MATH 46 WORNSHEET

Asymptotic analysis, Dominant balancing.

Smutt

A) Is  $f(t, \epsilon) = \epsilon tant$  uniformly convergent to zero on  $(0, \frac{\pi}{4})$ ?

(0, 7/2)?

does start enverge pointuite on (0, 1/2)?

B) Find the scaling of x with z that makes two terms of equal order and others of lower order in  $z \times z^4 + z \times z^3 - x^2 + 2x - 1 = 0$ 

Find the leading-order term in each of the four roots:

If time, continue to higher corrections for these roots:

MATH 46 WORKSHEET

Asymptotic analysis, Dominant balancing.

A/1/07 Bornett

A) Is  $f(t, \epsilon) = \epsilon t$ ant tant ):

uniformly convegant to zero on (0, 7/4)?

yes since Itamt/ € const on (0, %).

dow start enverge pointuite on  $(0, \frac{11}{2})$ ? no en  $(0, \frac{11}{2})$ ?

yes since for any  $t \in (b, 1/2)$ , tant is some number Cand f(t, z) = Cz - 19 as z - 10.

Find the scaling of x with & that makes two terms of equal order and others of lower order in

 $\xi x^4 + \xi x^3 - x^2 + 2x$ 1 = 0 quess  $X = \frac{1}{2}$ ?  $X = \frac{1}{2}$ ?

Emphical round to solve; field the line connecting a points in the (power of x, power of x) plane with all other points to the right (higher & power).

Find the leading-order term in each of the four roots :

regular mote (drop 1st two lens) - x2 + 2x0 - 1 = 0

so Xo = +1 (furice) Sub.  $X = \frac{y}{2h} \Rightarrow \xi = \frac{y^3}{2h} + \xi = 0$ 

X= +1 + \( \xi \) (\xi) (\xi) (\xi) \( \xi \) (\xi') \( \xi') \( \xi') \) \( \xi') \( \xi') \( \xi') \)

1012 2.