For each described operation, find standard matrix of, and whother is onto and one-tr-one

what size?

 $T(x_1 x_2) = (3x_1 - 2x_1 + x_2, -x_2)$   $T: \mathbb{R}^n - \mathbb{R}^m \quad \text{(What are on m?)}.$ 

A =

onto?

one-to-one?

b) T is reflection about line  $x_1 = X_1$  $(T: \mathbb{R}^2 \to \mathbb{R}^2)$ .

A =

onto?

one-to-one?

c) TEXR3-1RL

projects the point (x1y12) down vertically out the (x1y1) plane (the studen of a point under the widday sun).

A =

onto?

one to one?

7/5/06

For each described operation, find student unators of, and abother Tis outo out one-to-one columns given by

 $\mathcal{A} = (3\kappa_1, -2\kappa_1 + \kappa_2, -\kappa_2)$ T: RM R (What are or m?).

> 2 vectors cannot Span 1R3 since would need a privation each of 3 rows for this.

since no free vary, a pivot in every col.

T is reflection about line x2=X1 (T: R2-1 R2).

 $\overline{e_i}$ reflection

swaps the

unit vector.  $\overline{T(\overline{e_i})} = (01)$ could also ausure geometrically.

c) TixR3-1R2

projects the point (x1y,2) down vertically out the (x,y) plane (the standow of a point under the widden sun).

[T(E)] What sin?  $A = \begin{bmatrix} 3 & 0 \\ -2 & 1 \\ 0 & -1 \end{bmatrix} \sim \begin{bmatrix} \mathbf{e} + \mathbf{f} \\ \mathbf{e} \end{bmatrix}$ 

onto? No, since AR=6 mbraconsistant for all I in R3. one-to-one? Yes, since wha

Ax= t' & consister, it is unique (6 15 Emage of single x)

 $A = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \sim \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ 

onto? Yes since proof in every row.

Tone-to-one?

Yes since there are no free vans in Ax = T.

A = [10.0] in REP

onto? Yes since pivot in every row one-to-one? No since in Ax= 1, x3 is free var, not amire.