

## Definition of a control system:-

A system that manages, commands, directs or regulates the behaviour of other devices or systems.

- ఇది ఒక system, మనం చెప్పినట్లు చేసే machines or devices ని control చేస్తుంది.

Control systems are 2 types → open-loop → NO-feedback  
→ closed-loop → uses feedback to adjust output

### 1. Advantages of closed-loop systems :-

- Accuracy
- Error correction
- Disturbance rejection.

\* But more complex and costlier than open-loop systems.

### Basic elements of a control system:-

- ⇒ 1. Input
- 2. controller
- 3. Actuator
- 4. process/plant
- 5. output
- 6. Feedback sensor

### Examples of control system

- ⇒ Cruise control
- ⇒ fan speed regulator
- ⇒ air conditioner
- ⇒ autopilot systems

## purpose of feedback

Feedback helps maintain the desired output by comparing actual output with desired input and correcting any deviation.

⇒ Mathematical modelling:- systems are modeled using differential equations or transfer functions for analysis.

⇒ Block Diagrams:-

Representation of a control system using blocks to show components and their connections.

⇒ Control system objectives

- stability
- Accuracy
- Speed of response
- Disturbance Rejection
- Robustness.

Course Overview:- Designing controllers for dynamic systems.

Approach:- Visualizing systems in terms of inputs and outputs.

Example:- DC motor

Input:- Voltage

Output:- Rotational speed (RPM)

Goal:- Find the input voltage that produces the desired output speed.

Dynamic Systems Representation

- ⇒ Emphasis on transfer function
- ⇒ also touches state-space.



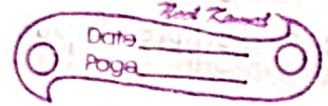
## controller design

→ focused on PID controllers

P → proportional

I → Integral

D → derivative



## \* \* performance Quantification tools:-

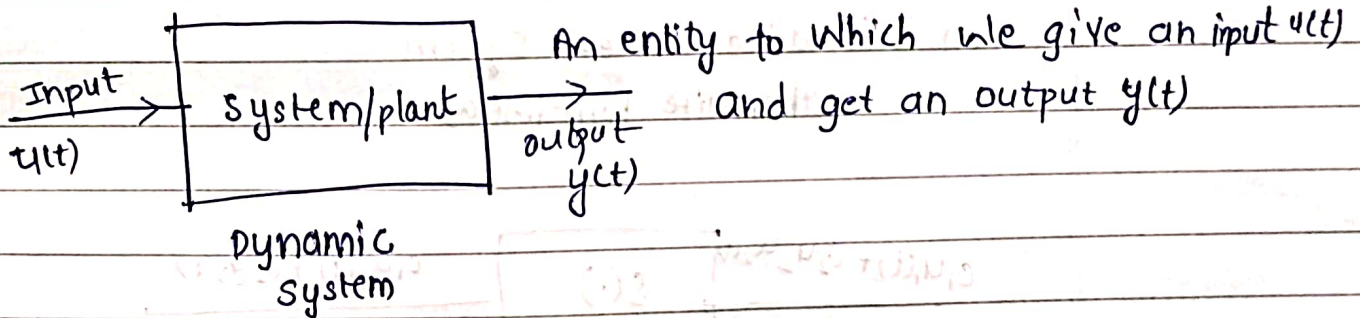
→ Root locus

⇒ Bode plot

→ Nyquist plot

⇒ Routh's stability criterion.

## System:-



↓  
Inputs, outputs are functions of time.

→ Time is independent variable

⇒ All variables are functions of time.  
↓  
associated with system

System:- A collection of objects / (a process) that is under study.

linear Time Invariant system

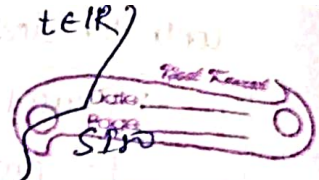
Mathematically, we can visualize a dynamic system as a mapping from  $u(t)$  to  $y(t)$ . That is,  $y(t) = S(u(t))$

classification of Dynamic system:-

(1) SISO & MIMO

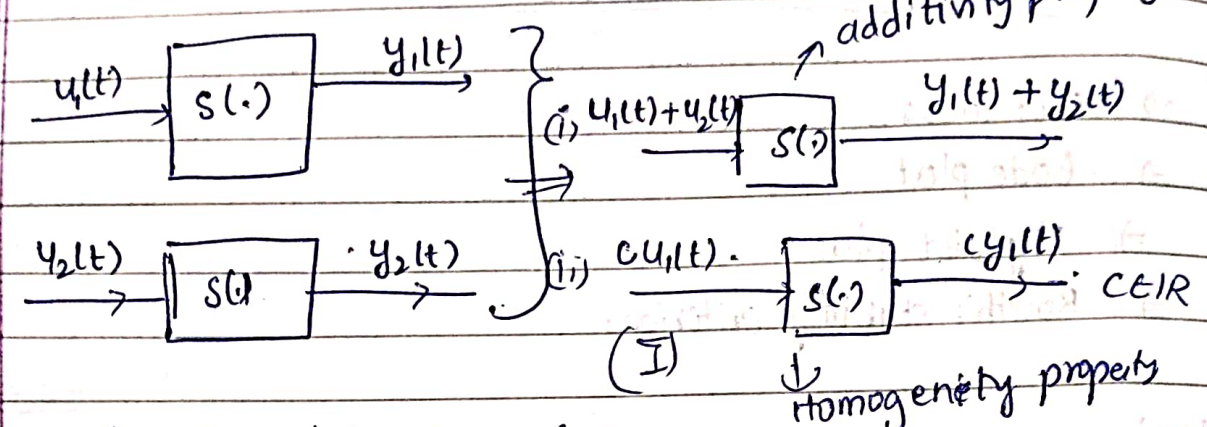


SISO: Single Input single output system  $\rightarrow u(t) : \mathbb{R} \rightarrow \mathbb{R} \quad t \in \mathbb{R}$   
 MIMO: Multiple Input Multiple output system  $\rightarrow y(t) : \mathbb{R} \rightarrow \mathbb{R}^p$

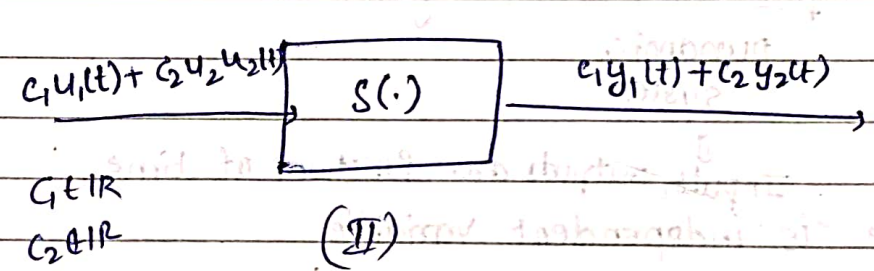


m inputs  
 p outputs  
 $m \geq 1$   
 $p \geq 1$   
 $u(t) : \mathbb{R} \rightarrow \mathbb{R}^m$   
 $y(t) : \mathbb{R} \rightarrow \mathbb{R}^p$

## 2) Linear v/s Nonlinear:-

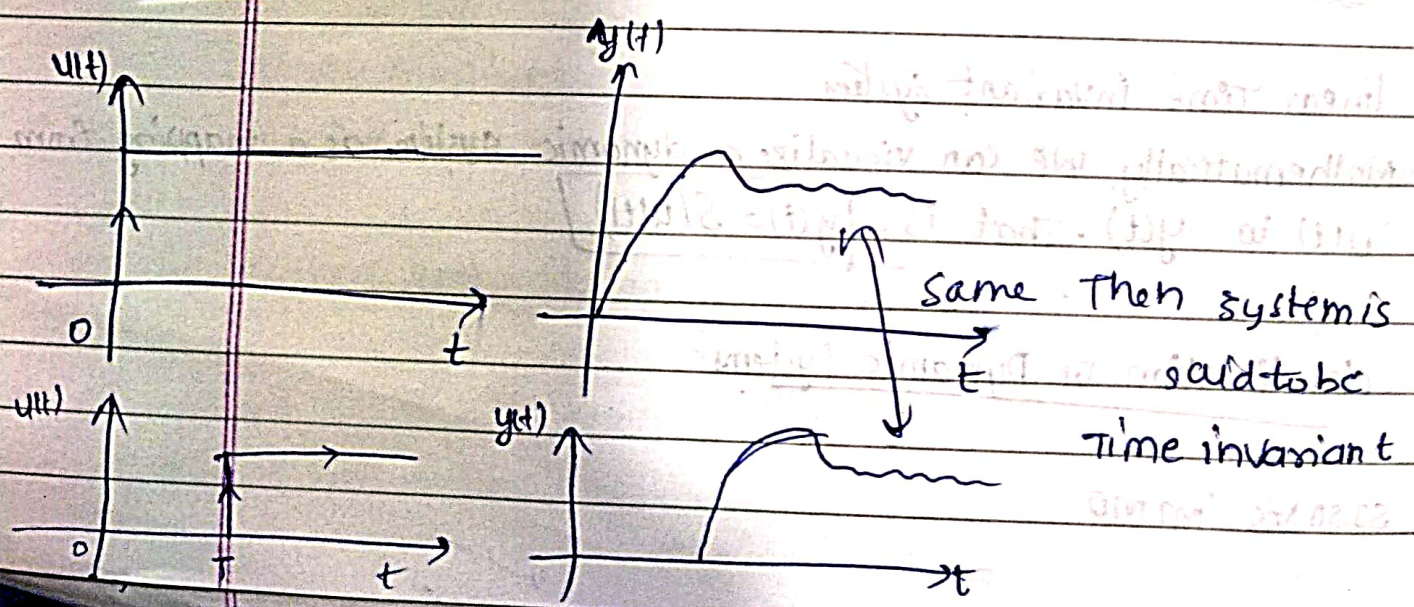


When (i) and (ii) are satisfied  
 then it is called linear system  
 otherwise Non-linear



principle of superposition

## 3) Time Varying system or Time Invariant system





A Time invariant system is one that provides the same output for the same input irrespective of when input is given

We work with Time Invariant system

mathematically  $y(t) = s(u(t))$

then Time invariance implies  $\Rightarrow \boxed{y(t-T) = s(u(t-T))} \forall T \in \mathbb{R}$

(4) Causal & Non-causal system :-

A causal system is one where the output at any instant of time depends only on past and current inputs

$\Rightarrow$  A causal system is NON-ANTICIPATIVE  
 $\Downarrow$   
Not depending on future inputs.

If  $y(t) \Rightarrow$  depends on  $x(t), x(t-1), x(t-2), \dots \Rightarrow$  it's causal & non-anticipative  
if  $y(t) \rightarrow$  depends on  $x(t+k) \quad k > 0 \Rightarrow$  it's non-causal & anticipative.

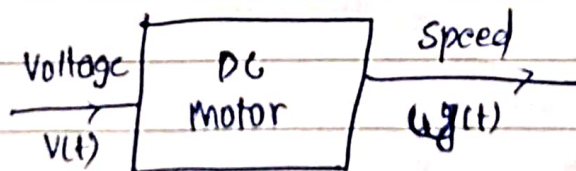
class of systems

$\Downarrow$   
we are going to focus

SISO LINEAR TIME INVARIANT CAUSAL DYNAMIC SYSTEMS  
LTI

useful class

CONTROL:- Making a system behave as desired



Q : If we wish to achieve a  $\omega_{des}$ , what is the input voltage that should be provided?

Approach:- (1) develop a mathematical representation for  $S(s) \rightarrow$  mathematical modelling

→ mathematical modelling of dynamic systems

- 2) Analyse the system response
- 3) design the controllers



1. physics based
2. Data Driven/ Empirical
3. Mixed approach