

Data Mining H.W. 3-21

Sai Parthibh Mandumula
(1002022847)

1. Let Anthony be represented as 'a'

Burton as 'b'

Caesar as 'c1'

Calpurnia as 'c2'

cleopatra as 'c3'

\therefore log weighted tf $\rightarrow \begin{cases} \log_{10} tf, & tf > 0 \\ 0, & \text{otherwise} \end{cases}$

* log weighted

| | Anthony & cleopatra | Scilius Caesar | The tempest | Hamlet |
|------------------|---------------------|----------------|-------------|--------|
| a \rightarrow | 3.195 | 2.86 | 2.69 | 3 |
| b \rightarrow | 1.60 | 3.19 | 2 | 1.30 |
| c1 \rightarrow | 3.36 | 1.30 | 3.35 | 3 |
| c2 \rightarrow | 0 | 2 | 0 | 0 |
| c3 \rightarrow | 2.75 | 0 | 0 | 2.77 |

* $\frac{\text{log weighted IDF}}{2DF}$

$\rightarrow \log_{10} \left(\frac{N}{df} \right)$

| | |
|----|------|
| a | 0.30 |
| b | 1.30 |
| c1 | 0.22 |
| c2 | 1.30 |
| c3 | 1.69 |

TF-IDF vector representation
Anthony & Cleopatra (A)

$$\rightarrow 0.957a + 2.02b + 0.73c_1 + 0c_2 + 4.64c_3$$

$$\text{Julius Caesar (J)} \rightarrow 0.86a + 4.15b + 0.29c_1 + 26c_2 + 0c_3$$

$$\text{The Tempest (T)} \rightarrow 0.81a + 2.6b + 0.24c_1 + 0c_2 + 0c_3$$

$$\text{Hamlet (H)} \rightarrow 0.9a + 1.69b + 0.66c_1 + 0c_2 + ~~2.84c_3~~ 4.84c_3$$

$$\|A\| = 5.236$$

$$\|J\| = 4.921$$

$$\|T\| = 2.82$$

$$\|H\| = 4.341$$

\therefore Normalized TF-IDF vector representation.

$$A \rightarrow 0.12a + 0.46b + 0.14c_1 + 0c_2 + 0.89c_3$$

$$J \rightarrow 0.17a + 0.83b + 0.06c_1 + 0.52c_2 + 0c_3$$

$$T \rightarrow 0.29a + 0.92b + 0.26c_1 + 0c_2 + 0c_3$$

$$H \rightarrow 0.21a + 0.39b + 0.15c_1 + 0c_2 + 0.80c_3$$

* Cosine similarities b/w 'Anthony & Cleopatra' and other

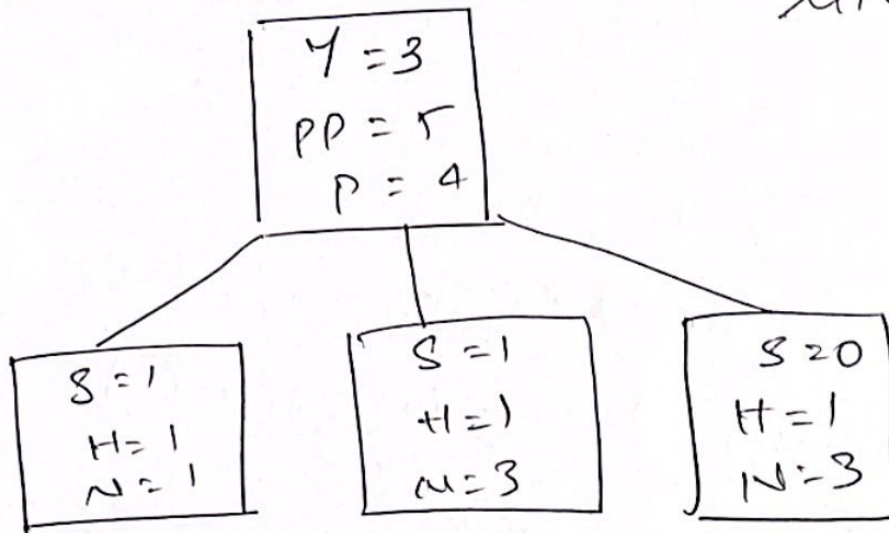
$$A - J = 0.371$$

$$A - T = 0.4566$$

$$A - H = 0.998$$

\therefore 'Anthony & Cleopatra' is most similar to 'Hamlet'.

② ① Age as the root



$$\text{Gini}(\text{Parent}) = 1 - \left[\frac{2^2 + 3^2 + 7^2}{12^2} \right] = 0.569$$

$$\text{Gini}(Y) = 1 - \left[\frac{1^2 + 1^2 + 1^2}{3^2} \right] = 0.67$$

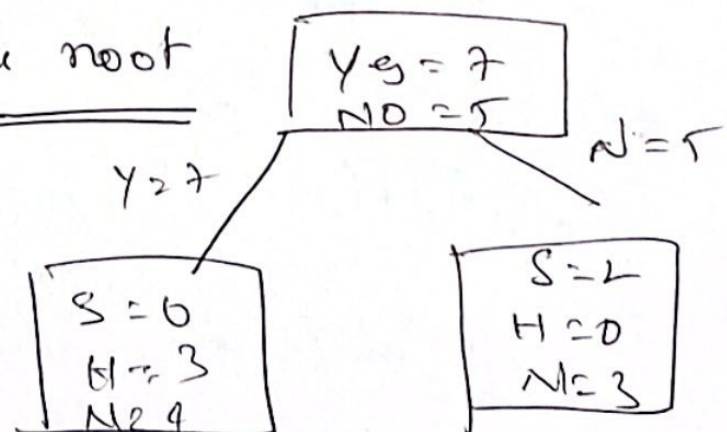
$$\text{Gini}(PP) = 1 - \left[\frac{1^2 + 1^2 + 3^2}{5^2} \right] = 0.56$$

$$\text{Gini}(P) = 1 - \left[\frac{1^2 + 3^2}{4^2} \right] = 0.375$$

$$\text{Child Split} = 3/12(0.67) + 5/12(0.56) + 4/12(0.375) = 0.525$$

$$\begin{aligned} \text{Gain} &= \text{Gini}(\text{Parent}) - \text{Gini}(\text{Child}) \\ &= 0.569 - 0.525 \\ &= \underline{\underline{0.044}} \end{aligned}$$

③ Stigmation as the root



$$GINI(Y) = 1 - \left[\frac{3^2 + 4^2}{7^2} \right] = 0.489$$

$$GINI(N) = 1 - \left[\frac{2^2 + 3^2}{5^2} \right] = 0.48$$

$$\text{Child Split} = \frac{7}{12} (0.489) + \frac{5}{12} (0.48) = 0.48525$$

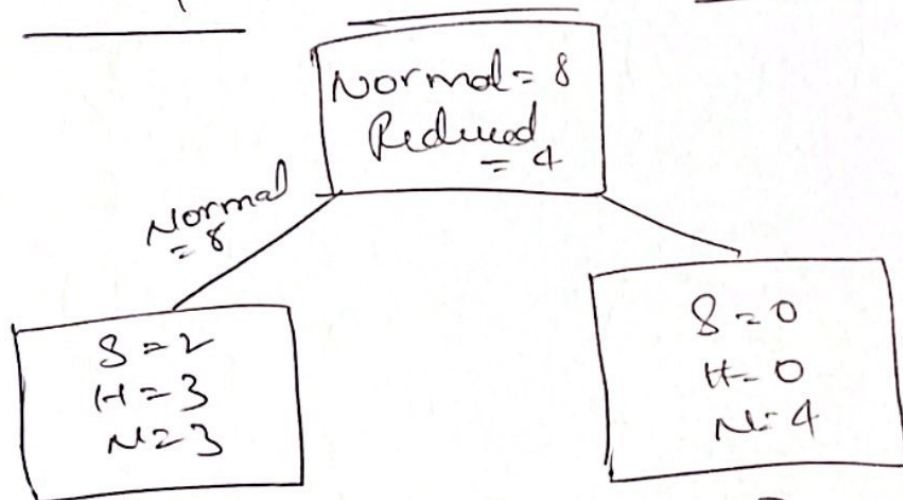
$$\text{Gain} = GINI(\text{Parent}) - GINI(\text{Child})$$

$$= 0.569 - 0.48525$$

$$= \underline{\underline{0.08375}}$$

$$\begin{array}{r} 0.569 \\ 0.48525 \\ \hline 0.08375 \end{array}$$

③ Leaf Production Rate as the root



$$GINI(N) = 1 - \left[\frac{2^2 + 3^2 + 3^2}{8^2} \right] = 0.656$$

$$GINI(R) = 1 - \left[\frac{4^2}{4^2} \right] = 0$$

$$\text{Child Split} = \frac{8}{12} [0.656] + \frac{4}{12} [0] = 0.437$$

$$\therefore \text{Gain} = \text{GINI}(\text{Parent}) - \text{GINI}(\text{child})$$

$$= 0.569 - 0.437$$

$$= 0.132$$

Since we get the highest gain with the ~~age~~ ^{Temperature} as the root, we will proceed with ~~age~~ ^{Temperature} as the root node.

③ Test Instance attribute

| outlook | Temperature | Humidity | windy |
|---------|-------------|----------|-------|
| Rainy | Cool | High | True. |

$$P(\text{play Golf} = Y/A) = P(A/\text{play Golf} = \text{Yes}) \cdot P(\text{play Golf} = \text{Yes})$$

$$P(\text{play Golf} = \text{No}/A) = P(A/\text{play Golf} = \text{No}) \cdot P(\text{play Golf} = \text{No})$$

we calculate the following

$$P(\text{play Golf} = \text{Yes}) = 9/14$$

$$P(\text{play Golf} = \text{No}) = 5/14 \rightarrow P(\text{outlook} = \text{Rainy}/\text{play Golf} = \text{Yes}) = 4/9$$

$$P(\text{Temperature} = \text{cool}/\text{play Golf} = \text{Yes}) = \frac{3}{9}$$

$$P(\text{Temperature} = \text{cool}/\text{play Golf} = \text{No}) = 1/5$$

$$P(\text{windy} = \text{True}/\text{play Golf} = \text{No}) = 3/9$$

$$P(\text{windy} = \text{True} / \text{Play Golf} = \text{N}) = 3/5$$

$$P(\text{outlook} = \text{Rainy} / \text{Play Golf} = \text{N}) = 3/5$$

$$P(\text{Humidity} = \text{High} / \text{Play Golf} = \text{N}) = 3/9$$

$$P(\text{Humidity} = \text{High} / \text{Play Golf} = \text{N}) = 4/5$$

~~P(windy)~~

$$P(\text{play Golf} = \text{Yes} / A) =$$

$$(2/9) (3/9) (3/9) (3/9) (1/14) = 5.29 \times 10^{-3}$$

$$P(\text{play Golf} = \text{No} / A) =$$

$$(3/5) (1/5) (4/5) (3/5) (5/14) = 20 \times 10^{-3}$$

Test attributes class \rightarrow play golf = No

4) a) Keeping the samples in mind,

Support Vectors (+ve class) $\rightarrow (0, 2), (2, 0)$

Support Vectors (-ve class) $\rightarrow (-2, -2)$

For the +ve hyperplane; $\vec{w} \cdot \vec{x} + b = 1$

For the -ve hyperplane; $\vec{w} \cdot \vec{x} + b = -1$

$$\rightarrow 0w_1 + 2w_2 + b = 1 \quad \text{--- (1)}$$

$$2w_1 + 0w_2 + b = -1 \quad \text{--- (2)}$$

$$-2\omega_1 - 2\omega_2 + b = -1$$

$$\Rightarrow 2\omega_1 + 2\omega_2 - b = 1 \quad \text{--- (3)}$$

By (1) in (3), and (2) in (3)

$$(1-b) + (1-b) - b = 1$$

$$2 - 3b = 1$$

$$\boxed{b = 1/3} \quad \text{--- (4)}$$

with (4) in (1) and (2), we get

$$\boxed{\begin{matrix} \omega_1 = 1/3 \\ \omega_2 = 1/3 \end{matrix}}$$

$$\textcircled{b} \text{ margin} = \frac{2}{\|w\|} = \frac{2}{0.471} = \underline{\underline{4.242}}$$

$$\|w\| = \sqrt{(1/3)^2 + (1/3)^2} \\ = \underline{\underline{0.471}}$$

$$\textcircled{c} \omega_1 x_1 + \omega_2 x_2 + b \\ (1/3 \times -1) + (1/3 \times -1) + 1/3 \\ = -1/3 - 1/3 + 1/3 = \underline{\underline{-1/3}}$$

So, the score ≤ 0 , it will lie ~~above~~ below the hyperplane. Hence, it will be of the ~~positive~~ negative class.