



# Matrix - Line Assignment

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## CONTENTS

### I. PROBLEM

The vertices of a triangle are  $[at_1t_2, a(t_1 + t_2)]$ ,  $[at_2t_3, a(t_2 + t_3)]$ ,  $[at_3t_1, a(t_3 + t_1)]$ . Find the orthocentre of the triangle.

$$R_1 \rightarrow R_1 - R_2$$

$$\begin{pmatrix} (t_3 - t_1) & 0 & a(t_3 - t_1) \\ t_1 & 1 & -a[t_1t_2t_3 + (t_2 + t_3)] \end{pmatrix}$$

$$R_1 \rightarrow \frac{1}{(t_3 - t_1)}$$

### II. SOLUTION

Orthocenter of a triangle is the point where perpendiculars drawn to the opposite side from each vertex of the triangle intersect.

$$\begin{pmatrix} 1 & 0 & a \\ t_1 & 1 & -a[t_1t_2t_3 + (t_2 + t_3)] \end{pmatrix}$$

To find the orthocenter first we find the equation of line AP which is given by

$$R_2 \rightarrow R_2 - t_1R_1$$

$$\mathbf{m}_1^\top (\mathbf{x} - \mathbf{A}) = 0 \quad (1)$$

$$\begin{pmatrix} 1 & 0 & a \\ 0 & 1 & -a[t_1t_2t_3 + (t_1 + t_2 + t_3)] \end{pmatrix}$$

where  $\mathbf{m}_1 = (\mathbf{B} - \mathbf{C})$

By making X and Y Coordinates of eq1 and eq2 as Identity Matrix there obtained Intersection point i.e., **Orthocentre**

Similarly the equation of line AP is given by

Therefore the Orthocentre of triangle is

$$\mathbf{m}_2^\top (\mathbf{x} - \mathbf{B}) = 0 \quad (2)$$

$$\mathbf{X} = \begin{pmatrix} a \\ -a[t_1t_2t_3 + (t_1 + t_2 + t_3)] \end{pmatrix}$$

where  $\mathbf{m}_2 = (\mathbf{B} - \mathbf{C})$

By Solving eq1 and eq2 we get two line equations are represented in matrix form

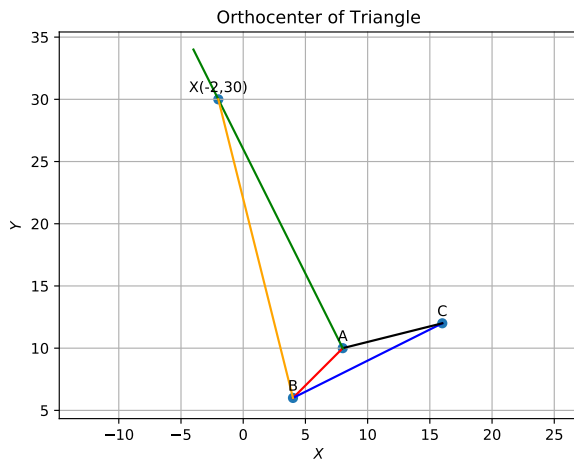
$$\begin{pmatrix} at_3(t_2 - t_1) & a(t_2 - t_1) & -a^2(t_2 - t_1)[t_1t_2t_3 + (t_1 + t_2)] \\ at_1(t_2 - t_3) & a(t_2 - t_3) & -a^2(t_2 - t_3)[t_1t_2t_3 + (t_2 + t_3)] \end{pmatrix}$$

$$R_1 \rightarrow \frac{1}{a(t_2 - t_1)} \quad R_2 \rightarrow \frac{1}{a(t_2 - t_3)}$$

$$\begin{pmatrix} t_3 & 1 & -a[t_1t_2t_3 + (t_1 + t_2)] \\ t_1 & 1 & -a[t_1t_2t_3 + (t_2 + t_3)] \end{pmatrix}$$

Symbol	Co-ordinates	Description
m1	$\begin{pmatrix} at_3(t_2 - t_1) \\ a(t_2 - t_1) \end{pmatrix}$	direction vector of m1
m2	$\begin{pmatrix} at_1(t_2 - t_3) \\ a(t_2 - t_3) \end{pmatrix}$	direction vector of m2
A	$\begin{pmatrix} at_1t_2 \\ a(t_1 + t_2) \end{pmatrix}$	direction vector of m1
B	$\begin{pmatrix} at_2t_3 \\ a(t_2 + t_3) \end{pmatrix}$	direction vector of m1
C	$\begin{pmatrix} at_3t_1 \\ a(t_3 + t_1) \end{pmatrix}$	direction vector of m1

### III. FIGURE



### IV. CodeLink

<https://github.com/Sairaghavendra36/Fwc-2022/blob/main/Matrix/Line/line.py>

Execute the code by using the command  
**python3 line.py**