Assignment: Probability

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13.1.17 ¹If A and B are events such that Pr(A|B) = Pr(B|A), then

- (a) $A \subset B$ but $A \neq B$
- **(b)** A = B
- (c) $A \cap B = \phi$
- (d) Pr(A) = Pr(B)

Solution:

Given,
$$Pr(A|B) = Pr(B|A)$$
 (13.1.4.1)

$$\implies \frac{\Pr(AB)}{\Pr(B)} = \frac{\Pr(BA)}{\Pr(A)}$$
 (13.1.4.2)

$$\Rightarrow \frac{\Pr(B)}{\Pr(B)} = \frac{\Pr(AB)}{\Pr(A)} (\text{Since}, \Pr(AB) = \Pr(BA)) \quad (13.1.4.3)$$

$$\implies \frac{1}{\Pr(B)} = \frac{1}{\Pr(A)} \tag{13.1.4.4}$$

$$\therefore \Pr(A) = \Pr(B) \tag{13.1.4.5}$$