

ENGINEERING MATHEMATICS





#Q. One of the eigen values of the matrix

$$\begin{pmatrix} 2 & 3 & 0 \\ 3 & 2 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$\rightarrow$$
 eigenvalue = 5 $\lambda_1 = 5$

A+12+2= Trace of matrix A

SVM=0

(a)
$$0 \text{ and } 0 - 5 \text{VM} = 0$$

1 and -1

$$\int \lambda_2 + \lambda_3 = 0$$

(SELF-arresment)



The normalized eigen vector corresponding to the eigen value 5 is

(a)
$$\frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ -1 \\ 1 \end{pmatrix}$$
 $A = \begin{bmatrix} 2 & 3 & 0 \\ 3 & 2 & 0 \\ 0 & D & 1 \end{bmatrix}$ (b) $\frac{1}{\sqrt{2}} \begin{pmatrix} -1 \\ 1 \\ 0 \end{pmatrix}$

$$\begin{bmatrix} 2 & 3 & 0 \\ 3 & 2 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$
 (b)
$$\frac{1}{\sqrt{2}} \begin{pmatrix} -1 \\ 1 \\ 0 \end{pmatrix}$$

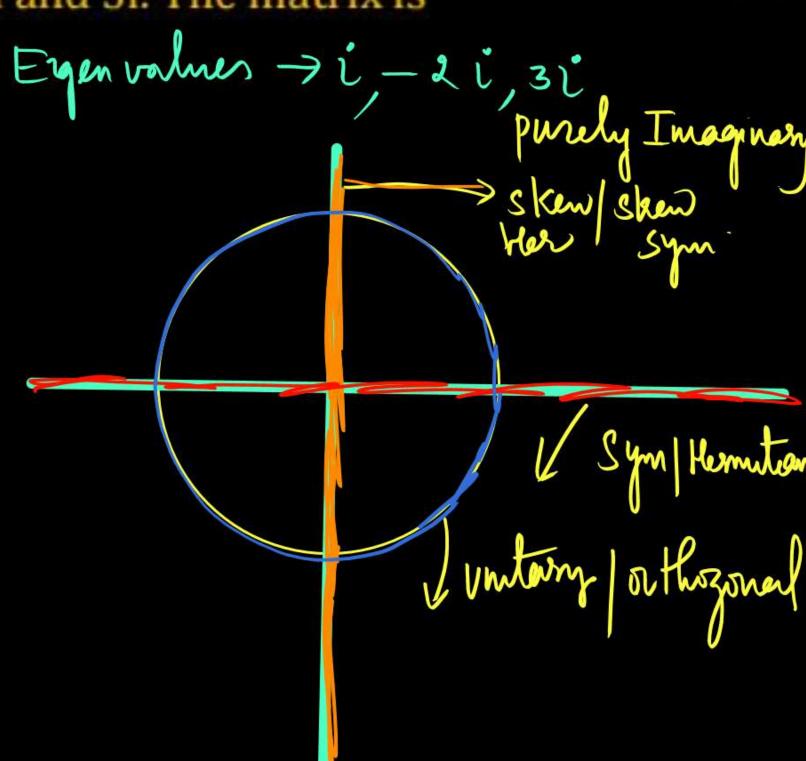
(c)
$$\frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 0 \\ -1 \end{pmatrix}$$





#Q. The eigenvalues of a matrix are i, - 2i and 3i. The matrix is

- (a) Unitary
- (b) Anti-Unitary
- (c) Hermitian





#Q. The eigenvalues and eigenvectors of the matrix [5]

(a) 6, 1 and
$$\begin{bmatrix} 4 \\ 1 \end{bmatrix}$$
, $\begin{bmatrix} 1 \\ -1 \end{bmatrix}$

(c) 6, 1 and
$$\begin{bmatrix} 4 \\ 1 \end{bmatrix}$$
, $\begin{bmatrix} 1 \\ -1 \end{bmatrix}$

(b) 2, 5 and
$$\begin{bmatrix} 4 \\ 1 \end{bmatrix}$$
, $\begin{bmatrix} 1 \\ -1 \end{bmatrix}$

(d) 2, 5 and
$$\begin{bmatrix} 4 \\ 1 \end{bmatrix}$$
, $\begin{bmatrix} 1 \\ -1 \end{bmatrix}$ $\lambda^2 + \lambda + 6 = 0$

12 (5+2) \tau+(10-4)

$$\lambda^{2} - 7 + 16 = 0$$

$$\lambda^{2} - 6 - 1 + 6 = 0$$

$$\lambda(1 - 6) - 1(1 - 6) = 0$$

$$\lambda(1 - 6) - 1(1 - 6) = 0$$

Slide-5



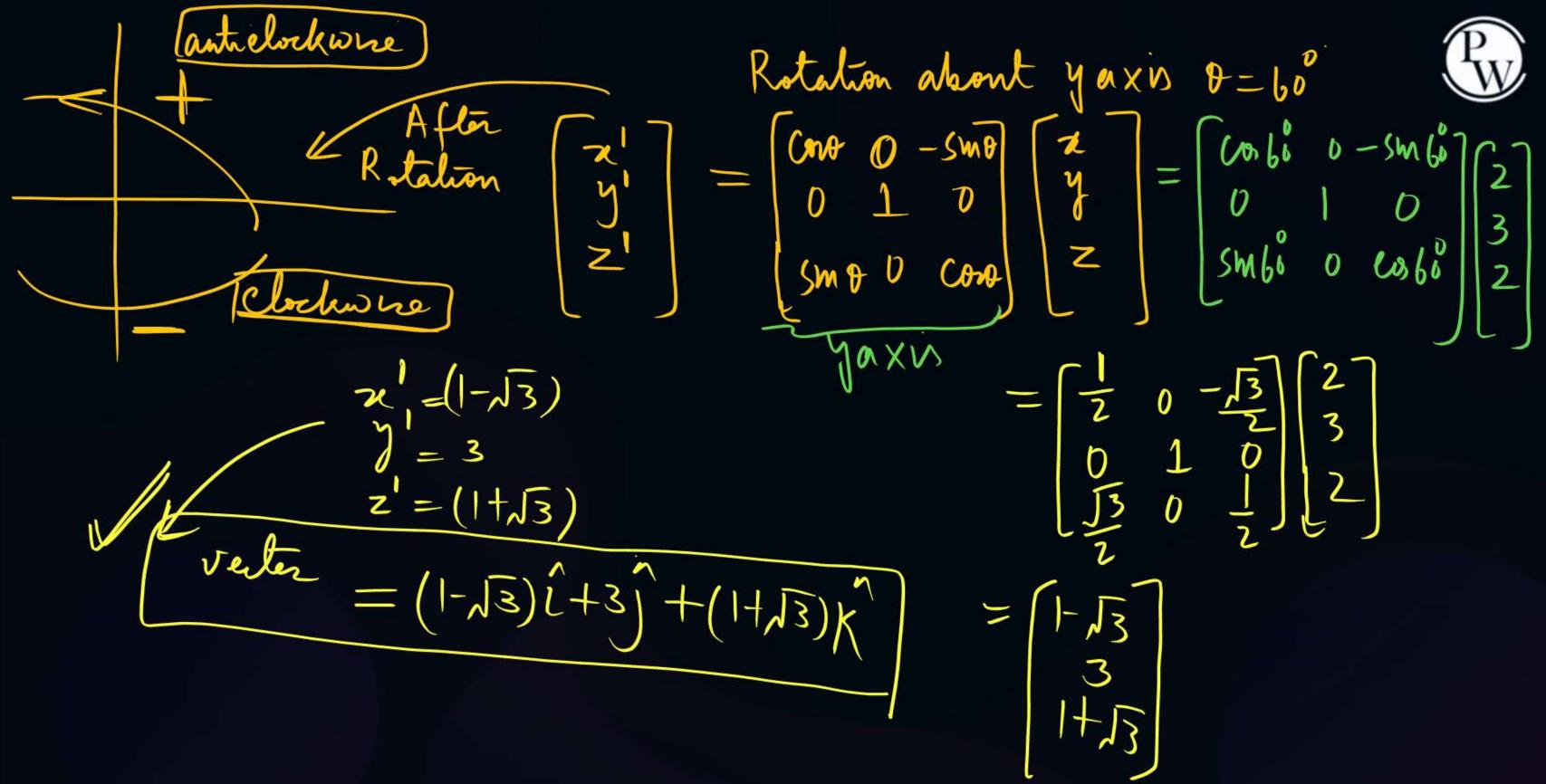
#Q. Consider a vector $\vec{p} = 2\hat{\imath} + 3\hat{\jmath} + 2\hat{k}$ in the coordinate system $(\hat{\imath}, \hat{\jmath}, \hat{k})$. The axes are rotated anti-clockwise about the Y axis by an angle of 60° .

The vector \vec{p} in the rotated coordinate system $(\hat{\imath}', \hat{\jmath}', \hat{k}')$ is

(a)
$$(1 - \sqrt{3})\hat{\imath}' + 3\hat{\jmath}' + (1 + \sqrt{3})\hat{k}'$$
 (b) $(1 + \sqrt{3})\hat{\imath}' + 3\hat{\jmath}' + (1 - \sqrt{3})\hat{k}'$

(c)
$$(1-\sqrt{3})\hat{\imath}' + (3+\sqrt{3})\hat{\jmath}' + 2\hat{k}'$$
 (d) $(1-\sqrt{3})\hat{\imath}' + (3-\sqrt{3})\hat{\jmath}' + 2\hat{k}'$

-> Xaxis Rotation -> yaxis " -> zaxis Rotation 8 = 60° X-axis - along 2° yaxis - along Xaxis Rotation Zaxvo - along kn Rotation about y axis $(x,y,z) \rightarrow (2,3,2)$ = 2 (+3) + 2 k





#Q. For arbitrary matrices E, F, G and H, if EF - FE = 0, then Trace (EFGH)

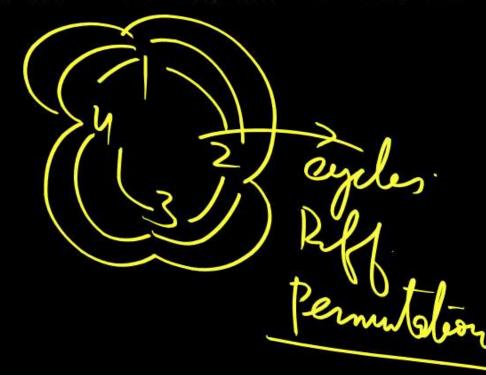
is equal



Taace (1234)

- Trace (2341

(d) Trace (EGHF)





$$\begin{bmatrix} ae^{i\alpha} & b \\ ce^{i\beta} & d \end{bmatrix}$$

#Q. An unitary matrix
$$\begin{bmatrix} ae^{i\alpha} & b \\ ce^{i\beta} & d \end{bmatrix}$$
 is given, where a, b, c, d, α and β are real. The inverse of the matrix is $ade^{i\alpha} - bee^{i\beta} \begin{bmatrix} U \end{bmatrix} V = \begin{bmatrix} \alpha e^{i\alpha} & b \\ ce^{i\beta} & d \end{bmatrix}$

(a)
$$\begin{bmatrix} ae^{i\alpha} & -ce^{i\beta} \\ b & d \end{bmatrix}$$

(c) $ae^{i\alpha} b$ $ce^{i\beta} d$

(b)
$$\begin{bmatrix} ae^{i\alpha} & ce^{i\beta} \\ b & d \end{bmatrix}$$

(d)
$$\begin{bmatrix} ae^{-i\alpha} & ce^{-i\beta} \\ b & d \end{bmatrix}$$

(b)
$$\begin{bmatrix} ae^{i\alpha} & ce^{i\beta} \\ b & d \end{bmatrix} = \begin{bmatrix} If V is Vintary matrix \\ V(V) & = I \\ V' & \text{multiply} \end{bmatrix}$$
(d)
$$\begin{bmatrix} ae^{-i\alpha} & ce^{-i\beta} \\ b & d \end{bmatrix} = \begin{bmatrix} If V is Vintary matrix \\ V(V) & = I \\ V' & \text{multiply} \end{bmatrix}$$

(d) [ae-ia ce-ib]
$$\begin{bmatrix}
V^{-1} \text{ mulliply} \\
V \end{bmatrix} = V^{-1} \end{bmatrix}$$

$$\begin{bmatrix}
V \end{bmatrix} = V \end{bmatrix}$$

$$V \end{bmatrix} =$$



- The eigenvalue of the matrix $A = \begin{bmatrix} 0 & i \\ i & 0 \end{bmatrix}$ are $\lambda^2 (1+0)\lambda + (0-1) = 0$
- Real and distinct
- Complex and distinct
- Complex and coinciding
- Real and coinciding (d)

$$= \frac{1}{\sqrt{1-0+(+1)}} = 0$$

$$= \frac{1}{\sqrt{1-0+(+1)}} = 0$$
and District

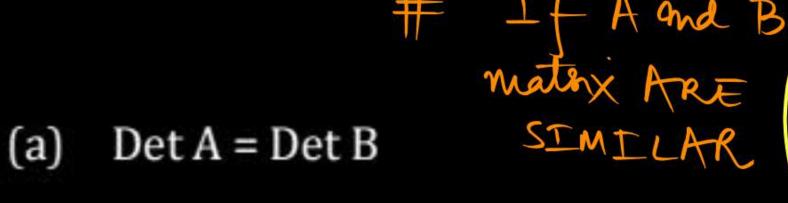


#Q. The eigen values of the matrix
$$\begin{pmatrix} 2 & 3 & 0 \\ 3 & 2 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$
 are Eyan values of the matrix

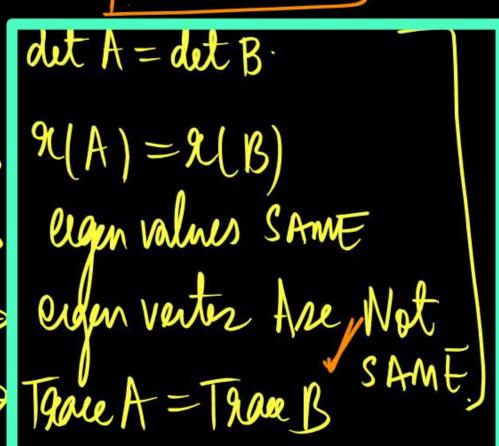
U det = product of ergen value = -5

#Q. Two matrices A and B are said to be similar if $B = P^{-1} AP$ for some

invertible matrix P. Which of the following statements is NOT TRUE?



- (b) Trace of A = Trace of B
- (c) A and B have the same eigenvectors
- (d) A and B have the same eigenvalues





#Q. A 3 × 3 matrix has elements such that its trace is 11 and its determinant is 36. The eigenvalues of the matrix are all known to be positive integers. The largest eigenvalues of the matrix is:

- (a) 18
- (b) 12
- (c) 9
- (d) 6

$$\lambda_{1} + \lambda_{2} + \lambda_{3} = 11$$
 $\lambda_{1} = 3$
 $\lambda_{1} = 3$
 $\lambda_{2} = 3$
 $\lambda_{3} = 2$
 $\lambda_{3} = 2$
 $\lambda_{3} = 2$
 $\lambda_{4} = 3$
 $\lambda_{5} = 3$
 $\lambda_{6} = 3$
 $\lambda_{7} = 3$
 $\lambda_{8} = 3$
 $\lambda_{8} = 3$
 $\lambda_{9} = 3$
 $\lambda_{1} = 3$
 $\lambda_{1} = 3$
 $\lambda_{2} = 3$
 $\lambda_{3} = 2$
 $\lambda_{4} = 3$
 $\lambda_{5} = 3$
 $\lambda_{6} = 3$
 $\lambda_{7} = 3$
 $\lambda_{7} = 3$
 $\lambda_{8} = 3$

Trace = 11

det 1=36

Largest eigenvalue =

- 6 Apro



#Q. The eigenvalues of the matrix
$$\begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$$
 are

(b)
$$0, -\sqrt{2}, \sqrt{2}$$

(c) $1/\sqrt{2}, 1/\sqrt{2}, 0$

(c)
$$1/\sqrt{2}, 1/\sqrt{2}, 0$$

(d)
$$\sqrt{2}$$
, $\sqrt{2}$, 0



#Q. The degenerate eigenvalues of the matrix
$$M = \begin{pmatrix} 4 & -1 & -1 \\ -1 & 4 & -1 \end{pmatrix} = degenerate$$
is Eyen values = 2, 5, 5

begin value = 5

repeated eigen values



#Q. The matrix
$$A = \frac{1}{\sqrt{3}} \begin{bmatrix} 1 & 1+i \\ 1-i & -1 \end{bmatrix}$$
 is

- (a) Orthogonal
- (b) Symmetric
- (c) Anti-symmetric
- (d) Unitary

$$A = \frac{1}{\sqrt{3}} \left[\frac{1+i}{1-i} - 1 \right]$$

$$A(A)^{T} = I \quad \text{Unitary}$$
materix





- #Q. Which of the following is INCORRECT for the matrix $M = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$
- (a) It is its own inverse
- (b) It is its own transpose
- (c) It is non-orthogonal
- (d) It has eigen values ± 1

Weekly TEST 06

Already

#Q. The symmetric pair of
$$P = {a \choose b}(a-2b)$$
 is:

(a)
$$\begin{pmatrix} a^2 - 2 & ba - 1 \\ ba - 1 & b^2 - 2 \end{pmatrix}$$

(c)
$$\begin{pmatrix} a(a-1) & b(a-1) \\ b(a-1) & b^2 \end{pmatrix}$$
 (d) $\begin{pmatrix} a(a-2) & b(a-1) \\ b(a-1) & b^2 \end{pmatrix}$

#Q.
$$(x \ y) \begin{pmatrix} 5 & -7 \\ 7 & 3 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = 15$$



The matrix equation above represents

(a) A circle of radius √15

(b) An ellipse of semi major axis√5

(c) A ellipse of semi major axis 5

d) A hyperbola



- #Q. The product PQ of any two real symmetric matrices P and Q is:
- (a) Symmetric for all P and Q
- (b) Never symmetric
- (c) Symmetric if PQ = QP
- (d) Antisymmetric for all P and Q

If Pseodnet P& of Amy Two real sym materix P and & is

Symmetri PR= RP

Later PR= RP

Later Commutative



- #Q. A matrix given by M = $\frac{1}{\sqrt{2}} \begin{pmatrix} i & 1 \\ 1 & i \end{pmatrix}$ The eigenvalues of the M are
- (a) Real and positive
- (b) Purely imaginary with modulus 1
- (c) Complex with modulus 1
- (d) Real and negative

$$M = \frac{1}{\sqrt{2}} \begin{bmatrix} i & 1 \\ 1 & i \end{bmatrix}$$

eigen values

Modular
$$Z = a + ib$$

$$|Z| = \sqrt{a^2 + b^2} \qquad \lambda_1 = \sqrt{1 + i} \qquad |-i| = \lambda_2$$



#Q. The inverse of the matrix
$$M = \begin{bmatrix} 0 & 1 & 1 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{bmatrix}$$
 is Inverse of matrix

(a) $M - I$

(b) $M^2 - I$

Step 2 $\lambda = M$

Step 3 Multiply with

(b)
$$M^2 - I$$

(c)
$$I - M^2$$

step 2
$$\lambda = M$$



#Q The normalized eigenvectors of the matrix $N = \begin{bmatrix} 0 & -i \\ i & 0 \end{bmatrix}$ are β_1 and

 β_2 with the eigenvalues λ_1 and λ_2 respectively and $\lambda_1 > \lambda_2$. If the eigenvector $\alpha = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 1 \end{pmatrix}$ is expressed as $\alpha = P\beta_1 + Q\beta_2$. Find $N = \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix} \beta_1$

the constant P and Q

(a)
$$\frac{1+i}{2}, \frac{1-i}{2}$$

(c)
$$\frac{1+i}{3}, \frac{1-i}{4}$$

(b)
$$\frac{2+i}{2}, \frac{1+i}{2}$$

(d)
$$\frac{i}{2}, \frac{1+i}{2}$$

$$X = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

$$N = \begin{cases} 0 - i \\ i \end{cases}$$

$$N = \begin{cases} 1 - 1 \\ -1 \end{cases}$$

$$N = \begin{cases} -1 \\ \sqrt{3} \\ -1 \end{cases}$$

$$N = \begin{cases} -1 \\ \sqrt{3} \\ \sqrt{3} \\ \sqrt{3} \end{cases}$$

Eigenvalues
$$\frac{\lambda^{2}-(0)\lambda+(0+1^{2})=0}{\lambda^{2}-1=0}$$

$$\frac{\lambda^{2}-1=0}{\lambda=\pm 1}$$



#Q. The trace of a 2×2 matrix is 4 and its determinant is 8. If one of the

eigenvalues is 2(1 + i), the other eigenvalue is

(b)
$$2(1+i)$$

(c)
$$(1 + 2i)$$

$$\frac{\lambda_1 + \lambda_2 = 47}{\lambda_1 \lambda_2 = 8} = \frac{\lambda_1}{\lambda_1}$$

$$= 2(1+i)$$



#Q. The eigenvalues of the matrix representing the following pair of linear

equation
$$x + iy = 0$$
, $ix + y = 0$ are

(a)
$$1+i, 1+i$$

(b)
$$1-i$$
, $1-i$

$$x+iy=0 \quad A=\begin{bmatrix} 1 & i \\ i & 1 \end{bmatrix}$$

$$\lambda^{2}-[1+i]\lambda+(1-i^{2})=0$$

$$\lambda^{2}-2\lambda+2=0$$

$$\lambda=1+i,1-i$$

$$x + y = 1$$
$$y + z = 1$$

$$x + z = 1$$

$$C = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \end{bmatrix}$$

$$ton Tainal$$

$$Solution$$

$$\begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \end{bmatrix}$$

$$\begin{cases} \text{rank } A = 3 \\ \text{rank } C = 3. \\ \text{No. of variables} \end{cases}$$

$$\text{This is condition} = 3.$$

- Equation are inconsistent
- Equations are consistent and a single non-trivial solution exists won Third
- Equation are consistent and many solutions exist
- Equation are consistent and only a trivial solution exists Twind= (0,0) WmTww = (4,6)C





Thank You!

