

Arrays

1) How to create an Array?

Data Type variable name [size];

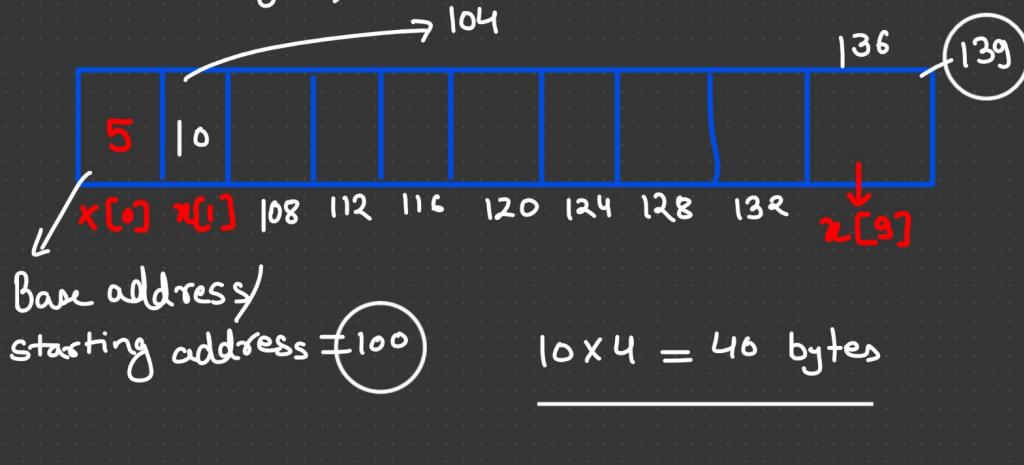
Ex:- `int x[10];`

$$x[0] = 5;$$

$$x[1] = 10;$$

⋮

`int = 4 byte`



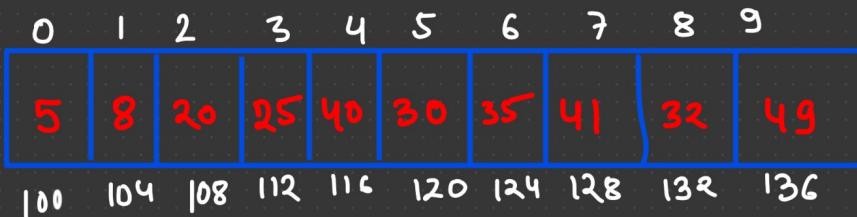
Array is collection of similar type of Elements, stored in contiguous memory allocation.

`int x[10];`

↓
Declaration

$$x = \text{Base address} = 100$$

$$x[0] = \text{Value at } 100. = 5$$



$$x+1 = 104$$

$$x[1] = \text{value at } 104 = 8$$

$$x+6 = 124$$

$$x[6] = \text{value at } 124 = 35$$

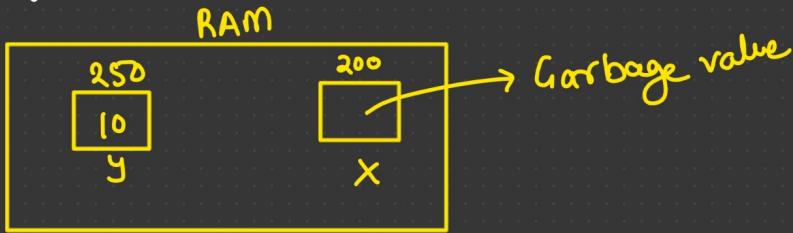
$$x[0] = x + 0 \times 4 = 100 + 0 = 100$$

$$x[2] = 100 + 2 \times 4 = 108$$

$$x[6] = 100 + 6 \times 4 = 124$$

Address = Base Address + (index \times size)

Initialization of an Array:-



`int x;` → Declaration
`x=50;` → Assignment
`int y = 10;` → Initialization

`int a[5];`
 ↓
Declare

1	2	3	4	5
0	1	2	3	4

`int a[5] = {1,2,3,4,5}; // Initialization`

`int a[5] = {1,2,3}; // 1, 2, 3, 0, 0`

`int a[] = {1,2,3,4,5}; // size = 5.`

2) Accessing Array Elements:-

```

for(i=0 ; i<n ; i++)
{
  printf("%d", a[i]);
}
  
```

$i = 0, a[0] = 5$
 $i = 1, a[1] = 10$
 $i = 2, a[2] = 15$
 $i = 3, a[3] = 25$
 $i = 4, a[4] = 35$

5	10	15	25	35
0	1	2	3	4

Q:- WAP to find maximum element from the array.



Write a program

20	18	10	15	30	25	35	28	32	40
0	1	2	3	4	5	6	7	8	9

max
40

```
max = a[0];  
for (i= 1 ; i< 10 ; i++)  
{  
    if [ max < a[i] ]  
        max = a[i];  
}  
printf(" Maximum is %d ", max);
```

Q:- Find the sum of all the elements in the given array.

1	4	5	3	4	7	6
0	1	2	3	4	5	6

Sum
x

$$1+4=5$$

$$5+5=10$$

$$10+3=13$$

$$13+4=17$$

Sum=0;

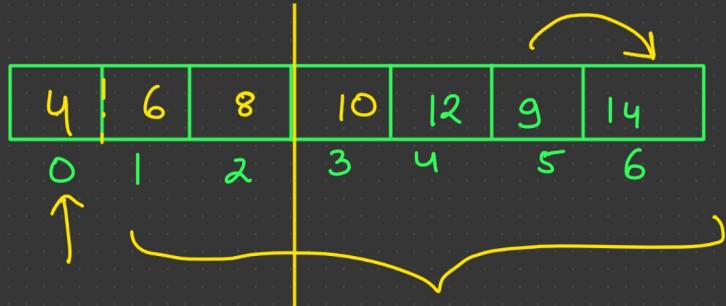
```
for(i=0 ; i< 7 ; i++)  
{  
    sum = sum + a[i];  
}
```

Q:- WAP to sort the given array in increasing order

$$\{ 2, 6, 4, 9, 8 \} \longrightarrow \{ 2, 4, 6, 8, 9 \}$$

$a[0]$

$\text{swap}(j_0, 6);$ | $\text{swap}(10, 6);$
 $\text{swap}(6, 4);$ | $\text{swap}(10, 8);$



$i=0$

$[1, 2, 3, 4, 5, 6]$

$i=1$

$[2, 3, 4, 5, 6]$

$i=2$

$[3, 4, 5, 6]$

$\text{for } (i=0; i < 6; i++)$

{

$\text{for } (j=i+1; j < 7; j++)$

{

$\text{if } (a[i] > a[j])$

$\text{swap}(a[i], a[j]);$

{ }

2D Array :-

	0	1	2	3	Columns
Row → 0	00	01	02	03	
→ 1	10	11	12	13	
→ 2	20	21	22	23	
→ 3	30	31	32	33	

Y-axis

(4,5)

(1,2)

X-axis

Matrix = $4 \times 4 = 16$ cells
 ↓ ↓
 Row Column

int a[4][4];

↓ ↓
 Row Column
 (0-3) (0-3)

int $a[5][4]$;

	0	1	2	3
0	0	1	2	3
1	1	2	3	4
2	2	3	4	5
3	3	4	5	6
4	4	5	6	7

$\uparrow i$

$\uparrow j$

```

for (i = 0 ; i <= 4 ; i++)
{
    for (j = 0 ; j <= 3 ; j++)
        a[i][j] = i + j;
}

```

Memory Representation of 2D Array -

int $a[4][4]$;

	0	1	2	3
0	1	2	3	4
1	5	6	7	8
2	9	10	11	12
3	13	14	15	16

Row 0 Row 1 Row 2 Row 3

100 104 108 112 116 120 124 128 132 136 140 144

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16

↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑

0 1 2 3 0 1 2 3 0 1 2 3 0 1 2 3

→ 16 byte → 16 byte → 16 byte → 16 byte

4x4

$$a[1][2] = 100 + [(4 \times 4) \times 1] + (4 \times 2) = 124$$

$$a[2][3] = 100 + [(4 \times 4) \times 2] + (4 \times 3) = 144$$

(no. of column) sizeof(int)

`int a[R][C];` $a[i][j]$

$$\text{Address} = \text{Base Address} + [C \times (\text{Size of Data Type}) \times i] + (\text{Size of DT}) \times j$$

Q:- Addition of two 3×3 matrix.

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 1 & -1 \\ 4 & 5 & 2 \end{bmatrix}_{3 \times 3}, \quad B = \begin{bmatrix} 3 & 1 & 4 \\ 2 & 0 & 6 \\ -1 & 2 & 4 \end{bmatrix}_{3 \times 3}$$

$$A+B = \begin{bmatrix} 4 & 3 & 7 \\ 4 & 1 & 5 \\ 3 & 7 & 6 \end{bmatrix}$$

$$i=0 \quad j=0, 1, 2$$

$$[0][0] \quad [0][1] \quad [0][2]$$

$$\begin{aligned} \text{int } a[3][3] &= \{1, 2, 3, 2, 1, -1, 4, 5, 2\}; \\ \text{int } b[3][3] &= \{3, 1, 4, 2, 0, 6, -1, 2, 4\}; \\ \text{int } c[3][3] &= \end{aligned}$$

`for (i=0 ; i<3 ; i++)`

{ `for (j=0 ; j<3 ; j++)`

$$\{ \quad c[i][j] = a[i][j] + b[i][j];$$

}

2

Q:- Matrix multiplication 2×2 .

$$A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \xrightarrow{R_1} \begin{bmatrix} 1 & 2 \\ 2 & 4 \end{bmatrix} \xrightarrow{R_2} \begin{bmatrix} 1 & 2 \\ 0 & 4 \end{bmatrix}, \quad B = \begin{bmatrix} C_1 & C_2 \\ 1 & -1 \\ 2 & 3 \end{bmatrix} \downarrow \begin{bmatrix} 00 & 01 \\ 10 & 11 \end{bmatrix} \times \begin{bmatrix} 00 & 01 \\ 10 & 11 \end{bmatrix}$$

$$A \times B = \begin{bmatrix} 1 \times 1 + 2 \times 2 & 1 \times (-1) + 2 \times 3 \\ 3 \times 1 + 4 \times 2 & 3 \times (-1) + 4 \times 3 \end{bmatrix}$$

$$\text{Res} \begin{bmatrix} 00 & 01 \\ 10 & 11 \end{bmatrix}$$

$$R=0 \times C_1$$

$$R=0 \times C_2$$

$$R=1 \times C_1$$

$$R=1 \times C_2$$

$$\text{for } (i=0; i<2; i++) \longrightarrow i=0$$

$$\text{for } (j=0; j<2; j++) \longrightarrow j=0$$

$$\text{for } (k=0; k<2; k++)$$

$$i=0, j=0 \longrightarrow \text{sum} = \begin{bmatrix} 00 & 00 \\ 00 & 00 \end{bmatrix} + \begin{bmatrix} 01 & 10 \\ 01 & 11 \end{bmatrix} + \begin{bmatrix} 00 & 01 \\ 10 & 11 \end{bmatrix}$$

$$\} \quad c[i][j] = \text{sum};$$

}

$$\left| \begin{array}{c} i=1 \\ j=1 \\ K=(0,1) \end{array} \right| \quad \begin{array}{c} i=1 \\ j=0, j=1 \\ K=(0,1) \end{array}$$

$$\boxed{a[i][k] * b[k][j]} \downarrow \text{sum}$$

$$\text{sum} = \text{sum} + a[i][k] * b[k][j]$$

$$\begin{matrix}
 & A & & B \\
 \left[\begin{array}{cc} 00 & 01 \\ 10 & 11 \end{array} \right] & & \left[\begin{array}{cc} 00 & 01 \\ 10 & 11 \end{array} \right]
 \end{matrix}$$

$(00) \xrightarrow{i \uparrow j \downarrow} (00) \times (00)$ + $(01) \xrightarrow{i \downarrow j \uparrow} (01) \times (10)$
 $\xrightarrow{\quad K=0 \quad}$ $\xrightarrow{\quad K=1 \quad}$
 $(10) \xrightarrow{i \downarrow j \uparrow} (10) \times (00)$ + $(11) \xrightarrow{i \uparrow j \downarrow} (11) \times (10)$
 $\xrightarrow{\quad K=0 \quad}$ $\xrightarrow{\quad K=1 \quad}$

$$\begin{array}{c}
 \text{Diagram 1: } \\
 \begin{array}{l}
 \text{Left: } (00) \times (01) \xrightarrow[K=0]{\text{Red arrow}} (00) + (01) = (01) \\
 \text{Right: } (01) \times (11) \xrightarrow[K=1]{\text{Red arrow}} (01) + (11) = (11)
 \end{array} \\
 \text{Diagram 2: } \\
 \begin{array}{l}
 \text{Left: } (10) \times (01) \xrightarrow[K=0]{\text{Red arrow}} (10) + (01) = (11) \\
 \text{Right: } (11) \times (11) \xrightarrow[K=1]{\text{Red arrow}} (11) + (11) = (11)
 \end{array}
 \end{array}$$

```
for(i=0 ; i<2 ; i++)
```

```
for (j=0 ; j<2 ; j++)  
{
```

```

sum = 0;
for(k=0; k<2; k++)
{
    sum = a[i][k] * b[k][j] + sum;
}

```

$$\sum_i c_i [j] = \text{sum}_j$$

{}

Q:- Find Transpose of the given matrix?

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 3 \\ 2 & 4 \end{bmatrix}$$

$$\begin{bmatrix} \underline{00} & \underline{01} & \underline{02} \\ \underline{10} & \underline{11} & \underline{12} \\ \underline{20} & \underline{21} & \underline{22} \end{bmatrix} \rightarrow \begin{bmatrix} 00 & 10 & 20 \\ 01 & 11 & 21 \\ 02 & 12 & 22 \end{bmatrix}$$

for ($i=0$; $i<3$; $i++$)

{
for ($j=0$; $j<3$; $j++$)

{
 $b[i][j] = a[j][i];$

}

}

$$\begin{bmatrix} 00 & 01 & 02 \\ 10 & 11 & 12 \end{bmatrix}$$

2×3

$$\begin{bmatrix} 00 & 10 \\ 01 & 11 \\ 02 & 12 \end{bmatrix}$$

3×2

Q:- Sum of right diagonal / left diagonal?

$$\begin{bmatrix} 00 & 01 & 02 \\ 10 & 11 & 12 \\ 20 & 21 & 22 \end{bmatrix}$$

Left

$$\begin{bmatrix} 00 & 01 & 02 \\ 10 & 11 & 12 \\ 20 & 21 & 22 \end{bmatrix}$$

Right

for ($i=0$; $i<3$; $i++$)
sum = $a[i][i] + \text{sum};$

{

if ($i+j==2$)
sum = $a[i][j] + \text{sum};$

for ($i=0$, $j=2$; $i<3$; $i++$, $j--$)
sum = $a[i][j] + \text{sum};$

3D Array :-

DaryMilk = 0

DaryMilk = 1

No. of DM
Row of DM
Col of DM
 $DM[0][1][2]$

00	01	02	03
10	11	12	13
20	21	22	23

00	01	02	03
10	11	12	13
20	21	22	23

3×4

$0 \rightarrow (12)$

3×4

$1 \rightarrow (12)$

$DM[1][1][2]$

1	2	3	4
---	---	---	---

$1 DM \rightarrow 12$ pieces (each row 4 piece)

$$\frac{12}{4} = 3$$

Box $\rightarrow 4 DM$

Size of Box = ?

`int a[3][4][2];`

`Box[4][3][4];`

$4 \times 3 \times 4$

no. of DM

no. of Row

no. of Col

0	0
1	
2	
3	

0	0	1	1
1			
2			
3			

0	2
1	
2	
3	

No. of element

$$= 3 \times 4 \times 2$$

$$= 24$$

$$a[1][2][1] = 3;$$

int $a[2][2][3] = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\};$

int $a[2][2][3] = \{ \{ \{1, 2, 3\}, \{4, 5, 6\} \}, \{ \{7, 8, 9\}, \{10, 11, 12\} \} \};$

1	2	3
4	5	6

7	8	9
10	11	12

0

1

int $a[] [2] [3] = \{ \underbrace{1, 2, 3}_{0}, \underbrace{4, 5, 6}_{0}, \underbrace{7, 8, 9}_{1}, \underbrace{10, 11, 12}_{1} \};$

1 matrix 2 matrix

int $a[] [3] [2] = \{ \underbrace{1, 2, 3, 4}_{0}, \underbrace{5, 6}_{0}, \underbrace{7, 8, 9}_{1}, \underbrace{10, 11}_{1}, \underbrace{12, 13, 14}_{1}, \underbrace{15, 16, 17}_{2}, 0 \}$

③

①

②

③

for ($i=0; i<3; i++$)

{
 for ($j=0; j<3; j++$)

{
 for ($k=0; k<2; k++$)

{
 $a[i][j][k] = i + j + k;$

{

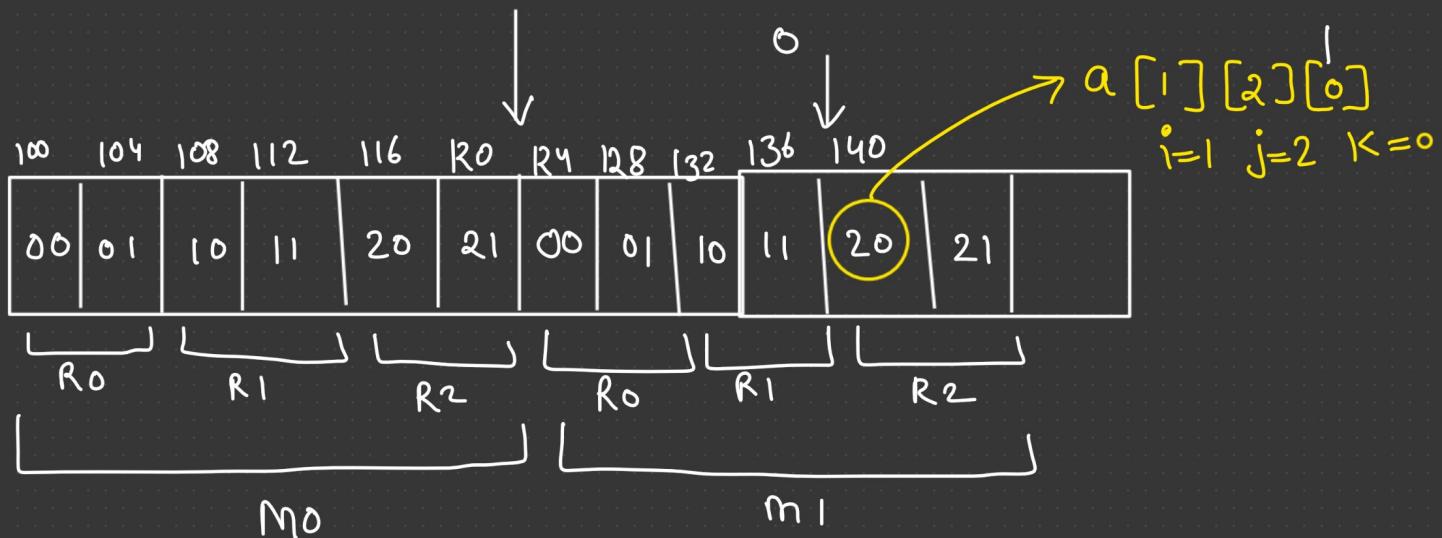
}

int a[2][3][2];

N R C

100	
00	01
10	11
20	21

00	01
10	11
20	21



$$\begin{aligned}
 a[1][2][0] &= 100 + [1 \times (3 \times 2 \times 4)] + [2 \times (2 \times 4)] + (0 \times 4) \\
 &= 100 + 24 + 16 + 0 = 140
 \end{aligned}$$

$$\text{Address} = \text{Base Address} + [i \times (R \times C) \times \text{size}] + [j \times (C \times \text{size})] + (k \times \text{size})$$