

Assignment - 4

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Simple linear regression

Sample(i)	x_i^a	y_i^b
1	7.6	157
2	7.1	174

Step 1: Read dataset, $\eta = 0.01$, $\text{epchecks} = 1$, $m = 1$, $c = -1$

Step 2: set iteration = 1

Step 3: set sample $i = 1$

Step 4: $\hat{y} = mx + c$

$$\hat{y} = 0(7.6) - 1 = -0.6$$

Step 5: $E = \frac{1}{2} (y_i^a - mx_i^a - c)^2$

$$E = \frac{1}{2} (157 - 0(7.6) - (-1))^2$$

$$= \frac{22620.16}{2} = 11310.08$$

Step 6: $\frac{\partial E}{\partial m} = -(y_i^a - mx_i^a - c) x_i^a$

$$= -(157 - 0.6)(7.6) = -1143.04$$

$$\frac{\partial E}{\partial c} = -(y_i^a - mx_i^a - c) = -(157 - 0.6) = -150.4$$

Step 7: $\Delta m = -\eta \frac{\partial E}{\partial m} = -(0.01)(-1143.04)$

$$= 11.4304$$

$$\Delta c = -\eta \frac{\partial E}{\partial c} = -(0.01)(-150.4) = 1.504$$

Step 8: $m = m + \Delta m = -1 + 11.4304 = 10.4304$

$$c = c + \Delta c = -1 + 1.504 = 0.504$$

Step 9: Sample $i = 1 \rightarrow 2$ & $i \leq n_s \rightarrow \text{step 4}$

Step-4: $y = (12.5304)(7.1) + 0.504$

$= y = 89.469$

Step-5: $E = \frac{1}{2} (174 - 89.469)^2$

$= 7127.011$

Step-6: $\frac{\partial E}{\partial m} = -((174 - (12.5304)(7.1) - (0.504))7.1)$

$= 600.164$

$\frac{\partial E}{\partial m} = 600.164$

Step-7: $\Delta m = -\eta \frac{\partial E}{\partial m} = -(0.01)(600.164)$

$= -(0.01)(7127.011)$

$= -71.27$

$\Delta c = -\eta \frac{\partial E}{\partial c} = -(0.01)(600.164) = -6.001$

Step 8: $m = 12.5304 + (-71.27) = -58.7396$

$c = 0.504 + (-6.001) = -5.497$

Step 9: Sample $i = i + 1 = 2 + 1 = 3$ $i_3 \leq n$, $T \rightarrow$ next step

Step-10: $\text{iter} = \text{iter} + 1 = 1 + 1 = 2$ $\text{iter}_2 > \text{epochs}$

Step 11: Stop $T \rightarrow$ next step