MATH 46 WORKSHEET : Greens functions

Consider $A = -\frac{d^2}{dx^2}$ on [0, 0] with Dividled BG

We wish to find the Green's func. to solve |Au = f with u[o]=0 u(1)=0

Write general solution to Au = O

Solve for u, (x) which obeys only left-end BC:

Lz(x) " " right-end BC:

Compute Wronskian W/x):

Write g(x, 4):

Sketch it for fixed 9:

g(x, 3)

(is it continuous ?) (what is the Simp in gradient?)

Write g (9,x) -- notice anyth my?

Sketch g(x, 3) 0 0

MATH 46 WORKSHEET: Grains functions P=1, 9=0. Consider A = - de on [0, 1] with Dirichlet BG We wish to find the Green's func. to solve Au = f with u[0] = 0 u(1) = 0Write general solution to Au = O u''=0so u(x) = Ax + B. Solve for U,(x) which obeys only left-end BC: $U_2(x)$ " " right-end BC: 1-xCompute Wronskian W/x): $u_1 u_2' - u_1' u_2 = \times - (1 - x)$ Write $g(x, q_1) = -\frac{1}{p(s)} \begin{cases} u_1(x) u_1(s), x < s \\ u_2(x) u_1(s), x > s \end{cases} = \begin{cases} x(1-s) & x < s \\ s(1-x) & x > s \end{cases}$ g(x, g)

(is it

continuous ?

everywhere ?)

What is the

symp in

gradients?) Sketch it for fixed 2: Write g (9,x) -- white anyth sy? Sketch g(x, 5) 0 0 9

yes, g(3,x) = g(x, 5)