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EEE 313 Spring 2014-2015

Bilkent University  
Department of Electrical and Electronics Engineering  
EEE 313 Electronic Circuit Design

Midterm 1

25 March 2015, 17:50

(4 questions, 120 minutes)

- This is a **closed book**, closed notes exam. No cheat sheet allowed.
- All cell-phones should be completely **turned off**.
- Use a calculator for numerical computations. Carry at least **4 significant digits** during calculations. Your final answer should be at least **3 significant digits**.
- Be sure to write the **units** of all numerical results.
- **Show all work clearly**.
- Please put your **final answer** for each part inside a box for easy identification. Do not give multiple answers, they will not be graded.
- Do not remove the **staple** from the exam sheets or separate pages of the exam. All extra pages must be stamped to your exam.
- You may leave the exam room when you are done. However, please do not leave during the **last five minutes** of the exam.
- At the end of the exam, please stay seated until **all** exam papers are collected.

**FET equations:**

**n-channel MOSFET**

$$i_D = K_n (v_{GS} - V_{Tn})^2 \quad \text{SAT}$$

$$i_D = K_n [2(v_{GS} - V_{Tn})v_{DS} - v_{DS}^2] \quad \text{NON-SAT}$$

**p-channel MOSFET**

$$i_D = K_p (v_{SG} + V_{Tp})^2 \quad \text{SAT}$$

$$i_D = K_p [2(v_{SG} + V_{Tp})v_{SD} - v_{SD}^2] \quad \text{NON-SAT}$$

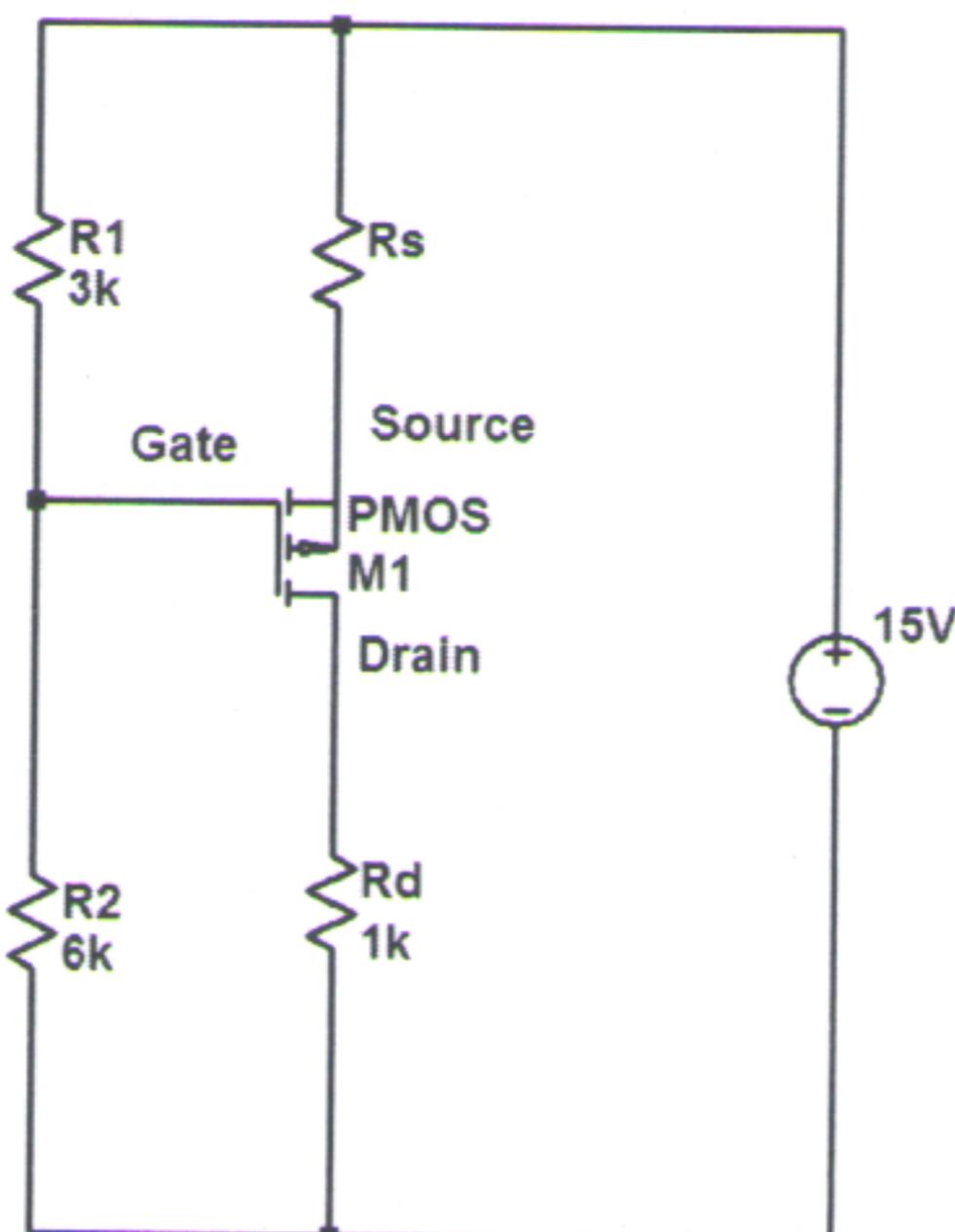
**n-channel JFET**

$$i_D = \frac{I_{DSS}}{V_p^2} (v_{GS} - V_p)^2 \quad \text{SAT}$$

$$i_D = \frac{I_{DSS}}{V_p^2} [2(v_{GS} - V_p)v_{DS} - v_{DS}^2] \quad \text{NON-SAT}$$

Please do not write below this line

1. 20 pts.	
2. 20 pts.	
3. 24 pts.	
4. 36 pts.	
Total 100 pts.	



- $V_{TP} = -2V$   ~~$V_{TP}=2V$~~  1) (20 points) At the enhancement-mode p-channel MOSFET circuit given above,

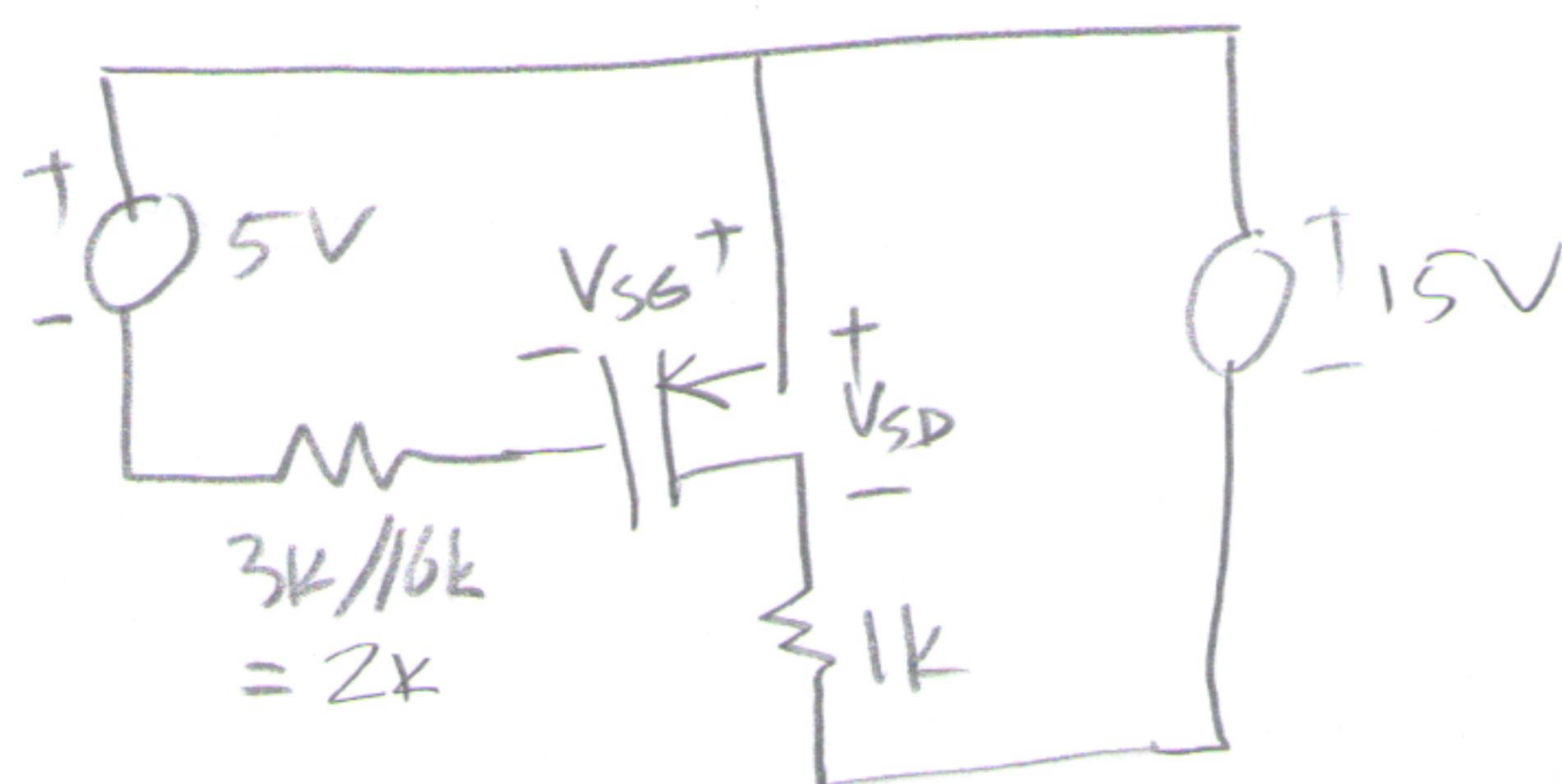
~~$V_{TP}=2V$~~  and  $K_p = 4 \times 10^{-3} \text{ A/V}^2$ .

- a) (10 points) Find the bias of the transistor for  $R_s = 0\Omega$  and verify the solution.

- b) (10 points) Find the bias of the transistor for  $R_s = 500\Omega$  and verify the solution.

Solutions

a-)



$$V_{SG} = 5V \Rightarrow I_D = K_p [V_{SG} + V_{TP}]^2 \text{ assuming SAT}$$

$$\Rightarrow I_D = 4 \times 10^{-3} [5 - 2]^2 = 4 \times 10^{-3} \times 9 = 36 \text{ mA}$$

$$V_{SD} = 15 - I_D \times 1000 \Omega = 15 - 36 = -21 \text{ V} \Rightarrow \text{not plausible}$$

$\Rightarrow$  not SAT

Assuming non-SAT =

$$I_D = K_p [2(V_{SG} + V_{TP})V_{SD} - V_{SD}^2] \text{ and}$$

$$V_{SD} = 15 - I_D \times 1000 \Rightarrow I_D = \frac{15 - V_{SD}}{1000}$$

$$\frac{15 - V_{SP}}{1000} = 4 \times 10^{-3} [2(5 - 2)V_{SD} - V_{SD}^2]$$

$$15 - V_{SD} = 4 \times 6 V_{SD} - 4 V_{SD}^2 \Rightarrow$$

$$4V_{SD}^2 - 25V_{SD} + 15 = 0$$

$$\frac{4}{9} V_{SD}^2 - \frac{25}{9} V_{SD} + \frac{15}{9} = 0$$

$$V_{SD,1,2} = \frac{-b}{2a} \pm \frac{\sqrt{b^2-4ac}}{2a} = \frac{25}{8} \pm \frac{\sqrt{625-240}}{8}$$

$$= \frac{25}{8} \pm \frac{\sqrt{385}}{8} = 3.125 \pm 2.252677$$

$= 0.672322, 5.5 \cancel{+ 2.252677} \Rightarrow \text{SAT not plausible}$

$$\Rightarrow I_D = \frac{15 - 0.672322}{1000\Omega} = 14.3277 \text{ mA but}$$

$I_D$  is also given by the transistor equation

$$I_D = K_P [2(V_{SG} - V_{TP})V_{SD} - V_{SD}^2]$$

$$= 4 \times 10^3 [2(5 - 2)0.672322 - 0.672322^2]$$

$$= 14.3276 \text{ mA } \leftarrow \text{same as above} \Rightarrow$$

Nonsat is verified



Assuming SAT:

$$I_D = K_P [V_{SG} + V_{TP}]^2 = 4 \times 10^3 [V_{SG} - 2]^2 = \frac{I_D - V_{SG}}{500} \Rightarrow$$

$$5 - V_{SG} = 2 [V_{SG} - 2]^2 = 2V_{SG}^2 - 8V_{SG} + 8 \Rightarrow$$

$$\frac{2}{9} V_{SG}^2 - \frac{7}{9} V_{SG} + \frac{3}{9} = 0 \Rightarrow$$

$$V_{SG,1,2} = \frac{7}{4} \pm \sqrt{\frac{49 - 4 \times 2 \times 3}{4}} = \frac{7}{4} \pm \frac{\sqrt{25}}{4} = \frac{7}{4} \pm \frac{5}{4} = \frac{12}{4}, \frac{2}{4} \cancel{, \frac{12}{4}}$$

$$V_{SG} = \frac{12}{4} = 3V \Rightarrow I_D = 4 \times 10^3 [3 - 1]^2 = 4 \text{ mA} \Rightarrow$$

$$V_D = 4 \times 10^3 \times 1000\Omega = 4V, V_S = 15 - 4 \times 10^3 \times 500 \cancel{<} 15 - 2 = 13V$$

$$V_{SD} = 13 - 4 = 9V > V_{SG} + (-2) = 3 - 2 = 1 \checkmark \Rightarrow \text{SAT}$$

$$V_{SG} = 5V - I_D \times 500\Omega = 5V - 4 \times 10^3 \times 500 = 5 - 2 = 3V \Rightarrow \checkmark$$

state and bias verified

Q-1 (b) An alternative solution:

$$15 = I_D (0.5 \times 10^3) + V_S \quad [I_D = 4 \times 10^{-3} (V_S - V_g + V_{TP})]$$

$$15 = 0.5 \times 10^3 \times 4 \times 10^{-3} [V_S - 10 - 2]^2$$

$$15 = 2 (V_S^2 - 24V_S + 273) = 0$$

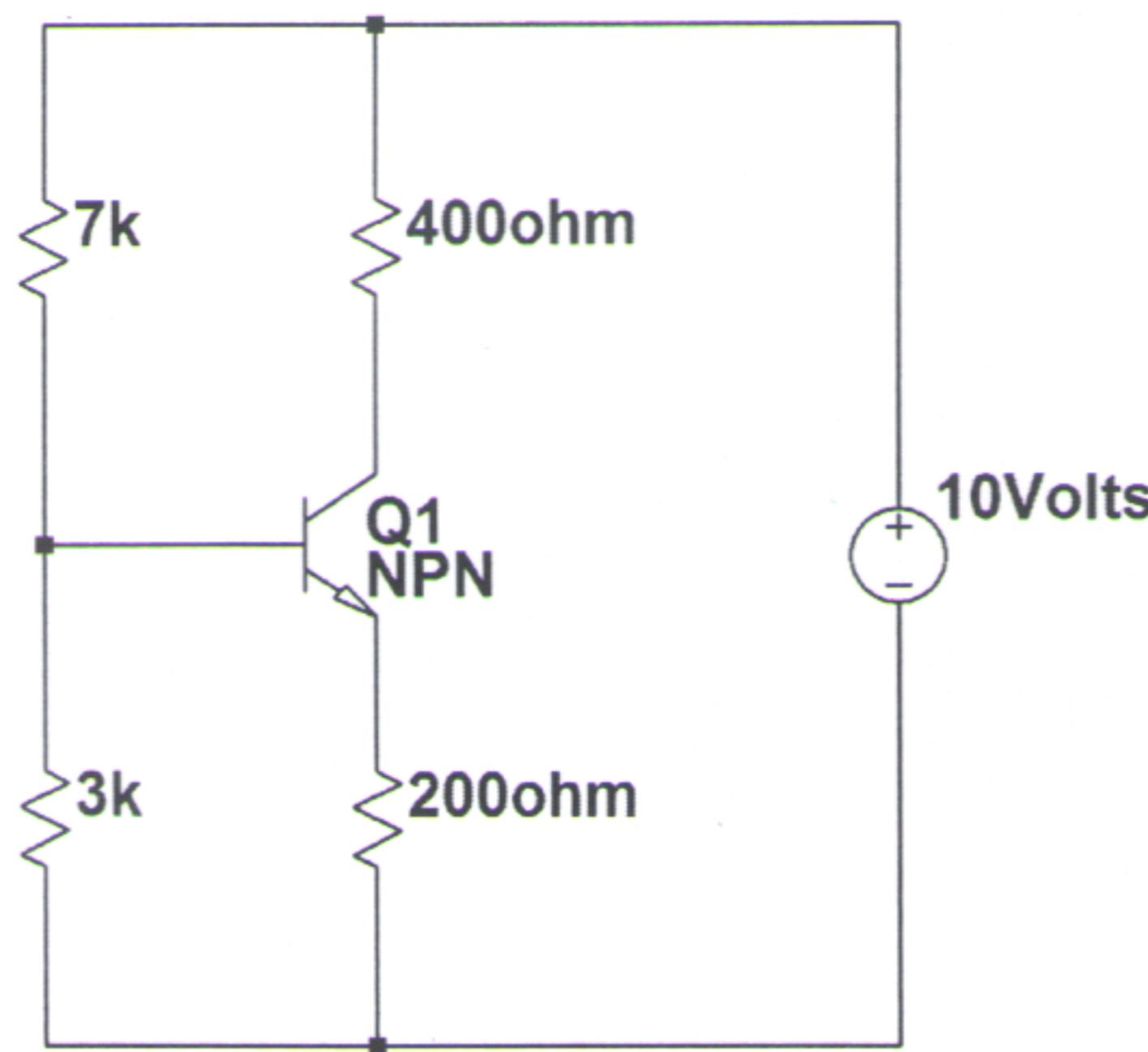
$$\begin{matrix} 2 & V_S^2 \\ a & b & c \end{matrix}$$

$$V_{S,1,2} = \frac{-b}{2a} \pm \frac{\sqrt{b^2 - 4ac}}{2a} = \frac{47}{4} \pm \frac{\sqrt{47^2 - 8 \times 273}}{4} = \frac{47}{4} \pm \frac{5}{4}$$

$$V_{S,1,2} = \frac{52}{4}, \frac{42}{4} = 13, 10.5$$

$$V_{SG} = 13 - 10, 10.5 - 10 = 3, \cancel{0.5} \rightarrow I_D = 0$$

$$\Rightarrow \boxed{V_{SG} = 3V}$$



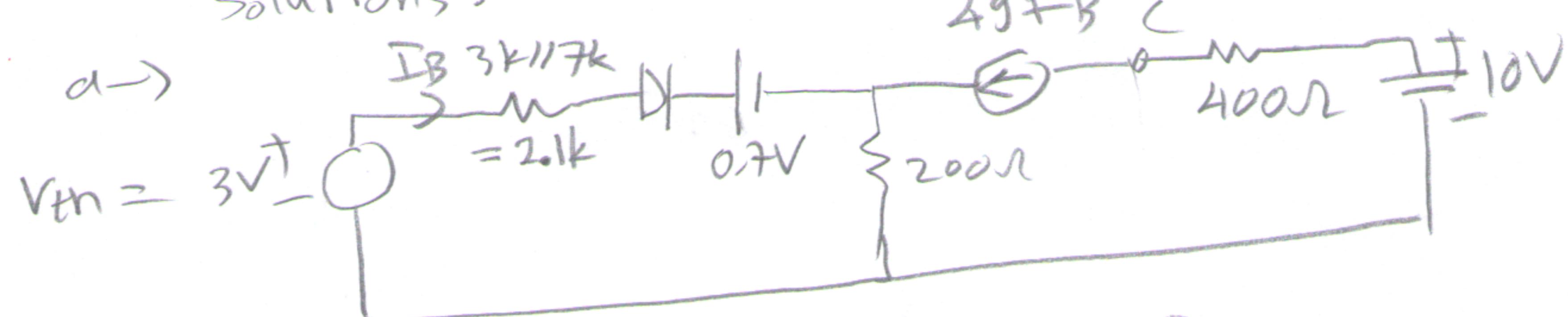
- 2) (20 points) At the circuit given above,  $\beta=49$ ,  $V_{CESAT}=0.4\text{Volts}$  and  $V_{BESAT}=0.7\text{Volts}$ .

a) (12 points) Find the quiescent values of the transistor voltage and currents.

b) (8 points) Verify the state of the transistor.

Solutions:

a →



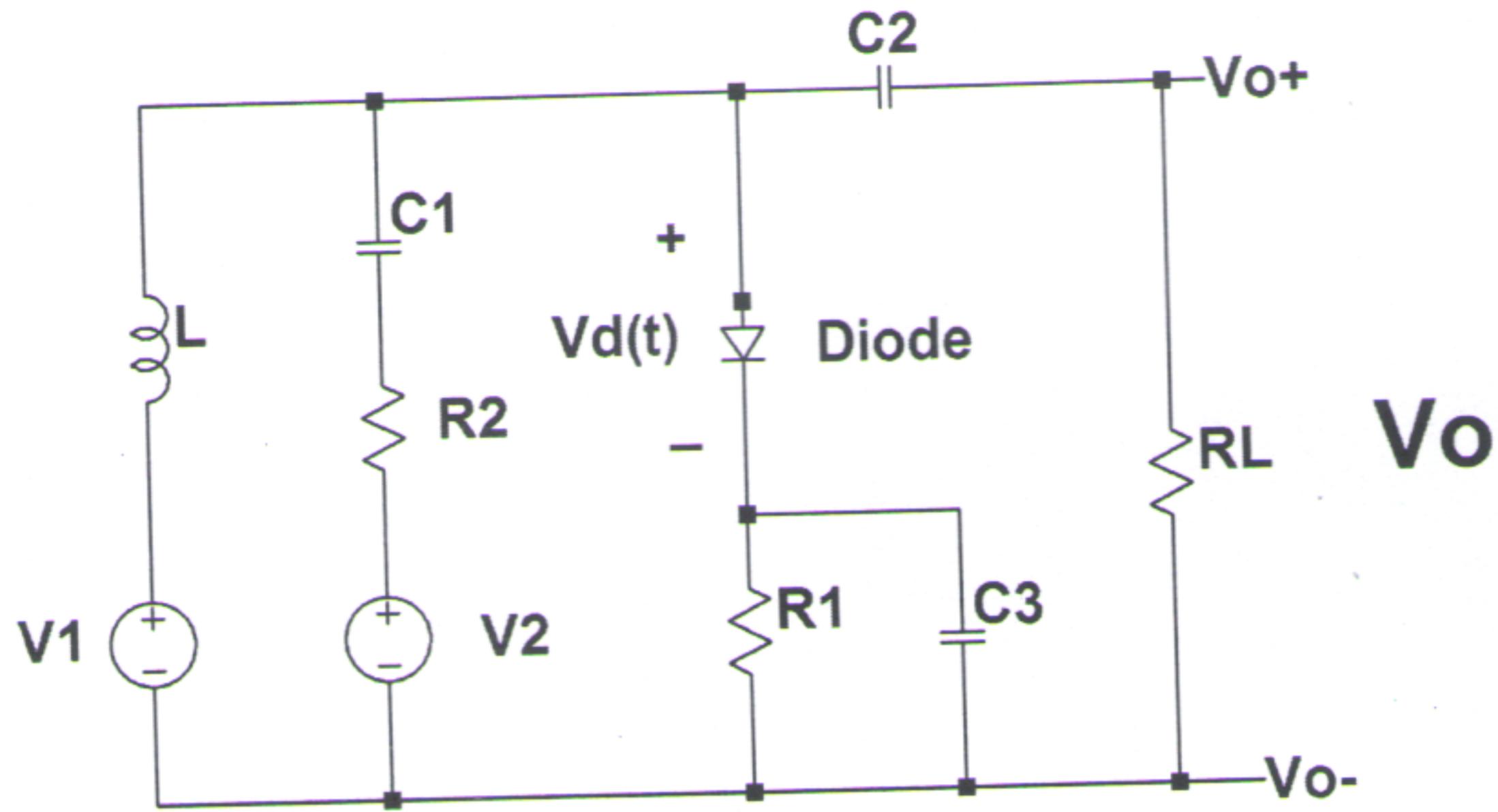
$$V_{th} = 3V = 2100I_B + 0.7V + (\beta + 1)F_B + 200 \Rightarrow$$

$$I_B = \frac{3 - 0.7}{2100 + 50 \times 200} = \frac{2.3}{12100} = 1.9008 \times 10^{-4} \text{A} = 190 \mu\text{A}$$

$$I_C = 49 \times 190 \mu\text{A} = 9.31 \text{mA} \quad I_E = 50 \times 190 \mu\text{A} = 9.5 \text{mA}$$

$$b-) V_{CE} = 10 - 9.31 \text{mA} \times 400\Omega - 9.5 \text{mA} \times 200\Omega = 10 - 3.724 - 1.9$$

$$V_{CE} = 4.376 \text{V} \Rightarrow \text{Forward Active}$$

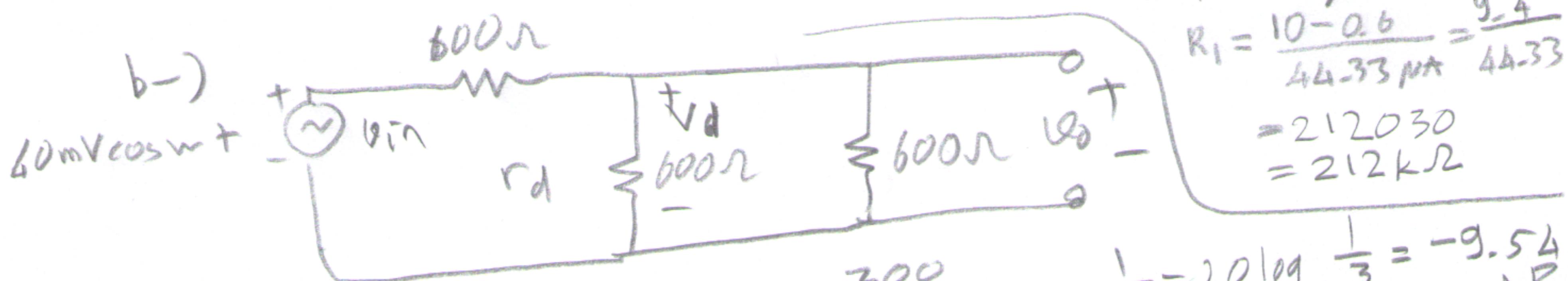


- 3) <sup>24</sup> (30 points) At the circuit given above, the diode  $V_T = 0.6$  Volts. The value of the resistor  $R_2$  is  $600\Omega$ .  $V_1 = 10$  Volts,  $RL = 600\Omega$ .  $C_1, C_2, C_3$  and  $L$  are very large.  $V_2(t)$  is equal to  $0.04\cos(\omega t)$  Volts. The diode is at room temperature and the ideality factor  $n=1$ . Answer the following:

- (6 points) Find the value of  $R_1$  to make the diode forward AC resistance equal to  $600 \Omega$ .
- (6 points) Draw the AC equivalent circuit, *for the value of  $R_1$  you have found*
- (6 points) Find the voltage gain of the circuit defined as  $\frac{V_o}{V_{in}}$  in dB's.
- (6 points) Do we expect to see an undistorted or distorted sinusoidal wave over the diode? Please state the reason behind your answer.

$$a) r_f = \frac{V_T}{I_{DQ}} = \frac{26.6 \text{ mV}}{I_{DQ}} = 600\Omega \Rightarrow I_{DQ} = \frac{26.6 \text{ mV}}{600} = 0.04433 \text{ mA}$$

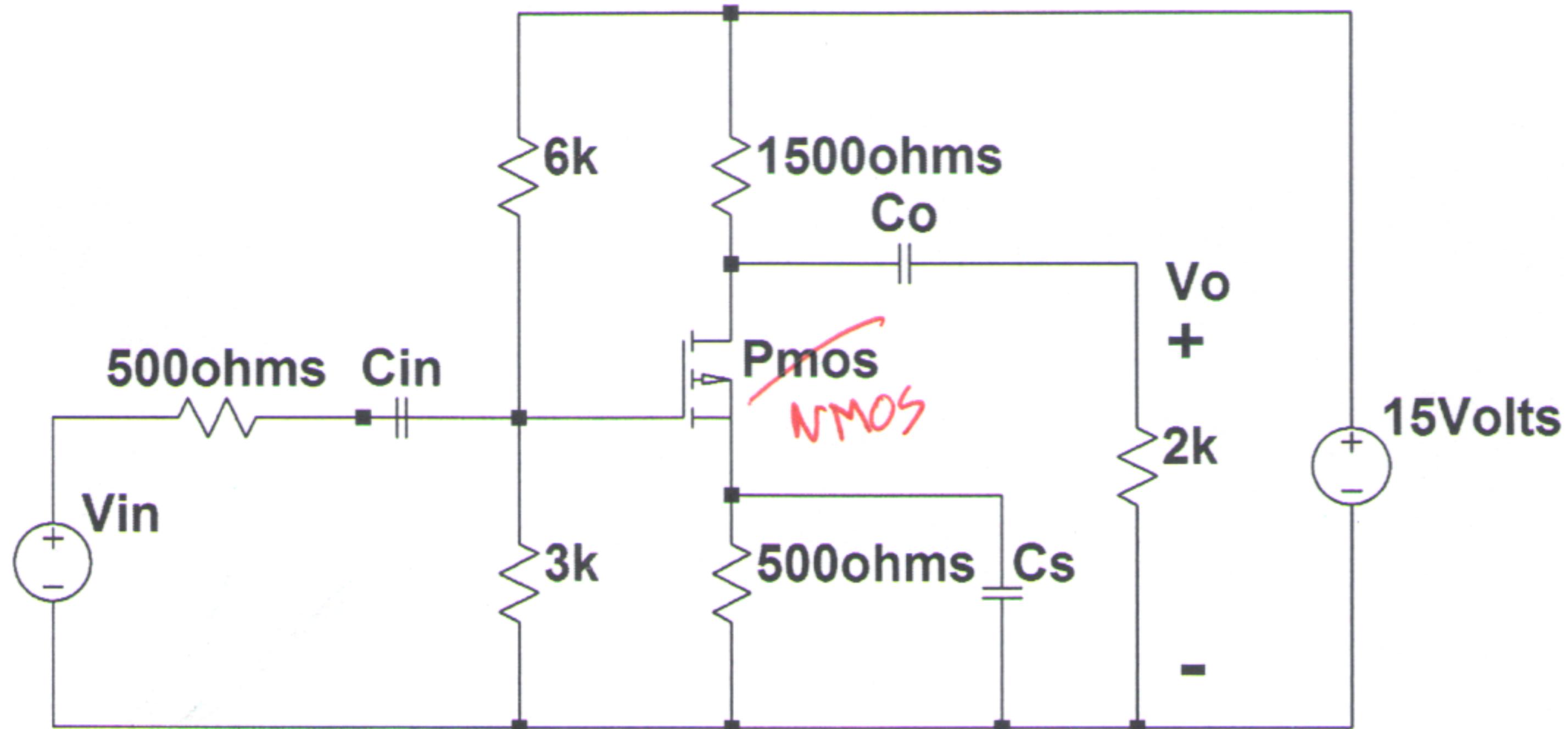
$$= 44.33 \mu\text{A} \Rightarrow R_1 = \frac{10 - 0.6}{44.33 \mu\text{A}} = \frac{9.4}{44.33} = 212030 \text{ } \Omega = 212 \text{ k}\Omega$$



$$c) \frac{V_o}{V_{in}} = \frac{600//600}{600 + 600//600} = \frac{300}{600 + 300} = \frac{1}{3} = 20 \log_{10} \frac{1}{3} = -9.54 \text{ dB}$$

$$d) V_d = \frac{V_{in}}{3} = \frac{40 \text{ mV}}{3} = 13.33 \text{ mV}_P \ll 26.6 \text{ mV}$$

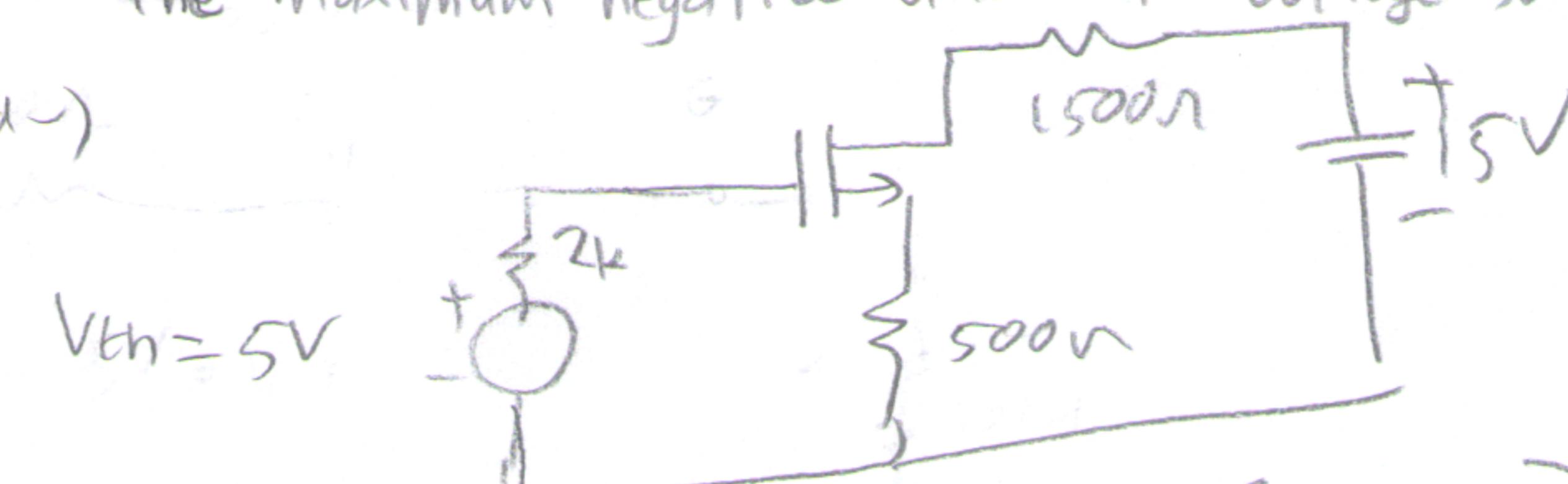
$\Rightarrow$  no distortion



4) (36 points) In the transistor amplifier circuit given above, a common-source amplifier is shown. It has the parameters; threshold voltage,  $V_{TN}=2\text{Volts}$ , transconductance parameter,  $K_n=4\text{mA/V}_2$  and Early voltage,  $V_A=100\text{V}$ .  $C_{in}$ ,  $C_o$  and  $C_s$  are very large. Be careful about the polarities of voltage sources.

- a. (6 points) Find the bias of the transistor assuming that  $V_A=\infty$ .
- b. (6 points) Draw the AC equivalent circuit assuming that  $I_D=4\text{mA}$ .
- c. (6 points) Assuming that  $I_D=4\text{mA}$ , find the small-signal gain,
- d. (6 points) Assuming that  $I_D=4\text{mA}$ , find the input resistance,
- e. (6 points) Assuming that  $I_D=4\text{mA}$ , find the undistorted maximum peak-to-peak swing.
- f. (6 points) Find the small signal voltage gain. Write the set of equations to find the maximum negative undistorted voltage swing.

(d)



$$I_D = K_n [V_{GS} - V_{TN}]^2 = 4 \times 10^{-3} [V_{GS} - 2]^2 \text{ but also}$$

$$V_{GS} = 5 - I_D \cdot 500 \Rightarrow I_D = \frac{5 - V_{GS}}{500} \Rightarrow$$

$$\frac{5 - V_{GS}}{500} = 4 \times 10^{-3} [V_{GS}^2 - 4V_{GS} + 4] \Rightarrow$$

$$5 - V_{GS} = 2[V_{GS}^2 - 4V_{GS} + 4] = 2V_{GS}^2 - 8V_{GS} + 8 \Rightarrow$$

$$2V_{GS}^2 - 7V_{GS} + 3 = 0$$

$$\Rightarrow V_{GS1,2} = \frac{-b}{2a} + \frac{\sqrt{b^2 - 4ac}}{2a} = \frac{7}{4} \pm \frac{\sqrt{49-24}}{4}$$

$$= \frac{7}{4} \pm \frac{5}{4} = \frac{12}{4}, \frac{2}{4} = 3, \cancel{V_{TN}} < V_{TN}$$

$$V_{GS} = 3V$$

$$I_D = 4 \times 10^3 [3-2]^2 = 4mA$$

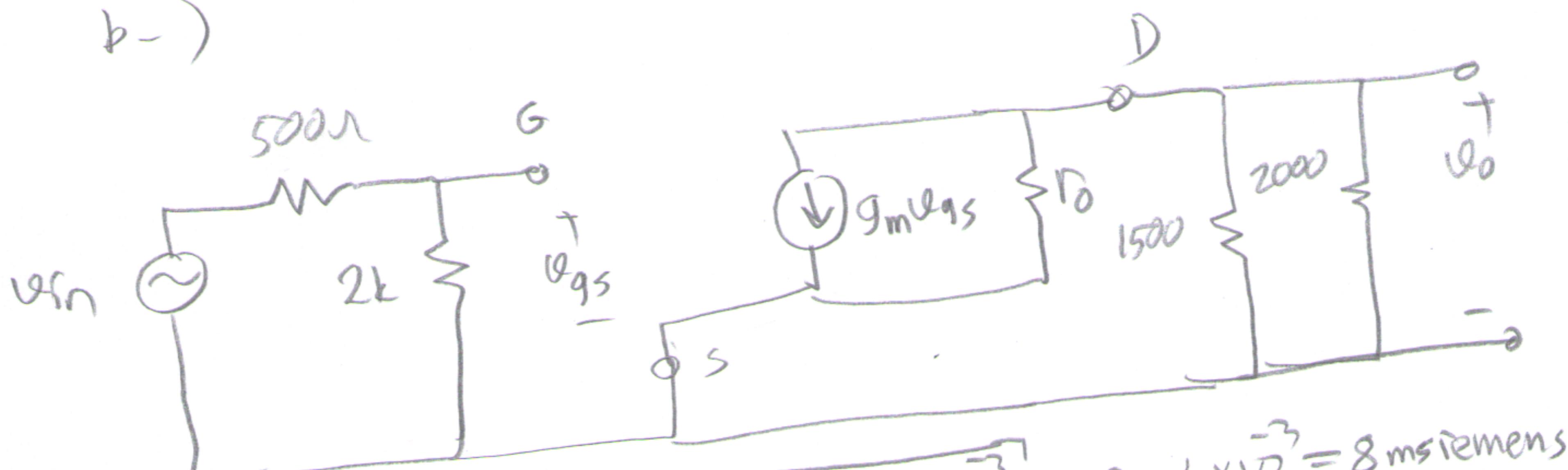
$$V_G = 4mA \times 500\Omega = 2V \Rightarrow V_{GS} = 5-2 = 3V \Rightarrow$$

$$V_G = 4mA \times 500\Omega = 2V \Rightarrow V_{GS} = 5-2 = 3V \Rightarrow$$

$$I_D = 4 \times 10^3 [3-2]^2 = 4mA \Rightarrow \checkmark \text{ SAT}$$

$$V_{DS} = 15V - 4 \times 10^3 \times 2000 = 15V - 8V = 7V \Rightarrow V_{GS} - V_{TN} = 3-2 = 1 \checkmark$$

b - )



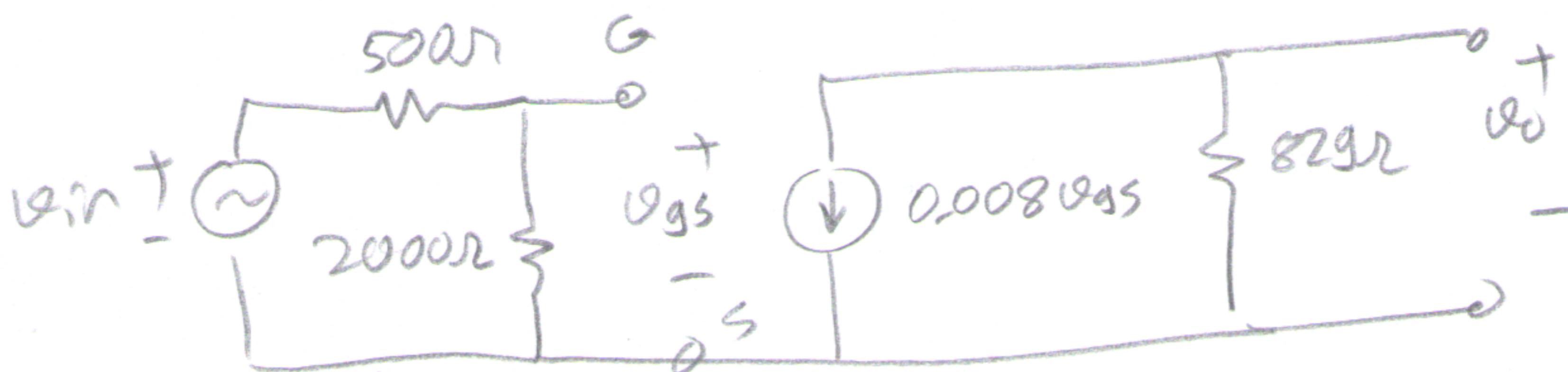
$$g_m = 2\sqrt{I_D K_n} = 2\sqrt{4 \times 10^3 \times 4 \times 10^3} = 2 \times 4 \times 10^3 = 8 \text{ msiemens}$$

$$r_o = \frac{V_A}{I_D} = \frac{100V}{4 \times 10^3 A} = 25 \times 10^3 \Omega = 25k\Omega \Rightarrow$$

The AC equivalent circuit becomes

$$R_{eq} = 25k \parallel 1.5k \parallel 2k = 25k \parallel 0.8571 = 0.8287k\Omega$$

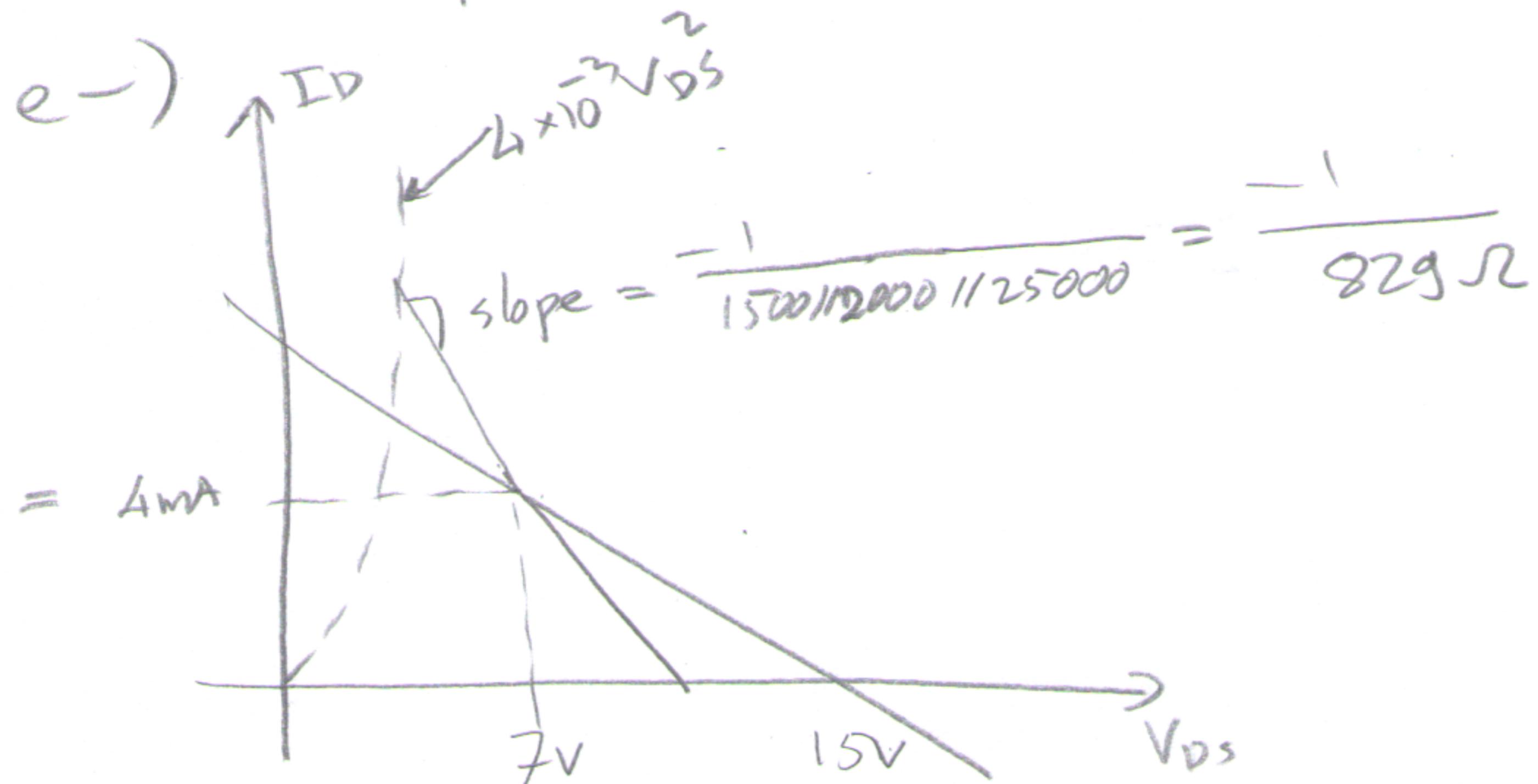
$$= 829\Omega$$



$$c-) \quad V_o = 0.008 \text{ V}_{DS} \times 829 = 829 \times 0.008 \times \frac{2000}{2500} \text{ (in } \Rightarrow)$$

$$\frac{V_o}{V_{IN}} = \frac{829 \times 0.008 \times 4}{5} = 5.3058$$

d-) The input resistance is  $2k\Omega$



$$V_+ = I_{DQ} \times R_D // R_L = 4 \text{ mA} \times 829 \Omega = 3.316 \text{ V}$$

f-) The AC load line is given by

$$\frac{\Delta I}{\Delta V} = -\frac{1}{829 \Omega} = \frac{I_D(t) - 4 \text{ mA}}{V_{DS}(t) - 7 \text{ V}}$$

$$-(V_{DS}(t) - 7) = (I_D(t) - 4 \text{ mA}) 829 \Omega \Rightarrow$$

$$829 I_D(t) - 4 \times 10^3 \times 829 = 7 - V_{DS}(t)$$

$$I_D(t) = \frac{7 + 3.316 - V_{DS}(t)}{829}$$

$$I_D(t) = \frac{10.316}{829} - \frac{1}{829} V_{DS}(t) \Rightarrow$$

$$I_D(t) = 0.012444 - \frac{1}{829} V_{DS}(t)$$

and

$$I_D(t) = K_n V_{DS}^2 = 4 \times 10^{-3} V_{DS}^2$$

IF the question (4-f) were to be solved:

$$f-) -\frac{V_{DS} - 10.316}{829} = 4 \times 10^{-3} V_{DS}^2$$

$$4 \times 10^{-3} V_{DS}^2 + 0.00121 V_{DS} - 0.01244 = 0$$

$$a=1 \quad b=0.3025 \quad c=-3.11 \quad V_{DS}^2 + \underbrace{0.3025}_{b} V_{DS} - \underbrace{-3.11}_{c} = 0$$

$$V_{DS_{1,2}} = \frac{-b}{2a} \pm \sqrt{\frac{b^2 - 4ac}{2a}} = \frac{-0.3025}{2} \pm \frac{(0.3025^2 + 4 \times 3.11)}{2}$$

$$V_{DS_{1,2}} = -\frac{0.3}{2} \pm \frac{\sqrt{2-4915}}{2} = -0.15 \pm 1.7172 \text{ V}$$

$$V_{DS_{1,2}} = -1.7172 \text{ V}$$

$$V_- = 7 - 1.7172 = 5.2828 \text{ V}$$