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# Assignment 2

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Abstract—This document explains the concepts of Matrix transpose, Matrix Equality by solving a problem.

Download the python code from

https://github.com/Sairam13001/AI5006/blob/master/Assignment\_2/assignment\_2.py

and latex-tikz codes from

https://github.com/Sairam13001/AI5006/blob/master/Assignment\_2/assignment\_2.tex

#### 1 Problem

If  $\mathbf{A} = \begin{pmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{pmatrix}$ , and  $\mathbf{A} + \mathbf{A}^{\top} = \mathbf{I}$ , then find the value of angle  $\alpha$ .

### 2 Explanation

- \* If two matrices **A** and **B** are equal then the corresponding elements are equal.
- Similarly, Addition of two matrices is addition of their corresponding elements.
- \* If  $A = \begin{pmatrix} a & b \\ c & d \end{pmatrix}$ , then transpose of A is :

$$\mathbf{A}^{\top} = \begin{pmatrix} a & c \\ b & d \end{pmatrix} \tag{2.0.1}$$

3 Solution

Given that,

$$\mathbf{A} = \begin{pmatrix} \cos \alpha - \sin \alpha \\ \sin \alpha & \cos \alpha \end{pmatrix}. \tag{3.0.1}$$

So, the transpose of A is:

$$\mathbf{A}^{\top} = \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix}. \tag{3.0.2}$$

Sum of Matrices A and its Transpose  $A^{T}$  is :

$$\mathbf{A} + \mathbf{A}^{\mathsf{T}} = \begin{pmatrix} 2\cos\alpha & 0\\ 0 & 2\cos\alpha \end{pmatrix}. \tag{3.0.3}$$

Also given,  $\mathbf{A} + \mathbf{A}^{\top} = \mathbf{I}$ , So:

$$\begin{pmatrix} 2\cos\alpha & 0\\ 0 & 2\cos\alpha \end{pmatrix} = \begin{pmatrix} 1 & 0\\ 0 & 1 \end{pmatrix} \tag{3.0.4}$$

That Implies,

$$2\cos\alpha = 1 \implies \cos\alpha = \frac{1}{2} \tag{3.0.5}$$

As per the cosine values, the angle  $\alpha$  is :

$$\alpha = \frac{\pi}{3} = 1.047 \tag{3.0.6}$$

The cosine function is plotted along with the point (x, (1.047, 0.5)) as shown below:

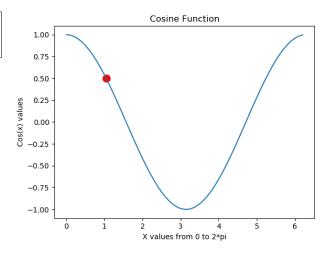


Fig. 0: Cosine Function