

Assignment - 7

- Q) Draw a decision tree diagram to predict no. of hours to play based on weather conditions like outlook, humidity, windy. Consider data set shown below.

Outlook	Temperature	Humidity	windy	hours to play.
Rainy	Hot	High	false	25
Rainy	Hot	High	True	30
Overcast	Hot	High	false	46
Sunny	Mild	High	false	45
Sunny	Cool	Normal	True	52
Sunny	Cool	Normal	True	23
Overcast	Cool	Normal	false	43
Rainy	Cool	Normal	false	38
Sunny	Mild	Normal	True	46
Rainy	Mild	Normal	True	48
Overcast	Mild	High	True	52
Overcast	Hot	Normal	false	44
Sunny	Mild	High	True	30

Termination Criteria $CVC = 10\%$ or min no. of samples = 4

~~100~~ 10
10/12/21

Calculation of mean, standard deviation, co-efficient of variation

$$\text{mean} = \frac{\sum x}{n} = \frac{557}{14} = 39.78$$

$$SD = \sqrt{\frac{\sum (x - \text{mean})^2}{n}} = 9.67$$

$$CV = \frac{SD}{\text{mean}} \times 100 = \frac{9.67}{39.78} \times 100 = 24.30$$

Here, data set is split into different attributes. The SD of each branch is calculated

$SD(\text{auto}) = \sum w(\text{branch}) \cdot SD(\text{branch})$ & then SDR (Standard reduction deviation reduction) is calculated.

$$SDR = SD - SD(\text{auto})$$

$$SD = 9.67$$

out look	mean	SD	CV	n	w(w)
Rainy	35.7	8.7	24.07	5	5/14
over cast	46.25	4.03	8.72	4	4/14
Sunny	39.2	12.2	31.0	5	5/14

$$\therefore SD(\text{out look}) = 5/14 \times 8.7 + \frac{4}{14} \times 4.03 + \frac{5}{14} \times 12.2 = 8.59$$

$$SDR(\text{out look}) = SD - SD(\text{out look})$$

$$= 9.67 - 8.59$$

$$= 1.08$$

Temperature

Temp	mean	SD	CV	n	w(V)
hot	36.25	10.34	30.6	4	4/14
cool	39	12.14	31.1	4	4/14
mild	43.6	8.38	19.65	6	6/14

$$\therefore SD(\text{temperature}) = \frac{4}{14} \times 10.34 + \frac{4}{14} \times 12.14 + \frac{6}{14} \times 8.38 = 10.01$$

$$SDR(\text{Temp}) = SD - SD(\text{temp}) = 9.67 - 10.01 = -0.34$$

Humidity

Humidity	mean	SD	CV	n	w(V)
High	37.51	10.11	26.92	7	7/14
normal	42	9.4	22.4	7	7/14

$$\therefore SD(\text{humidity}) = \frac{7}{14} \times 10.11 + \frac{7}{14} \times 9.4 = 9.77$$

$$SDR(\text{humidity}) = SD - SD(\text{humidity})$$

$$= 9.67 - 9.77 = -0.1$$

windy:

windy	mean	SD	CV	n	w(V)
True	37.6	11.6	30.8	6	6/14
False	41.3	8.41	20.3	8	8/14

$$\therefore SD(\text{windy}) = \frac{6}{14} \times 11.6 + \frac{8}{14} \times 8.41 = 9.77$$

$$SDR(\text{windy}) = SD - SD(\text{windy}) = 9.67 - 9.77 = -0.1$$

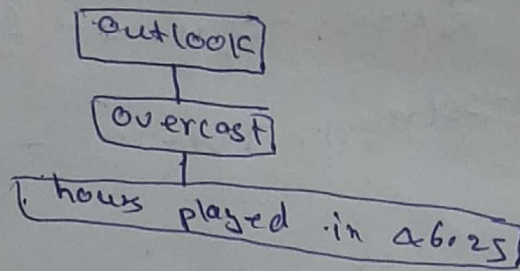
The value that has highest SDR is considered as root node (i.e., decision node)

considering termination criteria

CV is 10% or CV is $(n \leq)$

outlook.

overcast has CV of 8% which is less than threshold value therefore, we need not go to further splitting



we need to split sunny & rainy columns

summary

outlook	Temp	Humidity	windy	hours played
sunny	mild	high	false	45
sunny	cool	normal	false	52
sunny	cool	normal	true	23
sunny	mild	normal	false	46
sunny	mild	high	true	30

mean = 39.2, SD = 12.2, CV = 31.0

Temperature

Temp	mean	SD	CV	n	w(V)
mild	40.3	8.96	22.73	3	315
cold	35.5	20.50	54.66	2	215

$$SD(\text{Temp}) = \frac{3}{5} \times 8.96 + \frac{2}{5} \times 20.50 = 13.576$$

$$SDR(\text{Temp}) = SD - SD(\text{Temp}) = 12.2 - 13.576 = -1.37$$

humidity

humidity

high

mean

sd

cv

n

w(v)

37.5

10.6

28.26

2

2/5

normal

40.3

15.3

37.96

3

3/5

$$sd(humidity) = \frac{2}{5} \times 10.6 + \frac{3}{5} \times 15.3 = 13.42$$

$$sdr(humidity) = sd - sd(humidity)$$

$$= 12.2 - 13.42$$

$$= -1.22$$

windy

windy

false

mean

sd

cv

n

w(v)

47.66

3.78

7.94

3

3/5

True

26.5

4.94

18.65

2

2/5

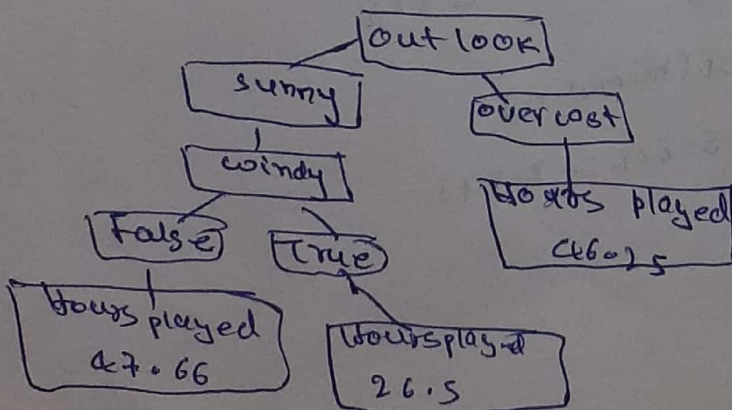
$$sd(windy) = \frac{3}{5} \times 3.78 + \frac{2}{5} \times 4.94 = 4.23$$

$$sdr(windy) = sd - sd(windy) = 12.2 - 4.23 = 7.97$$

In outlook, among temp, humidity & wind sdr value is high
for windy sdr = 7.97

Then check for cv value

Both true & false satisfy the cv value



Rainy

outlook	temp	humidity	windy	Hours played.
Rainy	hot	high	False	25
Rainy	hot	high	True	30
Rainy	mild	high	False	35
Rainy	cool	normal	False	38
Rainy	mild	normal	True	48

mean = 35.2, SD = 8.7, CV = 24.7

Temperature

Temp	mean	SD	CV	n	COV
Hot	27.5	3.53	12.83	2	215
Mild	41.5	9.19	22.14	2	215
Cool	38	0	0	1	115

$$SD(temp) = \frac{2}{5} \times 3.53 + \frac{2}{5} \times 9.19 + \frac{1}{5} \times 0 = 5.088$$

$$SDE(temp) = SD - SD(temp) = 8.7 - 5.088 = 3.612$$

Humidity

Humidity

Humidity	mean	SD	CV	n	COV
high	30	5	16.66	3	315
normal	43	7.07	16.44	2	215

$$SD(humidity) = \frac{3}{5} \times 5 + \frac{2}{5} \times 7.07 = 5.828$$

$$SDE(humidity) = SD - SD(humidity) = 8.7 - 5.828 = 2.872$$

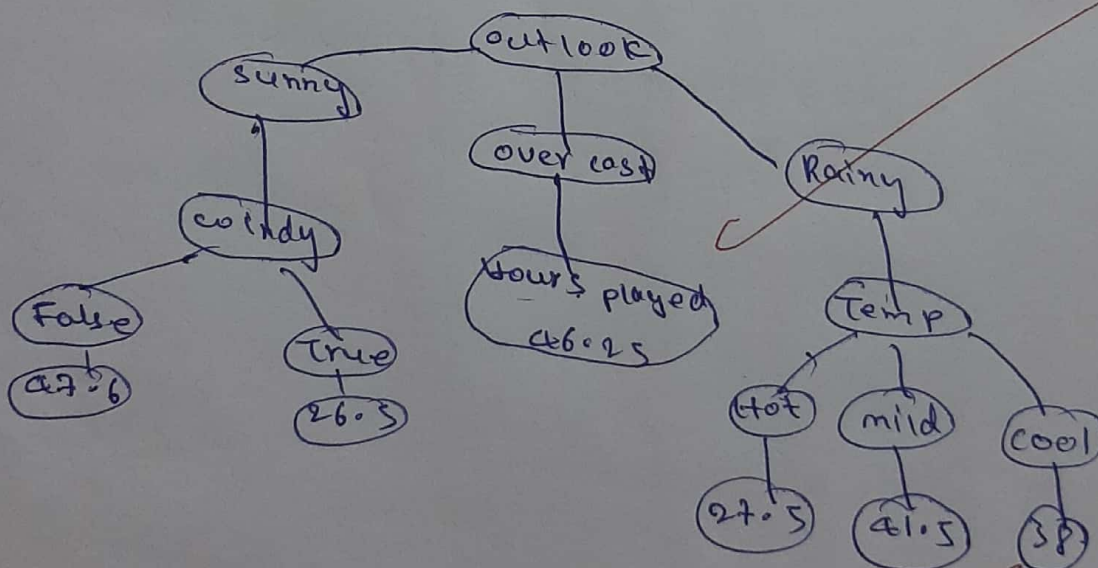
windy:-

windy	mean	sb	cv	n	w/w)
False	32.66	6.80	20.85	3	315
True	39	12.72	32.5	2	215

$$SD(windy) = \frac{3}{5} \times 6.80 + \frac{2}{5} \times 12.72 = 9.168$$

$$SPR(windy) = sb - sb(windy) = 8.7 - 9.168 = -0.468$$

Among temp, humidity & windy the SPR Value is high for temp (i.e. 3.612). Then check for cv value at hot, mild, cold. Satisfy the cv value Decision tree diagram to predict number of hours to play based on weather conditions



(Signature)