Each problem is worth 7.5 points.

- 1. The arclength of the curve $\mathbf{c}(t) = (2\cos t, \sqrt{3}t, 2\sin t)$ on $1 \le t \le 7$ is:
 - (a) $\sqrt{2}\pi$
 - (b) $6\sqrt{7}$
 - (c) 7π
 - (d) 54

- 2. The equation of the plane that passes through point (2,4,-1) and is perpendicular to l(t)=(-1,-2,3)t+(0,7,1) is:
 - (a) 7y + z + 1 = 28
 - (b) -x + 2y + 3z = -11
 - (c) 7y z + 1 = 22
 - (d) x + 2y 3z = 13

- 3. Without regard to orientation, match the following geometric curves (left column) to their parametrization (right column).
 - $(1) \ 9x^2 + 4y^2 = 4$
- (i) $\mathbf{c}(t) = (2\cos t, 2\sin t, 2\sin t + 1)$
- (2) $x^2 + y^2 = 4$
- intersect y = z 1 (ii) $\mathbf{c}(t) = (\frac{3}{2}\cos t \frac{1}{2}, \frac{3}{2}\sin t, \frac{3}{2}\cos t + \frac{3}{2})$ (3) $y = 4 \sqrt{1 x^2}$ (iii) $\mathbf{c}(t) = (\cos t, 4 \sin t)$ (4) $z = 4 x^2 y^2$ intersect x = z 2 (iv) $\mathbf{c}(t) = (\frac{2}{3}\cos t, \sin t)$

- (a) 1-(ii), 2-(iv), 3-(iii), 4-(i)
- (b) 1-(iv), 2-(i), 3-(iii), 4-(ii)
- (c) 1-(ii), 2-(i), 3-(iv), 4-(iii)
- (d) 1-(iv), 2-(ii), 3-(iii), 4-(i)

- 4. Evaluate $\int_1^2 \int_{x^3}^x e^{y/x} dy dx$.
 - (a) $e \frac{e^4}{2}$
 - (b) $4e e^4$
 - (c) Can't be evaluated without tables
 - (d) $2e \frac{e^4}{2}$

- 5. The rate of change of $f(x,y)=2x^2y+e^x$ in direction parallel to vector ${\bf v}=(3,4)$ at point $(0,\ln 2)$ is:
 - (a) $\frac{3}{5}$
 - (b) 0
 - (c) 3
 - (d) $4 \ln 2 + 2$

- 6. The volume inside the paraboloid $z = 4 x^2 y^2$ above z = 2 is:
 - (a) $\frac{8\sqrt{2}}{3}\pi$
 - (b) 4π
 - (c) 2π
 - (d) $\sqrt{2}\pi$

- 7. If $\nabla f = \mathbf{F}$, and $\mathbf{F} = (2y^2 1, 4xy + z, y)$, then f is:
 - (a) $(2y^2 1)x + zy$
 - (b) (2xy + z)y
 - (c) (z+2xy)y
 - (d) $2xy^2 x$

- 8. The work done by a force vector field $\mathbf{F} = \frac{1}{x}\mathbf{j}$ on a particle following the path given by $\frac{x^2}{2} + \frac{y^2}{4} = 1$ from point (0, -2) to (0, 2) (counterclockwise) is:
 - (a) 0
 - (b) $-\sqrt{2}\pi$
 - (c) π
 - (d) $\sqrt{2}\pi$

- 9. If $3x^3y-5x^2+yz=1$ is a level surface, then the direction of fastest change from the point (1,6,-2) is:
 - (a) (26,3,6)
 - (b) (26, 1, 6)
 - (c) (38, 3, 6)
 - (d) (44, 1, 6)

- 10. Let a surface be given parametrically by $\Phi(u,v)=(v,uv^2,u+v)$. The equation (in rectangular coordinates) of the plane tangent to the surface at point (x,y,z)=(2,4,3) is:
 - (a) y 4z = -8
 - (b) -3x + y 4z = -14
 - (c) -12x + y + 16z = 28
 - (d) y + 4z = 8

- 11. Evaluate $\int_{\mathbf{c}} -2ydx + 5xdy$ if \mathbf{c} is the counter-clockwise path around the triangle in the x-y plane with vertices (0,0), (2,1), and (5,0).
 - (a) 21
 - (b) $\frac{-21}{2}$
 - (c) $\frac{35}{2}$
 - (d) -7

- 12. The surface area of the portion of $z=1+x^2+y^2$ where $1\leq z\leq 2$ is:
 - (a) $\frac{\pi}{3} 5 \sqrt{5}$
 - (b) 4π
 - (c) $\frac{\pi}{6}(5\sqrt{5}-1)$
 - (d) $\frac{\pi}{4}(\sqrt{5}-1)$

- 13. If $f(x,y,z)=(3x^2+y,zx,4x^2+1)$ and g(u,v,w)=(5uv,w+3), then the size of the derivative matrix of the composition of f and g is:
 - (a) 3×3
 - (b) 3×2
 - (c) 2×3
 - (d) 3×1

- 14. Using the Fundamental Theorem of Line Integrals, evaluate $\int_{\mathbf{c}} 2y dx + 2x dy$ for $\mathbf{c}(t) = \left(\frac{1}{9-t^3}, \sqrt{2+t}\right)$ and $1 \le t \le 2$.
 - (a) $2 \frac{\sqrt{3}}{8}$
 - (b) $2\sqrt{3} 4$
 - (c) $\sqrt{3} + \frac{1}{8}$
 - (d) $4 \frac{\sqrt{3}}{4}$

- 15. Which of the following does NOT represent a sphere? (Consider all variables defined as cylindrical, spherical, or rectangular coordinates as usual).
 - (a) $z = \pm \sqrt{1 3r^2}$
 - (b) $\Phi(\theta, \phi) = (2\sin\phi\cos\theta, 2\sin\phi\sin\theta, 2\cos\phi)$
 - (c) $x^2 + y^2 8y + z^2 + 15 = 0$
 - (d) All of the above represent spheres

- 16. The flux through the surface $z=2xy+x^2$, in the positive z direction, of the vector field ${\bf F}=-{\bf i}+y^2{\bf j}+2xy^2{\bf k}$ over the region $D:[0,4]\times[0,2]$ is
 - (a) 48
 - (b) $56\frac{1}{3}$
 - (c) $82\frac{2}{3}$
 - (d) 36

- 17. Let $\mathbf{F} = F_1 \mathbf{i} + F_2 \mathbf{j}$. Let D be a closed region in the xy plane such that $\partial D = C$. Let C be parametrized by $\mathbf{c}(t)$ for $a \leq t \leq b$. Which of the following is NOT equal to $\int_C \mathbf{F} \cdot d\mathbf{s}$?
 - (a) $\int \int_D (\nabla \times \mathbf{F}) \cdot \mathbf{k} dx dy$
 - (b) $\int_a^b F_1 dx + F_2 dy$
 - (c) $\int_C \mathbf{F} \cdot \mathbf{n} ds$
 - (d) $\int \int_D \frac{\delta F_2}{\delta x} \frac{\delta F_1}{\delta y} dx dy$

- 18. The curl of $\mathbf{F} = (3z^2x, 2xy, -6y\cos z)$ is:
 - (a) $(-6\cos z, -3z^2, 6y)$
 - (b) $(-6\cos z, 6zx, 2y)$
 - (c) $(3z^2, 2x, 6y \sin z)$
 - (d) $(-6zx, 2y, 6y\sin z)$

- 19. Find $\int \int_S (\nabla \times \mathbf{F}) \cdot d\mathbf{S}$ if S is the surface $z = x^2 + y^2$ where $z \leq 4$, oriented so that the normal points into the paraboloid, and $\mathbf{F} = -zy\mathbf{i} + zx\mathbf{j} + z^3\mathbf{k}$.
 - (a) 0
 - (b) 32π
 - (c) 64π
 - (d) -64π

- 20. Find the flux out of the solid half unit sphere above the xy plane, if ${f F}=4z^3y{f i}+2y{f j}+(z^2-2z){f k}.$
 - (a) $\frac{2\pi}{3}(\pi+2)$
 - (b) $\frac{1}{4}$
 - (c) $\frac{4}{3}\pi$
 - (d) $\frac{\pi}{2}$