

Example 2.79 Obtain the star connected equivalent for the delta connected circuit shown in Fig. 2.130.

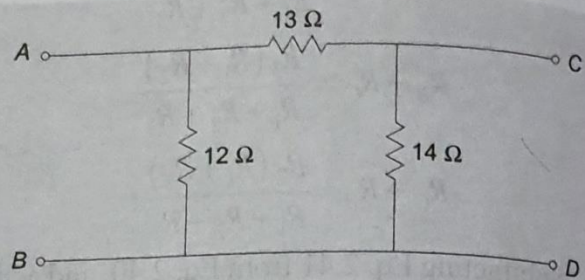


Fig. 2.130

Solution The above circuit can be replaced by a star connected circuit as shown in Fig. 2.131(a).

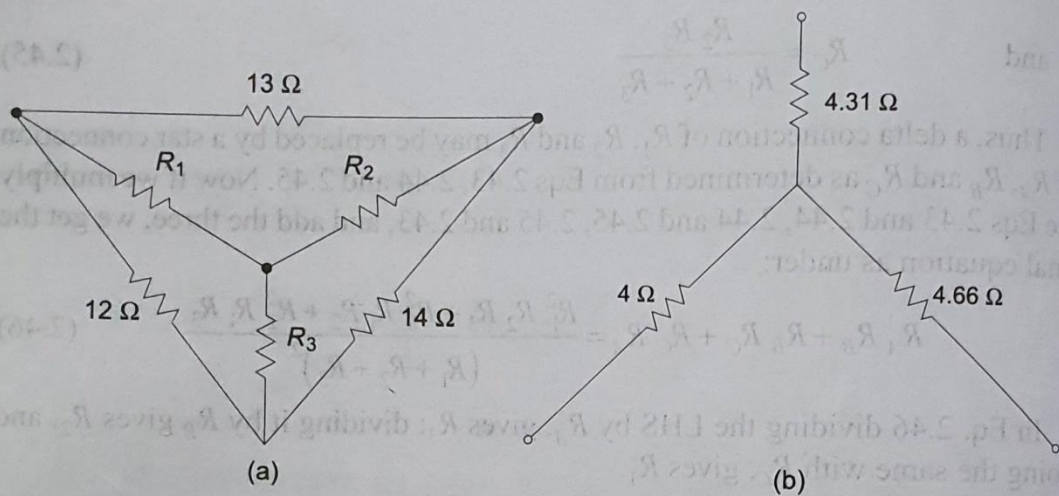


Fig. 2.131

Performing the Δ to Y transformation, we obtain

$$R_1 = \frac{13 \times 12}{14 + 13 + 12}, \quad R_2 = \frac{13 \times 14}{14 + 13 + 12}$$

and
$$R_3 = \frac{14 \times 12}{14 + 13 + 12}$$

$\therefore R_1 = 4 \Omega, R_2 = 4.66 \Omega, R_3 = 4.31 \Omega$

The star-connected equivalent is shown in Fig. 2.131 (b).

Example 2.80 Obtain the delta-connected equivalent for the star-connected circuit shown in Fig. 2.132.

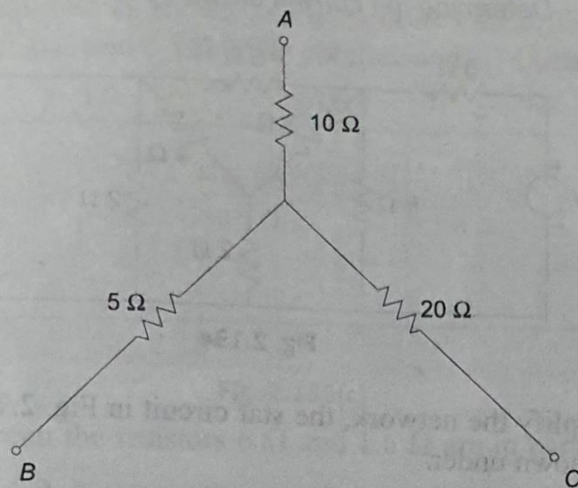


Fig. 2.132

Solution The above circuit can be replaced by a delta-connected circuit as shown in Fig. 2.133(a).

Performing the Y to Δ transformation, we get from the Fig. 2.133 (a)

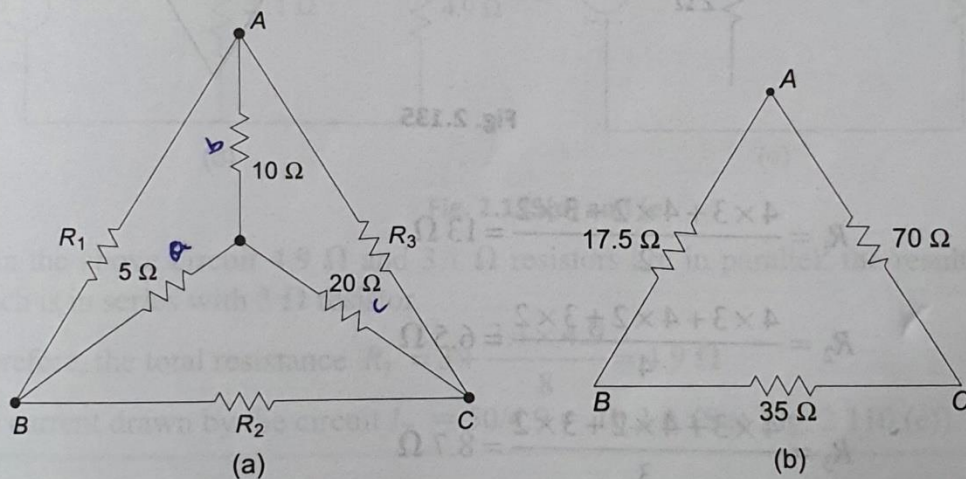


Fig. 2.133

$$R_1 = \frac{20 \times 10 + 20 \times 5 + 10 \times 5}{20} = 17.5 \Omega$$

$$R_2 = \frac{20 \times 10 + 20 \times 5 + 10 \times 5}{10} = 35 \Omega$$

and

$$R_3 = \frac{20 \times 10 + 20 \times 5 + 10 \times 5}{5} = 70 \Omega$$

The equivalent delta circuit is shown in Fig. 2.133 (b).

Example 2.81

Determine the current drawn by the circuit shown in Fig. 2.134.

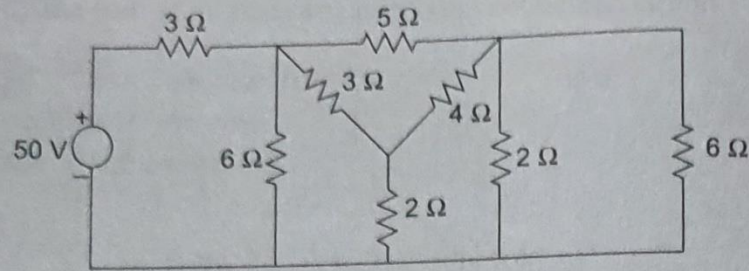


Fig. 2.134

Solution To simplify the network, the star circuit in Fig. 2.134 is converted into a delta circuit as shown under.

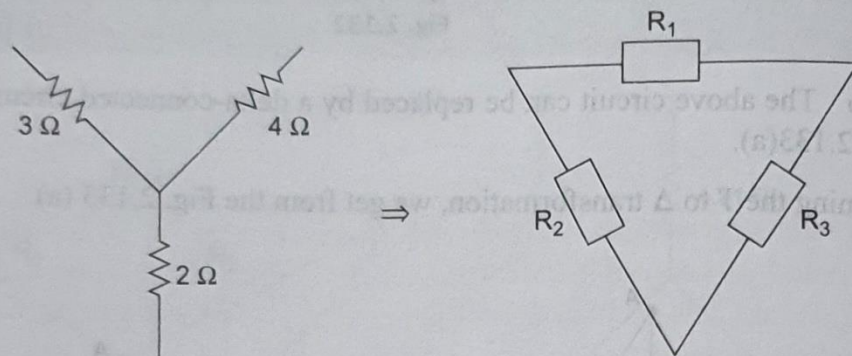


Fig. 2.135

$$R_1 = \frac{4 \times 3 + 4 \times 2 + 3 \times 2}{2} = 13 \Omega$$

$$R_2 = \frac{4 \times 3 + 4 \times 2 + 3 \times 2}{4} = 6.5 \Omega$$

$$R_3 = \frac{4 \times 3 + 4 \times 2 + 3 \times 2}{3} = 8.7 \Omega$$

The original circuit is redrawn as shown in Fig. 2.135(b).

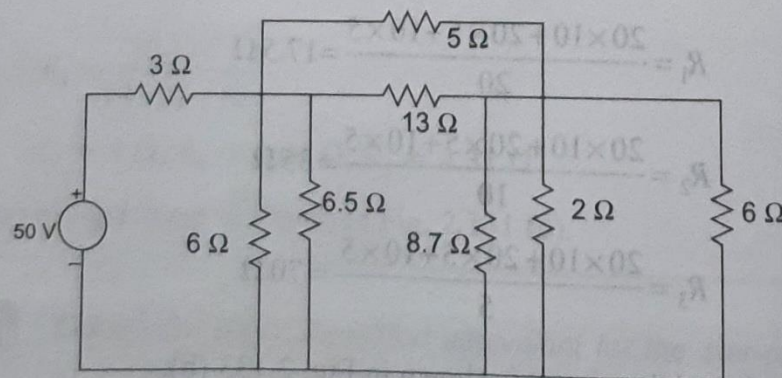


Fig. 2.135(b)

It is further simplified as shown in Fig. 2.110(c). Here the resistors $5\ \Omega$ and $13\ \Omega$ are in parallel, $6\ \Omega$ and $6.5\ \Omega$ are in parallel, and $8.7\ \Omega$ and $2\ \Omega$ are in parallel.

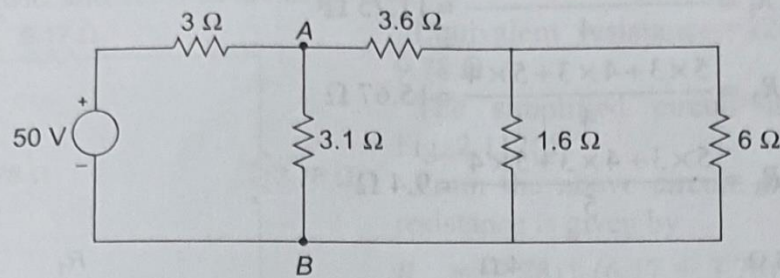


Fig. 2.135(c)

In the above circuit the resistors $6\ \Omega$ and $1.6\ \Omega$ are in parallel, the resultant of which is in series with $3.6\ \Omega$ resistor and is equal to $\left[3.6 + \frac{6 \times 1.6}{7.6}\right] = 4.9\ \Omega$ as shown in Fig. 2.110(d).

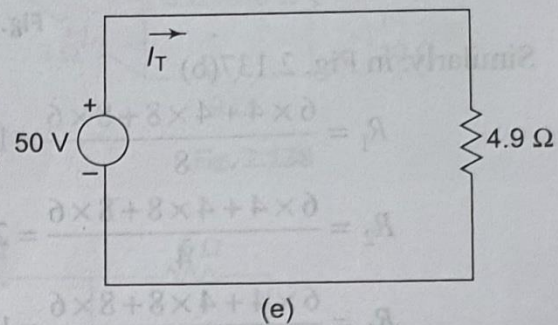
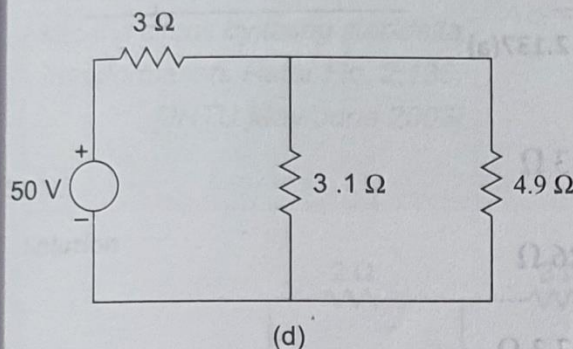


Fig. 2.135(d) and (e)

In the above circuit $4.9\ \Omega$ and $3.1\ \Omega$ resistors are in parallel, the resultant of which is in series with $3\ \Omega$ resistor.

Therefore, the total resistance $R_T = 3 + \frac{3.1 \times 4.9}{8} = 4.9\ \Omega$

The current drawn by the circuit $I_T = 50/4.9 = 10.2\ \text{A}$ (See Fig. 2.110 (e)).

Example 2.83 Find the voltage to be applied across AB in order to drive a current of 5A into the circuit by using star-delta transformation. Refer Fig. 2.138. [JNTU May/June 2006]

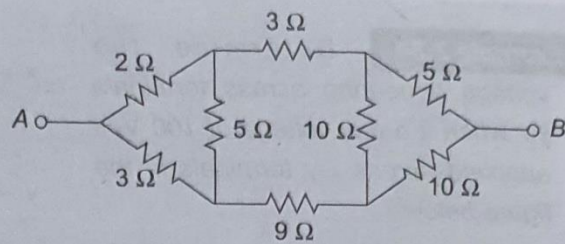


Fig. 2.138

Solution

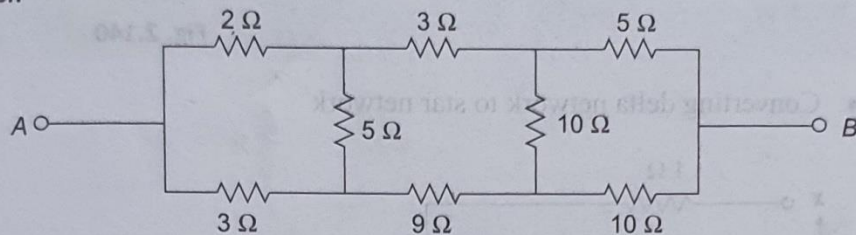


Fig. 2.139

Using star-delta transformation

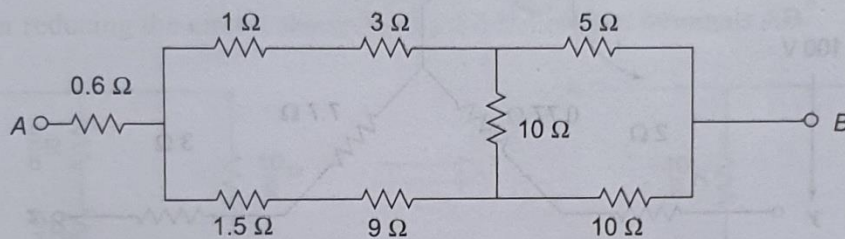


Fig. 2.139(a)

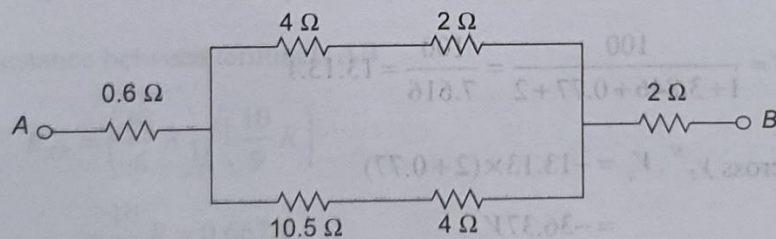


Fig. 2.139(b)

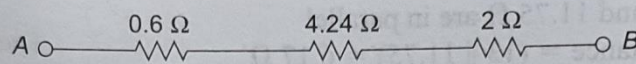
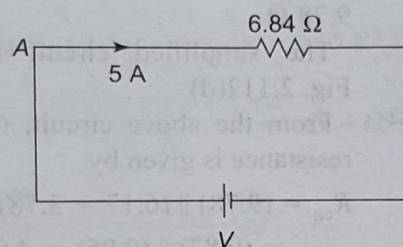


Fig. 2.139(c)



The voltage applied across V_{AB}

$$V_{AB} = 5 \times 6.84 = 34.2\text{V}$$