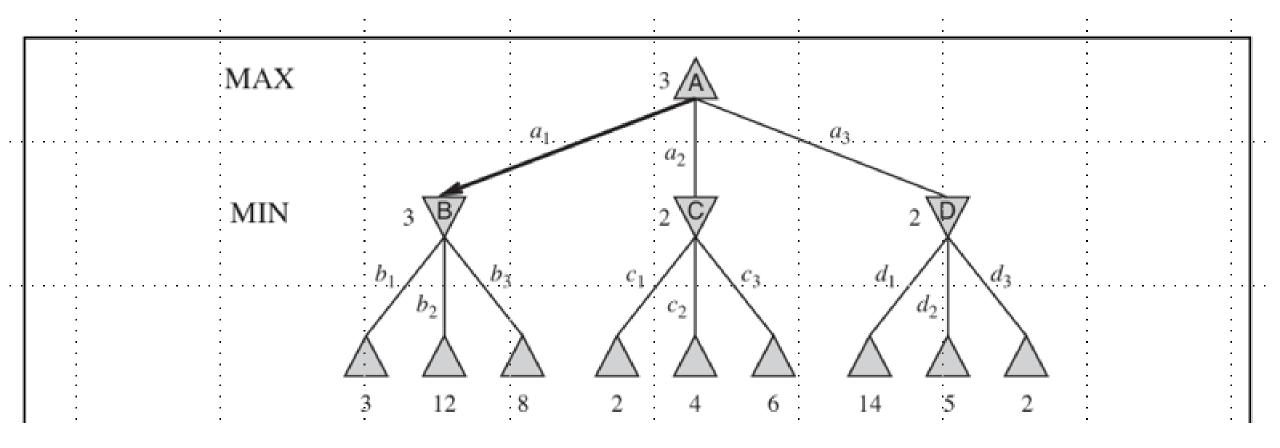
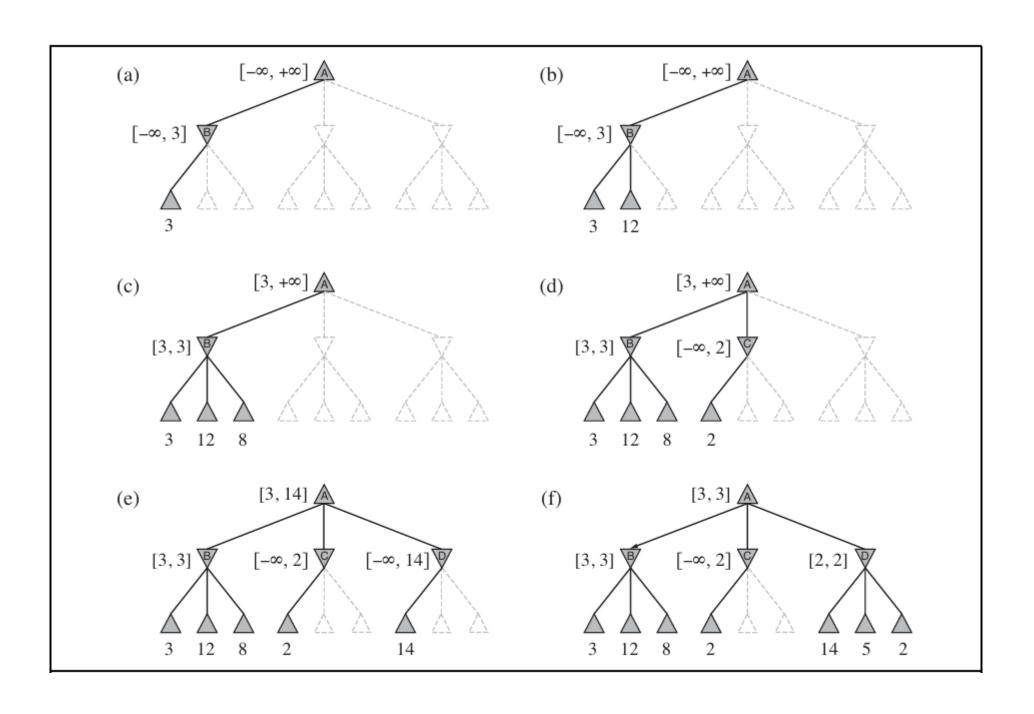
Alpha-Beta Pruning

- The problem with minimax search is that the number of game states it has to examine is exponential in the depth of the tree.
- Unfortunately, we can't eliminate the exponent, but it turns out we can effectively cut it in half.
- The trick is that it is possible to compute the correct minimax decision without looking at every node in the game tree.
- That is, we can borrow the idea of pruning to eliminate large parts of the tree from consideration.
- The particular technique we examine is called alpha—beta pruning.

- The Max player will only update the value of alpha.
- The Min player will only update the value of beta.
- While backtracking the tree, the node values will be passed to upper nodes instead of values of alpha and beta.
- We will only pass the alpha, beta values to the child nodes.

· The condition used by alpha beta pruning to prune the useless branches is:





```
\begin{aligned} \text{MINIMAX}(\textit{root}) &= \max(\min(3, 12, 8), \min(2, x, y), \min(14, 5, 2)) \\ &= \max(3, \min(2, x, y), 2) \\ &= \max(3, z, 2) \quad \text{where } z = \min(2, x, y) \leq 2 \\ &= 3. \end{aligned}
```

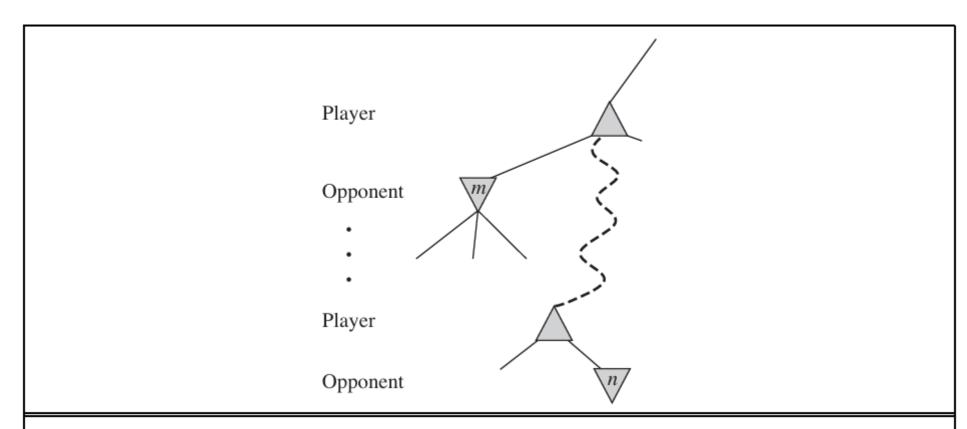


Figure 5.6 The general case for alpha—beta pruning. If m is better than n for Player, we will never get to n in play.

- α = the value of the best (i.e., highest-value) choice we have found so far at any choice point along the path for MAX.
- β = the value of the best (i.e., lowest-value) choice we have found so far at any choice point along the path for MIN.

```
function ALPHA-BETA-SEARCH(state) returns an action
   v \leftarrow \text{Max-Value}(state, -\infty, +\infty)
   return the action in ACTIONS(state) with value v
function MAX-VALUE(state, \alpha, \beta) returns a utility value
  if TERMINAL-TEST(state) then return UTILITY(state)
   v \leftarrow -\infty
  for each a in ACTIONS(state) do
      v \leftarrow \text{MAX}(v, \text{MIN-VALUE}(\text{RESULT}(s, a), \alpha, \beta))
     if v \geq \beta then return v
     \alpha \leftarrow \text{MAX}(\alpha, v)
   return v
function MIN-VALUE(state, \alpha, \beta) returns a utility value
   if TERMINAL-TEST(state) then return UTILITY(state)
   v \leftarrow +\infty
  for each a in ACTIONS(state) do
      v \leftarrow \text{MIN}(v, \text{MAX-VALUE}(\text{RESULT}(s, a), \alpha, \beta))
     if v \leq \alpha then return v
     \beta \leftarrow \text{MIN}(\beta, v)
  return v
```

Figure 5.7 The alpha–beta search algorithm. Notice that these routines are the same as the MINIMAX functions in Figure 5.3, except for the two lines in each of MIN-VALUE and MAX-VALUE that maintain α and β (and the bookkeeping to pass these parameters along).