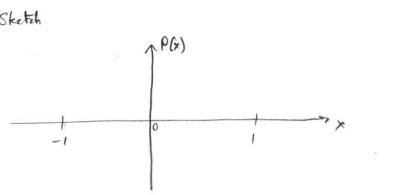
MATH 53 WORK SHEET: Motion in a Potential.

11/9/07 Banutt

Consider 
$$X'' + 1 - 3x^2 = 0$$

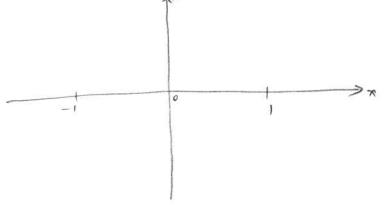


What is de =?

$$P(x) = ?$$

Write as 1st order system:

Sketch level curses of E(x,x) = 2x2 + P(x) in the phase plane:



Who are The equilibria! (comput & show on plane).

What kinds of periodic orbits can happen?

(What range of energies E may they have?).

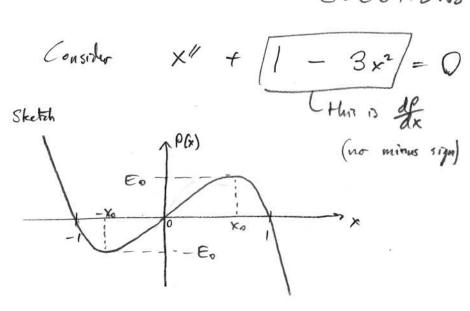
When is the motion unbounded?

Deduce the stability wong Jacoben DF at the eggnithbria:

11/4/07 Barnett

SOCUTIONS -

$$x'' + [1 - 3x^2] = 0$$



What is at =? 1-3x2

$$P(x) = ? \times - \times^3$$

Write as 1st order system:

$$x' = y$$
  
 $y' = -\frac{dP}{dx} = -1 + 3x^{2}$ 

Sketch level curses of E(x,x) = 2x2 + P(x) in the phase glane:

Willman The equilibria?

 $\frac{df}{dx} = 0 \quad \text{ie} \quad (-3x^2 = 0)$   $\times 0 = \pm \frac{1}{\sqrt{3}}$ 

$$x_{-} = \pm \frac{1}{2}$$

region which leads to bounded periodic motion. What kinds of periodic orbits can happen?

When is the motion unbounded? When is the motion unbounded?

It can be for any energy; but must be so for 
$$E > E_0$$
.  $= \frac{1}{3\sqrt{3}} = \frac{1}{3\sqrt{3}}$ 

Deduce the stability wong Jacoben DF at the segnitibria:

$$\times = \frac{1}{\sqrt{3}}$$
:  $\vec{D}\vec{F} = \begin{pmatrix} 0 & 1 \\ 6 \times & 0 \end{pmatrix} = \begin{pmatrix} 0 & 1 \\ 2\sqrt{3} & 0 \end{pmatrix} \xrightarrow{\text{eignals}} \lambda = \pm \sqrt{2\sqrt{3}}$ 

$$x_0 = \frac{-1}{13}$$
:  $5\tilde{f} = \begin{pmatrix} 0 & 1 \\ -253 & 0 \end{pmatrix}$  so  $\lambda = \pm i\sqrt{253}$ ,  $A = \pm i\sqrt{253}$ , win the monline stability then. Canyolar from at the bottom of well.