23 WORKSHEET: Wronskiams

A) Compute Wronskian W(E) for i) tsint, sint

ii)  $t^3$  ,  $5t^3$ 

B) Show sinht, cosht form a fundamental set of 3 solutions to y" - y = 0

\* Means: they selve the ODE (check!)

K Wronshan documb vomish.

> Show these two solutions match {y(0) = 1 and 5 y(0) = 0 8 y'(0) = 1

10/12/07 8. 10/7/93 Barriett.

MATH 23 WORKSHEET: Womskiems

~ SOLUTION -

A) Compute Wronskian W(E) for i) tsixt, sint W = yiyi - yzyi = | tsint sint | = tsinbcost - sint - trost sint | = - sinet.

ii)  $t^3$ ,  $5t^3$ 

 $W = \begin{pmatrix} t^3 & 5t^3 \\ 3t^2 & 15t^2 \end{pmatrix} = 15t^5 - 3(5)t^5 = 0$  for all t.

Note y, - fyz = 0. for all + (lin.)

B) Show sinht, cosht form a fundamental set of

solutions\* & y" - y = 0

know et, et are solus, from last Worksheet. \*\* Means: they

solve the ODE (check!)

K Wronshan doesn't So sight, cosht are linear combinations of flee

also

solve

W(sinht, cosht) = (ex-ex/ex+ex) - (ex-ex) (ex-ex) = -1/2 - 1/2 = -1/2 = -1/2 - 1/2 = -1/2 - 1/2 = -1/2 - 1/2 = -1/2 - 1/2 = -1/2 - 1/2 = -1/2 - 1/2 = -1/2 =

Show these two solutions match  $\{y(0)=1\}$  and  $\{y(0)=0\}$   $\{y'(0)=1\}$ 

sight at t=0 is  $e^{\circ}-e^{\circ}=0$  cosh t at t=0 is  $e^{\circ}t=0$  = 1

It sinht = cosh t . so y'(0) = 1 for ship.

Let cosh t' = sinht " y 10 = 0 for cosh.

Also oneful: coshet = 1 + sinhet.