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EEE 313 Spring 2009

Bilkent University
Department of Electrical and Electronics Engineering
EEE 313 Electronic Circuit Design

Final Examination

21 May 2009, 15:40

(3 questions, ~~120~~ minutes) *150 minutes*

- This is a **closed book**, closed notes exam. No cheat sheet allowed.
- All cell-phones should be completely **turned off**.
- Use a calculator for numerical computations. Carry at least **3 significant digits**. Double check your numerical calculations.
- Be sure to write the **units** of all numerical results.
- **Show** all work clearly.
- Please put your **final answer** for each part inside a box for easy identification. Do not give multiple answers, they will not be graded.
- Do not remove the **staple** from the exam sheets or separate pages of the exam. All extra pages must be stamped to your exam.
- You may leave the exam room when you are done. However, please do not leave during the **last five minutes** of the exam.
- At the end of the exam, please stay seated until **all** exam papers are collected.

FET equations:

n-channel MOSFET

$$i_D = K_n (v_{GS} - V_{TN})^2 \quad \text{SAT,}$$

$$i_D = K_n [2(v_{GS} - V_{TN})v_{DS} - v_{DS}^2] \quad \text{NON-SAT}$$

p-channel MOSFET

$$i_D = K_p (v_{SG} + V_{TP})^2 \quad \text{SAT,}$$

$$i_D = K_p [2(v_{SG} + V_{TP})v_{SD} - v_{SD}^2] \quad \text{NON-SAT}$$

n-channel JFET

$$i_D = \frac{I_{DSS}}{V_p^2} (v_{GS} - V_p)^2 \quad \text{SAT,}$$

$$i_D = \frac{I_{DSS}}{V_p^2} [2(v_{GS} - V_p)v_{DS} - v_{DS}^2] \quad \text{NON-SAT}$$

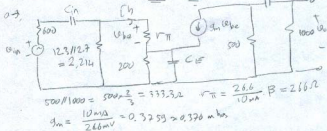
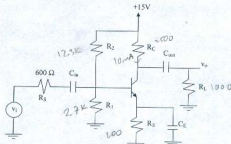
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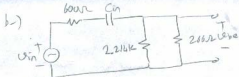
1. 40 pts.	
2. 30 pts.	
3. 30 pts.	
Total 100 pts.	

L (40 points) For the circuit shown below, assume

$I_{CQ} = 10 \text{ mA}$, $R_C = 500 \Omega$, $R_2 = 1 \text{ k}\Omega$, $R_E = 200 \Omega$, $R_1 = 2.7 \text{ k}\Omega$ and $R_2 = 12.3 \text{ k}\Omega$.

- a) (15 points) Find the gain of the amplifier assuming C_{in} , C_{out} and C_E are infinite.
 b) (10 points) Assuming C_{out} and C_E are very large, find C_{in} that makes the lower corner frequency 300 Hz .
 c) (15 points) Find the output peak-to-peak undistorted swing by finding out your own DC solution.





$$\frac{2.2k \times 200}{2.2k + 200} = R_{eq}$$

$$= 237.5 \Omega$$

$$\frac{u_{oe}}{u_{in}} = \frac{237.5 \Omega}{237.5 \Omega + 600 \Omega + \frac{1}{j\omega C_{in}}}$$

$$= \frac{j\omega 237.5 C_{in}}{1 + (237.5 + 600)j\omega C_{in}}$$

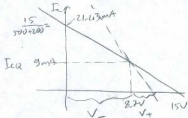
$$\omega_0 = 2\pi \times 300 \text{ Hz} = \frac{1}{837.5 C_{in}} \Rightarrow C_{in} = \frac{1}{2\pi \times 300 \times 837.5} = 0.633 \mu\text{F}$$

c-)



$$I_E = \frac{2.7V - 0.7V}{2.2k + 100 \times 200} = 89.23 \mu\text{A}$$

$$I_C = 89.23 \text{ mA}, I_E = 9 \text{ mA}$$



$$I_{CQ} = 15 - 9 \times 10^{-3} \times (200 \Omega)$$

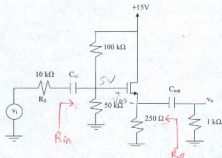
$$\frac{V_+}{I_{CQ}} = R_{th} / R_L = 333.3 \Omega$$

$$V_+ = 333.3 \times 9 \text{ mA} = 3 \text{ V}$$

$$V_{pp} = 2 \times 3 \text{ V} = 6 \text{ V}$$

2. (30 points) For the circuit shown below, $V_{TN} = 1V$ and $K_M = 2 \text{ mA/V}^2$

- (15 points) Find the gain of the amplifier defined as $\frac{v_o}{v_i}$ assuming C_{Ost} and C_{in} are very large.
- (5 points) Find the input impedance.
- (10 points) Find the output impedance.



a-)
$$I_D = 2 \times 10^{-3} (V_{GS} - 1)^2 = \frac{5 - V_{GS}}{250} = \frac{5 - V_{GS}}{0.25 \times 10^3}$$

$$5 - V_{GS} = 0.5 (V_{GS}^2 - 2V_{GS} + 1)$$

$$\frac{5}{0.5} - \frac{V_{GS}}{0.5} = V_{GS}^2 - 2V_{GS} + 1$$

$$10 - 2V_{GS} = V_{GS}^2 - 2V_{GS} + 1$$

$$V_{GS}^2 - 9 = 0 \quad V_{GS}^2 = 9 \Rightarrow V_{GS} = \pm 3V$$

$V_{GS} = -3V$ means cut-off $\Rightarrow V_{GS} = 3V$

$$I_D = 2 \times 10^{-3} (3 - 1)^2 = 2 \times 10^{-3} \times 4 = 8 \text{ mA} \Rightarrow$$

$$V_S = 8 \text{ mA} \times 250 \Omega = 2V$$

$$g_m = 2 \sqrt{I_D K_M} = 2 \sqrt{8 \times 10^{-3} \times 2 \times 10^{-3}} = 2 \times 4 \times 10^{-3} = 8 \times 10^{-3} \text{ mhos}$$

$$\frac{1}{r_m} = \frac{1}{g_m} = \frac{10^3}{8} = 125 \Omega$$

2 continued

$$\begin{aligned}\frac{V_o}{V_{in}} &= \frac{100k // 50k}{100k // 50k + 10k} \cdot \frac{250 // 11000\Omega}{250 // 11000 + \frac{1}{g_m}} \\ &= \frac{33.33k}{43.33k} \cdot \frac{200\Omega}{200\Omega + 125\Omega} \\ &= 0.473\end{aligned}$$

$$b) R_{in} = 100k // 50k = 33.33k$$

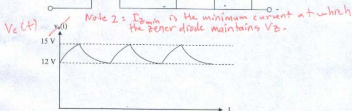
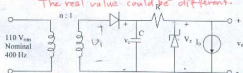
$$c-) R_o = \frac{1}{g_m} // 250\Omega = 125\Omega // 250\Omega$$

$$R_o = 83.33\Omega$$

3. (30 points) For the circuit shown below, the output voltage waveform is as shown in the figure. $V_F = V_{0.9V} = 1.5 \text{ V}$ and $V_Z = 10 \text{ V}$ and $I_{Z\min} = 20 \text{ mA}$

- (10 points) Find the value of "n" if the input voltage is $118 \text{ V}_{\text{rms}}$.
- (20 points) Design the output voltage regulator by choosing R and C values in order to sustain a DC output current equal to 200 mA . (Please find the maximum value of R and the minimum value of C, 10 points each).

Notes: 1/Nominal means the designated value.
The real value could be different.



$$a-) V_{o\min} = 12 \text{ V} = V_{i\text{peak}} - V_F = V_{i\text{peak}} - 1.5 = 15 \text{ V}$$

$$\frac{118\sqrt{2}}{n} = V_{i\text{p}} = 16.5 \text{ V} \Rightarrow$$

$$n = \frac{118\sqrt{2}}{16.5} = 10.08$$

b-) Let us first find R_{max} and $I_{Z\text{average}}$

$$R_{\text{max}} = \frac{12 \text{ V} - V_Z}{I_o + I_{Z\min}} = \frac{12 - 10}{0.2 + 0.02} = \frac{2}{0.22} = 9.09 \Omega \approx 9.1 \Omega$$

$$I_{R\text{max}} = \frac{15 \text{ V} - 10 \text{ V}}{9.1 \Omega} \quad I_{R\min} = \frac{12 \text{ V} - 10 \text{ V}}{9.1 \Omega}$$

$$I_{\text{av}} = \frac{5 + 2}{2} \cdot \frac{1}{9.1} = \frac{7.5}{9.1} = 0.824 \text{ mA} \rightarrow$$

3. continued

$$I\Delta t = C\Delta V \Rightarrow C = \frac{I\Delta t}{\Delta V}$$

$$C = \frac{0.274 \times 2.5 \times 10^{-3}}{3V} = 2.283 \times 10^{-5} F = 230 \mu F$$