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Topic 6: DID and TWFE

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Key points: This note is on the causal panel data, building upon Arkhangelsky and Imbens (2023).

Disclaimer: This note is compiled by Sai Zhang.

6.1 Panel Data Configurations

6.1.1 Data Types

6.1.1.1 Panel Data

For observations on N units, indexed by $i = 1, \dots, N$, over T periods, indexed by $t = 1, \dots, T$, the outcome of interest is denoted by Y_{it} , the treatment W_{it} . These observations may themselves consist of averages over more basic units:

$$\mathbf{Y} = \begin{pmatrix} Y_{11} & \cdots & Y_{1T} \\ \vdots & \ddots & \vdots \\ Y_{N1} & \cdots & Y_{NT} \end{pmatrix} \qquad \mathbf{W} = \begin{pmatrix} W_{11} & \cdots & W_{1T} \\ \vdots & \ddots & \vdots \\ W_{N1} & \cdots & W_{NT} \end{pmatrix}$$

we may also observe exogenous variables X_{it} or X_i . Typically, we focus on a balanced panel where for all units $i = 1, \dots, N$ we observe outcomes for all $t = 1, \dots, T$.

6.1.1.2 Grouped Repeated Cross-Section Data

In a GRCS data, we have observations on N units, each observed only once in period T_i for unit i. Different units may be observed at diffrent points in time, T_i typically takes on only a few values, with many units sharing the same value for T_i . The outcome Y_i and treatment W_i are indexed by the unit index i. The set of units is **partitioned** into 2 or more groups, with the group that unit i belongs to denoted by $G_i \in \mathcal{G} = \{1, 2, \dots, G\}$.

Define the average outcomes for each group-time-period pair:

$$\overline{Y}_{gt} \equiv \frac{\sum_{i=1}^{N} \mathbf{1}_{G_i = g, T_i = t} Y_i}{\sum_{i=1}^{N} \mathbf{1}_{G_i = g, T_i = t}}$$

for treatment

$$\overline{W}_{gt} \equiv \frac{\sum_{i=1}^{N} \mathbf{1}_{G_i = g, T_i = t} W_i}{\sum_{i=1}^{N} \mathbf{1}_{G_i = g, T_i = t}}$$

then treat the $G \times T$ group averages \overline{Y}_{gt} and \overline{W}_{gt} as the unit of observation, then the grouped data is just a panel. The major issue in practice is that the number of groups is very small comparing to proper panel data.

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6.1.1.3 Row and Column Exchangeable Data

The data are doubly indexed by $i=1,\cdots,N$ and $j=1,\cdots,J$, with outcomes Y_{ij} . They are different from panel data in that there is **no time ordering** for the second index. Many methods developed for panel data are also applicable here.

6.1.2 Shapes of Data Frames

6.1.3 Assignment Mechanisms

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References

Dmitry Arkhangelsky and Guido Imbens. Causal models for longitudinal and panel data: A survey. Technical report, National Bureau of Economic Research, 2023.