MATH 46 WORKSHEET : regular perturbation

Substitute y(t) = yo(t) + & y,(t) + & zy,(t) into $y' = -y + zy^2$ with IC y(0) = 1

Collect & tems:

what IC does yo(t) satisfy? Solve for it.

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What IC does yi (t) satisfy? [Hint sub series into original Ic] Solve for it.

MATH 46 WORKSHEET: : regular perturbation 4667.

SOLUTIONS see p. 88-90. Substitute : y(t) = yo(t) + & y(t) + & y(t) into y' = -y + zy' with IC(y(0) = 1) $y_0' + \epsilon y_1' + \epsilon y_2' + \cdots = -y_0 - \epsilon y_1 - \epsilon^2 y_2 + \cdots + \epsilon y_0^2 + 2\epsilon^2 y_0 y_1 + O(\epsilon^2) - \cdots$ IC gives

yold + = 2y=(0) + -.. = 1. Collect ϵ° tems: $y_{\circ}' = -y_{\circ}$ ie $y_{\circ}' + y_{\circ} = 0$ ie $y_{\circ}(t) = Ae^{-t}$ what IC does yo(t) satisfy? Solve for it. Taking & teme in IC gives yo()=1 50 A=1 ie $y_o(t) = e^{-t}$ Collect & tems: y' = - y, + yo What IC does ye (+) satisfy? [Hint sub series into original Ic] Solve for it. y.(0) = 0 50 $y_1' + y_1 = y_0^2 = e^{-2t}$ integrating factor e^t $e^t y_1 = \int e^{-t} dt + c$ IC makes c = +1 $y_1 = e^{-t}(e^{-t} + c) = -e^{-2t} + ce^{-t} = -e^{-2t} + e^{-t}$