**EAE 298 Aeroacoustics, Fall Quarter 2016**

**Homework #2: Solution of Lilley’s Equation and its Application to Jet Noise   
(Due Date: 11/08/2016)**

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|  | **Name :** |  |

An axisymmetric jet of radius has an exit mean velocity of and an exit mean density of . The ambient mean velocity is zero and the ambient mean density is .

Lilley’s equation for a parallel axisymmetric flow can be written

where

and and are the radial distributions of the axial velocity and speed of sound squared.

1. [25 points] Seek solutions of Lilley’s equation in the form  
      
   Show that Lilley’s equation reduces to  
   where is the radial distribution of the mean density. (Note: and is constant.)
2. [25 points] Determine the general form of solution (solution of the homogeneous equation) for the pressure fluctuation outside the jet in the ambient medium where the sources vanish. Make sure the solution is chosen to ensure decaying solutions or outgoing waves.
3. [25 points] Determine the general form of solution (solution of the homogeneous equation) in the potential core region where the mean velocity and density are constant and equal to the jet exit values.
4. [25 points] Consider a case in which the real jet is replaced by a vortex sheet at . If the solutions are to be matched at the vortex sheet, describe what matching conditions should be applied. Give both the physical description and the mathematical expressions.