

## Homework 8

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### ① Problem Solutions

SSR226.

Size of the Output of a Convolutional layer. is given by

$$\text{Size}(O) = \frac{I - K + 2P}{S} + 1$$

$I$  = Size of input image.

$K$  = Size(width) of Kernels used in the Conv Layer.

$N$  = Number of kernels

$S$  = Stride of Convolution Operation.

$P$  = Padding.

Size of a Max Pool Layer.

$$O = \frac{I - P_s}{S} + 1$$

$P_s$  = Poolsize.

Number of Parameters of a Convolution Layer.

$$W_c = K^2 \times C \times N$$

$$B_c = N$$

$$P_c = W_c + B_c.$$

$W_c$  = Number of weights of the conv layer

$B_c$  = Number of Biases of the conv layer

$P_c$  = Number of parameters of the conv layer

$K$  = Size(width) of Kernels used in Conv layer

$N$  = Number of kernels

$C$  = Number of Channels of the input image

Number of parameters of a fully connected (FC) layer connected to a Conv layer.

$$W_{cf} = O^2 \times N \times F$$

$$B_{cf} = F$$

$$P_{cf} = W_{cf} + B_{cf}$$

$W_{cf}$  = Number of weights of a FC layer which is connected to a Conv layer.

$B_{cf}$  = Number of biases of a FC layer which is connected to a Conv layer.

$O$  = Size of the output image of the previous Conv layer.

$N$  = Number of kernels in the previous Conv layer.

$F$  = Number of neurons in the FC layer

→ Input =  $64 \times 64 \times 3$

First convolution layer =  $5 \times 5 \times 3 \times 32$ .

First layer Convolution

$$\text{Output} = \frac{I - K + 2P}{S} + 1$$

$$\text{226} \rightarrow I = 64 \quad K = 5 \quad P = 0 \quad S = 1$$

$$= \frac{64 - 5 + 2 \times 0}{1} + 1$$

$$= 59 + 1 = 60$$

$$\boxed{CNV_1 = 60 \times 60 \times 32}$$

~~Notes~~

No of trainable parameters =

$$C = 3 \quad N = 32 \quad K = 5$$

$$W_c = K^2 \times C \times N = 5^2 \times 3 \times 32 = 2400$$

$$B_c = N = 32$$

$$\boxed{P_c = W_c + B_c = 32 + 2400 = 2432}$$

## Max Pool Layer 2x2

$$\text{Output image size} = \frac{I - P_s}{S} + 1$$

For 2D Max pooling

$$O = \frac{I}{2}$$

$$O = 30 \times 30 \times 32$$

There are no training parameters involved in MaxPool layer.

## Convolutional Layer 2:

$$\text{Convolutional} = 3 \times 3 \times 32 \times 64 \quad \text{Stride} = 2$$

$$\text{Output image size} = \frac{I - K + 2P}{S} + 1$$

$$I = 30 \quad K = 3 \quad P = 0 \quad S = 2$$

$$= \frac{30 - 3 + 2 \times 0}{2} + 1$$

$$= 14$$

$$\text{Output} = 14 \times 14 \times 64$$

Trainable Parameters =

$$N = 64 \quad C = 32$$

$$W_c = K^2 \times C \times N = 9 \times 32 \times 64$$

$$B_c = N = 64$$

$$P_c = W_c + B_c = 18496$$

## Fully Connected Layer:

~~Number of Neuron in FC layer~~ =  ~~$25 \times 25 \times 64$~~   
= ~~40000~~

$$O = 25$$

$$N = 64$$

$$F = 10$$

$$W_{CF} = O^2 \times N \times F$$

$$= 14 \times 14 \times 64 \times 10$$

$$= 125440$$

$$B_{CF} = F$$

$$= 10$$

$$P_{CF} = W_{CF} + B_{CF}$$

$$= 125440 + 10$$

$$= 125450$$

Total trainable parameters of Complete Architecture

$$= 146,378$$

The dimension of the weight Matrix of FC is =  $(12544, 10)$



(2) Problem.

For RNN

Input Sequence  $\{x_t\}$  with dimension  $n$ ,

Hidden State  $\{h_t\}$  with dimension  $k$ ,

Output Sequence  $\{y_t\}$  with dimension  $m$ ,

The Number of trainable parameters =

$$= k(k+m) + k.$$

$$= k^2 + km + k$$

(3) Problem

Let  $0 < p, q < 1$  and  $\epsilon = \log p - \log q$ .

Show that

$$\frac{p-q}{p} = 1 - e^{-\epsilon}$$

Applying log on Both Sides

$$\log\left(\frac{p-q}{p}\right) = \log(1 - e^{-\epsilon})$$

$$\frac{p-q}{p} = 1 - e^{-\epsilon}$$

$$x - \frac{q}{p} = x - e^{-\epsilon}$$

$$+ \frac{q}{p} = + e^{-\epsilon}$$

Apply log on both sides

$$\log \frac{q}{p} = \log(e^{-\epsilon})$$

$$\log q - \log p = -\epsilon$$

$$\epsilon = -\epsilon$$

$$\epsilon + O(\epsilon^2) = 1 - e^{-\epsilon}$$

$$\log p - \log q + \frac{\partial^2}{\partial x^2} \epsilon$$

$$\log p - \log q + \frac{\partial^2}{\partial x^2} (\log p - \log q) = 1 - e^{-\epsilon}$$

$$\log p - \log q + O(\epsilon + \epsilon) = 1 - e^{-\epsilon}$$

The KL divergence  $D_{KL}(p(x) || q(x)) = \int p(x) \log \frac{p(x)}{q(x)} dx$  is the expected amount of information

$\epsilon$  is the error

$$\log p - \log q + O(\epsilon + \epsilon) = 1 - e^{-\epsilon}$$

Applying Taylor series

$$\log p - \log q + O(\epsilon + \epsilon) = 1 - e^{-(\log p - \log q)}$$

The KL divergence  $D_{KL}(p(x) || q(x)) = \int p(x) \log \frac{p(x)}{q(x)} dx$  is the continuous form.

KL divergence gives the difference between the two probability distribution.

$$= \int p(x) (\log p(x) - \log q(x)) dx$$

$$= \int p(x) \epsilon dx$$

$\epsilon$  is the approximate error. So if the error is zero, only if both the distribution are same and probabilities are zero. This can be used to find error function.