

- From Section 5:

- Which of the following subsets  $H$  are subgroups? Please justify your assertions.
  1.  $G = (\mathbb{R}, +)$ ;  $H = \mathbb{Q}$
  2.  $G = (\mathbb{C}^\times, \cdot)$ ;  $H = \{a + bi : a, b \in \mathbb{R}, a^2 + b^2 = 1\}$ . *Hint:* Think about  $H$  visually. What shape does it make in the complex plane?
- How many subgroups of order 2 does  $\mathbb{Z}_2 \times \mathbb{Z}_2 \times \mathbb{Z}_2$  have? Please describe them all.
- Please solve Exercises 5.7, 5.8, and 5.18 from the textbook.
- In the cyclic group  $(\mathbb{Z}_{24}, \oplus)$ , find a generator for  $\langle 21 \rangle \cap \langle 10 \rangle$ .
- In the cyclic group  $(\mathbb{Z}_n, \oplus)$ , please give a general formula for the generator of  $\langle m \rangle \cap \langle k \rangle$ . Please justify your answer.

- From Section 6:

- Please solve Exercises 6.1 (parts a & d) and 6.3.
- Can we write  $D_4$  as a direct product of some of its subgroups? Please justify your answer.
- In the group  $\mathbb{Z}_{30} \times \mathbb{Z}_{20}$ , how many elements are there of order 15? How many cyclic subgroups are there of order 15?

\* Exercise 5.26