Differentiating Distributions



A C^1 function f(x)

$$\chi_{[a,b]}(x)$$

A piecewise C^1 function

$$T(x) = \begin{cases} f(x), & x < a \\ g(x), & x > a \end{cases}$$

$$f * T$$

$$\delta(x-a) - \delta(x-b)$$

$$(g(a^{+}) - f(a^{-})) \delta(x - a)$$

$$+ \begin{cases} f'(x), x < a \\ g'(x), x > b \end{cases}$$

$$f' * T = f * T'$$