



# INSTITUTE OF AERONAUTICAL ENGINEERING (Autonomous)

Dundigal, Hyderabad - 500 043

## COMPUTER SCIENCE AND ENGINEERING

### QUESTION BANK

|                    |  |                        |         |            |         |
|--------------------|--|------------------------|---------|------------|---------|
| Course Title       | DIFFERENTIAL EQUATIONS AND VECTOR CALCULUS |                        |         |            |         |
| Course Code        | AHSD08                                     |                        |         |            |         |
| Program            | B.Tech                                     |                        |         |            |         |
| Semester           | II   | COMMON TO ALL BRANCHES |         |            |         |
| Course Type        | Foundation                                 |                        |         |            |         |
| Regulation         | IARE - BT23                                |                        |         |            |         |
| Course Structure   | Theory                                     |                        |         | Practical  |         |
|                    | Lecture                                    | Tutorials              | Credits | Laboratory | Credits |
|                    | 3  | 1                      | 4       | -          | -       |
| Course Coordinator | Dr.P.Raja Kumari, Assistant Professor      |                        |         |            |         |

### COURSE OBJECTIVES:

The students will try to learn:

|     |  |
|-----|--|
| I   | The analytical methods for solving first and higher order differential equations with constant coefficients. |
| II  | The analytical methods for formation and solving partial differential equations .                            |
| III | The physical quantities of vector valued functions involved in engineering field..                           |
| IV  | The logic of vector theorems for finding line, surface and volume integrals..                                |

### COURSE OUTCOMES:

After successful completion of the course, students should be able to:

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| CO 1 | <b>Utilize</b> the methods of differential equations for solving the orthogonal trajectories and Newton's law of cooling.                          | Apply      |
| CO 2 | <b>Solve</b> the higher order linear differential equations with constant coefficients by using method of variation of parameters.                 | Apply      |
| CO 3 | <b>Make use of</b> analytical methods for PDE formation to solve boundary value problems.  | Apply      |
| CO 4 | <b>Identify</b> various techniques of Lagrange's method for solving linear partial differential equations which occur in Science and engineering.. | Apply      |
| CO 5 | <b>Interpret</b> the vector differential operators and their relationships for solving engineering problems.                                       | Understand |

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| CO 6 | <b>Apply</b> the integral transformations to surface, volume and line of different geometrical models. | Apply |
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### QUESTION BANK:

| Q.No  | QUESTION   | Taxonomy | How does this subsume the level   | CO's |
|---|--|----------|---|------|
| <b>MODULE I</b>   |  |          |   |      |
| <b>FIRST ORDER AND FIRST DEGREE ORDINARY DIFFERENTIAL EQUATIONS</b> |  |          |   |      |
| <b>PART A-PROBLEM SOLVING AND CRITICAL THINKING QUESTIONS</b>       |  |          |   |      |
| 1   | Find the general solution of the following differential equation<br>$x^2ydx - (x^3 + y^3)dy = 0$         | Apply    | Learner to recall the homogeneous differential equations, understand the exactness ,integrating factor and apply them to compute solution | CO 1 |
| 2   | Solve the given differential equation<br>$2xydy - (x^2 + y^2 + 1)dx = 0$ to get the general solution     | Apply    | Learner to recall the homogeneous differential equations, understand the exactness ,integrating factor and apply them to compute solution | CO 1 |
| 3   | Determine the general solution of the differential equation<br>$(1 + x^2)\frac{dy}{dx} + 2xy = 4x^2$ .   | Apply    | Learner to recall the homogeneous differential equations, understand the exactness ,integrating factor and apply them to compute solution | CO 1 |
| 4   | Find the general solution for the given linear differential equation<br>$\frac{dy}{dx} + 2y = e^x + x$ , | Apply    | Learner to recall the homogeneous differential equations, understand the exactness ,integrating factor and apply them to compute solution | CO 1 |

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| 5  | Prove that the system of parabolas $y^2 = 4a(x + a)$ is self orthogonal  | Apply | Learner to recall the differential equations, understand the orthogonal trajectories and apply them to compute solution                           | CO 1 |
| 6  | The temperature of a cup of coffee is $92^\circ\text{C}$ , when freshly poured the room temperature being $24^\circ\text{C}$ . In one minute it was cooled to $80^\circ\text{C}$ . How long a period must elapse, before the temperature of the cup becomes $65^\circ\text{C}$ . | Apply | Learner to recall the differential equations, understand the variable separable, rate of change of temperature and apply them to compute solution | CO 1 |
| 7  | Find the orthogonal trajectories of the family of curves $x^2 + y^2 = a^2$   | Apply | Learner to recall the differential equations, understand the orthogonal trajectories and apply them to compute solution                           | CO 1 |
| 8  | Solve the given first order differential equation $(x^4 e^x - 2mxy^2)dx + 2mx^2ydy = 0$  | Apply | Learner to recall the homogeneous differential equations, understand the exactness, integrating factor and apply them to compute solution         | CO 1 |
| 9  | Find the Orthogonal trajectories of the family of circles passing through origin and centre on x-axis  | Apply | Learner to recall differential equations, understand the Orthogonal trajectories and apply them to compute solution                               | CO 1 |
| 10 | The temperature of the body drops from $100^\circ\text{C}$ to $75^\circ\text{C}$ in ten minutes when the surrounding air is at $20^\circ\text{C}$ temperature. What will be its temperature after half an hour. When will the temperature be $25^\circ\text{C}$                  | Apply | Learner to recall differential equations, understand the Newton's law of cooling and apply them to compute solution                               | CO 1 |

| PART-B LONG ANSWER QUESTIONS |   |       |   |      |
|------------------------------|---|-------|---|------|
| 1                            | Solve the differential equation $(1 + e^{\frac{x}{y}})dx + e^{\frac{x}{y}}(1 - \frac{x}{y})dy = 0$ to obtain the general solution   | Apply | Learner to recall the differential equations, understand the exactness of the function and apply them to compute solution | CO 1 |
| 2                            | Find the required general solution for given differential equation $(xe^{xy} + 2y)\frac{dy}{dx} + ye^{xy} = 0$  | Apply | Learner to recall the differential equations, understand the exactness of the function and apply them to compute solution | CO 1 |
| 3                            | Check whether the given differential equation is exact or not and find the solution $x^3 \sec^2 y \frac{dy}{dx} + 3x^2 \tan y = \cos x$   | Apply | Learner to recall the differential equations, understand the exactness of the function and apply them to compute solution | CO 1 |
| 4                            | Find the solution for given differential equation $(x^2 - y^2)dx = 2xydy$ by checking its exactness   | Apply | Learner to recall the differential equations, understand the exactness of the function and apply them to compute solution | CO 1 |
| 5                            | An object cools from $120^\circ\text{F}$ to $95^\circ\text{F}$ in half an hour surrounded by air whose temperature is $70^\circ\text{F}$ . Find its temperature at the end of another half an hour. | Apply | Learner to recall differential equations, understand the Newton's law of cooling and apply them to compute solution       | CO 1 |
| 6                            | Show that the system of rectangular hyperbolas $x^2 - y^2 = a^2$ and $xy = c^2$ are mutually orthogonal trajectories  | Apply | Learner to recall differential equations, understand the Orthogonal trajectories and apply them to compute solution       | CO 1 |
| 7                            | Solve the ordinary differential equation $x(x - 1)\frac{dy}{dx} - y = x^2(x - 1)^2$   | Apply | Learner to recall the differential equations, understand the exactness of the function and apply them to compute solution | CO 1 |

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| 8  | Solve the following differential equation<br>$e^x \frac{dy}{dx} = 2xy^2 + ye^x$  | Apply | Learner to recall the differential equations, understand the Bernoulli's equation and apply them to compute solution                     | CO 1 |
| 9  | A body kept in air with temperature $25^\circ\text{C}$ cools from $140^\circ\text{C}$ to $80^\circ\text{C}$ in 20 minutes. Find when the body cools down to $35^\circ\text{C}$ | Apply | Learner to recall differential equations, understand the Newton's law of cooling and apply them to compute solution                      | CO 1 |
| 10 | Solve the given differential equation<br>$x(1-x^2)\frac{dy}{dx} + (2x^2-1)y = x^3$   | Apply | Learner to recall the differential equations, understand the linear DE, integrating factor and apply them to compute solution            | CO 1 |
| 11 | Find the required general solution for given differential equation<br>$\frac{dy}{dx}(x^2y^3 + xy) = 1$   | Apply | Learner to recall the differential equations, understand the Bernoulli's equation, integrating factor and apply them to compute solution | CO 1 |
| 12 | Solve the differential equation<br>$2\frac{dy}{dx} - y\sec x = y^3\tan x$  | Apply | Learner to recall the differential equations, understand the linear DE, integrating factor and apply them to compute solution            | CO 1 |
| 13 | Solve the differential equation<br>$(1-x^2)\frac{dy}{dx} + xy = y^3\sin^{-1}x$   | Apply | Learner to recall the differential equations, understand the linear DE, integrating factor and apply them to compute solution            | CO 1 |
| 14 | Solve the differential equation<br>$(xy^2 - x^2)dx + (3x^2y^2 + x^2y - 2x^3)dy = 0$  | Apply | Learner to recall the differential equations, understand the exactness of the function and apply them to compute solution                | CO 1 |

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| 15                                   | Find the required general solution for given differential equation $x^2 \frac{dy}{dx} = e^y - x$                    | Apply    | Learner to recall the differential equations, understand the linear DE, integrating factor apply them to compute solution     | CO 1 |
| 16                                   | Solve the following differential equation $\frac{dy}{dx} + \frac{y \cos x + \sin y + y}{\sin x + x \cos y + x} = 0$ | Apply    | Learner to recall the differential equations, understand the exactness, and apply them to compute solution                    | CO 1 |
| 17                                   | Find the orthogonal trajectories of the family of circles $x^2 + y^2 + 2gx + c = 0$ Where g is the parameter.       | Apply    | Learner to recall differential equations, understand the Orthogonal trajectories and apply them to compute solution           | CO 1 |
| 18                                   | Solve the first order differential equation $(x+1) \frac{dy}{dx} - y = e^{3x}(x+1)^2$                               | Apply    | Learner to recall differential equations, understand the linear DE, integrating factor and apply them to compute solution     | CO 1 |
| 19                                   | Find the required general solution for given differential equation $(x^2 - ay)dx = (ax - y^2)dy$ .                  | Apply    | Learner to recall differential equations, understand the exactness, integrating factor and apply them to compute solution     | CO 1 |
| 20                                   | Determine solution for the following differential equation $y(x^2y^2 + 2)dx + x(2 - 2x^2y^2)dy = 0$                 | Apply    | Learner to recall the differential equations, understand the exactness, integrating factor and apply them to compute solution | CO 1 |
| <b>PART-C SHORT ANSWER QUESTIONS</b> |   |          |   |      |
| 1                                    | Define differential equation  | Remember | —   | CO 1 |
| 2                                    | write the types of differential equations   | Remember | —   | CO 1 |
| 3                                    | Define ordinary differential equation   | Remember | —   | CO 1 |
| 4                                    | Define partial differential equation  | Remember | —   | CO 1 |
| 5                                    | Define the order and degree of a differential equation  | Remember | —   | CO 1 |
| 6                                    | what is integral of the differential equation   | Remember | —   | CO 1 |

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| 7  | Define the complete primitive of the equation  | Remember | —  | CO 1 |
| 8  | Define the particular solution of a differential equation  | Remember | —  | CO 1 |
| 9  | Obtain the differential equation by eliminating A and B from $Ax^2 + By^2 = 1$                   | Apply    |  | CO 1 |
| 10 | Obtain the differential equation $y = Ae^{-2t} + Be^{3x}$ by eliminating the arbitrary Constants | Apply    |  | CO 1 |
| 11 | Write the differential equation of the family of straight lines                                  | Remember | —  | CO 1 |
| 12 | Form a differential equation by eliminating 'a' from $r = 2a(\sin t - \cos t)$                   | Apply    | Learner to recall the differential equations of first order, understand formation and apply them to compute solution.                  | CO 1 |
| 13 | Solve the differential equation $dy/dx = e^{x-y} + x^2e^{-y}$                                    | Apply    | —  | CO 1 |
| 14 | Define the Homogenous differential equation  | Remember | —  | CO 1 |
| 15 | What is the condition for exactness  | Remember |  | CO 1 |
| 16 | Define a linear differential equation of first order   | Remember | —  | CO 1 |
| 17 | write the form of Bernoulli's equation   | Remember | —  | CO 1 |
| 18 | Define an orthogonal trajectory of the family of curves  | Remember | —  | CO 1 |
| 19 | Find the orthogonal trajectory of the family of $y=ax$   | Apply    | Learner to recall the differential equations of first order, understand the orthogonal trajectories and apply them to compute solution | CO 1 |
| 20 | State the Newton's law of cooling  | Remember | —  | CO 1 |

| MODULE II  |  |       |   |      |
|--|--|-------|---|------|
| ORDINARY DIFFERENTIAL EQUATIONS OF HIGHER ORDER        |  |       |   |      |
| PART A-PROBLEM SOLVING AND CRITICAL THINKING QUESTIONS |  |       |   |      |
| 1  | Solve the differential equation $(D^2 + 4)y = \sin 2x$ .   | Apply | Learner to recall the non-homogeneous differential equations, understand the method of variation of parameters and apply them to compute solution.              | CO 2 |
| 2  | Apply the method of variation of parameters to solve $(D^2 - 2D)y = e^x \sin x$                          | Apply | Learner to recall the non-homogeneous differential equations, understand the method of variation of parameters and apply them to compute solution.              | CO 2 |
| 3  | Using the of method of variation of Parameters, solve $\frac{d^2y}{dx^2} + y = \operatorname{Cosec} x$ . | Apply | Learner to recall the non-homogeneous differential equations, understand the method of variation of parameters and apply them to compute solution.              | CO 2 |
| 4  | Find the general solution of $y^{1111} + 8y^{11} + 16y = 0$ .  | Apply | Learner to recall the homogeneous differential equations, understand the complementary function and apply them to compute solution.                             | CO 2 |
| 5  | Solve the differential equation $y^{1111} + 18y^{11} + 81y = 64\cos x + 108\cos 3x$ .                    | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |



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| 6                                   | Using the method of variation of Parameters, solve $(D^2 + 4)y = \sec 2x$ .               | Apply | Learner to recall the concept of homogeneous differential equations, understand the procedure and apply complementary function, particular integral to find solution of non-homogeneous differential equations. | CO 2 |
| 7                                   | Using the method of variation of Parameters, solve $(D^2 + 1)y = \tan x$                  | Apply | Learner to recall the non-homogeneous differential equations, understand the method of variation of parameters and apply them to compute solution.  | CO 2 |
| 8                                   | Using the method of variation of Parameters, solve $(D^2 - 2D + 2)y = e^x \tan x$         | Apply | Learner to recall the non-homogeneous differential equations, understand the method of variation of parameters and apply them to compute solution.  | CO 2 |
| 9                                   | Using the method of variation of Parameters, solve $(D^2 - 6D + 9)y = \frac{e^{3x}}{x^2}$ | Apply | Learner to recall the non-homogeneous differential equations, understand the method of variation of parameters and apply them to compute solution.  | CO 2 |
| 10                                  | Using the of method of variation of Parameters, solve $(D^2 - 2D + 1)y = e^x \log x$ .    | Apply | Learner to recall the non-homogeneous differential equations, understand the method of variation of parameters and apply them to compute solution.  | CO 2 |
| <b>PART-B LONG ANSWER QUESTIONS</b> |   |       |   |      |

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|---|---|-------|---|------|
| 1 | Solve the differential equation<br>$(D^2 + 3D + 2)y = 2\cos(2x + 3) + 2e^x + x^2$ . | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 2 | Solve the differential equation<br>$(D^2 + 4)y = 96x^2 + \sin 2x - k$ .             | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 3 | Solve the differential equation<br>$(D^2 - 2D + 1)y = x^2 e^{3x} - \sin 2x + 3$     | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 4 | Solve the differential equation<br>$(D^3 - 6D^2 + 11D - 6)y = e^{-2x} + e^{-3x}$ .  | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 5 | Solve the differential equation<br>$(D^2 + 1)y = \sin x \sin 2x + e^x x^2$ .        | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |

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| 6  | Solve the differential equation<br>$(D^3 + 1)y = 3 + 5e^x$ .            | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 7  | Solve the differential equation<br>$(D^2 - 4)y = 2\cos^2 x$ .           | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 8  | Solve the differential equation<br>$(D^2 + 1)y = \sin x \sin 2x$ .      | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 9  | Solve the differential equation<br>$(D^2 + 9)y = \cos 3x + \sin 2x$ .   | Apply | Learner to recall the non homogeneous differential equations understand the complementary function and particular integral and apply them to compute solution.  | CO 2 |
| 10 | Solve the differential equation<br>$(D^2 + 5D - 6)y = \sin 4x \sin x$ . | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |

|    |   |       |   |      |
|----|---|-------|---|------|
| 11 | Solve the differential equation<br>$(D^2 + D + 1)y = \sin 2x$               | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 12 | By using method of variation of parameters solve $(D^2 + 4)y = \tan 2x$     | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 13 | Solve the differential equation<br>$(D^3 - 4D^2 - D + 4)y = e^{3x} \cos 2x$ | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 14 | Evaluate the differential equation<br>$(D^2 + 9)y = \cos 3x$                | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 15 | Find the differential equation<br>$(D^3 - 7D^2 + 14D - 8)y = e^x \cos 2x$ . | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |

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|----|---|-------|---|------|
| 16 | Solve the differential equation<br>$(D^3 - 4D^2 - D + 4)y = e^{3x}..$     | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 17 | Solve the differential equation<br>$(D^3 + 4D)y = \sin 2x$                | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution  | CO 2 |
| 18 | Solve the differential equation<br>$(D^2 + 4D + 4)y = 3\sin x + 4\cos x.$ | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO2  |
| 19 | By using method of variation of parameters solve $(D^2 + 1)y = \sin x$ .  | Apply | Learner to recall the non-homogeneous differential equations, understand the method of variation of parameters and apply them to compute solution.              | CO 2 |
| 20 | Solve the differential equation<br>$(D^3 - 1)y = e^x + \sin 3x + 2.$      | Apply | Learner to recall the non-homogeneous differential equations, understand the method of variation of parameters and apply them to compute solution.              | CO 2 |

**PART-C SHORT ANSWER QUESTIONS**

|   |   |       |   |      |
|---|---|-------|---|------|
| 1 | Write the solution of the<br>$\frac{d^2y}{dx^2} - 3 \frac{dy}{dx} + 2y = 0$ | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution                                | CO 2 |
| 2 | Write the solution of the<br>$(4D^2 - 4D + 1)y = 100$                       | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution                                | CO 2 |
| 3 | Define wronskian of the functions.  | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. and define wronskian function | CO 2 |
| 4 | Find the particular value of $\frac{1}{D-3} x$                              | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution.                               | CO 2 |
| 5 | Find the particular value of $\frac{1}{(D-2)(D-3)} e^{2x}$ .                | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution.                               | CO 2 |

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| 6  | Solve the differential equation $(D^4 - 2D^3 - 3D^2 + 4D + 4)y=0$ .                            | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 7  | Solve the differential equation $(D^4 - 1)y=0$ .   | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 8  | Write the particular values of $\frac{1}{(D^2+a^2)}\cos ax$ and $\frac{1}{(D^2+a^2)}\sin ax$ . | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 9  | Find the particular integral of $(D^2 - 3D + 2)y=\cos 3x$                                      | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 10 | Write the particular values of $\frac{1}{(D^2+4)}\sin 2x$ .                                    | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |

|    |  |       |   |      |
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| 11 | Solve the differential equation $\frac{d^3y}{dx^3} + y = 0$ .              | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 12 | Find the particular integral of $\frac{1}{(D^2-1)} x$ .                    | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 13 | Solve the differential equation $(D^2 + a^2)y = 0$ .                       | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 14 | Find the particular integral of $(D^2 + 2D)y = 24x$ .                      | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |
| 15 | Find the general solution of the differential equation $y'' + y' - 2y = 0$ | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution. | CO 2 |



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| 16 | What is general solution of higher order differential equation.                             | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution and define general solution of higher order differential equation | CO 2 |
| 17 | Write the solution of the $\frac{d^2y}{dx^2} - 5\frac{dy}{dx} + 6y = 0$ .                   | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution.  | CO 2 |
| 18 | Write the particular values of $\frac{1}{(D^2+9)}\cos 3x$ and $\frac{1}{(D^2+16)}\sin 4x$ . | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution.  | CO 2 |
| 19 | Solve the differential equation $(D^2 + D)y = 0$ .  | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution.  | CO 2 |
| 20 | Solve the differential equation $(D^4 - 16)y = 0$ .   | Apply | Learner to recall the non-homogeneous differential equations, understand the complementary function and particular integral and apply them to compute solution.  | CO 2 |

| MODULE III   |  |       |  |      |
|--|--|-------|--|------|
| PARTIAL DIFFERENTIAL EQUATIONS                         |  |       |  |      |
| PART A-PROBLEM SOLVING AND CRITICAL THINKING QUESTIONS |  |       |  |      |
| 1  | Form the partial differential equation by eliminating arbitrary function<br>$lx + my + nz = \phi(x^2 + y^2 + z^2)$           | Apply | Recall dependent and independent variables, explain partial derivatives, and apply it to form PDE by eliminating arbitrary function..                                | CO 3 |
| 2  | Form the partial differential equation by eliminating arbitrary function<br>$xy + yz + zx = f\left(\frac{z}{(x+y)}\right)$ . | Apply | Recall dependent and independent variables, explain partial derivatives, and apply it to form PDE by eliminating arbitrary function.                                 | CO 3 |
| 3  | Form the partial differential equation by eliminating arbitrary function from<br>$f(x^2 - y^2, x^2 - z^2) = 0$               | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order. | CO 3 |
| 4  | Form the partial differential equation by eliminating the arbitrary function from<br>$z = f(x + ct) + g(x - ct)$             | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order. | CO 4 |
| 5  | Form the partial differential equation by eliminating the arbitrary function from<br>$z = f(x + iy) + g(x - iy)$             | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order. | CO 4 |

| CIE-II                       |  |       |  |      |
|------------------------------|--|-------|--|------|
| 6                            | Solve the partial differential equation. $(z^2 - 2yz - y^2)p + (xy + xz)q = xy - zx$                               | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order. | CO 4 |
| 7                            | Solve $p\sqrt{x} + q\sqrt{y} = \sqrt{z}$   | Apply | Recall dependent and independent variables, explain partial derivatives, and apply standard forms to solve nonlinear partial differential equations..                | CO 4 |
| 8                            | Solve $\frac{p}{x^2} + \frac{q}{y^2} = z$ .  | Apply | Recall dependent and independent variables, explain partial derivatives, and apply standard forms to solve nonlinear partial differential equations.                 | CO 4 |
| 9                            | Solve $xp + yq = 1$ .  | Apply | Recall dependent and independent variables, explain partial derivatives, and apply standard forms to solve nonlinear partial differential equations                  | CO 4 |
| 10                           | Solve $y^2zp + zx^2q = xy^2$   | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order. | CO 4 |
| PART-B LONG ANSWER QUESTIONS |  |       |  |      |
| 1                            | Form the partial differential equation by eliminating arbitray function from $f(x^2 + y^2 + z^2, z^2 - 2xy) = 0$ . | Apply | Recall dependent and independent variables, explain partial derivatives, and applyit to form PDE by eliminating arbitrary function..                                 | CO 3 |

|   |  |       |  |      |
|---|--|-------|--|------|
| 2 | Form a partial differential equation by eliminating a, b, c from $\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$                         | Apply | Recall dependent and independent variables, explain partial derivatives, and apply it to form PDE by eliminating arbitrary constants.                                | CO 3 |
| 3 | Form the partial differential equation by eliminating arbitrary constants<br>$z = ax^3 + by^3$   | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order. | CO 4 |
| 4 | Form the partial differential equation by eliminating the constants from $(x - a)^2 + (y - b)^2 = z^2 \cot^2 \alpha$ where $\alpha$ is a parameter | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order. | CO 4 |
| 5 | Form the partial differential equation by eliminating arbitrary function<br>$z = f(x) + e^y g(x)$  | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order. | CO 4 |
| 6 | Find the differential equation of all spheres whose centres lie on z-axis with a given radius r. .   | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order. | CO 4 |
| 7 | Form the partial differential equation by eliminating arbitrary function f from<br>$z = xy + f(x^2 + y^2)$   | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order. | CO 4 |

|               |  |       |  |      |
|---------------|--|-------|--|------|
| 8             | Form the partial differential equation by eliminating arbitrary constants from<br>$2z = \sqrt{(x+a)} + \sqrt{(y-a)}$ . | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order  | CO 4 |
| 9             | Form the partial differential equation by eliminating a and b from<br>$\log(az-1) = x+ay+b$                            | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order. | CO 4 |
| 10            | Form the partial differential equation by eliminating arbitrary function f from<br>$xyz = f(x^2+y^2+z^2)$              | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order. | CO 4 |
| <b>CIE-II</b> |  |       |  |      |
| 11            | Solve the partial differential equation<br>$px^2 + qy^2 = z(x+y)$ .  | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order. | CO 4 |
| 12            | Solve $p - x^2 = y^2 + q$ .  | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order. | CO 4 |
| 13            | Solve the partial differential equation<br>$y^2p + x^2q = x^2y^2z^2$   | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order. | CO 4 |

|    |  |       |  |      |
|----|--|-------|--|------|
| 14 | Solve the partial differential equation<br>$ptanx + qtany = tanz$ .              | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order. . | CO 4 |
| 15 | Solve the partial differential equation<br>$(x - a)p + (y - b)q + (c - z) = 0$ . | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order.   | CO 4 |
| 16 | Solve $px^2 + qy^2 = z(x + y)$ .   | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order.   | CO 4 |
| 17 | Solve the partial differential equation<br>$pz - qz = z^2 + (x + y)^2$ .         | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order..  | CO 4 |
| 18 | Solve the partial differential equation<br>$\frac{y^2z}{x}p + xzq = y^2$ .       | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order..  | CO 4 |
| 19 | Solve<br>$x(y^2 - z^2)p - y(z^2 + x^2)q = z(x^2 + y^2)$ .                        | Apply | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order    | CO 4 |

|                                      |   |          |   |      |
|--------------------------------------|---|----------|---|------|
| 20                                   | Solve $(x - y)p + (y - x - z)q = z..$   | Apply    | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order | CO 4 |
| <b>PART-C SHORT ANSWER QUESTIONS</b> |   |          |   |      |
| 1                                    | Define order and degree with reference to partial differential equation.                                  | Remember | -   | CO 3 |
| 2                                    | Form the partial differential equation by eliminate the arbitrary function from $z = yf(y/x)$ .           | Apply    | Recall dependent and independent variables, explain partial derivatives, and apply it to form PDE by eliminating arbitrary constants.                               | CO 3 |
| 3                                    | Form the partial differential equation by eliminating arbitrary function $z = f(x^2 + y^2)$               | Apply    | Recall dependent and independent variables, explain partial derivatives, and apply it to form PDE by eliminating arbitrary functions.                               | CO 3 |
| 4                                    | Form the partial differential equation by eliminating arbitrary constants $z^2 = (x - a)^2 + (y - b)^2$ . | Apply    | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order | CO 4 |
| 5                                    | Form the partial differential equation by eliminating arbitrary constants from $z = ax + by$              | Apply    | Recall dependent and independent variables, explain partial derivatives, and apply it to form PDE by eliminating arbitrary constants.                               | CO 4 |

|               |  |          |   |      |
|---------------|--|----------|---|------|
| 6             | Form the partial differential equation by eliminating arbitrary constants h,k from $(x - h)^2 + (y - k)^2 + z^2 = a^2$ | Apply    | Recall dependent and independent variables, explain partial derivatives, and apply it to form PDE by eliminating arbitrary constants.                               | CO 4 |
| 7             | Eliminate the arbitrary constants from $z = (x^2 + a)(y^2 + b)$ .  | Apply    | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order | CO 4 |
| 8             | Eliminate the arbitrary function from $z = f(\sin x + \cos y)$ .   | Apply    | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order | CO 4 |
| 9             | Eliminate the arbitrary function from $f(x^2 - y^2, x - z) = 0$  | Apply    | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order | CO 4 |
| 10            | Eliminate the arbitrary function from $z = yf(x) + xg(y)$  | Apply    | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order | CO 4 |
| <b>CIE-II</b> |  |          |   |      |
| 11            | Solve $xp + yq = 3z$ .   | Remember |   | CO 4 |
| 12            | Solve $xp + yq = 1$ ..   | Apply    | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order | CO 4 |



|    |  |          |   |      |
|----|--|----------|---|------|
| 13 | Solve $px + qy = z$                                | Apply    | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order | CO 4 |
| 14 | Solve, $p + 3q = 5z + \tan(y - 3x)$                | Apply    | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order | CO 4 |
| 15 | Solve. $2p + 3q = 1$                               | Remember | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order | CO 4 |
| 16 | Solve. $(x + y)p - (x + y)q = z$                   | Apply    | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order | CO 4 |
| 17 | Solve. $p - q = \log(x + y)$ .                     | Apply    | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order | CO 4 |
| 18 | Solve. $y^2p - xyq = x(z - 2y)$ .                  | Apply    | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method to solve linear partial differential equations of first order | CO 4 |
| 19 | Explain linear partial differential equation.<br>. | Remember | -   | CO 4 |

|   |  |            |  |      |
|---|--|------------|--|------|
| 20  | write the general solution of first order linear differential equation.  | Remember   | -  | CO 4 |
| <b>MODULE IV</b>  |  |            |  |      |
| <b>VECTOR DIFFERENTIATION</b>                                 |  |            |  |      |
| <b>PART A-PROBLEM SOLVING AND CRITICAL THINKING QUESTIONS</b> |  |            |  |      |
| 1   | Find the angle between the surfaces $x^2 + y^2 + z^2 = 9$ and $z = x^2 + y^2 - 3$ at the point (2,-1,2)  | Understand | Learner to recall vector and scalar functions, explain gradient and obtain the transformation between surface and volume of a bounded region of cube.                                      | CO 5 |
| 2   | Find the angle between the normals to the surfaces $x^2 = yz$ at the points (1,1,1) and (2,4,1).   | Understand | Learner to recall vector and scalar functions, explain gradient and apply to the surfaces.   | CO 5 |
| 3   | Prove that $\text{div}(\text{grad} r^m) = m(m+1)r^{m-2}$ where $\vec{r} = x\vec{i} + y\vec{j} + z\vec{k}$  | Understand | Learner to recall vector and scalar functions, explain gradient and apply line integral to obtain the work done by the force.  | CO 5 |
| 4   | Show that the vector $(x^2 - yz)\vec{i} + (y^2 - zx)\vec{j} + (z^2 - xy)\vec{k}$ is irrotational and find its scalar potential function.   | Understand | Learner to recall vector and scalar functions, explain curl of the gradient, and apply it to obtain irrotational and scalar potential function   | CO 5 |
| 5   | Determine a unit vector normal to the surface $xy^3z^2 = 4$ at the point (-1,-1,2)   | Understand | Learner to recall vector and scalar functions, explain gradient and apply Gauss divergence theorem to obtain the transformation between surface and volume of a bounded region of cylinder | CO 5 |
| 6   | Find the directional derivative of $\phi(x, y, z) = x^2yz + 4xz^2$ at the point (1, -2, -1) in the direction of the normal to the surface $f(x, y, z) = x \log z - y^2$ at (-1,2,1). | Understand | Learner to recall vector and scalar functions, explain the gradient, and apply it to obtain the direction derivative of the function.  | CO 5 |

|                                     |  |            |   |      |
|-------------------------------------|--|------------|---|------|
| 7                                   | Prove that $\nabla r^n = nr^{n-2}\bar{r}$  | Understand | Learner to recall vector and scalar functions, explain gradient and of a bounded region of parabolas.   | CO 5 |
| 8                                   | Show that $\nabla f(r) = \frac{\bar{f}(r)}{r}$ where $r = xi + yj + zk$  | Understand | Learner to recall vector and scalar functions, explain gradient and apply Green's theorem to obtain the transformation of a bounded region of parabolas.                        | CO 5 |
| 9                                   | Find the directional derivative of the function $xy^2 + yz^2 + zx^2$ along the tangent to the curve $x = t, y = t^2, z = t^3$ at the point (1,1,1)   | Understand | Learner to recall vector and scalar functions, explain gradient and to obtain the transformation between bounded region of a plane.   | CO 5 |
| 10                                  | If the temperature at any point in space is given by $t = xy + yz + zx$ , find the direction in which temperature changes most rapidly with distance from the point (1,1,1) and determine the maximum rate of change | Understand | Learner to recall vector and scalar functions, explain gradient and apply Stoke's theorem to obtain the transformation between line and surface of a bounded region of a plane. | CO 5 |
| <b>PART-B LONG ANSWER QUESTIONS</b> |  |            |   |      |
| 1                                   | If the vector field F is irrotational find the constants a,b,c where $\bar{f} = (x+2y+az)\bar{i} + (bx-3y-z)\bar{j} + (4x+cy+2z)\bar{k}$ and also find its scalar potential.   | Understand | Learner to recall vector and scalar functions, explain gradient and apply it to obtain solution of line integral.   | CO 5 |
| 2                                   | Find the constants a and b so that the surface $ax^2 - byz = (a+2)x$ will be orthogonal to the surface $4xx^2y + z^3 = 4$ at the point (1,-1,2)  | Understand | Learner to recall vector and scalar functions, explain gradient and normal forces, and apply it to compute solution .   | CO 5 |

|   |  |            |   |      |
|---|--|------------|---|------|
| 3 | Show that $\bar{A} = 3y^4z^2i + 4x^3z^2j - 3x^2y^2k$ is solenoidal   | Understand | Learner to recall vector and scalar functions, explain gradient and normal forces, and apply it to compute solution .   | CO 5 |
| 4 | Prove that $\bar{A} = (6xy + z^3)i + (3x^2 - z)j + (3xz^2 - y)k$ is irrotational and find the scalar function .            | Understand | Learner to recall vector and scalar functions, explain gradient and normal forces, and apply it to compute solution .   | CO 5 |
| 5 | If $\nabla f = (y^2 - 2xyz^3)i + (3 + 2xy - x^2z^3)j + (6z^3 - 3x^2yz^2)k$ , find f if $f(1,0,1)=8$ .                      | Understand | Learner to recall vector and scalar functions, explain gradient and normal forces, and apply it to compute solution .   | CO 5 |
| 6 | Find the curl of $\bar{V} = e^{xyz}(\bar{i} + \bar{j} + \bar{k})$ at the point (1,2,3)                                     | Understand | Learner to recall vector and scalar functions, explain gradient ,divergence and curl and apply it to compute solution . | CO 5 |
| 7 | If $f(r)$ is differentiable and $r = (x^2 + y^2 + z^2)^{1/2}$ , show that $f(r)\bar{r}$ is irrotational                    | Understand | Learner to recall vector and scalar functions, explain gradient ,divergence and curl and apply it to compute solution . | CO 5 |
| 8 | If $f = x^2yz$ and $g = xy - 3z^2$ , calculate $\nabla(\nabla f \cdot \nabla g)$   | Understand | Learner to recall vector and scalar functions, explain gradient ,divergence and curl and apply it to compute solution   | CO 5 |
| 9 | Find the angle of intersection of the spheres $x^2 + y^2 + z^2 = 29$ and $x^2 + y^2 + z^2 + 4x - 6y - 8z = 47$ at (4,-3,2) | Understand | Learner to recall vector and scalar functions, explain gradient ,divergence and curl and apply it to compute solution   | CO 5 |

|    |  |            |   |      |
|----|--|------------|---|------|
| 10 | Determine the angle between the normals to the surface $xy = z^2$ at the points (4,1,2) and (3,3,-3) .   | Understand | Learner to recall vector and scalar functions, explain gradient ,divergence and curl and apply it to compute solution . | CO 5 |
| 11 | Calculate the angle between the normals to the surface $2x^2 + 3y^2 = 5z$ at the points (2,-2,4) and (-1,-1,1)   | Understand | Learner to recall vector and scalar functions, explain gradient ,divergence and curl and apply it to compute solution   | CO 5 |
| 12 | Find the directional derivative of the function $\phi = xy^2 + yz^3$ at the point P (1,-2,-1) in the direction to the surface                                    | Understand | Learner to recall vector and scalar functions, explain gradient ,divergence and curl and apply it to compute solution   | CO 5 |
| 13 | Determine the constants a,b,c so that $\bar{A} = (2x + 3y + az)\bar{i} + (bx + 2y + 3z)\bar{j} + (2x + cy + 3z)\bar{k}$ is irrotational.Find the scalar function | Understand | Learner to recall vector and scalar functions, explain gradient ,divergence and curl and apply it to compute solution . | CO 5 |
| 14 | Determine curl of $xyz^2\bar{i} + yxz^2\bar{j} + zxy^2\bar{k}$ at the point (1,2,3)  | Understand | Learner to recall vector and scalar functions, explain gradient ,divergence and curl and apply it to compute solution   | CO 5 |
| 15 | Find the value of constant b such that $\bar{A} = (bxy - z^3)\bar{i} + (b - 2)x^2\bar{j} + (1 - b)xz^2\bar{k}$ has its curl identically equal to zero.           | Understand | Learner to recall vector and scalar functions, explain gradient ,divergence and curl and apply it to compute solution   | CO 5 |
| 16 | Determine $div \bar{f}$ where $\bar{f} = r^n \bar{r}$ and calculate n if it is solenoid ?  | Understand | Learner to recall vector and scalar functions, explain gradient ,divergence and curl and apply it to compute solution   | CO 5 |

|                                      |  |            |  |      |
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| 17                                   | If $a = x + y + z, b = x^2 + y^2 + z^2, c = xy + yz + zx$ , prove that $[\text{grada}, \text{gradb}, \text{gradc}] = 0$ .  | Understand | Learner to recall vector and scalar functions, explain gradient, divergence and curl and apply it to compute solution e      | CO 5 |
| 18                                   | Prove that $(y^2 - z^2 + 3yz - 2x)i + (3xz + 2xy)j + (3xy - 2xz + 2z)$ is both solenoidal and irrotational.  | Understand | Learner to recall vector and scalar functions, explain gradient, divergence and curl and apply it to compute solution        | CO 5 |
| 19                                   | Find the directional derivative of $\nabla \cdot (\nabla f)$ at the point (1,-2,1) in the direction of the normal to the surface $xy^2z = 3x + z^2$ where $f = 2x^3y^2z^4$ . | Understand | Learner to recall vector and scalar functions, explain gradient, divergence and curl and apply it to compute solution        | CO 5 |
| 20                                   | Calculate $\nabla^2 f$ when $f = 3x^2z - y^2z^3 + 4x^3y + 2x - 3y - 5$ at the point (1,1,0)  | Understand | Learner to recall vector and scalar functions, explain gradient, divergence and curl and apply it to compute solution        | CO 5 |
| <b>PART-C SHORT ANSWER QUESTIONS</b> |  |            |  |      |
| 1                                    | Define gradient of scalar point function.  | Remember   | —  | CO 5 |
| 2                                    | Define divergence of vector point function.  | Remember   | —  | CO 5 |
| 3                                    | Define curl of vector point function.  | Remember   | —  | CO 5 |
| 4                                    | State Laplacian operator.  | Remember   | —  | CO 5 |
| 5                                    | Find $\text{curl } \bar{f}$ where $\bar{f} = \text{grad}(x^3 + y^3 + z^3 - 3xyz)$  | Remember   | —  | CO 5 |
| 6                                    | Find the angle between the normal to the surface $xy = z^2$ at the points (4, 1, 2) and (3, 3, -3).  | Apply      | Learner to recall vector and scalar functions, explain gradient and apply it to obtain the angle between the normal surfaces | CO 5 |
| 7                                    | Find a unit normal vector to the given surface $x^2y + 2xz = 4$ at the point (2,-2,3).   | Apply      | Learner to recall vector and scalar functions, explain gradient and apply it to obtain the unit vector of normal surfaces.   | CO 5 |

|    |   |          |   |      |
|----|---|----------|---|------|
| 8  | If $\vec{a}$ is a vector then prove that $\vec{\nabla}(\vec{a} \cdot \vec{r}) = \vec{a}$  | Apply    | Learner to recall vector and scalar functions, explain gradient and apply it to obtain the required solution of normal surfaces | CO 5 |
| 9  | Define ir rotational vector and solenoidal vector of vector point function.   | Remember | —   | CO 5 |
| 10 | Show that $\vec{\nabla}(f(r)) = \frac{(r)}{r} f'(r)$  | Apply    | Learner to recall vector and scalar functions, explain gradient and apply it to obtain the required solution of normal surfaces | CO 5 |
| 11 | Prove that $\vec{f} = yz\vec{i} + zx\vec{j} + xy\vec{k}$ is irrotational vector.  | Apply    | Learner to recall vector and scalar functions, explain gradient and apply it to obtain the irrotational vector                  | CO 5 |
| 12 | Show that $(x + 3y)\vec{i} + (y - 2z)\vec{j} + (x - 2z)\vec{k}$ is solenoidal.  | Apply    | Learner to recall vector and scalar functions, explain gradient and apply it to obtain conservation of mass                     | CO 5 |
| 13 | Show that $\vec{\nabla} \times (\vec{\nabla}(\phi)) = 0$ where $\phi$ is scalar point function.   | Apply    | Learner to recall vector and scalar functions, explain gradient and apply it to obtain solution of scalar point function        | CO 5 |
| 14 | Define the derivative of vector function  | Remember | —   | CO 5 |
| 15 | Prove that $[\text{div} \vec{\nabla} \times = 0]$ where .<br>$\vec{f} = f_1\vec{i} + f_2\vec{j} + f_3\vec{k}$                               | Remember | —   | CO 5 |
| 16 | what is unit tangent vector   | Remember | —   | CO 5 |
| 17 | If $\vec{A} = 5t^2\vec{i} + t\vec{j} - t^3\vec{k}$ and $\vec{B} = \sin t\vec{i} - \cos t\vec{j}$ find $\frac{d}{dt}(\vec{A} \cdot \vec{B})$ | Remember | —   | CO 5 |
| 18 | Define the operator del   | Remember | —   | CO 5 |
| 19 | Define the divergence of a vector   | Remember | —   | CO 5 |
| 20 | Define the curl of a vector   | Remember | —   | CO 5 |

| MODULE V   |   |       |  |      |
|--|---|-------|--|------|
| VECTOR INTEGRATION                                     |   |       |  |      |
| PART A-PROBLEM SOLVING AND CRITICAL THINKING QUESTIONS |   |       |  |      |
| 1  | Verify Gauss divergence theorem for $\vec{f} = x^2\vec{i} + y^2\vec{j} + z^2\vec{k}$ taken over the cube bounded by $x=0, x=a, y=0, y=b, z=0, z=c$ .  | Apply | Learner to recall vector and scalar functions, explain gradient and apply Gauss divergence theorem to obtain the transformation between surface and volume of a bounded region of cube     | CO 6 |
| 2  | Using Gauss divergence theorem evaluate $\iint_S \vec{F} \cdot d\vec{s}$ for the $\vec{F} = y\vec{i} + x\vec{j} + z^2\vec{k}$ for the cylinder region S given by $x^2 + y^2 = a^2, z = 0$ and $z = b$ . | Apply | Learner to recall vector and scalar functions, explain gradient and apply Gauss divergence theorem to obtain the transformation between surface and volume of a bounded region of cylinder | CO 6 |
| 3  | Using Green's theorem in the plane evaluate $\int_C (2xy - x^2)dx + (x^2 + y^2)dy$ where C is the region bounded by $y = x^2$ and $y^2 = x$ .   | Apply | Learner to recall vector and scalar functions, explain gradient and apply Green's theorem to obtain the transformation between line and double integral of a bounded region of parabolas.  | CO 6 |
| 4  | Applying Green's theorem evaluate $\int_C (xy + y^2)dx + (x^2)dy$ where C is the region bounded by $y = \sqrt{x}$ and $y = x^2$ .   | Apply | Learner to recall vector and scalar functions, explain gradient and apply Green's theorem to obtain the transformation between line and double integral of a bounded region of parabolas.  | CO 6 |



|   |   |       |  |      |
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| 5 | Verify Green's Theorem in the plane for $\int_C (3x^2 - 8y^2)dx + (4y - 6xy)dy$ where C is the region bounded by $x=0$ , $y=0$ and $x + y=1$ .  | Apply | Learner to recall vector and scalar functions, explain gradient and apply Stoke's theorem to obtain the transformation between line and surface of a bounded region of a plane.          | CO 6 |
| 6 | Verify Stokes theorem for $\vec{F} = (y - z + 2)\vec{i} + (yz + 4)\vec{j} - xz\vec{k}$ where S is the surface of the cube $x=0$ , $y=0$ , $z=0$ and $x=2$ , $y=2$ , $z=2$ above the xy-plane. | Apply | Learner to recall vector and scalar functions, explain gradient and apply Stoke's theorem to obtain the transformation between line and surface of a bounded region of a plane.          | CO 6 |
| 7 | Verify Gauss divergence theorem for the vector point function $\vec{F} = (x^3 - yz)\vec{i} - 2xy\vec{j} + 2z\vec{k}$ over the cube bounded by $x = y = z = 0$ and $x = y = z = a$ .           | Apply | Learner to recall vector and scalar functions, explain gradient and apply Gauss divergence theorem to obtain the transformation between surface and volume of a bounded region of cube . | CO 6 |
| 8 | Verify Green's theorem in the plane for $\int_C (3x^2 - 8y^2)dx + (4y - 6xy)dy$ where C is a region bounded by $y = \sqrt{x}$ and $y = x^2$   | Apply | Learner to recall vector and scalar functions, explain gradient and apply Green's theorem to obtain the transformation between surface and volume of a bounded region of cube ..         | CO 6 |
| 9 | If $\vec{F} = (x^2 + y^2)\vec{i} - 2xy\vec{j}$ evaluate $\int \vec{F} \cdot d\vec{r}$ where curve c is the rectangle in xy-plane bounded by $y = 0, y = b, x = 0, x = a$ .                    | Apply | Learner to recall vector and scalar functions, explain gradient and apply Gauss divergence theorem to obtain the transformation between surface and volume of a bounded region of cube . | CO 6 |

|                                     |   |       |  |      |
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| 10                                  | If $\vec{F} = (2x + y^2)\vec{i} + (3y - 4x)\vec{j}$ evaluate $\int_c \vec{F} \cdot d\vec{r}$ around a triangle ABC in the xy-plane with A(0,0), B(2,0), C(2,1) in the counter clock wise direction and opposite direction | Apply | Learner to recall vector and scalar functions, explain gradient and apply Gauss divergence theorem to obtain the transformation between surface and volume of a bounded region of cube .   | CO 6 |
| <b>PART-B LONG ANSWER QUESTIONS</b> |   |       |  |      |
| 1                                   | Evaluate $\iint_s \vec{F} \cdot d\vec{s}$ if $\vec{F} = yz\vec{i} + 2y^2\vec{j} + xz^2\vec{k}$ and S is the Surface of the cylinder $x^2 + y^2 = 9$ contained in the first octant between the planes $z=0$ and $z=2$ .    | Apply | Learner to recall vector and scalar functions, explain gradient and normal forces, and apply it to value the area of the cylinder .  | CO 6 |
| 2                                   | Find the work done in moving a particle in the force field $\vec{F} = 3x^2\vec{i} + (2zx - y)\vec{j} + z\vec{k}$ along the straight line from (0,0,0) to (2,1,3) .  | Apply | Learner to recall vector and scalar functions, explain gradient and apply line integral to value the work done by the force.   | CO 6 |
| 3                                   | Find the circulation of $\vec{F} = (2x - y + 2z)\vec{i} + (x + y - z)\vec{j} + (3x - 2y - 5z)\vec{k}$ along the circle $x^2 + y^2 = 4$ in the xy plane.   | Apply | Learner to recall vector and scalar functions, explain gradient and apply line integral to value the work done by the force.   | CO 6 |
| 4                                   | Verify Gauss divergence theorem for the vector point function $\vec{F} = (x^3 - yz)\vec{i} - 2xy\vec{j} + 2z\vec{k}$ over the cube bounded by $x = y = z = 0$ and $x = y = z = a$ .                                       | Apply | Learner to recall vector and scalar functions, explain gradient and apply Gauss divergence theorem to obtain the transformation between surface and volume of a bounded region of cylinder | CO 6 |
| 5                                   | Verify Gauss divergence theorem for $2x^2y\vec{i} - y^2\vec{j} + 4xz^2\vec{k}$ taken over the region of first octant of the cylinder $y^2 + z^2 = 9$ and $x=2$ .  | Apply | Learner to recall vector and scalar functions, explain gradient and apply Gauss divergence theorem to obtain the transformation between surface and volume of a bounded region of cylinder | CO 6 |

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| 6  | Verify Green's theorem in the plane for $\int_C (x^2 - xy)dx + (y^2 - 2xy)dy$ where C is a square with vertices (0,0) ,(2,0) ,(2,2),(0,2).   | Apply | Learner to recall vector and scalar functions, explain gradient and apply Green's theorem to obtain the transformation between line and double integral of a square bounded region . | CO 6 |
| 7  | Applying Green's theorem evaluate $\int_C (y - \sin x)dx + \cos y dy$ where C is the plane triangle enclosed by $y = 0$ , $y = \frac{2x}{\pi}$ , and $x = \frac{\pi}{2}$ .                         | Apply | Learner to recall vector and scalar functions, explain gradient and apply Green's theorem to obtain the transformation between line and double integral of a square bounded region . | CO 6 |
| 8  | Apply Green's Theorem in the plane for $\int_C (2x^2 - y^2)dx + (x^2 + y^2)dy$ where C is a is the boundary of the area enclosed by the x-axis and upper half of the circle $x^2 + y^2 = a^2$ .    | Apply | Learner to recall vector and scalar functions, explain gradient and apply Green's theorem to obtain the transformation between line and double integral of a triangle bounded region | CO 6 |
| 9  | Verify Stokes theorem for $\vec{f} = (2x - y)\vec{i} - yz^2\vec{j} - y^2z\vec{k}$ where S is the upper half surface of the sphere $x^2 + y^2 + z^2 = 1$ bounded by the projection of the xy plane. | Apply | Learner to recall vector and scalar functions, explain gradient and apply Stoke's theorem to the transformation between line and surface of a bounded region of sphere.              | CO 6 |
| 10 | Verify Stokes theorem for $\vec{f} = -y^3\vec{i} + x^3\vec{j}$ where S is the circular disc $x^2 + y^2 \leq 1$ , $z=0$ .   | Apply | Learner to recall vector and scalar functions, explain gradient and apply Stoke's theorem to the transformation between line and surface of a bounded region of sphere               | CO 6 |

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| 11 | If $\vec{F} = 4xz\vec{i} - y^2\vec{j} + yz\vec{k}$ evaluate $\int_S \vec{F} \cdot \vec{n} ds$ where S is the surface of the cube $x=0, x=a, y=0, y=a, z=0, z=a$    | Apply | Learner to recall vector and scalar functions, explain gradient and apply Gauss divergence theorem to obtain the transformation between surface and volume of a bounded region of cube. | CO 6 |
| 12 | If $\vec{f} = (5xy - 6x^2)\vec{i} + (2y - 4x)\vec{j}$ evaluate $\int_C \vec{f} \cdot d\vec{r}$ along the curve C in $y = x^3$ plane from (1,1) to (2,8)            | Apply | Learner to recall vector and scalar functions, explain gradient and apply line integral to obtain the work done by the force.   | CO 6 |
| 13 | Evaluate the line integral $\int_C (x^2 + xy)dx + (x^2 + y^2)dy$ where C is the square formed by lines $x = \pm 1, y = \pm 1$ .                                    | Apply | Learner to recall vector and scalar functions, explain gradient and apply line integral to obtain the work done by the force  | CO 6 |
| 14 | Evaluate by Stokes theorem $\int_C (e^x dx + 2y dy - dz)$ where c is the curve $x^2 + y^2 = 9$ and $z=2$   | Apply | Learner to recall vector and scalar functions, explain gradient and apply Stoke's theorem to obtain the transformation between line and surface of a bounded region of a plane          | CO 6 |
| 15 | Verify Stokes theorem for the function $x^2\vec{i} + xy\vec{j}$ integrated round the square in the plane $z=0$ whose sides are along the line $x=0, y=0, x=a, y=a$ | Apply | Learner to recall vector and scalar functions, explain gradient and apply Stoke's theorem to obtain the transformation between line and surface of a bounded region of a plane          | CO 6 |

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| 16                                   | Evaluate by Stokes theorem<br>$\int_C (x+y)dx + (2x-z)dy + (y+z)dz$ where C is the boundary of the triangle with vertices (0,0,0),(1,0,0),(1,1,1)  | Apply    | Learner to recall vector and scalar functions, explain gradient and apply Stoke's theorem to obtain the transformation between line and surface of a square bounded region               | CO 6 |
| 17                                   | Verify Green's theorem in the plane for<br>$\int_C (3x^2 - 8y^2)dx + (4y - 6xy)dy$ where C is a region bounded by $y = \sqrt{x}$ and $y = x^2$ .   | Apply    | Learner to recall vector and scalar functions, explain gradient and apply Green's theorem to obtain the transformation between line and double integral of a bounded region of parabola  | CO 6 |
| 18                                   | Determine whether the force field<br>$\vec{F} = 2xz\vec{i} + (x^2 - y)\vec{j} + (2z - x^2)\vec{k}$ is conservative or not  | Apply    | Learner to recall vector and scalar functions, explain gradient and apply line integral to obtain the work done by the force.  | CO 6 |
| 19                                   | Evaluate<br>$\int \int_s \vec{A} \cdot \vec{n} ds$ where $\vec{A} = z\vec{i} + x\vec{j} - 3y^2z\vec{k}$ and s is the surface of the cylinder $x^2 + y^2 = 16$ included in the first octant between $z=0$ and $z=5$ | Apply    | Learner to recall vector and scalar functions, explain gradient and volume integral to obtain the transformation between line and surface of a square bounded region                     | CO 6 |
| 20                                   | Evaluate by Green's theorem<br>$\int (y - \sin x)dx + \cos x dy$ where 'C' is the triangle enclosed by the lines<br>$y = 0, x = \pi/2, \pi y = 2x$ .   | Apply    | Learner to recall vector and scalar functions, explain gradient and apply Green's theorem to obtain the transformation between line and double integral of a bounded region of parabola. | CO 6 |
| <b>PART-C SHORT ANSWER QUESTIONS</b> |  |          |  |      |
| 1                                    | Define gradient of scalar point function.  | Remember | —  | CO 6 |
| 2                                    | Define divergence of vector point function.  | Remember | —  | CO 6 |
| 3                                    | Define curl of vector point function.  | Remember | —  | CO 6 |

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| 4  | State Laplacian operator.  | Remember | —   | CO 6 |
| 5  | State Stokes theorem of transformation between line integral and surface integral.             | Remember | —   | CO 6 |
| 6  | Define line integral on vector point function.   | Remember | —   | CO 6 |
| 7  | State Green's theorem  | Remember | —   | CO 6 |
| 8  | Define the line integral of vector point function  | Remember | —   | CO 6 |
| 9  | Define surface integral of vector point function $\vec{F}$ .                                   | Remember | —   | CO 6 |
| 10 | Define volume integral on closed surface S of volume V.  | Remember | —r  | CO 6 |
| 11 | State Green's theorem of transformation between line integral and double integral.             | Remember | —   | CO 6 |
| 12 | State Gauss divergence theorem of transformation between surface integral and volume integral. | Remember | —   | CO 6 |
| 13 | What is the surface area of the surface S whose equation is $F(x,y,z)=0$ ?                     | Apply    | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method | CO 6 |
| 14 | Find the surface area of the plane $x + 2y + 2z = 12$ cut off by $x=0, y=0, x=1, y=1$          | Apply    | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method | CO 6 |
| 15 | Find the surface area of $z = x^2 + y^2$ included between $z=0$ $z=1$                          | Apply    | Recall dependent and independent variables, explain Lagrange's Linear equation, apply suitable method | CO 6 |
| 16 | Evaluate $\int y^2 dx - 2x^2 dy$ along the parabola $y = x^2$ from $(0, 0)$ to $(2, 4)$        | Apply    | Recall dependent and independent variables, apply suitable method                                     | CO 6 |
| 17 | Compute the area of the ellipse $x = a \cos^3 t$<br>$y = b \sin t$                             | Apply    | Recall dependent and independent variables, apply suitable method t                                   | CO 6 |
| 18 | What is the surface area of a curved surface   | Apply    | Remember  | CO 6 |
| 19 | what are the applications of line integral   | Remember | —   | CO 6 |
| 20 | Define volume integral on closed surface S of volume V.  | Remember | —   | CO 6 |

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**HOD CSE**