Assignment on Confidence Interval

1. Suppose we want to estimate the average weight of an adult male in Dekalb County, Georgia. We draw a random sample of 1,000 men from a population of 1,000,000 men and weigh them. We find that the average man in our sample weighs 180 pounds, and the standard deviation of the sample is 30 pounds. What is the 95% confidence interval?

- 2. The operations manager of a large production plant would like to estimate the mean amount of time a worker takes to assemble a new electronic component. Assume that the standard deviation of this assembly time is 3.6 minutes.
- a) After observing 120 workers assembling similar devices, the manager noticed that their average time was 16.2 minuted. Construct a 92% confidence interval for the mean assembly time.
- b) How many workers should be involved in this study inorder to have the mean assembly time estimated upto ±15 seconds with 92% confidence?

(a)
$$m = 13.6$$

(a) $m = 120$, $M = 16.2$ $Confi = 52\%$.
(c) $T = 16.2 \pm 1.75 \times \frac{3.6}{5120}$
 $= 16.2 \pm 10.575$
 $= (15.625, 16.775)$
(b) $C \cdot I = \pm 15/60$ min $Confi = 121$. $N = 10$
(c) $C \cdot I = 1.75 \times \frac{3.6}{510}$
Scanned with $C \cdot I = 1.75 \times \frac{3.6}{510}$

- 3. Suppose a consumer advocacy group would like to conduct a survey to find the proportion 'p' of consumers who bought the newest generation of an MP3 player were happy with their purchase.
- a) How large a sample 'n' should they take to estimate 'p' with 2% margin of error and 90% confidence?
- b) The advocacy group took a random sample of 1000 consumers who recently purchased this MP3 player and found that 400 were happy with their purchase. Find a 95% confidence interval for 'p'.

(a)
$$Z = \int_{0}^{\infty} P_{0}$$

$$S.E = \int_{0}^{\infty} \frac{P_{2}}{n}$$

$$\frac{2}{100} = \int_{0}^{\infty} \frac{0.9 \times 0.1}{n}$$

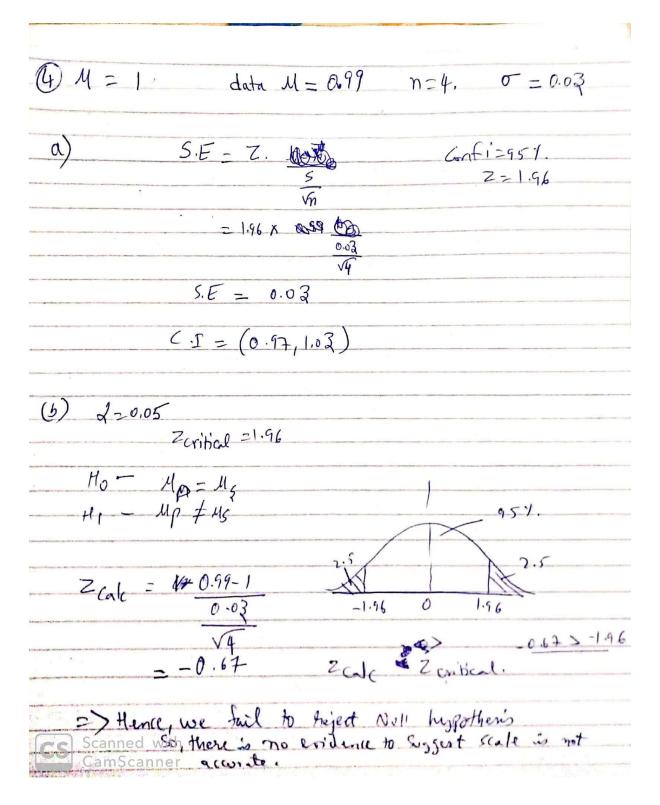
$$\frac{2 \times 2}{100} \times \frac{10 \times 10}{9} = \frac{1}{n}$$

$$n = \frac{1}{100} \times \frac{100}{1000} = \frac{1}{n}$$
(b) $m = 10000 \qquad p = \frac{1}{1000} = 0.4 \qquad 9 = 0.6 \qquad \text{Con } 6:95\%$

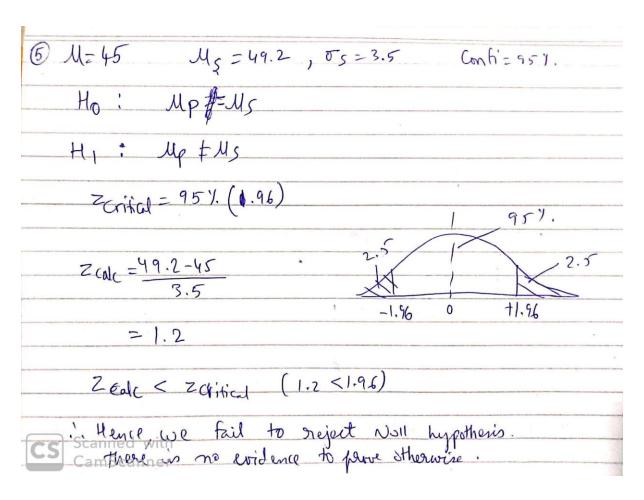
$$S.E = Z \times \sqrt{\frac{P_{0}2}{n}}$$

$$= 1.96 \times \frac{1000}{1000} = 0.03.$$
(CS) Scanned Tith $(0.37, 0.43)$

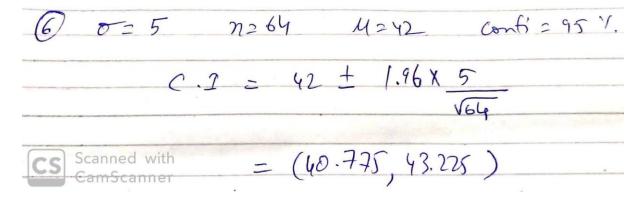
- 4. To assess the accuracy of a laboratory scale, a standard weight that is known to weigh 1 gram is repeatedly weighed 4 times. The resulting measurements (in grams) are : 0.95, 1.02, 1.01, 0.98. Assume that the weighings by the scale when the true weight is 1 gram are normally distributed with mean μ .
- a) Use these data to compute a 95% confidence interval μ .
- b) Do these data gives evidence at 5% significance level that the scale is not accurate?



5. The time needed for college students to complete a certain maze follows a normal distribution with a mean of 45 seconds. To see if the mean time time μ (in seconds) is changed by vigorous exercise, we have a group of nine college students exercise vigorously for 30 minutes and then complete the maze. The sample mean and standard deviation of the collected data is 49.2 seconds and 3.5 seconds respectively. Use these data to perform an appropriate test of hypothesis at 5% level of significance.



6. Installation of a certain hardware takes a random amount of time with a standard deviation of 5 minutes. A computer technician installs this hardware on 64 different computers, with the average installation time of 42 minutes. Compute a 95% confidence interval for the mean installation time.



7. A topic of interest in ophthalmology is whether or not spherical refraction differs between the left and right eye on average. In a study to investigate this, refraction was measured on the left and right eye of 17 patients. The differences (right - left) in diopters were d1,d2,···d17 and elementary calculations gave $\sum di=-3.50$ and $\sum di^2=19.13$. Provide a 90% confidence interval (to 2dp) for the average difference (right - left).

8. What is the smallest sample size required to provide a 95% confidence interval for a mean, if it important that the interval be no longer than 1cm? You may assume that the population is normal with variance 9 cm ^2.

(8) 02 = 9a	2 , 0 = 3 Cm.	Confic 95%.	Z=1.96.
	Intern		
	Jesterala	7.0	
	Jin lound 2	2. 5	
		, G(× ?	
,	=	1.96 × 3	
CS Scanned with CamScanner	η:	= 35	

9. The recommended retail price of a brand of designer jeans is \$150. The price of the jeans in a sample of 16 retailers is on average \$141 with a sample standard deviation of 4. If this is a 'random' sample and the prices can be assumed to be normally distributed, construct a 95% confidence interval for the average sale price.

9
$$\mu = 141$$
, $\sigma = 4$ $n = 16$, $consi = 95 V$. $Z = 1.96$
 $recommed = 150$.

 $C.T = M \pm Z... \sigma$
 $= 141 \pm 1.96 \times 4$
 $\sqrt{16}$

Scanned with $C.T = (139.04, 142.96)$

CamScanner

10. Alcohol abuse has been described by college presidents as the number one problem on campus and is an important cause of death in young adults. A survey of 17,096 students in U.S. four-year colleges collected information on drinking behavior and alcohol-related problems. The researches defined 'frequent binge-drinking' as having five or more drinks in a row three or more times in the past two weeks. According to their definition, 3,314 students were classified as frequent binge-drinkers. Construct a 90% confidence interval around the true proportion of binge-drinkers.

(10)
$$n = 14,096$$
 $p = 3314 | 17026 = 0.194$, $q = 0.806$
Confi = 9 o'/. $z = 1.64$
(.I = $p = 2.5$ Z. p

11. A random sample of 100 items is taken, producing a sample mean of 49. The population std deviation is: 4.49 construct a 90% confidence interval to estimate the population mean.

(I)
$$M_s = 49$$
, $M_s = 100$ $O_p = 4.49$ $Confi = 90$ V .

 $Z = 1.64$

$$C.Z = M_S + Z.$$

$$= 49 + 1.64, 4.49$$

$$\sqrt{100}$$

CS Scanned with $CamScanner$ $= (48.26, 49.74)$

12. Click fraud has become a major concern as more and more companies advertise on the internet. When Google places an ad for a company with its search results, the company pays a fee to Google each time someone clicks on the link. That's fine when it's a person who's interested in buying a product or service, but not so good when it's a computer program pretending to be a customer. An analysis of 1200 clicks coming into a company's site during a week identified that 175 of these clicks are fraudulent. Compute the confidence interval with 95% confidence for the proportion of fraudulent clicks.

(12)
$$n = 1200$$
, $p = 175/1200$ $an 6' = 977.$ $z = 1.96$

$$9 = 0.854$$

$$c. 7 = p + z. fp2$$

$$= 0.146 + 196. fo.146 \times 0.854$$

$$= 0.146 + 196. fo.146 \times 0.854$$

$$= 0.126, fo.166$$

13. Of the 59 basket-ball players, 15 are left-handed. Find the true percentage of left-handed players at 95% confidence.

13)
$$n \ge 5.1$$
, $p = 15/59$, $confi = 95.1$, $z = 1.56$

$$= 0.25$$

$$q = 0.75$$

$$= 0.75 + 1.96 \cdot 0.75 \cdot 0.75$$

$$= 0.14 \cdot 0.36$$

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14. A group of investors wants to develop a chain of fast food restaurants. In determining the potential costs for each facility, they must consider, among other expenses, the average monthly electric bill. They decide to sample fast food restaurants currently opening to estimate the monthly costs of electricity. They want to be 90% confident of their results and want the error of the interval estimate to be no more than \$100. They estimate the such bill have the standard deviation 475. How large the sample should they take?

14) Confi = 90%. Z=1.64
$$\sigma$$
 = 1.64 \times 475

CS Scanned with CamScanner $\eta = 61$

15. A marketing director of a large department store wants to estimate the average number of customers who enter the store every five minutes. She randomly selects five-minute intervals and counts the number of arrivals at the store. She obtains the figures 68, 42, 51, 57, 56, 80, 45, 39, 36 and 79. Using this data, the analyst computes a 95% confidence interval to estimate the mean value for all five-minute intervals. What interval value does she get?

15) lon h' = 95!, r = 1.96 lon h' = 95!

= (45.45,65.15)