

space curves

①

①⑨ $x = \cos 4t, y = t, z = \sin 4t$

All the points (x, y, z) on the curve satisfy

$$x^2 + z^2 = 1$$

So curve is on a cylinder (with axis the y -axis).

On the curve $y = t$,

hence the curve is a helix. (VI)

②⑩ $x = t, y = t^2, z = e^{-t}$

All the pts (x, y, z) on the curve satisfy

$y = x^2$. Also note that $y \geq 0$ & $z \geq 0$

& $(0, 0, 1)$ is on the curve (if $t = 0$)

As $t \rightarrow \infty, (x, y, z) \rightarrow (\infty, \infty, 0)$ &

as $t \rightarrow -\infty, (x, y, z) \rightarrow (-\infty, \infty, \infty)$

So curve (II)

(21) $x=t, y=\frac{1}{1+t^2}, z=t^2$

(2)

$y, z \geq 0$

The curve passes thr^o $(0, 1, 0)$ (when $t=0$).

As $t \rightarrow \infty, (x, y, z) \rightarrow (\infty, 0, \infty)$

as $t \rightarrow -\infty, (x, y, z) \rightarrow (-\infty, 0, \infty)$

So the curve (IV)

(22) $x = e^{-t} \cos 10t, y = e^{-t} \sin 10t, z = e^{-t}$

$x^2 + y^2 = e^{-2t} (\cos^2 10t + \sin^2 10t) = e^{-2t} = z^2$

Hence the curve is on the cone

$x^2 + y^2 = z^2$

$z > 0$ & hence the curve (I)

(23) $x = \cos t, y = \sin t, z = \sin 5t$

$x^2 + y^2 = \cos^2 t + \sin^2 t = 1$

Hence the curve is on a cylinder with z -axis ~~axis~~ as its axis.

$\gamma(t) = \gamma(t + 2\pi)$

& hence curve (V)

(24)

(3)

$$x = \cos t, \quad y = \sin t, \quad z = \ln t.$$

$$x^2 + y^2 = \cos^2 t + \sin^2 t = 1$$

curve is on a cylinder with axis the z -axis.

$$\text{As } t \rightarrow 0, \quad z \rightarrow -\infty$$

& hence III