

### Question 4.2:

Theorem of expansion of integers in an integer base says that given  $a, b \in \mathbb{N}$ , with  $b > 1$  there exist non-negative integers  $x_0, x_1, \dots, x_n$  such that  $a = x_0 + x_1 b + x_2 b^2 + \dots + x_n b^n$ , with  $0 \leq x_i < b$  and  $x_n \neq 0$ . This is the representation of  $a$  in base  $b$ . The representation  $a$  in base  $b$  is unique.  $\square$

Since, the subset  $\langle 1, q, q^2 \rangle$  is canonical and by using the theorem above. Then for any  $(q \text{ or } n) \geq 2$ , system  $\mathcal{C}$  is canonical.