

Date: 4/2/19

Digital Systems - Notes

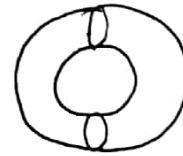
①

FOUR VARIABLE K-MAP

$$F(A,B,C,D) = \sum m(0,2,3,8,9,14,15)$$

AB \ CD	00	01	11	10
00	m_0	m_1	m_2	m_3
01	m_4	m_5	m_6	m_7
11	m_{12}	m_{13}	m_{14}	m_{15}
10	m_8	m_9	m_{10}	m_{11}

→ imagine that the columns are wrapped around

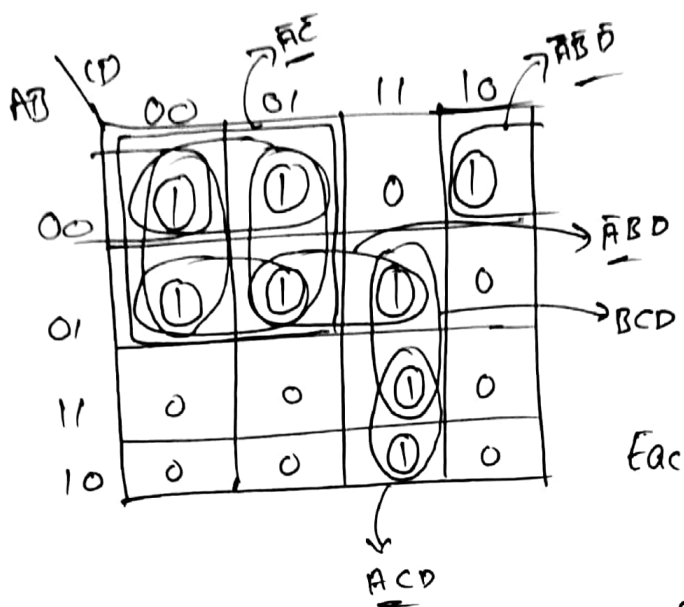


→ columns and rows both are wrapped around

CD \ AB	00	01	11	10
00	0	4	12	8
01	1	5	13	9
11	3	7	15	11
10	2	6	14	10

AB \ CD	00	01	11	10
00	0	4	12	8
01	1	5	13	9
11	3	7	15	11
10	2	6	14	10

AB \ CD	00	01	11	10
00	0	4	12	8
01	1	5	13	9
11	3	7	15	11
10	2	6	14	10



$$F = \sum m(0, 1, 2, 4, 5, 7, 11, 15)$$

Principle : $\bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D = \bar{A}\bar{B}\bar{C}$

Each () term in the wrapper is called an "Implicant" (because it implies that the funcⁿ is 1)

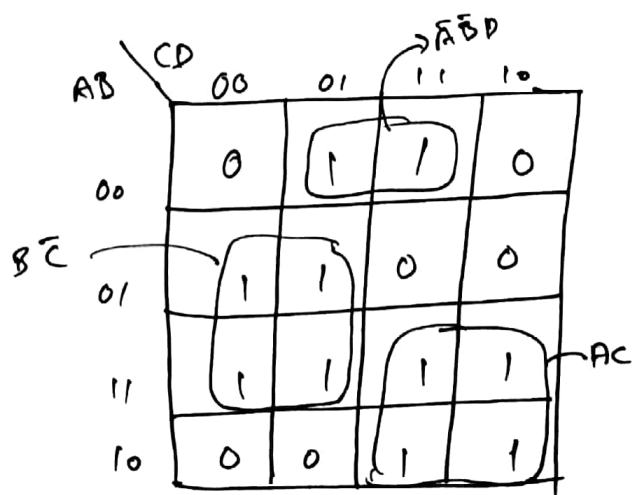
- All minterms (1's) have to be covered
- A 1 can be covered more than once.
- Prime Implicant - An implicant in which no new 1's can be added without dropping the existing 1's and covering the maximum possible 1's

Essential Prime Implicants: $\bar{A}\bar{C}$, $\bar{A}\bar{B}D$, ACD

Non-essential Prime Implicants: BCD , $\bar{A}BD$

$$F = \bar{A}\bar{C} + \bar{A}\bar{B}D + ACD + \underbrace{BCD + \bar{A}BD}_{\substack{\downarrow \\ \text{Choose} \\ \text{any one term}}}$$

$$F = \sum m(1, 3, 4, 5, 10, 11, 12, 13, 14, 15)$$



$$F = \sum m(0, 2, 3, 4, 8, 10, 11, 15)$$

