

Quadratic Equation

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10th Maths - Chapter 4

This is Problem-2 from Exercise 4.2

1. John and Jivanti together have 45 marbles. Both of them lost 5 marbles each, and the product of the number of marbles they now have is 124. We would like to find out how many marbles they have to start with.

Solution:

Given Data:

Let, the number of marbles John has = x .

Therefore, number of marbles Jivanti has = $45 - x$

After losing 5 marbles each,

Number of marbles John has = $x - 5$

Number of marbles Jivanti has = $45 - x - 5 = 40 - x$

Given that the product of their marbles is 124.

This can also be written as: $x^2 - 45x + 324 = 0$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad (1)$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad (2)$$

$$x = \frac{45 \pm \sqrt{-45^2 - 4 \times 1 \times 324}}{2 \times 1} \quad (3)$$

$$x = \frac{45 + \sqrt{2025 - 1296}}{2} \quad (4)$$

$$x = \frac{45 + \sqrt{729}}{2} \quad (5)$$

$$(6)$$

1st condition

$$x = \frac{45 + 27}{2} \quad (7)$$

$$x = \frac{72}{2} \quad (8)$$

$$x = 36 \quad (9)$$

$$(10)$$

2nd condition

$$x = \frac{45 - 27}{2} \quad (11)$$

$$x = \frac{18}{2} \quad (12)$$

$$x = 9 \quad (13)$$

Hence there roots are x=36 and x=9