so is to test the autocorrelations.

Starting points:

1. The null hypothesis H_0: the stock returns are i.i.d.
2. The standard error for any single sample autocorrelation equals asymptotically $1/\sqrt{T}$, see Box and Pierce (1970) for a detailed discussion.
3. The standard error would be large, (0.1 if $T = 100$), not so easy to detect small autocorrelation

Any autocorrelation test would have to solve these issues.

1.1.2.1 Q-statistics

Because the stock returns are i.i.d. (H_0), different autocorrelations are uncorrelated with one another. Box and Pierce (1970) calculates a sum of K squared sample autocorrelations:

$$Q_K = T \sum_{j=1}^{K} \hat{\rho}_j^2 \tag{1.2}$$

where $\hat{\rho}_j = \hat{Corr}(r_t, r_{t-j})$. Q is asymptotically distributed χ^2 with K degrees of freedom.

Pros: It solves the problem of the large standard errors.

Cons: It does NOT use the sign of the autocorrelations (squared). What could happen is that the expected reutrns are not constant, instead, they are each individually small but all have the same sign.

1.1.2.2 Variance ratio

One way to take the sign of autocorrelations into consideration is the variance ratio statistic. This statistic was introduced to the finance literature by Lo and MacKinlay (1988) and Poterba and Summers (1988).

The basic setting is: for a holding period K, the log return of this entire period $r_t(K)$ is the sum of all the one-period returns r_{t+i}:

$$r_t(K) \equiv r_t + r_{t+1} + \cdots + r_{t+K-1}$$

and the variance ratio over the period K would be defined as:

$$VR(K) = \frac{Var(r_t(K))}{K \cdot Var(r_t)}$$

If there are not autocorrelations, then the i.i.d. returns would have identical variance in each period from t to $t + K$, and $Var(r_t(K)) = Var(r_t + \cdots + r_{t+K-1}) = Var(r_t) + \cdots + Var(r_{t+K-1}) = K \cdot Var(r_t)$. Thus, $VR(K) = 1$. If we rewrite the definition of the variance ratio as:

$$VR(K) = \frac{Var(r_t(K))}{K \cdot Var(r_t)} = 1 + \underbrace{2 \sum_{j=1}^{K-1} \left(1 - \frac{j}{K}\right) \hat{\rho}_j}_{\text{weighted average of the first } K-1 \text{ sample autocorrelations}} \tag{1.3}$$

Then by comparing $VR(K)$ with 1, we can deduct the direction of the autocorrelations:

$VR(K) > 1$	predominantly **positive** autocorrelations
$VR(K) = 1$	no autocorrelations
$VR(K) < 1$	predominantly **negative** autocorrelations: mean reversion

Notice that the weight term $1 - \frac{j}{K}$ increases as j approaches K[2].

The asymptotic variance of the variance-ratio statistic, under H_0 (i.i.d. returns), is:

$$Var(\hat{VR}(K)) = \frac{4}{T} \sum_{j=1}^{K-1} \left(1 - \frac{j}{K}\right)^2 = \frac{2(2K-1)(K-1)}{3KT} \xrightarrow{K \to \infty} \frac{4K}{3T} \tag{1.4}$$

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[2]Cochrane (1988) showed that the estimator of VR(K) can be interpreted in terms of the frequency domain. It is asymptotically equivalent to 2π times the normalized spectral density estimator at the zero frequency, which uses the Bartlett kernel.

When $K \to \infty$, $T \to \infty$, and $K/T \to 0$ (Priestley, 1981, p. 463), the true return process can be serially correlated and heteroskedastic, but the variance of the variance-ratio is still given as:

$$Var(\hat{VR}(K)) = \frac{4K}{3T} \cdot VR(K)^2 \tag{1.5}$$

Notice that this can be quite large with a large $VR(K)$. This is due to the fact that $K/T \to 0$ is a dangerous assumption because in practice K is often large relative to the sample size. To tackle this, Lo and MacKinlay (1988) develop alternative asymptotics assuming $K/T \to \delta$ where $\delta > 0$. Through Monte Carlo simulations, they demonstrated that this new distribution is a more robust approximation to the small-sample distribution of the VR statistic. Most current applications of the VR statistic cite $K/T \to \delta > 0$ as the justification for using Monte Carlo distributions (i.e. set at $K = \delta T$) as representative of the VR statistic's sampling distribution. Some recent challenges of this result are discussed in Section 1.1.3.

To accommodate r_t's exhibiting conditional heteroskedasticity, Lo and MacKinlay (1988) proposed a heteroskedasticity-robust variance estimation of VR(K) as:

$$Var^*(\hat{VR}(K)) = 4 \sum_{j=1}^{K-1} \left(1 - \frac{j}{K}\right)^2 \cdot \frac{\sum_{t=j+1}^{T}(r_t - \bar{r})^2 (r_{t-j} - \bar{r})^2}{\left[\sum_{t=1}^{T}(r_t - \bar{r})^2\right]^2}$$

where $\bar{r} = \frac{1}{T} \sum_{t=1}^{T} r_t$ is the estimated mean of returns.

1.1.2.3   Regression approach

Fama and French (1988) established a regression approach to test AR(K). The basic idea is to regress the K-period return on the lagged K-period return:

$$r_t(K) = \alpha_K + \beta_K r_{t-K}(K) + \epsilon_t^K$$

The coefficient β_K would then be:

$$\beta_K = \frac{Cov[r_t(K), r_{t-K}(K)]}{Var[r_{t-K}(K)]} = 2 \left[\frac{VR(2K)}{VR(K)} - 1\right] = \frac{2\sum_{j=1}^{K-1}\left(\frac{\min(j, 2K-j)}{K}\right)\rho_j}{VR(K)} \tag{1.6}$$

It is clear to see that:

$\beta_K > 0$	predominantly **positive** autocorrelations
$\beta_K = 0$	no autocorrelations
$\beta_K < 0$	predominantly **negative** autocorrelations: mean reversion

1.1.3   Extension: Other variance-ratio tests

As summarized by Charles and Darné (2009), the intuition behind the VR test is rather simple, but conducting a statistical inference using the VR test is less straightforward. In this bonus subsection, I briefly summarize some recent development of individual VR tests, multiple VR tests and bootstrapping VR tests. For more detailed discussion, see Charles and Darné (2009) for a review.

1.1.3.1 Individual VR tests

Conventional VR tests, such as the Lo and MacKinlay test, are asymptotic tests: their sampling distributions are approximated by their limiting distributions. In practice, the asymptotic theory provides a poor approximation to the small-sample distribution of the VR statistic, which impeded the use of the statistic. In general, the ability of the asymptotic distribution to approximate the finite-sample distribution depends crucially on the value of K. For a large K relative to T, Lo and MacKinlay (1990a) have proved that the VR statistics are severely biased and right skewed. Several alternative tests try to tackle this issue.

Chen and Deo (2006) Test: they suggested a simple power transformtaion of the VR statistic when K is NOT too large. This transformation is able to solve the right-skewness problem and robust to conditional heteroskedasticity. They showed that the transformed VR statistic leads to significant gain in power against mean reverting alternative. They define the VR statistic based on the periodogram and this new statistic is precisely the normalized discrete periodogram average estimate of the spectral density of a stationary process at the origin.

Wright (2000) Test: they proposed a non-parametric alternative using signs and ranks. This test outperforms the Lo and MacKinlay test in 2 ways:

(1) As the rank and sign tests have an exact sampling distribution, there is no need to resort to asymptotic distribution approximation.
(2) The tests may be more powerful against a wide range of models displaying serial correlation, including fractionally integrated alternatives.

The rank-based tests display low-size distortions under conditional heteroskedasticity. One thing to notice is that the sign test assumes a zero drift value, Luger (2003) extended this test with unknown drift.

Choi (1999) Test: To overcome the issue that the arbitrary and *ad hoc* choice of K, Choi (1999) proposed a data-dependent procedure to determine the optimal value of K. This test is based on frequency domain following Cochrane (1988). However, instead of using Bartlett kernel as Cochrane, Choi employed the quadratic spectral kernel since it's optimal in estimating the spectral density at the zero frequency.

1.1.3.2 Multiple VR tests

All the tests above are individual tests, where the null hypothesis is tested for an individual value of K. However, to determine whether a time series is a random walk, we need to rule out all possibilities, meaning that for all values of K, the null hypothesis can not be rejected. It is necessary to conduct a joint test where a multiple comparison of VRs over a set of different time horizons is made. However, conducting separate individual tests for a number of K values may lead to over rejection of the null hypothesis. Several tests have been developed for this problem, with the joint null hypothesis $H_0 : \forall K_i, V(K_i) = 1$ against the alternative $H_1 : \exists K_i, V(K_i) \neq 1$

Chow and Denning (1993) Test: This test statistic is defined as

$$MVR_1 = \sqrt{T} \max_{1 \leq i \leq m} |M_1(K_i)|$$

where $M_1(K_i) = \frac{VR(K_i)-1}{\sqrt{2(2K-1)(K-1)/3KT}}$. This is based on the idea that the decision regarding the null hypothesis can be obtained from the maximum absolute value of the individual VR statistics. Then, they applied the Sidak probability inequality and give an upper bound to the critical values taken in the studentized maximum modulus (SMM) distribution. The statistic follows the SMM distribution with m and T degrees of freedom, where m is the number of K values. To accommodate heteroskedasticity, one can change $M_1(K_i)$ into a heteroskedasticity-robust individual VR test.

Whang and Kim (2003) Test: They use a subsampling technique to develop a multiple VR test. When sample size (T) is relatively small, this test outperforms the conventional VR tests, and shows little to no serious size distortions. The statistic is:

$$MVR_T = \sqrt{T} \max_{1 \leq i \leq m} |VR(K_i) - 1|$$

and the sampling distribution function for the MVR_T statistic is asymptotically a maximum of a multivariate normal vector with an unknown covariance matrix, which would be complicated to estimate. Therefore, they proposed to approximate the null distribution by means of the subsampling approach. For a subsample of size b: $(x_t, \cdots, x_{t-b+1})$ where $t = 1, \cdots, T - b + 1$. The statistic MVRs calculated from all individual subsamples would generate a $(1-\alpha)$th percentile for the $100(1-\alpha)\%$ critical value. To implement this subsampling technique, a choice of block length b must be made. Whang and Kim (2003) recommended the interval of $(2.5T^{0.3}, 3.5T^{0.6})$, but they also found that the size and power properties of their test are not sensitive to b.

Belaire-Franch and Contreras (2004) Test: This is a multiple rank and sign VR tests, an extension to the Wright's rank- and sign-based tests. The test is based on the definition of Chow and Denning (1993) procedure. The rank-based procedures are exact under the i.i.d. assumption whereas the sign-based procedures are exact under both the i.i.d. and martingale difference sequence assumption. They showed that rank-based tests are more powerful than their sign-based counterparts.

Richardson and Smith (1991, Wald-Type Test): They suggested a joint test based on the following Wald statistic:

$$MVR_{RS}(K) = T(\mathbf{VR} - \mathbf{1})' \mathbf{\Phi}^{-1} (\mathbf{VR} - \mathbf{1})$$

where $\mathbf{VR}$ is the $K \times 1$ vector of sample K VRs, $\mathbf{1}$ is the $K \times 1$ unit vector; Φ is the covariance matrix of $\mathbf{VR}$. This statistic $MVR_{RS}(K)$ follows a χ^2 distribution with K degrees of freedom. One thing to remember about this test is that the VR tests are computed over Long lags with overlapping observations, the distribution of the VR test is NON-normal.

Cecchetti and Lam (1994, Wald-Type Test): They also developed a Wald-type multiple VR statistic that incorporates the correlations between VR statistics at various horizon and weights them according to their variances:

$$MVR_{CL}(K) = [\mathbf{VR}(K) - \mathbb{E}[\mathbf{VR(K)}]]' \mathbf{\Psi}^{-1}(K)[\mathbf{VR}(K) - \mathbb{E}[\mathbf{VR(K)}]]$$

Again, $\mathbf{VR}(K)$ is a vector of VR statistics and $\mathbf{\Psi}$ is a measure of the covariance matrix of $\mathbf{VR}$; and again, this statistic follows a χ^2 distribution with K degrees of freedom.

However, after using Monte Carlo techniques to study the empirical distribution of $MVR_{CL}(K)$, they have found that it has large positive skewness, not χ^2.

Chen and Deo (2006, Wald-Type Test): They proposed a joint VR test based on their individual power transformed VR statistic, also following a χ^2 distribution with K degrees of freedom. One feature sets the Chen and Deo test apart from the Richardson and Smith test and the Cecchetti and Lam test: this test is with ONE-sided alternative (i.e., $H_1 : \exists K_i$ s.t. $VR(K_i) < 1$).

1.1.3.3   Bootstrapping VR tests

Instead of using the subsampling method, some researchers proposed to employ a bootstrap method, which is distribution-free and can be used to estimate the sampling distribution of the VR statistic when the distribution of the original population is unknown.

Kim (2006) Test: Kim (2006) applied the wild bootstrap to the Lo and MacKinlay test and the Chow and Denning test in 3 stages:

(1) From a bootstrap sample of T observations $X_t^* = \eta_t X_t$, where η_t is a random sequence with $E(\eta) = 0, E(\eta^2) = 1$ and $t = 1, \cdots, T$

(2) For the bootstrap sample generated in (1), calculate $VR^* = VR(X^*, K_i)$

(3) Repeat (1) and (2) for a sufficient amount of times m, to form a bootstrap distribution of the test statistic $\left\{ VR(X^*, K_j; j) \right\}_{j=1}^{m}$

Conditional on X_t, X_t^* is a serially uncorrelated sequence with zero mean and variance X_t^2. Thus, wild bootstrapping approximates the sampling distributions under the null hypothesis, which is a desirable property for a bootstrap test. To perform the test, a specific form of η_t should be chosen. Kim (2006) recommended using the standard normal distribution for η_t.

Malliaropulos and Priestley (1999) Test: They used a weighted bootstrap method proposed by Wu et al. (1986), which is heteroskedasticity-robust and done by resampling normalized returns instead of actual returns. The bootstrap scheme can be summarized in 4 steps:

(1) For each t, draw a weighting factor z_t^* with replacement from the empirical distribution of normalized returns $z_t = (r_t - \bar{r})/\sigma(r)$, where $t = 1, \cdots, T, \bar{(r)} = E(r), \sigma(r) = Var(r)$.

(2) Form the bootstrap sample of T observations $\tilde{r}_t^* = z_t^* r_t$

(3) Calculate the VR statistic $VR^*(K)$ from the sample r_t^*

(4) Repeat steps (1) and (2) M times, obtaining $VR^*(K; m)_{1 \leq m \leq M}$

Using this procedure, resampling from normalized returns, the weighted bootstrap method accounts for the possible non-constancy of the variance of returns. This weighted bootstrap scheme is designed to overcome the difficulty that resampling methods may generate data that are less dependent than the original data. One thing to notice is that Malliaropulos and Priestley's method is not asymptotically pivotal and not supported by any asymptotic theory or Monte Carlo evidence to evaluate its properties, unlike Kim's method.

1.2   Autocorrelations in returns: empirical evidence

With the models introduced in Section 1.1.2, the mean reversion in stock returns has been examined empirically over the years. The common ground is that there are autocorrelations, but the directions of autocorrelations are indefinite across different settings.

A brief summary is listed below, and the details are discussed in the corresponding sub-sections.

1.2.1   Mean Riverse: Negative autocorrelations

1.2.2   Positive autocorrelations

Due to the positive cross-autocorrelations among individual stocks, **Stock indexes** have predominantly positive high-frequency autocorrelations.

1.2.2.1   Lo and MacKinlay (1988, 1990a)

Lo and MacKinlay (1988, 1990a) presented evidence that broad market indexes have predominantly positive high-frequency autocorrelations. In 1988, they found a 30% AR(1) with weekly returns of *September 1962* to *December 1985*, while higher-order ARs are also positive although smaller in magnitude. In 1990a, they found similar results with the sample period extended to *December 1987*. They proposed that the equal-weighted index autocorrelation could be rewritten into the sum of own-autocovariances and cross-autocovariances of the component securities. Given that the autocorrelations of individual stock returns are generally negative, they deduced that the cross-autocovariances must be positive and large enough to exceed the sum of the negative own-autocovariances. They built the following model and showed the importance of the forecastability *across* securities for contrarian profits:

Consider a stylized contrarian investment strategy: buy stocks at time t that were losers at time $t - k$ and sell stocks at t that were winners at $t - k$. This strategy can be formally written as

$$\omega_{i,t}(k) = -\frac{1}{N}(R_{i,t-k} - R_{m,t-k}), \ i = 1, \cdots, N$$

where $R_{m,t-k} = \frac{1}{N}\sum_{i=1}^{N} R_{i,t-k}$ is the market (equal-weighted) index return.

By construction, $\vec{\omega}_t(k) \equiv [\omega_{1,t}(k), \cdots, \omega_{N,t}(k)]'$ is an arbitrage portfolio since the weights sum to zero. Such a strategy is designed to take advantage of stock market overreactions since the stocks whose returns deviate more from the market index return will be given higher weights (more positive for huge losers and vice versa). Profit generated from this strategy is $\pi_t(k) = \sum_{t=1}^{N} \omega_{i,t}(k)R_{i,t}$, rewrite this profit, get:

$$\pi_t(k) = \sum_{i=1}^{N} \omega_{i,t}(k)R_{i,t} = -\frac{1}{N}\sum_{i=1}^{N}\left(R_{i,t-k} - R_{m,t-k}\right)R_{i,t} = -\frac{1}{N}\sum_{i=1}^{N} R_{i,t-k}R_{i,t} + R_{m,t-k}R_{m,t}$$

take expectation, get:

$$E[\pi_t(k)] = -\frac{1}{N} \sum_{i=1}^{N} E\left[R_{i,t-k}R_{i,t}\right] + E\left[R_{m,t-k}R_{m,t}\right]$$

$$= -\frac{1}{N} \sum_{i=1}^{N} \left(Cov\left[R_{i,t-k}, R_{i,t}\right] + \mu_i^2\right) + \left(Cov\left[R_{m,t-k}, R_{m,t}\right] + \mu_m^2\right)$$

where $\mu_m \equiv E[R_{m,t}] = \mu'\iota/N$. Reorganizing this equation into 3 components:

$$E[\pi_t(k)] = -\frac{1}{N}tr(\Gamma_k) - \frac{1}{N}\sum_{i=1}^{N}\mu_i^2 + \frac{\iota'\Gamma_k\iota}{N^2} + \mu_m^2$$

$$= \underbrace{\left\{\frac{\iota'\Gamma_k\iota}{N^2} - \frac{1}{N}tr(\Gamma_k)\right\}}_{\mathbf{L_k}} - \left\{\frac{1}{N}\sum_{i=1}^{N}(\mu_i - \mu_m)^2\right\}$$

$$= \underbrace{\frac{1}{N^2}\left[\iota'\Gamma_k\iota - tr(\Gamma_k)\right]}_{\mathbf{C_k}} + \underbrace{\left(-\frac{N-1}{N}\right)tr(\Gamma_k)}_{\mathbf{O_k}} - \underbrace{\frac{1}{N}\sum_{i=1}^{N}(\mu_i - \mu_m)^2}_{\sigma^2(\mu)} \qquad (1.7)$$

where $tr(\cdot)$ indicates the trace operator (sum of diagonal elements).

The three components are:

- : $\mathbf{C_k}$ depends ONLY on the off-diagonals of the auto-covariance matrix Γ_k
- : $\mathbf{O_k}$ depends ONLY on the diagonals of the auto-covariance matrix Γ_k
- : $\sigma^2(\mu)$ is independent of Γ_k

Or, cross-autocovariances dictate $\mathbf{C_k}$, own-autocovariances dicate $\mathbf{O_k}$, this is the separation needed.

With this decomposition, the authors explained that the profitability of such a contrarian strategy could be perfectly consistent with a **positively autocorrelated market index** and **negatively autocorrelated individual security returns**.

They also presented 5 illustrative scenarios:

A. *I.I.D. returns*
    - $\forall k, \Gamma_k = 0, L_k = C_k = O_k = 0$, thus, $E[\pi_t(k)] = -\sigma^2(\mu) \leq 0$.
    - *Intuition*: When returns do follow random walks, any cross-sectional variation in expected returns would generate negative expected profits when trading with a contrarian strategy. Since the strategy is reduced to shorting the higher and buying the lower mean return securities. BUT, $\sigma^2(\mu)$ is generally small.
B. *Stock market overreaction*
    - *Assumption*: negative self-autocorrelations and zero cross-autocorrelations, i.e., the diagonal elements of Γ_k are negative, the non-diagonal elements are

0. Thus, ignoring the small $\sigma^2(\mu)$, the expected profit is

$$E[\pi_t(k)] \simeq L_k = O_k = -\left(\frac{N-1}{N}\right) tr(\Gamma_k) = -\left(\frac{N-1}{N}\right) \sum_{i=1}^{N} \gamma_{ii}(k) > 0$$

- *Intuition*: In a overreacting market, "what goes up must come down" and vice versa. Thus, a contrarian investment strategy is profitable on average. A special case is the model of "fads": the sum of a random walk and an AR(1)[3].

C. *White noise and lead-lag relations*
  - *Assumption*: $\forall i \in [1, \cdots, N]$, the return is given by: $R_{i,t} = \mu_i + \beta_i \Lambda_{t-i} + \epsilon_{i,t}$, where $\beta_i > 0$, Λ is a serially independent common factor with zero mean and variance σ_λ^2, $\epsilon_{i,t}$ is assumed to be both cross-sectionally and serially independent. When $k < N$, the autocovariance matrix Γ_k has zeros in all entries except along the kth superdiagonal. On the kth superdiagonal, the elements are $\gamma_{i,i+k} = \sigma_\lambda^2 \beta_i \beta_{i+k}$, the profit is:

$$E[\pi_t(k)] \simeq L_k = C_k = \frac{\sigma_\lambda^2}{N^2} \sum_{i=1}^{N-k} \beta_i \beta_{i+k} > 0$$

  - *Intuition*: This is an artifact of the dependence of the ith security's return on a lagged common factor, where the lag is determined by i. Notice that the returns are serially independent, but sotck i's returns can be predicted with past returns of stock j, where $j < i$. With this cross-correlation, a contrarian strategy can still profit, as long as the cross autocovariances are sufficiently large.

D. *Nonsynchronous trading and lead-lag effects*[4]
  - *Assumption*:
  "Virtual" return: the returns for security $i \in [1, \cdots, N]$ are generated by: $R_{i,t} = \mu_i + \beta_i \Lambda_i + \epsilon_{i,t}$. Λ_t is some zero-mean, i.i.d. common factor, $\epsilon_{i,t}$ is zero-mean, serially and cross-sectionally independent. But this time the returns are *unobservable*, i.e., "virtual".
  Non-trade: in each period t, security i has an i.i.d. probability of p_i to be NOT traded. If not traded, a security's *observed* return $R_{i,t}^o$ is 0 while its true return is still given by $R_{i,t} = \mu_i + \beta_i \Lambda_i + \epsilon_{i,t}$.
  Observed return: The observed return of security i in period t is the sum of its virtual returns of all the past **consecutive non-trading** periods. Formally, $R_{i,t}^o = \sum_{k=0}^{\infty} X_{i,t}(k) R_{i,t-k}$. The weights $X_{i,t}(k) \equiv (1-\delta_{i,t})\delta_{i,t-1} \cdots \delta_{i,t-k}$, where δ_i is the (i.i.d.) non-trading indicator. $X_{i,t}(k)$ is also an indicator:

$$X_{i,t}(k) = \begin{cases} 1 & i \text{ is traded at } t, \text{ but not in any of the } k \text{ previous periods} \\ 0 & \text{otherwise} \end{cases}$$

---

[3]Notice that only AR(1) statisfies this conclusion.
[4]See Lo and MacKinlay (1990b) for a detailed discussion.

Nontrading duration: the nontrading duration, or the number of past consecutive periods that security i is not traded, is $\tilde{k}_{i,t} \equiv \sum_{k=1}^{\infty} \left(\prod_{j=1}^{k} \delta_{i,t-j} \right)$, its expectation is $E[\tilde{k}_{i,t}] = \frac{p_i}{1-p_i}$.

Portfolio return: for an equal-weighted portfolio of securities with common nontrading probability p_κ, the observed return to portfolio can be approximated as $R^o_{port,t} \to \mu_{port} + (1 - p_{port})\beta_{port} \sum_{k=0}^{\infty} p^k_{port} \Lambda_{t-k}$, where β_{port} is the average β of the securities. Then the observed return of the portfolio over q periods is $R^o_{port,T}(q) \equiv \sum_{t=(T-1)q+1}^{Tq} R^o_{port,t}$.

- *Intuition*:

  The "nontrading" problem aims to fix one problem: the prices of distinct securities are mistakenly assumed to be sampled simultaneously. Prices actually happen in different periods, but are treated as if they were observed at the same time. The "power" of a stock on others is related to how frequently it is traded: For a more frequently traded portfolio a, and a less frequently traded portfolio b, $R_{a,t-1}$ predicts $R_{b,t}$ better than $R_{b,t-1}$ predicts $R_{a,t}$. HOWEVER! This cannot fully explain the magnitude of weekly cross-autocorrelations.

E. *Positively dependent common factor and bid-ask spread*

- *Assumption:*

  $R_{i,t}$ as the sum of: (a) a positively autocorrelated common factor, (b) idiosyncratic white noise, (c) a bid-ask spread process. Formally,

  $$R_{i,t} = \mu_i + \beta_i \Lambda_i + \eta_{i,t} + \epsilon_{i,t}$$

  where $E[\Lambda_t] = 0$, $E[\Lambda_{t-k}\Lambda_t] \equiv \gamma_\lambda(k) > 0$ (positively autocorrelated common factor), $E[\epsilon_{i,t}] = E[\eta_{i,t}] = 0$ (idiosyncratic noise), $Var[\epsilon_{i,t}] = \sigma_i^2$.

  The bid-ask spread has a AR(1) as $E[\eta_{i,t-1}\eta_{i,t}] = -s_i^2/4$, where s_i is the percentage bid-ask spread. All higher-order ARs and all cross-correlations are zero.

  The autocovariance matrices are given by:

  $$\Gamma_k = \begin{cases} \gamma_\lambda(1)\vec{\beta}\vec{\beta}' - \frac{1}{4}diag[s_1^2, \cdots, s_N^2], & k = 1 \\ \gamma_\lambda(k)\vec{\beta}\vec{\beta}', & k > 1 \end{cases}$$

  where $\vec{\beta} \equiv [\beta_1, \cdots, \beta_N]'$. The autocovariance matrices are all symmetric, which is the signature departing this model from the lead-lag process. The profitability is:

  $$L_k = \begin{cases} -\frac{\gamma_\lambda(1)}{N} \sum_{i=1}^{N}(\beta_i - \frac{\sum_{i=1}^{N}\beta_i}{N})^2 + \frac{N-1}{N^2} \sum_{i=1}^{N} \frac{s_i^2}{4}, & k = 1 \\ -\frac{\gamma_\lambda(k)}{N} \sum_{i=1}^{N}(\beta_i - \frac{\sum_{i=1}^{N}\beta_i}{N})^2, & k > 1 \end{cases}$$

- *Intuition:*

  This model, developed by Roll (1984), will yield a positively autocorrelated market index since the white-noise and bid-ask components will be averaged out, leaving the common factor Λ_t. However, for individual securities,

the bid-ask spread could dominate the common factor, yielding negative autocorrelations.

The positive profit of a contrarian strategy on returns generated by this model is solely due to the bid-ask spread (or the negative AR). In other words, if the portfolio is weighted using lags 2 or higher, the strategy will only generate negative profit.

With the profit decomposed in Equation (1.7), Lo and MacKinlay used 551 stocks that have no missing weekly returns from Jul 6, 1962 to Dec 31, 1987. They made the estimates for individual stocks and for 3 size-sorted quintiles. Their results can be summarized as:

1. From lag 1 to even lag 4, the esimated expected profits $\hat{E}[\pi_t(k)]$ are positive. This contradicts the prediction of the common factor plus bid-ask spread model (positive only at lag 1, negative for higher lags).

2. Although $\hat{E}[\pi_t(k)]$ is significant even at lag 4, the two components of the profits $\hat{C}_k$ and $\hat{O}_k$ are NOT significant. This suggests that $\hat{C}_k$ and $\hat{O}_k$ are negatively correlated and cancelling each other's noise. Since both $\hat{C}_k$ and $\hat{O}_k$ are functions of second moments and co-moments, the correlations are perhaps a result of co-skewness or kurtosis.

3. The cross-autocorrelation matrices for the size-sorted quintiles show that current returns of smaller stocks are correlated with past returns of large stocks. This asymmetry of autocorrelation matrices implies the autocovariance matrix Γ_k is also asymmetric, contradicting the bid-ask spread model again.

4. the cross-autocorrelation matrices also contradicts, at least partially, the non-trading model since they require an unrealistically high probability of non-trading.

1.2.2.2 Froot and Perold (1995)

Froot and Perold (1995) examined the positive autocorrelations of high-frequency index returns with various market indexes and trade frequencies. The authors linked the positive correlations to an information-based explanation: slow dissemination and inefficient processing of market-wide information. They build a simple model and show the index's theoretical autocorrelations fall with an increase in the dissemination speed of market-wide information. Furthurmore, they attribute this decrease of positve index autocorrelations entirely to cross-stock autocorrelations. Self-autocorrelations of stocks are relatively persistent.

A brief summary of the model:

1. N stocks, managed by risk-neutral specialists individually. The true value is $V_t^i \equiv V_t + \xi_t^i$, where V_i and ξ_t^i follow independent random walks where the innovations are i.i.d. normal: $\Delta V_t = u_t \sim \mathcal{N}(0, \sigma_u^2)$, $\Delta \xi_t^i = e_t^i \sim \mathcal{N}(0, \sigma_e^2)$

2. Trading cost and technical delays of information dissemination:
   - delayed observation of value: V_t^i is observed at $t+1$
   - instant observation of order flow: $F_t^i = u_t + e_t^i + v_t^i$, where $u_t + e_t^i$ is an informed-traders' component, the i.i.d. $v_t^i \sim \mathcal{N}(0, \sigma_v^i)$ is the "liquidity"

traders' component.

- optimal price: $P_t^i = \lambda F_t^i + V_{t-1}^i$ where $\lambda = \frac{\sigma_u^2 + \sigma_e^2}{\sigma_u^2 + \sigma_e^2 + \sigma_v^2}$ is the OLS estimator of $u_t + e_t^i$ on F_t^i.
- price change from $t-1$ to t: $\Delta P_t^i = \lambda(u_t + e_t^i + \Delta v_t^i) + (1-\lambda)(u_{t-1} + e_{t-1}^i)$

3. Self-autocorrelations and cross-autocorrelations:
   - Self-autocovariances: $Cov(\Delta P_t^i, \Delta P_{t-1}^i) = 0$
   - Cross-autocovariances: $Cov(\Delta P_t, \Delta P_{t-1}) = \frac{N-1}{N}(1-\lambda)\lambda \sigma_u^2 > 0$

4. Fast market-wide information dissemination:
   - V_t is observable at t instead of $t+1$: V_t trade is costless, so traders would earn positive net profits unless innovation in V_t are fully incorporated in current prices. A futures market might serve as a *billboard*, making the current value publicly observable.
   - optimal price: $P_t^i = \lambda'(F_t^i - u_t) + V_{t-1}^i + u_t$, where $\lambda' = \frac{\sigma_e^2}{\sigma_e^2 + \sigma_v^2}$
   - price change of stock i at t: $\Delta P_t^i = \lambda'(e_t^i + \Delta v_t^i) + (1-\lambda')e_{t-1}^i + u_t$
   - cross-stock autocovariances: $Cov(\Delta P_t, \Delta P_{t-1}) = \frac{N-1}{N}Cov(u_t, u_{t-1}) = 0$, it disappears!

Empirical evidence

- *Main results*: Froot and Perold (1995) first examine a very short-horizon return series: 15-minute returns of S&P 500 cash index from 1983-02 to 1989-12. They found 2 main results:
  1. There are significant positive autocorrelations for 15-minute index returns.
  2. The positive autocorrelations declined/disappeared in the 1980s.

They rule out two alternative interpretations: **bid-ask bounce** and **nontrading effect** as the driving force of this decrease in autocorrelation (in other words, separate overreaction from the **information dissemination**).

- *Bid-ask bounce*: As described above, bid-ask bounce could lower the level of AR coefficients. In 1980s, bid-ask spread increased, leading to an increase in bounce; Investors tended to trade more frequently in portfolios, leading to greater synchronousness of buys and sells, leading to higher bid-ask bounce. These two facts could be linked to the decline/disappearance of the positive ARs.

  To rule this explanation out, Froot and Perold examined higher-order ARs. Bid-ask bounce would lead to equal-size reduction in all ARs, instead of just AR(1). The empirical evidence proved otherwise.

  They also separated bid-ask component from the last-trade index. They define L_t as the index of last-trade prices and M_t the index of extant midquotes for each last-trade price, the returns of them as $l_t = \ln(L_t/L_{t-1})$ and $m_t = \ln(M_t/M_{t-1})$. $L_t - M_t$ measures the distance between the last trade index and the log bid-ask error $l_t - m_t \simeq \Delta(L_t - M_t)$ as ϵ_t.

  $\frac{Cov(l_t, l_{t-1}) - Cov(m_t, m_{t-1})}{Var(l_t)} = \frac{Cov(\epsilon_t, \epsilon_{t-1})}{Var(l_t)} + \frac{Cov(m_t, \epsilon_{t-1})}{Var(l_t)} + \frac{Cov(m_{t-1}, \epsilon_t)}{Var(l_t)}$ can be used to measure bid-ask effects. They report that the bid-ask component only accounts for 1/3 of the change in the AR of last trade index.

  $\leftarrow$ If $\epsilon_t > 0$, there is a greater fraction of buys at time t then at time $t-1$

  When considering the three sub-components individually, they report:

- $\frac{Cov(\epsilon_t, \epsilon_{t-1})}{Var(l_t)}$, a pure measure of Roll-type bounce, declines marginally from 1983 to 1988, while the self-autocovariance $\frac{\sum_i^N (\omega^i)^2 Cov(\epsilon_t^i, \epsilon_{t-1}^i)}{Var(l_t)}$ of the index (squared-weighted sum of self-ARs of all stocks) increases. This means that bid-ask bounce in individual stocks becomes less important and the average bid-ask spread narrows, while cross-correlation in bid-ask bounce becomes more negative and portfolio trading increases. But in general, the number is too small to explain the change in the correlation of the last-trade index.

- $\frac{Cov(m_t, \epsilon_{t-1})}{Var(l_t)}$ measures the correlation between past increases in buys/sells and current increases/decreases in the midquote index, this measure is large and positive empirically but converging to 0 over time. 2 possible explanations are considered:

  (1) **eating-through-the-roder-book (ETOB)**: Suppose there is a limit order at the ask price and more limit orders with higher prices, then buy orders come in and deals are made firstly at the ask price and then move to higher price orders gradually. This way, when buy order flow is positively autocorrelated (for example, big trades are broken up and executed sequentially), an increase in buy order tends to forecast an increase in the ask price, therefore, an increase in the future midquote index.

  (2) **sluggish-response-to-roder-flow (SRFI)**: The order-flow information of a given stock is incorporated into quotes for other stocks slowly over time. For example, a buy order at the ask of GM stock (increases ϵ_{t-1}) might provide incremental information about the value of Ford, and therefore might be associated with an increase in Ford's quotes.

  The main difference between **ETOB** and **SRFI** is that ETOB is an own-stock effect, while SRFI is a cross-stock effect. And Froot and Perold show that **SRFI** appears to be correct, which means that bid-ask bounce cannot explain the empirical observations.

- $\frac{Cov(m_{t-1}, \epsilon_t)}{Var(l_t)}$ measures the covariance between past increases/decreases in the midquote index and current buys/sells. This statistic is negative and decreasing over time. 2 possible explanations were considered as well:

  (1) **see-'em-coming (SEC)**: specialists expect the upcoming order flow and raise/reduce prices as buy/sell orders arrive (bid-ask prices rise/fall as buy/sell orders peak locally, therefore m_{t-1} and ϵ_t are negatively correlated).

  (2) **slow-responce-to-price-information (SRPI)**: some stocks' quoted prices respond slowly to information (sticky), when the quickly-responding stocks trade at higher/lower quote prices, the "sticky" stocks' quoted prices remain the same. Smart investors will buy/sell these sticky stocks to profit.

  Once again, SEC is an own-stock effect while SRPI is a cross-stock effect. Emperically, the authors proved that SRPI appears correct.

In summary, Froot and Perold proved that bid-ask effects only account for 1/3 of the decline of AR. of this 1/3, nearly 1/2 might be attributed to slow-responce-to-information hypotheses (SRFI and SRPI).

- *Nontrading*: They examined two factors of the non-trading effect: trade frequency and degree of synchronousness. They calculated a measure of *staleness*: the difference between last-trade midquote m_t and the *current* midquote cm_t: $m_t = cm_t + s_t = cm_t + (m_t - cm_t)$, where cm_t is the return on the current midquote index, free of staleness and bid-ask bounce. Empirically, the decline of AR of cm_t is greater than that of m_t, which means that nontrading staleness does NOT explain the reduction of index's AR.

Define equally-weighted current midquote index as eq_t (versus value-weighted index cm_t) and $z_t = cm_t - eq_t$, then decompose the autocovariance of cm_t, get: $\frac{Cov(cm_t,cm_{t-1})}{Var(l_t)} = \frac{Cov(eq_t,eq_{t-1})}{Var(l_t)} + \frac{Cov(eq_t,z_{t-1})}{Var(l_t)} + \frac{Cov(z_t,eq_{t-1})}{Var(l_t)} + \frac{Cov(z_t,z_{t-1})}{Var(l_t)}$, loosely speaking, the four items on the right-hand side can be seen as a predictability matrix:

		Predictee	
		small stocks	large stocks
Predicter	small stocks	$\frac{Cov(eq_t,eq_{t-1})}{Var(l_t)}$	$\frac{Cov(z_t,eq_{t-1})}{Var(l_t)}$
	large stocks	$\frac{Cov(eq_t,z_{t-1})}{Var(l_t)}$	$\frac{Cov(z_t,z_{t-1})}{Var(l_t)}$

If stocks respond symmetrically to market-wide information, the decline in the AR of cm_t would be distributed equally across the four components. However, the authors showed than the decline in AR of cm_t was driven by $\frac{Cov(eq_t,eq_{t-1})}{Var(l_t)}$ and $\frac{Cov(z_t,eq_{t-1})}{Var(l_t)}$, in other words, it has become more difficult to predict small stocks' returns, no matter with other small stocks' returns or large stocks' returns.

To incorporate information dissemination, consider $\frac{Cov(m_t,m_{t-1})}{Var(l_t)} - \frac{Cov(cm_t,cm_{t-1})}{Var(l_t)} = \frac{Cov(s_t,s_{t-1})}{Var(l_t)} + \frac{Cov(s_t,cm_{t-1})}{Var(l_t)} + \frac{Cov(cm_t,s_{t-1})}{Var(l_t)}$, where s_t is the new information in quotes beyond that reflected in the trade. They found that the changes of both $\frac{Cov(s_t,s_{t-1})}{Var(l_t)}$ and $\frac{Cov(s_t,cm_{t-1})}{Var(l_t)}$ are negligible, while $\frac{Cov(cm_t,s_{t-1})}{Var(l_t)}$ was negative and rising over time, which means the responsiveness of current quotes (cm_t) to information between $t-1$ and the last trade as of time $t-1$ (s_{t-1}) declines, the evdience of more rapid dissemination of market-wide information.

With market excess return data from Kenneth French's website, I replicate the AR(1)s of daily returns from 1926 to

1.3   Excess volatility puzzle

[insert text]

1.4   Decomposing prices

[insert text]

1.4.1   Campbell-Schiller decomposition

[insert text]

1.4.2   Lettau-Ludvigson decomposition

[insert text]

1.5   Prediction zoo

[insert text]

1.6   Issues and extensions

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TERM STRUCTURE OF RETURNS

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In this chapter, I summarize the stylized facts and models of intrest rates, and, combining with the time-series and cross-sectional properties of equities, discuss how the term structure of equity can be incorporated into the asset pricing dynamic. Instead of assuming the risk-free rate to be one period, as classic asset pricing models implying in the Euler equations and SDFs, one would expect that an ideal asset pricing model could not only explain the dynamic of equity, but reconcile the property of the term structure of interest rates as well.

The first part of this chapter summarizes studies of risk free bonds and the term structure of this asset class.

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