

START WRITING FROM HERE

2. Exercises on number Systems

2.1 Exercises (Number System conversions)

1. Convert the following decimal numbers into binary and hexadecimal numbers:

a. 108

2	108	
2	54	0
2	27	0
2	13	1
2	6	1
2	3	0
2	1	1
	0	1

16	108	
16	6	12 - c
	0	6

Hexadecimal : 6C

Binary : 1101100

b. 4848

2	4848	
2	2424	0
2	1212	0
2	606	0
2	303	0
2	151	1
2	75	1
2	37	1
2	18	1
2	9	0
2	4	1
2	2	0
2	1	0
	0	1

16	4848	
16	303	0
16	18	15 - f
16	1	2
	0	1

Hexadecimal : 12f0

Binary : 10010111000

c. 9000

2	9000	
2	4500	0
2	2250	0
2	1125	0
2	562	1
2	281	0
2	140	1
2	70	0
2	35	0
2	17	1
2	8	1
2	4	0
2	2	0
2	1	0
	0	1

16	9000	
16	562	- 8
16	35	- 2
16	2	- 3
	0	- 2

Hexadecimal : 2328

Binary : 10001100101000

2. Convert the following binary numbers into decimal and hexadecimal numbers.

a. 10000000

$$1 \cdot 2^7 + 0 \cdot 2^6 + 0 \cdot 2^5 + 0 \cdot 2^4 + 0 \cdot 2^3 + 0 \cdot 2^2 + 0 \cdot 2^1 + 0 \cdot 2^0$$

$$2^7 = 128$$

Decimal : 128

16	128	
16	8	- 0
	0	- 8

Hexadecimal : 80

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2.1 Exercises (Number System conversions)

1. Convert the following decimal numbers into binary and hexadecimal numbers:

a. 108

2	108	
2	54	0
2	27	0
2	13	1
2	6	1
2	3	0
2	1	1
	0	1

Binary : 1101100

16	108	
16	6	12 - C
	0	6

Hexadecimal : 6C

b. 4848

2	4848	
2	2424	0
2	1212	0
2	606	0
2	303	0
2	151	1
2	75	1
2	37	1
2	18	1
2	9	0
2	4	1
2	2	0
2	1	0
	0	1

Binary : 100101111000

16	4848	
16	303	0
16	18	15 - f
16	1	2
	0	1

Hexadecimal : 12f0

c. 9000

2	9000	
2	4500	0
2	2250	0
2	1125	0
2	562	1
2	281	0
2	140	1
2	70	0
2	35	0
2	17	1
2	8	1
2	4	0
2	2	0
2	1	0
	0	1

16	9000	
16	562	- 8
16	35	- 2
16	2	- 3
	0	- 2

Hexadecimal : 2328

Binary : 10001100101000

2. Convert the following binary numbers into decimal and hexadecimal numbers.

a. 10000000

$$10000000_2 = 2^7 + 2^6 + 2^5 + 2^4 + 2^3 + 2^2 + 2^1 + 2^0$$

$$2^7 = 128$$

Decimal : 128

16	128	
16	8	- 0
	0	- 8

Hexadecimal : 80

b. 1010101010

$$\begin{array}{ccccccc}
 1 & 0 & 1 & 0 & 1 & 0 & 1 & 0 \\
 | & | & | & | & | & | & | & | \\
 2^9 & 2^8 & 2^7 & 2^6 & 2^5 & 2^4 & 2^3 & 2^2
 \end{array}$$

$$\begin{aligned}
 &= 2^9 + 2^8 + 2^7 + 2^6 + 2^5 + 2^4 \\
 &= 2 + 8 + 32 + 128 + 512 + 2048 \\
 &= 2730
 \end{aligned}$$

Decimal : 2730

16	2730		
16	170	- 10	- A
16	10	- 10	- A
	0	- 10	- A

Hexadecimal : AAA

c. 1000011000

$$\begin{array}{ccccccc}
 1 & 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 & 0 \\
 | & | & | & | & | & | & | & | & | & | \\
 2^9 & 2^8 & 2^7 & 2^6 & 2^5 & 2^4 & 2^3 & 2^2 & 2^1 & 2^0
 \end{array}$$

$$\begin{aligned}
 &= 2^3 + 2^4 + 2^7 \\
 &= 8 + 16 + 512 \\
 &= 536
 \end{aligned}$$

Decimal : 536

16	536		
16	33	- 8	
16	2	- 1	
	0	- 2	

Hexadecimal : 218

3. Convert the following hexadecimal numbers into binary and decimal numbers.

a. 1234

$$\begin{aligned}
 4 \times 16^0 &= 4 \\
 3 \times 16^1 &= 48 \\
 2 \times 16^2 &= 512 \\
 1 \times 16^3 &= 4096 \\
 &= 4096 + 512 + 48 + 4 \\
 &= 4660 \\
 \text{Decimal : } &4660
 \end{aligned}$$

2	4660		
2	2330	- 0	
2	1165	- 0	
2	582	- 1	
2	291	- 0	
2	145	- 1	
2	72	- 1	
2	36	- 0	
2	18	- 0	
2	9	- 0	
2	4	- 1	
2	2	- 0	
2	1	- 0	
2	0	- 1	

Binary : 1001000110100

b. POF

$$P \times 16^2 = 2048$$

$$O \times 16^1 = 0$$

$$F - 15 \times 16^0 = 15$$

$$= 2048 + 15$$

$$= 2063$$

Decimal : 2063

Binary : 100000001111

2	2063	
2	1031	- 1
2	515	- 1
2	257	- 1
2	128	- 1
2	64	- 0
2	32	- 0
2	16	- 0
2	8	- 0
2	4	- 0
2	2	- 0
2	1	- 0
	0	- 1

c. ABCDE

$$A - 10 \times 16^4 = 655360$$

$$B - 11 \times 16^3 = 45056$$

$$C - 12 \times 16^2 = 3072$$

$$D - 13 \times 16^1 = 208$$

$$E - 14 \times 16^0 = 14$$

$$= 655360 + 45056 + 3072 + 208 + 14$$

$$= 703710$$

Decimal : 703710

Binary : 10101011111101110

2	703710	
2	351855	- 0
2	175927	- 1
2	87963	- 1
2	43981	- 1
2	21990	- 1
2	10995	- 0
2	5497	- 1
2	2748	- 1
2	1374	- 1
2	687	- 1
2	343	- 1
2	171	- 1
2	85	- 1
2	42	- 1
2	21	- 0
2	10	- 1
2	5	- 0
2	2	- 1
2	1	- 0
	0	- 1

4. convert the following decimal numbers into binary equivalent.

a. 123.456 D

123

2	123	
2	61	- 1
2	30	- 1
2	15	- 0
2	7	- 1
2	3	- 1
2	1	- 1
	0	- 1

Binary : 1111011

0.456 D \Rightarrow 0.45613

$$0.45613 \times 2 = 0.91226 \quad \text{carry } 0$$

$$0.91226 \times 2 = 0.82452 \quad \text{carry } 1$$

$$0.82452 \times 2 = 0.64904 \quad \text{carry } 1$$

$$0.64904 \times 2 = 0.29808 \quad \text{carry } 1$$

$$0.29808 \times 2 = 0.59616 \quad \text{carry } 0$$

Binary : .01110

123.456 D Binary equivalent

\Rightarrow 1111011.01110

b. 19.25 D

19

2	19	
2	9	- 1
2	4	- 1
2	2	- 0
2	1	- 0
	0	- 1

Binary : 10011

0.25 D \Rightarrow 0.2513

$$0.2513 \times 2 = 0.5026 \quad \text{carry } 0$$

$$0.5026 \times 2 = 0.0052 \quad \text{carry } 1$$

$$0.0052 \times 2 = 0.0104 \quad \text{carry } 0$$

$$0.0104 \times 2 = 0.0208 \quad \text{carry } 0$$

$$0.0208 \times 2 = 0.0416 \quad \text{carry } 0$$

Binary : .01000

19.25 D's Binary equivalent is 10011.01000