~ SOLUTIONS ~

Here we explore the fundamental soln for the heat equation - without calculus!

$$E \begin{bmatrix} e & r & t & u & c & \mathcal{H} \\ 1 & 1 & 1 & -3 & -1 \\ 1 & 1 & -1 & -1 \end{bmatrix}$$

$$\Theta \begin{bmatrix} e & r & t & u & c & \mathcal{H} \\ 1 & 1 & 1 & -1 & -1 \\ 0 & 1 & -1 & -1 \end{bmatrix}$$

Pulse of energy sized e released at origin at time t=0. The medium has heat capacity c (energy per volume per degree) and thermal conductivity It (power per length per degree). The temperature at distance r and time t is u (we take u= 0 every where for t<0)

- a) Using fundamental units energy (E), length (L), time (T), temperature (D), fill in the dimensions of the m=6 quantities in the problem above (scheck with me).

(MC)

How does scaling in d) change in general space dimension d? (we had d=3 above;

note that K has units ET-1 L2-d D' in general d) Turns out u ~ t-d/2

Note g(TI) = e-TI/2

A result we'll get to later.) but have to redo lin. algebra.

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