

### Linear programming sensitivity analysis:

Reg no: 23913

#### QUESTION A)

1. Formulate an LP that describes the production plans that the firm can use to maximize its profits

x1	x2	x3	x4			
70	140	60	110			
0	0	0	1333.333	146666.7		
40	40	30	30	40000	<=	40000
2	5	2	4	5333.333	<=	6000

**ANS:** So, the maximum profit is \$146666.7

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2. What would happen if the price of unfinished chairs went up?

**ANS:** Now the price of unfinished chairs is \$60 it can go until  $(60+50)$  \$110. Although the production of unfinished chairs is 0. No change in profit.

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3. What would happen if the price of unfinished tables went up?

**ANS:** Now the price of unfinished tables is \$70 it can go until  $(70+76.6667)$  \$146.6667. Although the production of unfinished tables is 0. So, No change in profit.

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4. What if the price of finished chairs fell to \$100?

**ANS:** If the price of finished chairs fell to \$100. Since the allowable decrease of this is \$105. So, there exist a new optimal solution

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5. How would profit change if lumber supplies changed?

**ANS:** Every foot of wood cost \$3.6667. So,

Allowable Increase – 45000

Allowable Decrease – 0

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6. How much would you be willing to pay an additional carpenter?

**ANS:** Out of 6000 working hours, we are utilizing only 5333.333 hours. So,

Allowable Decrease – 666.666

7. Suppose that industrial regulations complicate the finishing process, so that it takes one extra hour per chair or table to turn an unfinished product into a finished one. How would this change your plans?

x1	x2	x3	x4			
70	140	60	110			
3.13E-13	1000	0	0	140000		
40	40	30	30	40000	<=	40000
2	6	2	5	6000	<=	6000

**ANS:** If we change the finishing process by 1 unit each. The new constraint will be

$$2x_1 + 6x_2 + 2x_3 + 5x_4 \leq 6000$$

So, the maximum profit will change to \$140000. It is comparatively less. So, spending extra time for finishing process is reducing the total profit and **now we started producing 1000 finished tables from 0 tables and stopped producing 1333 finished chairs.**

8. The owner of the firm comes up with a design for a beautiful hand-crafted cabinet. Each cabinet requires 250 hours of labour (this is 6 weeks of full time work) and uses 50 board feet of lumber. Suppose that the company can sell a cabinet for \$200, would it be worthwhile?

x1	x2	x3	x4				
70	140	60	110	200			
0	0	0	1328.767	2.739726	146712.3		
40	40	30	30	50	40000	<=	40000
2	5	2	4	250	6000	<=	6000

**ANS:** After adding the 200 additional profit and 50 foot woods and 250 hours. We got \$146712.3 profit. We see there is an increase in profit.

So, it is recommended to make the hand-crafted cabinet.

