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Assignment 2

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Abstract—This document explains the concepts of Matrix transpose, Matrix Equality by solving a problem.

Download the python code from

https://github.com/Sairam13001/AI5006/blob/master/Assignment_2/assignment_2.py

and latex-tikz codes from

https://github.com/Sairam13001/AI5006/blob/master/Assignment_2/assignment_2.tex

1 Problem

$$\mathbf{A} = \begin{pmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{pmatrix}$$

and $\mathbf{A} + \mathbf{A}^{\mathsf{T}} = \mathbf{I}$, then find the value of angle α .

2 EXPLANATION

The Complex number equivalent to the matrix is:

$$\begin{pmatrix} a & -b \\ b & a \end{pmatrix} \implies \begin{pmatrix} a \\ b \end{pmatrix} \tag{2.0.1}$$

$$\mathbf{A} = \begin{pmatrix} a \\ b \end{pmatrix} \implies \mathbf{A}^{\top} = \begin{pmatrix} a \\ -b \end{pmatrix} \tag{2.0.2}$$

And addition of **A** with A^{T} results in :

$$\binom{a}{b} + \binom{a}{-b} = \binom{2a}{0} \tag{2.0.3}$$

3 Solution

So, According to the given question $\mathbf{A} + \mathbf{A}^{\mathsf{T}}$ is :

$$\begin{pmatrix} \cos \alpha \\ \sin \alpha \end{pmatrix} + \begin{pmatrix} \cos \alpha \\ -\sin \alpha \end{pmatrix} = \begin{pmatrix} 2\cos \alpha \\ 0 \end{pmatrix}$$
 (3.0.1)

Given that $\mathbf{A} + \mathbf{A}^{\mathsf{T}} = \mathbf{I}$:

$$\begin{pmatrix} 2\cos\alpha\\ 0 \end{pmatrix} = \begin{pmatrix} 1\\ 0 \end{pmatrix} \tag{3.0.2}$$

That Implies,

$$2\cos\alpha = 1 \implies \cos\alpha = \frac{1}{2} \tag{3.0.3}$$

As per the cosine values, the angle α is :

$$\alpha = \frac{\pi}{3} = 1.047 \tag{3.0.4}$$

The cosine function is plotted along with the point (x, cos(x)) = (1.047, 0.5) as shown in Fig. 0:

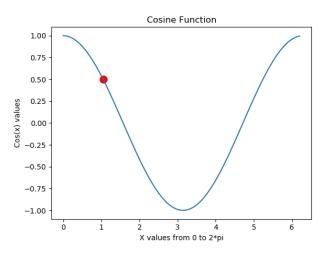


Fig. 0: Cosine Function