Math 111 Syllabus (cross-listed with Math 81) based on Lang, Algebra

- 1. [3 days: II.2, II.4 II.5] Commutative rings, prime and maximal ideals, CRT, evaluation and reduction homomorphisms, Localization of rings (field of fractions), irreducibles, primes, UFDs, PIDs, Euclidean domains.
- 2. [3 days: IV.1 IV.3] Polynomials in one variable, over UFDs, Gauss's lemma, irreducibility criteria.
- 3. [3 days: V.1] Finite and Algebraic Field Extensions.
- 4. [3 days: V.2 V.3] Splitting fields, normal extensions, and algebraic closures; uniqueness.
- 5. [4 days: V.4 V.5] Separable extensions, primitive element theorem, Finite fields.
- 6. [1 day: V.6] Inseparability (intro only)
- 7. [4 days: VI.1]Galois Extensions: Fundamental theorem, composite extensions
- 8. [3 days: VI.2] Galois groups of polynomials.
- 9. [3 days: VI.3] Cyclotomic extensions and polynomials

Optional topics: group rings, polynomial rings in several variables, compass and straightedge constructions, solvability by radicals, infinite Galois groups