### Factor\_Analysis.R

#### saiprasad

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```
# Factor Analysis
HCV<- read.csv("HCV-Egy-Data.csv")</pre>
View(HCV)
attach(HCV)
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
Survivorship = HCV$Survivorship <- if_else( RNA.EOT>= 400000 , 'NC','C')
cbind(data.frame(Survivorship),HCV)
##
         Survivorship Age Gender BMI Fever Nausea. Vomting Headache Diarrhea
## 1
                                    35
                     C
                        56
                                 1
                                            2
                                                             1
                                                                       1
## 2
                     C
                        46
                                 1
                                    29
                                            1
                                                             2
                                                                       2
                                                                                 1
                                    33
                                            2
                                                             2
                                                                       2
                                                                                 2
## 3
                    NC
                        57
                                 1
                                                             2
## 4
                    NC 49
                                 2
                                    33
                                            1
                                                                       1
                                                                                 2
                                                                       2
## 5
                     C
                        59
                                 1
                                    32
                                            1
                                                             1
                                                                                 1
                                            2
                                                             2
                                                                       2
## 6
                     C
                        58
                                 2
                                    22
                                                                                 1
## 7
                     C
                      42
                                 2
                                    26
                                            1
                                                             1
                                                                       2
                                                                                 2
## 8
                     C
                        48
                                 2
                                    30
                                            1
                                                             1
                                                                       2
                                                                                 2
                     C
                                    23
                                                                       2
                                                                                 2
## 9
                        44
                                 1
                                            1
                                                             1
## 10
                     C
                        45
                                 1
                                    30
                                            2
                                                             1
                                                                       2
                                                                                 2
                                 2
                                            2
                                                                       2
## 11
                    NC
                       37
                                    24
                                                             1
                                                                                 1
                                    22
                                            2
                                                             2
                                                                       1
## 12
                     C
                        36
                                                                                 1
                     C
                                 2
                                    25
                                            2
## 13
                        45
                                                             1
                                                                       1
                                                                                 1
                                                             2
## 14
                     C
                        34
                                 1
                                    22
                                            1
                                                                       1
                                                                                 1
                   NC
                                 2
                                            2
                                                             2
                                                                       2
                                                                                 1
## 15
                        40
                                    32
## 16
                    NC
                        58
                                 1
                                    34
                                            2
                                                             1
                                                                       1
                                                                                 1
                                                             2
                                                                       2
                                                                                 2
## 17
                     C
                        61
                                 1
                                    35
                                            1
## 18
                     C
                        55
                                 2
                                    24
                                            2
                                                             1
                                                                       2
                                                                                 2
## 19
                   NC
                        56
                                 1
                                    27
                                            1
                                                             2
                                                                       2
                                                                                 2
                                            2
                                 2
                                                             2
                                                                       1
## 20
                   NC
                        35
                                    23
                                                                                 1
                        57
                                 2
                                    23
                                            1
                                                                       2
## 21
                    NC
```

```
hcv pca <- prcomp(HCV pca, scale=TRUE)
summary(hcv pca)
## Importance of components:
                            PC1
                                   PC2
                                          PC3
                                                  PC4
                                                         PC5
                                                                 PC<sub>6</sub>
## Standard deviation
                        1.08404 1.05059 1.0387 1.02934 1.01426 1.01148
## Proportion of Variance 0.09793 0.09198 0.0899 0.08829 0.08573 0.08526
## Cumulative Proportion 0.09793 0.18991 0.2798 0.36810 0.45383 0.53909
##
                                   PC8
                                          PC9
                           PC7
                                                 PC10
                                                       PC11
                                                               PC12
## Standard deviation
                        0.9962 0.98907 0.97517 0.95981 0.9327 0.90452
## Proportion of Variance 0.0827 0.08152 0.07925 0.07677 0.0725 0.06818
## Cumulative Proportion 0.6218 0.70331 0.78255 0.85932 0.9318 1.00000
plot(hcv_pca)
# A table containing eigenvalues and %'s accounted, follows. Eigenvalues are
the sdev^2
(eigen hcv <- round(hcv pca$sdev^2,2))
## [1] 1.18 1.10 1.08 1.06 1.03 1.02 0.99 0.98 0.95 0.92 0.87 0.82
names(eigen hcv) <- paste("PC",1:12,sep="")</pre>
eigen_hcv
## PC1 PC2 PC3 PC4 PC5 PC6 PC7 PC8 PC9 PC10 PC11 PC12
## 1.18 1.10 1.08 1.06 1.03 1.02 0.99 0.98 0.95 0.92 0.87 0.82
sumlambdas <- sum(eigen_hcv)</pre>
sumlambdas
## [1] 12
propvar <- round(eigen_hcv/sumlambdas,2)</pre>
propvar
## PC1 PC2 PC3 PC4 PC5 PC6 PC7 PC8 PC9 PC10 PC11 PC12
cumvar hcv <- cumsum(propvar)</pre>
cumvar_hcv
## PC1 PC2 PC3 PC4 PC5 PC6 PC7 PC8 PC9 PC10 PC11 PC12
## 0.10 0.19 0.28 0.37 0.46 0.54 0.62 0.70 0.78 0.86 0.93 1.00
matlambdas <- rbind(eigen_hcv,propvar,cumvar_hcv)</pre>
matlambdas
                  PC2 PC3 PC4 PC5 PC6 PC7
                                               PC8 PC9 PC10 PC11 PC12
## eigen hcv 1.18 1.10 1.08 1.06 1.03 1.02 0.99 0.98 0.95 0.92 0.87 0.82
## propvar
             ## cumvar hcv 0.10 0.19 0.28 0.37 0.46 0.54 0.62 0.70 0.78 0.86 0.93 1.00
```

```
rownames(matlambdas) <- c("Eigenvalues", "Prop. variance", "Cum. prop.</pre>
variance")
rownames(matlambdas)
## [1] "Eigenvalues"
                         "Prop. variance"
                                            "Cum. prop. variance"
eigvec.hcv <- hcv pca$rotation
print(hcv_pca)
## Standard deviations (1, .., p=12):
## [1] 1.0840427 1.0505938 1.0386641 1.0293370 1.0142649 1.0114786 0.9961803
  [8] 0.9890660 0.9751702 0.9598120 0.9327088 0.9045197
##
##
## Rotation (n x k) = (12 \times 12):
##
                       PC1
                                  PC2
                                             PC3
                                                        PC4
                -0.09529935
## Age
                           ## Gender
                -0.01044315 -0.316250295 -0.07203548 0.198455085
                0.52480080 0.088540649 -0.24781518 0.107734234
## Nausea.Vomting
## Jaundice
                ## Epigastric.pain -0.36243330 0.087014225 -0.40100204 -0.424062232
                -0.31925445 -0.018338105 0.01645813
## WBC
                                                 0.205418062
## Plat
                 0.55719490 -0.204281272 -0.04274376
                                                 0.006393138
                 ## AST.1
## ALT.1
                 ## ALT.after.24.w -0.18820970 0.008476448 -0.38978528 -0.004039055
                -0.13955452   0.282607286   -0.34255100   0.449136202
## RNA.Base
## RNA.EOT
                -0.03831018 -0.561716624 -0.47462581
                                                 0.083473231
##
                        PC5
                                  PC6
                                             PC7
                                                        PC8
## Age
                -0.002212279 -0.37355037 -0.04875916 -0.44436803
## Gender
                -0.677696273 -0.22936402 -0.29458461
                                                 0.28262743
## Nausea.Vomting
                0.236489116 -0.03939247 0.38658341 0.10081836
                -0.091079291 0.59055330 0.08817802 0.01018116
## Jaundice
                                       0.06035269 -0.49894025
## Epigastric.pain -0.107455186 -0.04176427
## WBC
                -0.350199687 -0.12886045
                                       0.73719558 -0.05030833
## Plat
                                       0.24574326 -0.29402786
                -0.184948482 -0.16921682
## AST.1
                -0.299205035 0.29242475
                                       0.12604131 0.24969134
## ALT.1
                -0.327303100 -0.10706918 -0.28177087 -0.18531477
## ALT.after.24.w
                 0.206078032 -0.52920937 0.11414766 0.44898794
## RNA.Base
                 0.234651816 -0.12214543 -0.17512225 -0.01675482
## RNA.EOT
                 ##
                        PC9
                                  PC10
                                            PC11
## Age
                 ## Gender
                ## Nausea.Vomting -0.014602955 -0.13365869 -0.63442826 -0.07783699
## Jaundice
                 0.320862480 -0.27375624 0.14539380 -0.30519221
## Epigastric.pain -0.014426575 -0.14347333 -0.19835482 -0.44093897
## WBC
                -0.281821277 -0.02758649 0.05666123 0.29435529
## Plat
                 0.091339000 0.28486892 0.47530120 -0.34763250
## AST.1
                 0.326466725 0.53259952 -0.04585550
## ALT.1
                -0.134042709 -0.42464147 0.19333300 0.38153525
```

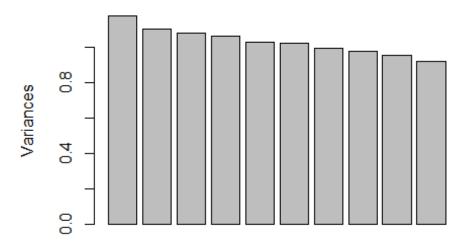
```
## ALT.after.24.w
                 0.401358681 -0.17496164 0.28277459 -0.06118809
## RNA.Base
                -0.456743248   0.49191702   0.04710736   -0.16687657
## RNA.EOT
                 # Taking the first four PCs to generate linear combinations for all the
variables with four factors
pcafactors.hcv <- eigvec.hcv[,1:4]</pre>
pcafactors.hcv
##
                                   PC2
                       PC1
                                             PC3
                                                         PC4
## Age
                -0.09529935
                            0.284882543
                                       0.31747295
                                                  0.338906000
## Gender
                -0.01044315 -0.316250295 -0.07203548 0.198455085
## Nausea.Vomting
                 0.52480080 0.088540649 -0.24781518
                                                  0.107734234
## Jaundice
                -0.10889929 0.057223969 -0.15761428 0.550381317
## Epigastric.pain -0.36243330 0.087014225 -0.40100204 -0.424062232
## WBC
                -0.31925445 -0.018338105 0.01645813 0.205418062
## Plat
                 0.55719490 -0.204281272 -0.04274376
                                                  0.006393138
## AST.1
                 ## ALT.1
                 0.061155423
## ALT.after.24.w -0.18820970 0.008476448 -0.38978528 -0.004039055
                -0.13955452  0.282607286  -0.34255100  0.449136202
## RNA.Base
## RNA.EOT
                -0.03831018 -0.561716624 -0.47462581
                                                  0.083473231
# Multiplying each column of the eigenvector's matrix by the square-root of
the corresponding eigenvalue in order to get the factor loadings
unrot.fact.hcv <- sweep(pcafactors.hcv,MARGIN=2,hcv pca$sdev[1:4],`*`)
unrot.fact.hcv
##
                       PC1
                                   PC2
                                             PC3
                                                         PC4
## Age
                -0.10330856
                           0.299295831 0.32974776 0.348848478
## Gender
                -0.01132082 -0.332250596 -0.07482067
                                                  0.204277158
## Nausea.Vomting
                 -0.11805147 0.060119147 -0.16370829
## Jaundice
                                                  0.566527842
## Epigastric.pain -0.39289316  0.091416605 -0.41650642 -0.436502936
## WBC
                -0.34608544 -0.019265900 0.01709447 0.211444407
                 0.60402305 -0.214616636 -0.04439641
## Plat
                                                  0.006580694
## AST.1
                 ## ALT.1
                 0.062949538
## ALT.after.24.w -0.20402735 0.008905303 -0.40485597 -0.004157549
## RNA.Base
                0.462312501
## RNA.EOT
                -0.04152987 -0.590135998 -0.49297679 0.085922083
# Computing communalities
communalities.hcv <- rowSums(unrot.fact.hcv^2)</pre>
communalities.hcv
##
                               Nausea.Vomting
                                                   Jaundice
             Age
                        Gender
##
       0.3306795
                      0.1578459
                                    0.4108581
                                                  0.3653047
## Epigastric.pain
                           WBC
                                        Plat
                                                     AST.1
##
       0.5267344
                      0.1651473
                                    0.4129185
                                                  0.3595138
```

```
##
             ALT.1 ALT.after.24.w
                                           RNA.Base
                                                             RNA.EOT
##
                         0.2056321
         0.4308627
                                          0.4513626
                                                           0.6003939
# Performing the varimax rotation. The default in the varimax function is
norm=TRUE thus, Kaiser normalization is carried out
rot.fact.hcv <- varimax(unrot.fact.hcv)</pre>
View(unrot.fact.hcv)
rot.fact.hcv
## $loadings
##
## Loadings:
                   PC1
                          PC2
                                  PC3
                                         PC4
##
## Age
                   -0.190 0.142 0.439
                                          0.287
## Gender
                           -0.390
## Nausea.Vomting
                    0.630
                                          0.112
## Jaundice
                                          0.568
                           -0.190
## Epigastric.pain -0.228 0.247 -0.639
                                          0.226
## WBC
                   -0.322 -0.103
## Plat
                    0.570 -0.203 0.115 -0.184
## AST.1
                    0.107 0.546 -0.223
## ALT.1
                    0.470 0.343
                                          0.287
## ALT.after.24.w
                                  -0.403
                                          0.204
## RNA.Base
                                  -0.105
                                          0.661
## RNA.EOT
                    0.117 -0.595 -0.480
##
                    PC1
                          PC2
                                 PC3
##
                                       PC4
## SS loadings
                  1.162 1.096 1.085 1.074
## Proportion Var 0.097 0.091 0.090 0.090
## Cumulative Var 0.097 0.188 0.279 0.368
##
## $rotmat
##
               \lceil,1\rceil
                             [,2]
                                       [,3]
         0.93119621 -0.005476209 0.3020940 -0.2039187
## [1,]
         0.04203690 0.906775699 0.1510461
## [2,]
                                             0.3913768
## [3,] -0.36023297
                     0.049131561 0.8413855 -0.3998608
## [4,] 0.03658853 -0.418705066 0.4218941 0.8033385
# The print method of varimax omits loadings less than abs(0.1). In order to
display all the loadings, it is necessary to ask explicitly the contents of
the object $loadings
fact.load.hcv <- rot.fact.hcv$loadings[1:9,1:4]</pre>
fact.load.hcv
##
                             PC1
                                         PC2
                                                      PC3
                                                                    PC4
## Age
                   -0.189641232   0.14209632   0.438620690
                                                            0.286594181
## Gender
                    0.009918388 -0.39042271 -0.030374813
                                                            0.066294905
## Nausea.Vomting
                    0.630454087 0.02215453
                                              0.016129583
                                                            0.112404278
## Jaundice
                   -0.027700318 -0.19009027
                                              0.074691098
                                                            0.568176281
## Epigastric.pain -0.227949410 0.24734830 -0.639483053 -0.068218412
## WBC
                   -0.321504881 -0.10326758 -0.003870194 0.226059074
```

```
## Plat
                   0.569675983 -0.20285354 0.115476608 -0.184128639
## AST.1
                   ## ALT.1
# Computing the rotated factor scores for the 30 European Countries. Notice
that signs are reversed for factors F2 (PC2), F3 (PC3) and F4 (PC4)
scale.hcv <- scale(HCV[1:29])</pre>
scale.hcv
##
                          Gender
                                                 Fever Nausea. Vomting
                  Age
                                         BMI
##
      [1,]
           1.10241532 -0.9789225
                                 1.56795830
                                             0.9690704
                                                           -1.0047041
##
      [2,] -0.03634155 -0.9789225  0.09600468 -1.0311717
                                                            0.9945993
##
           1.21629100 -0.9789225 1.07730709
                                             0.9690704
                                                            0.9945993
      [3,]
##
      [4,] 0.30528551 1.0207938 1.07730709 -1.0311717
                                                            0.9945993
##
      [5,]
          1.44404238 -0.9789225
                                 0.83198149 -1.0311717
                                                           -1.0047041
##
      [6,] 1.33016669 1.0207938 -1.62127455 0.9690704
                                                            0.9945993
##
      [7,] -0.49184430 1.0207938 -0.63997214 -1.0311717
                                                           -1.0047041
      [8,] 0.19140982 1.0207938 0.34133028 -1.0311717
##
                                                           -1.0047041
                                                           -1.0047041
##
      [9,] -0.26409293 -0.9789225 -1.37594895 -1.0311717
##
     [10,] -0.15021724 -0.9789225
                                 0.34133028 0.9690704
                                                           -1.0047041
##
     [11,] -1.06122274 1.0207938 -1.13062334 0.9690704
                                                           -1.0047041
##
     [12,] -1.17509843 -0.9789225 -1.62127455
                                             0.9690704
                                                            0.9945993
##
     [13,] -0.15021724 1.0207938 -0.88529774
                                             0.9690704
                                                           -1.0047041
##
     [14,] -1.40284980 -0.9789225 -1.62127455 -1.0311717
                                                            0.9945993
##
     [15,] -0.71959568 1.0207938 0.83198149 0.9690704
                                                            0.9945993
##
     [16,]
          1.33016669 -0.9789225
                                 1.32263270
                                            0.9690704
                                                           -1.0047041
##
     [17,]
           1.67179375 -0.9789225
                                 1.56795830 -1.0311717
                                                            0.9945993
##
     [18,]
           0.98853963 1.0207938 -1.13062334 0.9690704
                                                           -1.0047041
##
     [19,]
           1.10241532 -0.9789225 -0.39464653 -1.0311717
                                                            0.9945993
##
     [20,] -1.28897411 1.0207938 -1.37594895
                                            0.9690704
                                                            0.9945993
          1.21629100 1.0207938 -1.37594895 -1.0311717
##
     [21,]
                                                           -1.0047041
##
     [22,] -1.51672549 -0.9789225 -0.88529774 0.9690704
                                                           -1.0047041
##
     [23,] -0.60571999 -0.9789225 -1.37594895 -1.0311717
                                                            0.9945993
##
     [24,] -0.83347136 1.0207938 0.09600468 -1.0311717
                                                            0.9945993
##
     [25,] -1.51672549 1.0207938 -1.13062334 -1.0311717
                                                            0.9945993
##
     [26,] -0.37796862 1.0207938 1.32263270
                                             0.9690704
                                                            0.9945993
##
     [27,] 0.53303688 -0.9789225 1.32263270 0.9690704
                                                           -1.0047041
## attr(,"scaled:center")
##
                                                          Gender
                              Age
##
                     4.631913e+01
                                                    1.489531e+00
##
                              BMI
                                                           Fever
##
                     2.860866e+01
                                                    1.515523e+00
##
                   Nausea.Vomting
                                                        Headache
##
                     1.502527e+00
                                                    1.496029e+00
##
                         Diarrhea Fatigue...generalized.bone.ache
##
                     1.502527e+00
                                                    1.498917e+00
##
                         Jaundice
                                                 Epigastric.pain
##
                     1.501083e+00
                                                    1.503971e+00
##
                              WBC
                                                             RBC
```

##	7.533386e+03	4.422130e+06
##	HGB	Plat
##	1.258773e+01	1.583481e+05
##	AST.1	ALT.1
##	8.277473e+01	8.391625e+01
##	ALT4	ALT.12
##	8.340578e+01	8.351047e+01
##	ALT.24	ALT.36
##	8.370903e+01	8.311769e+01
##	ALT.48	ALT.after.24.w
##	8.362960e+01	3.343827e+01
## ##	RNA.Base	RNA.4
##	5.909512e+05 RNA.12	6.008956e+05 RNA.EOT
##	2.887536e+05	2.876603e+05
##	2.887330E+03 RNA.EF	Baseline.histological.Grading
##	2.913783e+05	9.761733e+00
##	Baselinehistological.staging	3.7017336100
##	2.536462e+00	
	attr(,"scaled:scale")	
##	Age	Gender
##	8.781506e+00	5.000709e-01
##	BMI	Fever
##	4.076215e+00	4.999395e-01
##	Nausea.Vomting	Headache
##	5.001742e-01	5.001648e-01
##	Diarrhea	Fatiguegeneralized.bone.ache
##	5.001742e-01	5.001794e-01
##	Jaundice	Epigastric.pain
##	5.001794e-01	5.001648e-01
##	WBC	RBC
##	2.668220e+03	3.463577e+05
##	HGB	Plat
##	1.713511e+00	3.879479e+04
##	AST.1	ALT.1
##	2.599324e+01	2.592280e+01
## ##	ALT4 2.652973e+01	ALT.12 2.606448e+01
##	2.032973E+01 ALT.24	2.000448E+01 ALT.36
##	2.620599e+01	2.639903e+01
##	ALT.48	ALT.after.24.w
##	2.622395e+01	7.073569e+00
##	RNA.Base	RNA.4
##	3.539354e+05	3.623151e+05
##	RNA.12	RNA.EOT
##	2.853507e+05	2.645595e+05
##	RNA.EF	Baseline.histological.Grading
##	2.677007e+05	4.023896e+00
##	Baselinehistological.staging	
##	1.121392e+00	





```
fit.pc <- principal(HCV[1:29], nfactors=4, rotate="varimax")</pre>
fit.pc
## Principal Components Analysis
## Call: principal(r = HCV[1:29], nfactors = 4, rotate = "varimax")
## Standardized loadings (pattern matrix) based upon correlation matrix
##
                                      RC1
                                            RC2
                                                  RC3
                                                        RC4
                                                               h2
                                                                    u2 com
## Age
                                          0.06 -0.05
                                                      0.27 0.091 0.91 1.4
                                    -0.10
## Gender
                                    -0.01
                                          0.05
                                                 0.08 -0.09 0.017 0.98 2.6
## BMI
                                    -0.02 - 0.04
                                                 0.15 -0.51 0.287 0.71 1.2
## Fever
                                    0.02
                                          0.09
                                                 0.18 0.01 0.043 0.96 1.5
## Nausea.Vomting
                                    0.05 - 0.52
                                                 0.26 0.08 0.346 0.65 1.5
## Headache
                                    -0.02 -0.08
                                                 0.05
                                                       0.35 0.129 0.87 1.1
## Diarrhea
                                    0.03
                                          0.03
                                                 0.35
                                                       0.16 0.148 0.85 1.5
## Fatigue...generalized.bone.ache 0.05
                                          0.13
                                                 0.00 -0.02 0.021 0.98 1.3
## Jaundice
                                    0.04
                                          0.07 -0.09
                                                       0.34 0.133 0.87 1.3
## Epigastric.pain
                                    0.11
                                          0.39
                                                 0.03 -0.09 0.169 0.83 1.3
## WBC
                                    -0.10
                                          0.18 -0.09 -0.18 0.084 0.92 3.1
## RBC
                                    -0.06 -0.32 -0.04 -0.03 0.109 0.89 1.1
## HGB
                                    0.04 -0.17 -0.17 -0.41 0.227 0.77 1.7
## Plat
                                    0.11 - 0.34
                                                 0.36 -0.15 0.281 0.72 2.6
## AST.1
                                    -0.04 0.01
                                                 0.07
                                                       0.00 0.007 0.99 1.6
## ALT.1
                                    -0.04 -0.08
                                                 0.58 0.11 0.356 0.64 1.1
## ALT4
                                    0.05 -0.10 -0.24 0.17 0.101 0.90 2.3
## ALT.12
                                    -0.08 0.04 -0.46 0.16 0.242 0.76 1.3
```

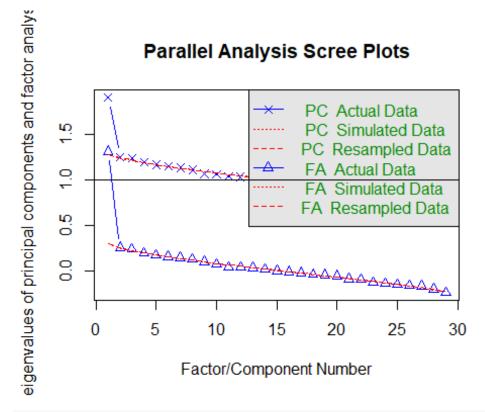
```
## ALT.24
                                   0.06 -0.38 -0.33 0.02 0.260 0.74 2.0
                                    0.06 -0.07 0.01 0.19 0.044 0.96 1.5
## ALT.36
                                   -0.01 0.40 0.19 0.13 0.212 0.79 1.6
## ALT.48
## ALT.after.24.w
                                   0.00
                                         0.22 0.09 0.09 0.066 0.93 1.6
## RNA.Base
                                   -0.02 0.11 0.15 0.31 0.131 0.87 1.8
## RNA.4
                                         0.19 0.01 -0.21 0.083 0.92 2.2
                                   -0.07
## RNA.12
                                   0.76 0.05 0.01 0.04 0.581 0.42 1.0
                                   0.78 0.08 -0.04 0.00 0.613 0.39 1.0
## RNA.EOT
## RNA.EF
                                   0.78  0.06 -0.03  0.05  0.620  0.38  1.0
                                 -0.07 0.16 0.04 -0.14 0.050 0.95 2.5
## Baseline.histological.Grading
                                  0.03 -0.20 0.03 0.28 0.118 0.88 1.9
## Baselinehistological.staging
##
##
                         RC1 RC2 RC3 RC4
## SS loadings
                        1.88 1.25 1.22 1.22
## Proportion Var
                        0.06 0.04 0.04 0.04
## Cumulative Var
                        0.06 0.11 0.15 0.19
## Proportion Explained 0.34 0.22 0.22 0.22
## Cumulative Proportion 0.34 0.56 0.78 1.00
## Mean item complexity = 1.7
## Test of the hypothesis that 4 components are sufficient.
## The root mean square of the residuals (RMSR) is 0.06
## with the empirical chi square 3895.88 with prob < 0
##
## Fit based upon off diagonal values = -0.68
round(fit.pc$values, 3)
## [1] 1.896 1.249 1.235 1.192 1.163 1.147 1.129 1.107 1.062 1.059 1.035
## [12] 1.028 1.024 1.010 0.985 0.974 0.962 0.959 0.928 0.908 0.885 0.866
## [23] 0.862 0.847 0.833 0.796 0.766 0.565 0.529
fit.pc$loadings
##
## Loadings:
##
                                   RC1
                                          RC2
                                                 RC3
                                                        RC4
## Age
                                                         0.275
## Gender
## BMI
                                                  0.147 -0.514
## Fever
                                                  0.183
## Nausea.Vomting
                                          -0.520
                                                 0.255
## Headache
                                                         0.347
## Diarrhea
                                                  0.346 0.165
## Fatigue...generalized.bone.ache
                                          0.135
## Jaundice
                                                         0.343
## Epigastric.pain
                                   0.106 0.385
## WBC
                                   -0.105 0.180
                                                        -0.180
## RBC
                                          -0.320
## HGB
                                          -0.169 -0.172 -0.408
```

```
0.112 -0.340 0.359 -0.154
## Plat
## AST.1
## ALT.1
                                                    0.580 0.111
## ALT4
                                            -0.104 -0.243 0.171
## ALT.12
                                                   -0.455 0.162
## ALT.24
                                            -0.381 -0.334
## ALT.36
                                                           0.190
## ALT.48
                                             0.402 0.186 0.128
## ALT.after.24.w
                                             0.225
## RNA.Base
                                             0.112 0.151 0.308
## RNA.4
                                             0.189
                                                          -0.206
## RNA.12
                                     0.759
## RNA.EOT
                                     0.778
## RNA.EF
                                     0.783
## Baseline.histological.Grading
                                                           -0.138
                                             0.158
## Baselinehistological.staging
                                            -0.199
                                                           0.277
##
##
                     RC1
                           RC2
                                 RC3
                                        RC4
## SS loadings
                  1.884 1.250 1.219 1.219
## Proportion Var 0.065 0.043 0.042 0.042
## Cumulative Var 0.065 0.108 0.150 0.192
# Loadings with more digits
for (i in c(1,3,2,4)) { print(fit.pc$loadings[[1,i]])}
## [1] -0.0958724
## [1] -0.04948666
## [1] 0.06362426
## [1] 0.2745433
# Communalities
fit.pc$communality
##
                                                               Gender
                                Age
##
                        0.091062507
                                                         0.017148673
##
                                BMI
                                                                Fever
##
                        0.287460763
                                                         0.042658501
##
                     Nausea.Vomting
                                                             Headache
##
                        0.345852672
                                                         0.129429831
##
                           Diarrhea Fatigue...generalized.bone.ache
##
                        0.148330647
                                                         0.020932605
##
                           Jaundice
                                                     Epigastric.pain
##
                        0.133236702
                                                         0.168757196
##
                                WBC
                                                                  RBC
##
                        0.084375524
                                                         0.108709457
##
                                HGB
##
                        0.226575779
                                                         0.280929541
##
                              AST.1
                                                                ALT.1
##
                        0.006993762
                                                         0.356042693
##
                               ALT4
                                                               ALT.12
##
                        0.101470264
                                                         0.241949189
```

```
##
                           ALT.24
                                                           ALT.36
##
                                                      0.044408419
                      0.260153753
##
                           ALT.48
                                                   ALT.after.24.w
##
                      0.212487180
                                                      0.066164981
##
                         RNA.Base
                                                            RNA.4
##
                      0.131088563
                                                      0.083108957
##
                           RNA.12
                                                          RNA.EOT
##
                      0.581119980
                                                      0.612871462
##
                                    Baseline.histological.Grading
                           RNA.EF
##
                      0.619617868
                                                      0.050100301
##
      Baselinehistological.staging
##
                      0.118334956
# Rotated factor scores, Notice the columns ordering: RC1, RC3, RC2 and RC4
fit.pc$scores
##
                    RC1
                                 RC2
                                               RC3
                                                            RC4
##
      [1,] -1.0622643100 0.080761668 -1.5094106350 -1.962632045
##
      [2,] -0.0026786175 -0.044020173 0.0736538382
                                                   0.886102392
##
      [3,]
           0.6996290407 -3.216649251 -1.4067382361 -0.057261850
##
            1.5163346531 -0.776414526 -0.1281427476
      [4,]
                                                    0.681424373
##
      [5,]
           4.9057352496
                         0.476636781
                                     0.5326617845
                                                    0.313016961
##
      [6,] -1.5191976947
                         0.402707723 -0.2361002782
                                                    1.890172046
##
      [7,]
           0.3715288048
                         0.243918957 -1.6544416873
                                                    0.508715596
##
           1.0528134353
                         0.282429290
                                     1.0349324442
                                                    0.572492606
      [8,]
##
      [9,] -0.4624751429
                         0.369648174 -0.6615023183
                                                    0.590944129
##
     [10,]
           0.2959360322
                         0.303746811 -1.0721971649
                                                    1.098803257
##
                         0.695569255
                                     1.0678222322
                                                    1.621447274
     [11,]
           0.5072113382
##
     [12,]
           0.8254115604
                         0.458076783 -0.2398940534 -1.405320375
##
                         1.014090963
                                     0.9403751880 -1.245043164
     [13,] -1.2033769829
##
     [14,]
           1.1785640985 -0.271905934 -0.4626974933 -0.298366405
##
     [15,]
           0.1100394954 -0.289805069
                                     1.3012403268 -0.563134500
##
     [16,] -0.1863439454   0.279091024 -0.8554825546 -1.323897864
                                     1.3649506001
##
     [17,] -1.3677347159 -0.953862198
                                                    0.674939536
##
     [18,]
           1.556618732
##
     [19,]
           0.7823548200 -0.657807268
                                     1.3852125249
                                                    0.765636497
##
     [20,]
           0.9836496936
                        0.349039338
                                     0.5334288872
                                                    1.673576535
##
                         0.411599173 -0.7863017569
     [21,]
           0.6756799086
                                                    0.876200476
##
     [22,] -1.3528130191
                         0.296732421 -0.6216050314
                                                    1.033441596
##
     [23,] -0.8954196002
                         0.212892557 -0.2961383286
                                                    0.921981624
##
     [24,]
           0.7115976706 -1.271476758
                                     1.4876628894 -0.352473825
##
     [25,]
           0.6025828120
                         0.394462546
                                     0.8027628881
                                                   0.636466590
##
     [26,] -1.3885480928 -1.030634107
                                      0.5949796104 -0.150762610
##
     [27,]
            ##
     [28,]
           0.0552936021 -0.007343432
                                      0.9477563169 -0.451740170
##
     [29,] -1.2756600924 -0.847188753
                                      0.5566900065 0.433490670
##
     [30,] 0.7423287554 0.672957693 -1.8607013524 -0.525549256
##
     [31,] -0.6595104332 0.686749854
                                     0.1452406500 -1.149481326
##
     [32,] -0.2485054317 -1.229862373
                                      1.4107446897
                                                    0.815026590
##
     [33,] 1.1758079231 1.387365844 -0.1315387113
                                                    0.188171397
```

```
0.0311235683 -0.219399571 -0.6624545051
                                                    0.098782267
##
     [35,]
           0.8008224945 1.339360078 1.0819966981
                                                    1.121787320
# Play with FA utilities
```

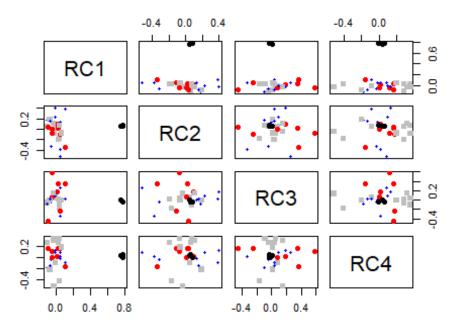
fa.parallel(HCV[1:29]) # See factor recommendation



## Parallel analysis suggests that the number of factors = 1 and the number of components = 1

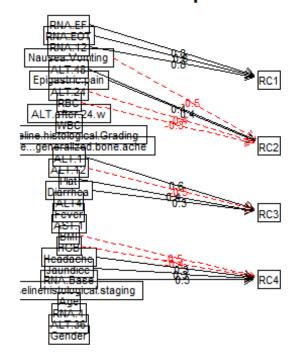
fa.plot(fit.pc) # See Correlations within Factors

# **Principal Component Analysis**



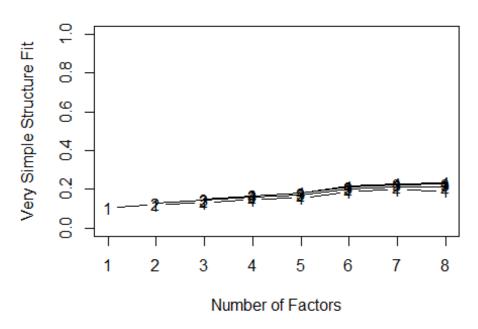
fa.diagram(fit.pc) # Visualize the relationship

# **Components Analysis**



vss(HCV[1:29]) # See Factor recommendations for a simple structure

#### Very Simple Structure



```
##
## Very Simple Structure
## Call: vss(x = HCV[1:29])
## VSS complexity 1 achieves a maximimum of 0.2 with 7
## VSS complexity 2 achieves a maximimum of 0.22 with 7 factors
##
## The Velicer MAP achieves a minimum of 0 with
                                                     factors
                                                  1
## BIC achieves a minimum of -2353.19 with 1 factors
## Sample Size adjusted BIC achieves a minimum of -1155.61 with
##
## Statistics by number of factors
     vss1 vss2
                  map dof chisq prob sqresid fit RMSEA
                                                           BIC SABIC complex
## 1 0.11 0.00 0.0024 377
                            374 0.54
                                           27 0.11
                                                       0 -2353 -1156
                                                                          1.0
## 2 0.12 0.13 0.0038 349
                                           27 0.13
                                                       0 -2198 -1089
                                                                          1.3
                            327 0.80
                                                       0 -2046 -1023
## 3 0.13 0.14 0.0052 322
                            283 0.94
                                           26 0.15
                                                                          1.6
## 4 0.15 0.16 0.0068 296
                            248 0.98
                                           26 0.17
                                                       0 -1893
                                                                 -953
                                                                          1.7
## 5 0.16 0.17 0.0085 271
                            221 0.99
                                           25 0.18
                                                       0 -1740
                                                                 -879
                                                                          1.8
## 6 0.19 0.20 0.0104 247
                            189 1.00
                                           24 0.22
                                                       0 -1598
                                                                 -814
                                                                          1.8
                                                       0 -1464
                                                                 -752
## 7 0.20 0.22 0.0123 224
                            157 1.00
                                           23 0.24
                                                                          2.1
## 8 0.19 0.21 0.0145 202
                            133 1.00
                                           23 0.24
                                                       0 -1328
                                                                 -686
                                                                          2.0
##
     eChisq SRMR eCRMS
## 1
        699 0.025 0.026 -2028
## 2
        594 0.023 0.025 -1931
## 3
        499 0.021 0.024 -1830
## 4
        425 0.019 0.023 -1716
## 5
        369 0.018 0.022 -1591
        311 0.017 0.021 -1475
## 6
```

## 7 255 0.015 0.020 -1365 ## 8 209 0.014 0.019 -1252