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Course Code: ACSD05



## INSTITUTE OF AERONAUTICAL ENGINEERING

(Autonomous)

B.Tech II SEMESTER CIE - I EXAMINATIONS MAY - 2024 Regulation: BT23

## ESSENTIALS FOR PROBLEM SOLVING

(CSE | CSE (AI & ML) | CSE (DS) | CSE (CS) | CSIT | IT | ECE | EEE)

Time: 2 Hours

Max Marks: 20

## Answer any FOUR questions

All parts of the question must be answered in one place only

- 1. (a) Draw the following graphs:
  - i) Null graph  $N_5$
  - ii) Complete graph  $K_6$
  - iii) Complete bipartite graph  $K_{7.4}$
  - iv) Union of  $K_{l,3}$  and  $W_4$

[BL: Apply CO: 1 | Marks: 2]

- (b) The following five items refer to the graph G defined as follows. The set of vertices is  $V = \{0, 1, 2, 3, 4, 5, 6, 7, 8\}$ , and two vertices u and v are adjacent if  $|u-v| \in \{1, 4, 5, 8\}$ . Determine the order and the size of the following subgraphs of G:
  - i) The subgraph induced by even vertices.
  - ii) The subgraph induced by odd vertices.
  - iii) The subgraph induced by the set  $\{0, 1, 2, 3, 4\}$ .
  - iv) A spanning subgraph with as many edges as possible but without cycles.

[BL: Apply CO: 1 | Marks: 3]

- 2. (a) Summarize digraph. Let G5 be a digraph where V(G5) = a, b, c, d and
  - $A(G5) = \{ab, ba, cc, dc, db, da\}$ . Draw the digraph for G5

[BL: Apply CO: 1 | Marks: 2]

- (b) suppose that in a group of 5 people: A, B, C, D, A and E, the following pairs of people are acquainted with each other. a) A and C b) A and D c) B and D d) C and D e) C and D
  - i) Draw a graph G to represent this situation.
  - ii) List the vertex set, and the edge set, using set notation.

In other words, show sets V and E for the vertices and edges, respectively, in  $G = \{V, E\}$ . c)

Draw an adjacency matrix for G.

[BL: Apply CO: 1 | Marks: 3]

- 3. (a) Explain how matrices can be used to represent and analyze walks in graphs. Discuss the adjacency matrix and its properties? [BL: Understand| CO: 2|Marks: 2]
  - (b) Consider the following graph as shown in Figure 1

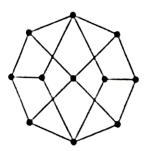


Figure 1

- i) Find a Hamilton path. Can your path be extended to a Hamilton cycle?
- ii) Is the graph bipartite? If so, how many vertices are in each "part"?
- iii) Use your answer to part (b) to prove that the graph has no Hamilton cycle.
- iv) Suppose you have a bipartite graph G in which one part has at least two more vertices than the other. Prove that G does not have a Hamilton path.

[BL: Apply CO: 2|Marks: 3]

- 4. (a) Illustrate the following methods to tour a graph:
  - i) Eulerian Tours
  - ii) Hamiltonian Paths / Cycles
  - iii) Dijkstra's Algorithm

[BL: Understand | CO: 2|Marks: 2]

(b) AA salesman needs to visit 5 cities (A, B, C, D, E) exactly once and return to the starting city. The distances between the cities are as follows:

A to B: 10 units

A to C: 15 units

A to D: 20 units

A to E: 25 units

B to C: 35 units

B to D: 30 units

B to E: 35 units

C to D: 40 units

C to E: 45 units

D to E: 50 units

Using the brute-force approach, find the shortest possible route for the salesman to visit all cities and return to the starting city. Show the step-by-step process including all permutations and calculations of total distances.

[BL: Apply] CO: 2|Marks: 3|

- 5. (a) What is the smallest number of colors that can be used to color the vertices of a cube so that no two adjacent vertices are colored identically? [BL: Understand] CO: 3|Marks: 2]
  - (b) A tree is a connected graph with no cycles as shown in Figure 2

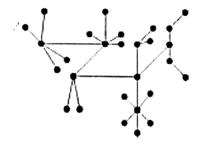


Figure 2

- i) Describe a procedure to color for the tree given in Figure 2.
- ii) The chromatic number of  $C_n$  is two when n is even. What goes wrong when n is odd?
- iii) Prove that your procedure from part (a) always works for any tree.
- iv) Now, prove using induction that every tree has chromatic number 2.

[BL: Apply CO: 3 | Marks: 3]