Math 114 (cross-listed with Math 74) - Algebraic Topology

3-4 weeks on the fundamental group and covering spaces.

6-7 weeks on homology theory

The Fundamental Groups and Covering Spaces

- 1. Homotopy, definition of π_1 and its basic properties, van Kampen Theorem
- 2. Covering spaces: lifting properties, the Galois correspondance, deck transformations, the universal cover
- 3. Applications and examples

Homology Theory

- 1. Basic homological algebra: chain complexes, exact sequences, chain maps, chain homotopy
- 2. Construction of the singular homology of a pair of spaces
- 3. Eilenberg-Steenrod axioms: excision, exactness, homotopy
- 4. Computational techniques (Mayer-Vietoris sequence,...)
- 5. Applications (Brouwer fixed point theorem, hairy ball theorem, ..)