## Ramsey's theorem and computability theory Professor Tamara Lakins, Allegheny College

Thursday, April 25, 2002 102 Bradley Hall, 4 pm Tea 3:30 pm, Math Lounge

**Abstract:** An infinite version of Ramsey's theorem states that for every coloring of  $[\omega]^n$  (the set of all n-element subsets of  $\omega$ ) by finitely many colors, there is an infinite set A which is homogeneous for that coloring, i.e., all elements of  $[A]^n$  have the same color. After an introduction to the necessary background in computability theory, we present a survey of results concerning the complexity of infinite homogeneous sets for effectively given (computable or computably enumerable) colorings.