Combinatorics of permutations

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Thursday, January 30, 2014 008 Kemeny, 4:00PM (Tea: 300 Kemeny, 3:30 pm)

Abstract

For a permutation p, let $S_n(p)$ be the number of permutations on n letters avoiding p. A decade ago, Marcus and Tardos proved the celebrated Stanley–Wilf conjecture that, for each permutation p, $S_n(p)^{1/n}$ tends to a finite limit L(p). Backed by numerical evidence, it has been conjectured by various researchers over the years that L(p) is on the order of k^2 for every permutation p on k letters. We disprove this conjecture, showing that L(p) is exponential in a power of k for almost all permutations p on k letters. The proof uses ideas from extremal and probabilistic combinatorics.

This talk should be accessible to graduate students.