

Introduction to Schema refinement:

Schema refinement is intended to address and refinement approach based on decompositions. Redundant storage of information is the root cause of this problem i.e., associated with relational schema.

Problems caused by redundancy:

→ Storing the same information redundantly i.e., in more than one place with in a database can lead to several problems

- i) Redundant storage:- Some information is stored repeatedly.
- ii) Update Anomalies:- If one copy of such repeated data is updated, and inconsistency is created unless all copies are similarly updated.
- iii) Insertion Anomalies:- It may not be possible to store certain information unless some other, unrelated, information is stored as well.

- w) Deletion Anomalies:- It may not be possible to delete certain information without losing some other, unrelated,

information as well.

Name	rating	hourly-wages	hours-worked
Arsh	8	10	40
Smiley	8	10	30
Smith	5	7	30
Gudu	5	7	32
Madam	8	10	40

→ rating → hourly-wages [hourly-wages functionally dependent on rating]

→ Null values help in some cases of redundancy problems but it cannot provide a proper solution to the problem.

→ decomposition: - decomposition can eliminate Redundancy

→ functional dependencies [FD] can be used to identify such a situations and suggest refinements to the problem schema

→ A decomposition of a relational schema R consists of replacing the relational schema by two or more Relation schemas that each contain a subset of the attributes of R and together include all attributes in R.

Ex:  $\rightarrow$  Table 1 (name, rating, hourly-worked)  
Table 2 (rating, hourly-wages)

Table - 1

name rating hourly-worked

Aush	8	40
Smiley	8	30
Smith	5	30
Gudie	5	32
Madam	8	40

decomposition problems:

decomposing a relation schema can create more problems than it solves. Two important questions must be asked repeatedly.

Q1) Do we need to decompose a relation

A) Normalisation

Q2) What problems (if any) does a given decomposition cause?

A) i) Loss less JOIN decomposition property

ii) dependency preservation property

### \* FUNCTIONAL DEPENDENCY:

A FD is a kind of integrity constraint that generalizes the concept of key.

Let R be a Relation Schema & let X, Y be non-empty sets of attributes in R.

An instance 'r' of R satisfies the FD

study-worked  
exercises

$x \rightarrow y$  if the following holds for  
every pair of tuples  $t_1$  &  $t_2$  in  $R$ .

Table 2

h-wages  
10  
 $\neq$

can create  
important  
y.  
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$x \rightarrow y$  if  $t_1 \cdot x = t_2 \cdot x$ , then  $t_1 \cdot y = t_2 \cdot y$

$x \rightarrow y$  is read as  $x$  Functionally determines  $y$   
or simply called as  $x$  determines  $y$

A	B	C	D
a <sub>1</sub>	b <sub>1</sub>	c <sub>1</sub>	d <sub>1</sub>
a <sub>1</sub>	b <sub>2</sub>	c <sub>1</sub>	d <sub>2</sub>
a <sub>2</sub>	b <sub>2</sub>	c <sub>2</sub>	d <sub>2</sub>
a <sub>2</sub>	b <sub>2</sub>	c <sub>2</sub>	d <sub>3</sub>
a <sub>3</sub>	b <sub>3</sub>	c <sub>2</sub>	d <sub>4</sub>

if

$a_1 \rightarrow c_3$    
  $a_1 \rightarrow c_4$    
 not FD

$a_2 \rightarrow c_1$    
  $a_3 \rightarrow c_1$    
 FD

$A \rightarrow B$  (NO)

$A \rightarrow C$  (YES)

$A \rightarrow D$  (NO)

$B \rightarrow C$  (NO)

$B \rightarrow D$  (NO)

$C \rightarrow D$  (NO)

Reasoning about functional dependencies:-

Workers (ssn, name, lot, did, sname)

$ssn \rightarrow did$  holds [FD]

$did \rightarrow lot$  holds [FD]

then  $ssn \rightarrow lot$  holds [FD]

\* Closure set of FD's:-

The set of all FD's implied by a given set F of FD's is called the closure of F denoted as  $[F^+]$

Inference Rules of FD's:- [Armstrong's Axioms]

→ x, y and z to denote set of attributes over a relation schema R:

i) Reflexivity: If  $x \supseteq y$ , then  $x \rightarrow y$

ii) Augmentation: If  $x \rightarrow y$ , then

$$xz \rightarrow yz \text{ for any } z$$

iii) Transitivity: If  $x \rightarrow y$  and  $y \rightarrow z$  then

$$x \rightarrow z$$

Some additional rules added

iv) Union or Additive Rule: →

If  $x \rightarrow y$  and  $x \rightarrow z$ , then  $x \rightarrow yz$

v) Decomposition: If  $x \rightarrow yz$  then

$$x \rightarrow y \text{ and } x \rightarrow z$$

vi) Pseudo-transitive Rule: If  $\alpha \rightarrow yz$

$yz \rightarrow w$  then  $\alpha \rightarrow w$

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$x \rightarrow y$

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$x \rightarrow yz$

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$F(CSJD, P, Q, V)$

eg:-  $C \rightarrow CSJD, P, Q, V$

$JP \rightarrow C$

$SD \rightarrow P$

Ref  $\rightarrow C \rightarrow C, C \rightarrow S, C \rightarrow J, C \rightarrow P, C \rightarrow D,$   
 $C \rightarrow Q, C \rightarrow V$

Arg:- If  $SD \rightarrow P$  then  $SD \rightarrow JP$ .

transitivity  $\rightarrow$  If  $JP \rightarrow C \& C \rightarrow CSJD, P, Q, V$  then

$JP \rightarrow CSJD, P, Q, V$

\* Attribute closure ( $x^+$ ):-

closure =  $x$  ;

repeat until there is no change:

if there is an FD  $U \rightarrow V$  in  $F$  such that  $U \subseteq \text{closure}$ , then set  $\text{closure} =$   $\text{closure} \cup V$

Ex:- Compute the closure of the following closure UV

R(A, B, C, D, E) set F of FD's for Relation schema R and

FD's are  $AB \rightarrow C, CD \rightarrow E, DE \rightarrow B$

list the candidate keys for R.

$A^+ = \{A\}$

$B^+ = \{B\}$

$C^+ = \{C\}$

$D^+ = \{D\}$

$E^+ = \{E\}$

$AB^+ = \{A, B, C\}$

$AC^+ = \{A, C\}$

$AD^+ = \{A, D\}$

$AE^+ = \{A, E\}$

$ABC^+ = \{A, B, C\}$

$ABD^+ = \{A, B, D, E\}$

$ABE^+ =$

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B7

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$$BC^+ = \{B, C\}$$

$$BD^+ = \{B, D\}$$

$$BE^+ = \{B, E\}$$

$$CD^+ = \{C, D, E, B\}$$

$$DE^+ = \{D, E, B\}$$

$$ABE^+ = \{A, B, C\}$$

$$Ex-2 \quad R = \{A, B, C, D, E\}$$

$$A \rightarrow BC, \quad CD \rightarrow E, \quad B \rightarrow D, \quad E \rightarrow A$$

$$[A^+] = \{A, B, C, D, E\}$$

$$[B^+] = \{B, D\}$$

$$[C^+] = \{C\}$$

$$[D^+] = \{D\}$$

$$[E^+] = \{E, A, B, C, D\} \notin$$

$$AB^+ = \{B, C, D, E, A\}$$

$$AC^+ = \{A, B, C, D, E\}$$

$$\{A, E\}$$

CD, BC are candidate keys

11/2/20

super key:- Specifies that no two distinct tuple can have same value for super key.  
set of attributes used to differ all tuples. It may have redundant values  
→ superset of attributes to the candidate key is super key. but not every super key not a candidate key.

definition of superkey:-

A super key is a set of attributes with in a table whose values can be used to uniquely identify a tuple.

Ex:- BOOK

BId	Bname	Author	
B1	XYZ	A1	{BId}
B2	ABC	A1	SK = {Bname, Author}
B3	XYZ	A2	{BId, Bname}
B4	PQR	A3	{BId, Bname, Author}
B5	SRP	A1	↓
B6	ABC	A3	trival SK

The redundant values are accepted in SK  
Candidate key:- A candidate key is a minimal set of attributes necessary to identify a tuple this is also called as

minimal super key

Ex:-  $CK = \{B, C\}$

NOTE:- If more than one are candidate keys then if the database designer can select one key from two, the one key which is selected by database designer is declared as primary key.

and those which are not selected as PK is called Alternate key.

→ CK & PK are same which is used to identify tuples uniquely within the relation.

→ PK is the minimal Super key.

→ Normally PK is composed of only a single attribute but it is possible to have a PK composed of more than one attribute then the more no. of primary keys are called as composite attributes.

Ex:- ①  $R(A, B, C, D, E)$

$A \rightarrow C$      $C \rightarrow B$      $D \rightarrow E$

$$A^+ = \{A, C, B\}$$

$$B^+ = \{B\}$$

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$$C^+ = \{C, B\}$$

$$D^+ = \{D, E\}$$

$$E^+ = \{E\}$$

$$\{AB^+\} = \{A, B, C\}$$

$$\{AC^+\} = \{A, C, B\}$$

$$\{AD^+\} = \{A, C, B, D, E\}$$

$$\{AE^+\} = \{A, E, C, B\}$$

$$\{BC^+\} = \{B, C\}$$

$$\{BD^+\} = \{B, D, E\}$$

$$\{BE^+\} = \{B, E\}$$

$$\{CD^+\} = \{C, B, D, E\}$$

$$\{CE^+\} = \{C, B, E\}$$

$$\{DE^+\} = \{D, E\}$$

$$\{ABC^+\} = \{A, B, C\}$$

$$\{ABD^+\} = \{A, B, D, C, E\}$$

$$\{ABE^+\} = \{A, B, E, C\}$$

$$\{ACD^+\} = \{A, C, D, B, E\}$$

$$\{ACE^+\} = \{A, C, B, E\}$$

$$\{ADE^+\} = \{A, D, E, C, B\}$$

$$\{BCD^+\} = \{B, C, D, E\}$$

$$\{BCE^+\} = \{B, C, E\}$$

$$\{BDE^+\} = \{B, D, E\}$$

$$\{CDE^+\} = \{C, D, E, B\}$$

$$\{ABC^+\} = \{A, B, C, D, E\}$$

$$\{ACDE^+\} = \{A, C, D, E, B\}$$

$$SK = \{AD, ACD,$$

$$ADE, ABCD,$$

$$ACDE, ABCDE,$$

$$ADBE\}$$

$$CK = \{AD\}$$

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- 2)  $R(A, B, C, D, E, F)$   
 $A \rightarrow C, C \rightarrow D, D \rightarrow B, E \rightarrow F$
- $A^+ = \{A, C, D, B\}$        $ABC^+ = \{$   
 $B^+ = \{B\}$        $CK = \{A, E\}$   
 $C^+ = \{C, D, B\}$   
 $D^+ = \{D, B\}$   
 $E^+ = \{E, F\}$   
 $F^+ = \{F\}$
- $AB^+ = \{A, B, C, D\}$   
 $AC^+ = \{A, C, D, B\}$   
 $AD^+ = \{A, D, C, B\}$   
 $AE^+ = \{A, C, D, B, E, F\}$   
 $AF^+ = \{A, C, D, B, F\}$   
 $BC^+ = \{B, C, D\}$   
 $BD^+ = \{B, D\}$   
 $BE^+ = \{B, E, F\}$   
 $BF^+ = \{B, F\}$   
 $CD^+ = \{C, D, B\}$   
 $CE^+ = \{C, D, B, E, F\}$   
 $CF^+ = \{C, D, B, E, F\}$   
 $DE^+ = \{D, B, E, F\}$   
 $DF^+ = \{D, B, F\}$

③  $R(A, B, C, D, E)$

$A \rightarrow BCDE$ ,  $BC \rightarrow ADE$

$A^+ = \{B, C, D, E, A\}$

$B^+ = \{B\}$

$BC^+ = \{A, D, E, B, C\}$

$CK = \{A^+\}$ ,

$\{BC^+\}$

$PK = \{A\}$

M/2120

Normal Form's:

Breaking table or relation into more relations. The relation is going to be decompose with the help of Normal forms.

→ Normalization is a database design technique which organises table in a manner that reduces redundancy and dependency of data.

→ It divides larger tables to smaller tables and links them using relationships.

→ It is a systematic approach of decomposing tables to eliminate data redundancy and undesirable characteristics like

insertion, deletion and update Anomalies.

→ It is a multi step process that puts data into tabular form removing duplicated data from relation tables.

→ Normalization is used for mainly two

purpose:

By eliminating redundant data from database  
or decreasing data dependency rate make  
data more logically consistent.

• Implementations rules are divided into:  
Following normal forms [First Normal,  
Second and 3rd of which is perform better,  
options]

1. First Normal Form [1NF]
2. Second Normal Form [2NF]
3. Third Normal Form [3NF]
4. Boyce-Codd Normal Form [BCNF]
5. Fourth Normal Form [4NF]
6. Fifth Normal Form [5NF].

1NF:-

- i) It should follow the following rules
- ii) It should only have single valued attributes (Attribute)
- iii) Each record needs to be unique
- iv) All the columns in a table should have unique names
- v) No composite values
- vi) Values stored in column should be of the same domain

(useless data  
to sense re)

id into the  
realization  
& decomposi-

ex:-

Student		
roll no	Name	courses
101	A	DBMS, SC, FLAT
102	B	FLAT, DS
103	C	DS, DBMS, SE

student table is not in 1NF. To make  
student table in 1NF.

Student		
roll no	Name	courses
101	A	DBMS
101	A	SE
101	A	FLAT
102	B	FLAT
102	B	DS
102	C	DS
103	C	DBMS
103	C	SE
103	C	

2NF:

i) for a relation to be in the second NF  
it should be in the 1NF

ii) And it should not have partial dependency  
(or) it should contains only fully  
functional dependency.

Ex:-  $F(A, B, C, D, E, F)$

$A \rightarrow BCDEF$

$BC \rightarrow ADEF$

$B \rightarrow F$

$D \rightarrow E$

$A^+ = \{A, B, C, D, E, F\}$

$BC^+ = \{B, C, A, D, E, F\}$

$B^+ = \{B, F\}$

$D^+ = \{D, E\}$

CK: A, BC [prime attributes]

(NPA) Nonprime attributes:- D, E, F

NPA  $\rightarrow$  D is fully functional dependent on A, BC

E is fully FD on A/BC

F is not fully FD on BC.

there is a problem with F so it is placed in another tab.  
to make it in 2NF.

$F(A, B, C, D, E, F)$

$F1(A, C, D, E, B)$

$A \rightarrow BCDE$

$BC \rightarrow ADE$

$D \rightarrow E$

$F2(B, F)$

$B \rightarrow F$

common attribute

$\alpha: R(A, B, C, D, E)$

$AB \rightarrow C$

$C \rightarrow D$

$B \rightarrow E$

$$AB^+ = \{A, B, C, D, E\}$$

$$XY \rightarrow W$$

$$Y \rightarrow W$$

(partial).

$$C^+ = \{C, D\}$$

$$B^+ = \{B, E\}$$

(PA) CK :  $\{AB\}$

NPA :  $\{C, D, E\}$

C is fully FD on AB.

D is not fully FD on AB

E is not fully FD on AB

$R(A, B, C, D, E)$

$\overline{R_1(A, B, C, D)}$

$\overline{R_2(B, E)}$

$AB \rightarrow C$

$B \rightarrow E$

$C \rightarrow D$

CFI-B

CK: -AB

NPA: -E

NPA: -C, D

2NF

2NF

3NF:

- i) Relation should be in 2NF
- ii) Relation should not contain any Transitive dependency.

$X \rightarrow Y$  be the non-trivial FD is in 3NF if  $X$  should be candidate key or super key or  $Y$  should be prime attribute

[Note:- there should not be the case that a NPA is determined by another NPA]

$R_1(A, B, C, D)$

$AB \rightarrow C$

$C \rightarrow D$

$AB^+ = \{A, B, C, D\}$

$CK = \{AB\}$  (PA)

NPA =  $C, D$

$R_1(A, B, C, D)$

$R_1(A, B, C)$

$AB \rightarrow C$

3NF

Also in BCNF

$R_3(G, D)$

$C \rightarrow D$

NF

BCNF

$R_2(B, E)$

$B \rightarrow E$

3NF

BCNF

NF

contain any

(0)

Initial FD is

>e candidate  
would be

case that

Another

from  
 $E^c \rightarrow ①$

$F(a, b, c, d, e, f)$

$F_1(a, b, c, d, e)$

$A \rightarrow BCD$

$BC \rightarrow ADE$

$D \rightarrow E$

$F_2(b, f)$

$B \rightarrow F$

3NF

BCNF

$A^+ = \{a, b, c, d, e\}$

$BC^+ = \{b, c, a, d, e\}$

$D^+ = \{d, e\}$

$PA = \{a, bc\}$

$F_1(a, b, c, d, e)$

$F_{1.1}(a, b, c, d)$

$A \rightarrow BCD$

$BC \rightarrow AD$

$PA \rightarrow A, BC$

$F_{1.2}(d, e)$

$D \rightarrow E$

$PA \rightarrow D$

3NF

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BCNF

2.1.1

BCNF:

- i) It has to be in 3NF
- ii) In relation  $x \rightarrow y$  is a non-trivial FD if X should contain candidate key or super key

Ex:  $R(A, B, C, D)$

$A \rightarrow BCD$

$BC \rightarrow AD$

$D \rightarrow B$

$$A^+ = \{A, B, C, D\}$$

$$B^+ = \{B, C, A, D\}$$

$$D^+ = \{D, B\}$$

$$CR = \{A, BC\}$$

NPA  $\rightarrow D$

It is in 3NF

$R(A, B, C, D)$  If we take

$R_1(A, C, B)$

$A \rightarrow BCD$

$BC \rightarrow AD$

$R_2(B, D)$  then it will

not be in

3NF

satisfying

transitive  
property

~~$B \rightarrow D$~~

$D \rightarrow B$

CK: {<sup>SCFA</sup>  
 $A, C$ }

NPA-D

BCNF:

$P_A \rightarrow D$

$NPA \rightarrow B$

BCNF

determin.

1)  $R($

$VY \rightarrow$

$WX \rightarrow$

$ZY \rightarrow$

2)  $R($

$A \rightarrow$

$BE \rightarrow$

3)  $R(f$

$A \rightarrow$

$BC \rightarrow$

$AE \rightarrow$

4)  $R($

$N$

$OF$

$R$

5)

6)

determine NF for given relations.

-trivial  
candidate key

1)  $R(v, w, x, y, z)$

$$v \cdot y \rightarrow w$$

$$w \cdot x \rightarrow z$$

$$z \cdot y \rightarrow v$$

3NF

2)  $R(A, B, C, D, E)$

$$A \rightarrow B \cdot C$$

$$B \cdot C \cdot D \rightarrow A \cdot E$$

2NF

3)  $R(A, B, C, D, E, F, G)$

$$A \rightarrow B$$

$$A^+ = \{A, B\}$$

1NF

$$B \cdot C \rightarrow D \cdot E$$

$$B \cdot C^+ = \{B, C, D, E\}$$

$$A \cdot E \cdot F \rightarrow G$$

$$A \cdot E \cdot F^+ = \{A, E, F, B, G\}$$

4)  $R(N, O, P, Q, R)$

$$N^+ = \{O, P, Q, N, R\} \Rightarrow P.A$$

$$N \rightarrow O \cdot P \cdot Q$$

$$O \cdot P \cdot Q^+ = \{O, P, Q, R\} \quad 2NF$$

$$O \cdot P \cdot Q \rightarrow R$$

$$R^+ = \{P, Q, R\}$$

$$R \rightarrow P \cdot Q$$

5)  $R(A, B, C, D, E)$

$$A \cdot B^+ = \{A, B, C, D, E\} \Rightarrow P.A$$

$$A \cdot B \rightarrow C$$

$$B^+ = \{D, B\}$$

(1NF)

$$B \rightarrow D$$

$$C^+ = \{C, E\}$$

$$C \rightarrow E$$

6)  $R(A, B, C, D)$

$$A \cdot B^+ = \{A, B, C, D, A\}$$

$$A \cdot B \rightarrow C \cdot D$$

$$B^+ = \{A, B, C, D\}$$

3NF

$$B \rightarrow A$$

$$C^+ = \{C, B, A, D\}$$

B.CNF

$$C \rightarrow D$$

2M1

1)  $R(v, w, x, y, z)$ 

$vY \rightarrow w$

$wx \rightarrow z$

$zy \rightarrow v$

$VY^+ = \{v, y, w\}$

$wx^+ = \{w, x, z\}$

$zy^+ = \{z, y, v, w\}$

(2NF)  $VY^+ W^+ (v, y, w)$ 

17/10/20 VYWXZ

4NF:

- for a table to satisfy the fourth normal form it should satisfy the following conditions

1) It should be in the BCNF

2) The table should <sup>not</sup> have any multi-valued dependency (or)

In Relation R for every multi-valued dependency ( $X \rightarrow\!\!\! \rightarrow Y$ ) that hold over relation R has to be a)  $Y \subseteq X$  or

$XY = R$  (or)

b)  $X$  is a Super Key2)  $R(A, B, C, D, E)$ 

$A \rightarrow BC$

$D \rightarrow AE$

$A^+ = \{A, B, C\}$

$D^+ = \{D, A, E, B\}$

$PA = D$

2NF

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$C, D, E$ )  
G.  
 $E$   
 $B, C \}$   
 $A, E, B, C \}$

multi-valued dependency:

A table is said to have multi-valued dependency if the following conditions are true.

- 1) For a dependency  $A \rightarrow B$  if for a single value of A multiple value of B exists then the table may have multi-valued dependency.
- 2) Also a table should have at least 3 columns for it to have a multi-valued dependency. (OR)

A multi-valued dependency consists of at least 2 attributes that are dependent on third attribute that's why it always requires at least 3 attributes.

- 3) And for a relation  $R(A, B, C)$  if there is a multivalued dependency between A & B then B & C should be independent of each other. (OR)

Multi-valued dependency occurs when two attributes in a table are independent of each other but both depend on a third attribute.

- If all these conditions are true for any relation or table then it is said to have multi-valued dependency.

Eg: student

sid	course	hobby	course
1	science	cricket	1
1	maths	hockey	1
2	C#	cricket	2
3	PHP	HOCKEY	2

so there is a multi valued dependency  
which leads to unnecessary repetition  
of data and other anomalies as well.

Hobbies

sid	Hobby
1	cricket
1	hockey
2	cricket
2	HOCKEY

- To make the student in 4<sup>th</sup> NF decompose the student table into two tables they are course table & hobbies table
- Now course tables & hobbies tables are in 4NF

→ A table can also have functional dependency along with multivalued dependency. In that case the functional dependency columns are moved in a separate table and the multi valued dependent columns are moved to separate table.

Eg: → Student 1

sid address course hobby

sid → address (FD)

sid → course

sid → hobby

decomposed into 3 tables:

(sid → address) (sid → course) (sid → hobby)

I table

II table

III table

Address table

course table

hobby table

NOTE:- for fourth NF a relation has to be in BCNF and a given relation contain more than one multi valued attributes.

Eg: → sid subject activity

| music Tennis

| Accounting Tennis

| music Swimming

| Accounting Swimming

sid → subject

sid → activity

Table 4		
std subject		
1	MUSIC	
1	ACCOUNTING	

Table 2	
std	Activity
1	TENNIS
1	SWIMMING

Inference  
Axioms  
three of  
1) MVD

Table 5

P	M	F	$P \rightarrow M$
P1	M1	F1	
P1	M2	F2	$P \rightarrow F$
P1	M1	F2	
P1	M2	F1	
P2	M3	F2	

multivalued dependency

Addit

other

M'

4

S.

- 1) MVD occurs when 2 attributes in a table are independent of each other but both depend on a third attribute.
- 2) A MVD consists of at least 2 attributes that are dependent on a 3<sup>rd</sup> attribute that why it always requires at least 3 attributes  
If  $R(x, y, z)$  p.c. If  $x \rightarrow y$  holds over Relation R  
and  $z = R - xy$

NO

A/

NC

a

\* MVDS: If  $x \rightarrow y$  holds over R, then

$$\Pi_{yz}(\sigma_{x=z}(R)) = \Pi_y(\sigma_{x=z}(R)) \times \Pi_z(\sigma_{x=z}(R))$$

Inference rules consists of the 3 Armstrong Axioms

three of the additional rules involve only MVD's

1) MVD complementation:- If  $x \rightarrow\!\!> y$ , then

$$x \rightarrow\!\!> R - xy$$

2) MVD augmentation:- If  $x \rightarrow\!\!> y$  and

$$w \supseteq z, \text{ then } w x \rightarrow\!\!> y$$

3) MVD transitivity:- If  $x \rightarrow\!\!> y$  and

$$y \rightarrow\!\!> z \text{ then } x \rightarrow\!\!> (z-y)$$

Additional Rules:

The remaining 2 rules relate FD's and MVD's

4) Replication: If  $x \rightarrow y$ , then  $x \rightarrow\!\!> y$

5) Coalescence: If  $x \rightarrow y$  and there is a  $w$  such that  $w \cap y$  is empty,  $w \supseteq z$ , and  $y \supseteq z$ , then  $x \rightarrow z$

Note:- Every FD is also an MVD

AKF definition  $\rightarrow$  If R has to be in BCNF

Note:- 1) Trivial FDs - a set of attributes which are called a trivial if the set of attributes are included in that attribute.

2in1

so  $X \rightarrow Y$  is a TFD if  $Y$  is a subset of  $X$   
 2) Non-trivial FD:— when  $A \rightarrow B$  holds true,  
 where  $B$  is not a subset of  $A$ .

22/2/20 5NF:-

A relation is in 5<sup>th</sup> normal form if it is  
 in 4NF and not contains any join dependency.  
 → 5NF is satisfied when all the tables are  
 broken into as many tables as possible in  
 order to avoid redundancy.  
 → 5NF is also known as project-JOIN NF

### [PJ/NF]

Ex:- suppliers parts project

S1	P1	π1
S1	P2	π2
S2	P1	π1
S2	P1	π2

NOTE: If Join dependency not exist then  
 the relation R is in 5NF else if  
 Join dependency exists then it is  
 trivial Join dependency then that relation  
 is in Join dependency, else if all  $R_i$   
 where  $R_1 \rightarrow R_1, R_2, \dots, R_n$

e.g.  $\tau = 1, 2, \dots, n$  is superkey then  
it is said to be in 5NF

R1		R2		R3	
suppliers	parts	suppliers	project	parts	project
S1	P1	S1	T1	P1	T1
S1	P2	S1	T2	P2	T2
S2	P1	S2	T1	P1	T2
		S2	T2		

$R1 \bowtie R2$

suppliers parts project

S1	P1	T1
S1	P1	T2
S1	P2	T1
S1	P2	T2
S2	P1	T1
S2	P1	T2

$R1 \bowtie R2 \bowtie R3$

suppliers parts project

S1	P1	T1
S1	P1	T2
S1	P2	T2

## Properties of decomposition

### → Relational Decomposition:-

When the relation in a relational model is not in appropriate NF then the decomposition of relation is required.

→ In a database it breaks the table into multiple tables.

→ If the relation has no proper decomposition then it may lead to problems like loss of information.

→ decomposition is used to eliminate some of the problems of bad design like Anomalies, inconsistencies and redundancy.

### → Types of decompositions:

There are two types:

1) Loss less decomposition

2) dependency preserving

Loss less decomposition: If the information is not lost from the relation i.e. decompd then the decomposition will be loss less.

→ The loss less decomposition guarantees that the join of relations will result in the same relation as it was decomposed.

the relation is said to be loss less decomposition  
if Natural Joins of all the decomposition  
give the original relation.

Ex:- employee-department table.

Emp-ID	Emp-Name	Emp-age	Dept-city	Dept-ID	Dept-Name
22	Denim	28	mumbai	824	Sales
33	Alina	25	Delhi	438	marketing
46	Stephan	30	Banglore	869	Finance
52	Katherine	36	Mumbai	575	Production
60	Jack	40	Noida	678	Testing

Employee table

Emp-ID	Emp-name	Emp-age	Emp-city
22	Denim	28	mumbai
33	Alina	25	Delhi
46	Stephan	30	Banglore
52	Katherine	36	Mumbai
60	Jack	40	Noida

Department table

emp-ID	Dept-ID	Dept-Name
22	824	Sales
33	438	Marketing
46	869	Finance
52	575	Production
60	678	Testing

Employee  $\bowtie$  Department

Emp-ID	Emp-name	Emp-age	Dept-city	Dept-ID	Dept-Name
22	Denim	28	mumbai	824	Sales
33	Alina	25	Delhi	438	marketing
46	Stephan	30	Banglore	869	Finance
52	Katherine	36	Mumbai	575	Production
60	Jack	40	Noida	678	Testing

hence the decomposition is loss-less join decomposition.

→ dependency preserving:

It is an important constraint of the database. In the dependency preservation at least one decomposed table must satisfy every dependency

→ If a relation R is decomposed into Relation R<sub>1</sub> and R<sub>2</sub> then the dependencies of R either must be a part of R<sub>1</sub> or R<sub>2</sub> or must be derivable from the combination of functional dependencies of R<sub>1</sub> & R<sub>2</sub>.

→ for example:- Suppose there is a relation R (A, B, C, D) with functional dependency set A → BC the relation R is decomposed into R<sub>1</sub>(A, B, C) & R<sub>2</sub>(A, D) which is dependency preserving. bcoz functional dependency A → BC is a part of relation R<sub>1</sub>(A, B, C).