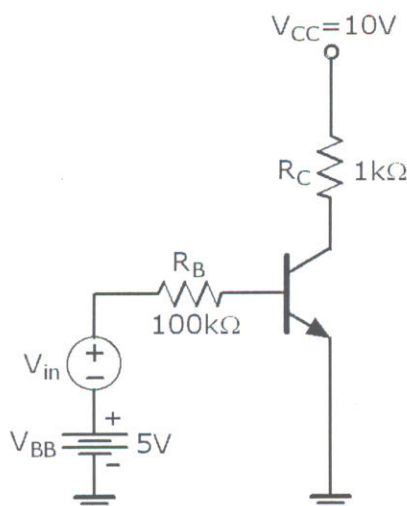


1. (18 points) For the following circuit, let $\beta = 120$, $V_{BE(on)} = 0.7V$ and $V_{CE(sat)} = 0.3V$.

- 8pts a. Assume that $V_{in} = 0V$. Determine the Q-point (dc operating point) values, I_{CQ} and V_{CEQ} . Draw the dc load line and the Q-point.
 4pts b. Find the peak value of V_{in} that drives the transistor into SATURATION.
 4pts c. Find the peak value of V_{in} that drives the transistor into CUTOFF.
 2pts d. Find the maximum peak value of V_{in} for linear operation (i.e. the transistor operates in the forward-active mode).



SOLUTION:

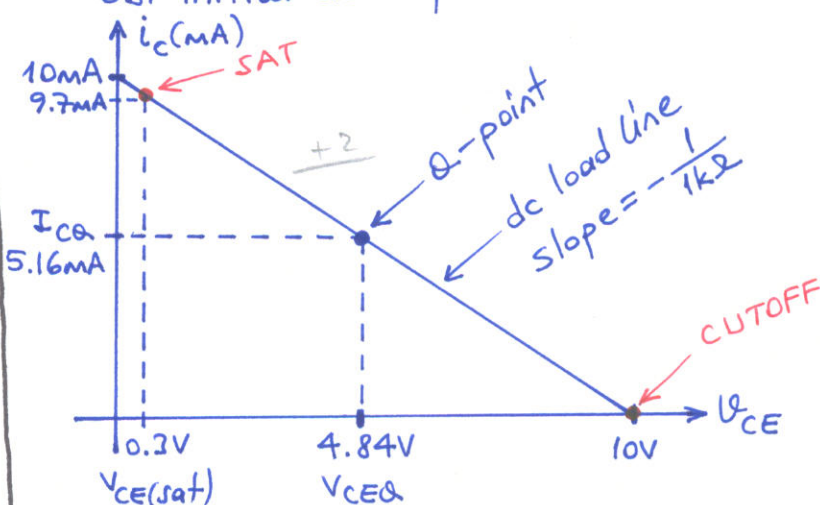
(a) Assume that the transistor is in the forward-active mode.

$$I_{BQ} = \frac{V_{BB} + V_{in} - V_{BE(on)}}{R_B} = \frac{5 - 0.7}{100k\Omega} = 43\mu A$$

$$I_{CQ} = \beta I_{BQ} = 5.16mA$$

$$V_{CEQ} = V_{CC} - I_{CQ} R_C = 4.84V$$

Our initial assumption is correct.



(b) At the edge of SAT and ACT regions:

$$V_{CE} = V_{CE(sat)} = 0.3V$$

$$I_{C(sat)} = \frac{V_{CC} - V_{CE(sat)}}{R_C} = 9.7mA$$

$$I_B = \frac{I_C}{\beta} = 80.8333\mu A$$

$$V_{BB} + V_{in} - I_B R_B - V_{BE(on)} = 0$$

$$V_{in} = I_B R_B + V_{BE(on)} - V_{BB} = 8.0833 + 0.7 - 5 = 3.7833V$$

For large ac input signal
 $V_p = 3.7833V$

(c) In the cutoff mode: $I_B = I_C = I_E = 0A$.

$$V_{in} = V_{BE(on)} - V_{BB} = 0.7 - 5 = -4.3V$$

For large ac input signal
 $V_p = 4.3V$

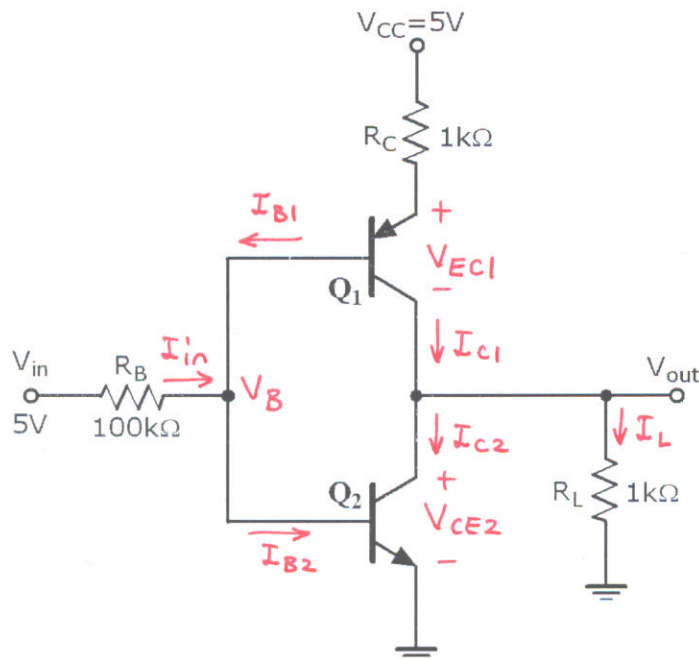
(d) For linear operation of the amplifier, the transistor must operate in the forward-active mode. If the transistor is driven into either SAT or CUTOFF regions, the output voltage will be distorted.

Therefore, the maximum peak value of V_{in} for a linear operation is

$$V_{in} = 3.7833V \text{ For low frequency large ac signal.}$$

In DC mode: $-4.3 < V_{in} < 3.7833V$

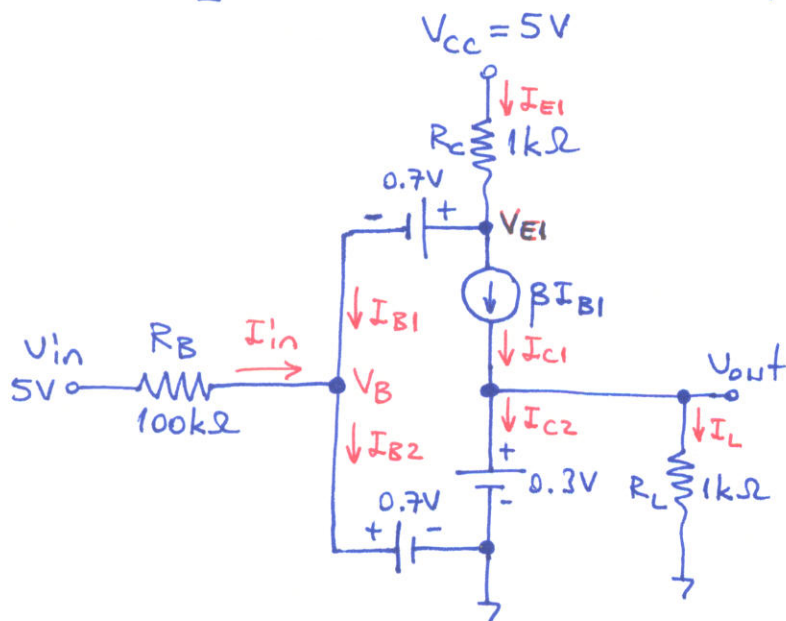
2. (20 points) For the following circuit, find the states of the transistors and the Q-point values (I_{C1} , V_{EC1} , I_{C2} and V_{CE2}). Let $\beta = 100$, $V_{BE(on)} = V_{EB(on)} = 0.7V$ and $V_{CE(sat)} = V_{EC(sat)} = 0.3V$.



SOLUTION:

If both transistors are assumed to be OFF, all currents are zero and $V_B = 5V$. This voltage forces Q_2 to be ON. If we assume that Q_2 is ON, then $V_B = 0.7V$ and this voltage forces Q_1 to be ON. Therefore, both transistors must be ON. Let's assume that both Q_1 and Q_2 are in the ACT mode. Then $I_{C2} > I_{C1}$ since $I_{B2} > I_{B1}$. This results in a negative load current ($I_L < 0$) and a negative output voltage ($V_{out} < 0$).

This means that V_{CE2} becomes negative and it is an inconsistency. Because, V_{CE} cannot be negative in the forward-active mode. So our assumption is wrong. Now, let's assume that Q_1 is in ACT mode and Q_2 is in SAT mode. Then, the equivalent circuit will be as follows.



Note that $V_B = 0.7V$, $V_{E1} = 1.4V$

$$I_{E1} = \frac{V_{CC} - V_{E1}}{R_C} = \frac{5 - 1.4}{1k\Omega} = 3.6 \text{ mA}$$

$$I_{B1} = \frac{I_{E1}}{\beta + 1} = 35.6436 \mu\text{A}$$

$$I_{C1} = \alpha I_{E1} = 3.5644 \text{ mA}$$

$$V_o = V_{C1} = V_{C2} = 0.3V$$

$$V_{EC1} = V_{E1} - V_{C1} = 1.4 - 0.3 = 1.1V$$

$$I_{B2} = I_{in} + I_{B1} = \frac{V_{in} - V_B}{R_B} + I_{B1}$$

$$I_{B2} = \frac{5 - 0.7}{100k\Omega} + 35.6436 \mu\text{A}$$

$$I_{B2} = 78.6436 \mu\text{A}$$

$$I_L = \frac{V_{out}}{R_L} = \frac{0.3V}{1k\Omega} = 0.3 \text{ mA}$$

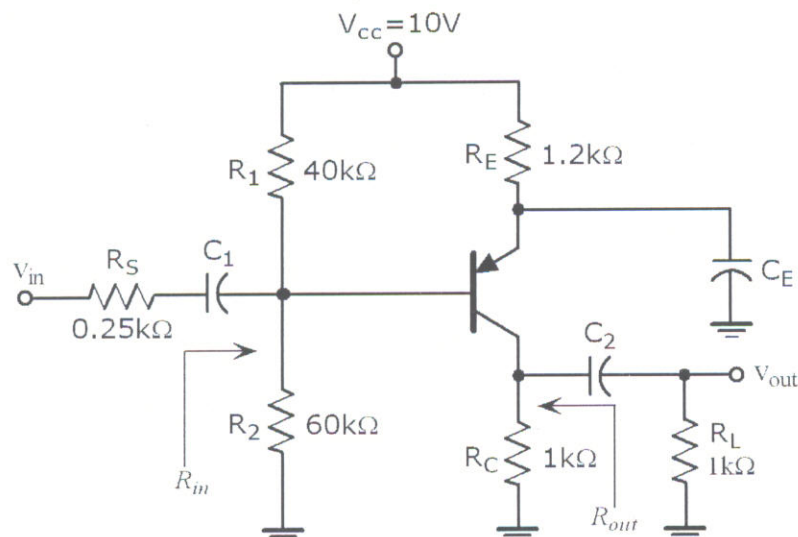
$$I_{C2} = I_{C1} - I_L = 3.5644 - 0.3 = 3.2644 \text{ mA}$$

$$\beta_{\text{forced}} = \frac{I_{C2}}{I_{B2}} = 41.5 \quad \text{and} \quad V_{CE2} = 0.3V$$

our assumption is correct.

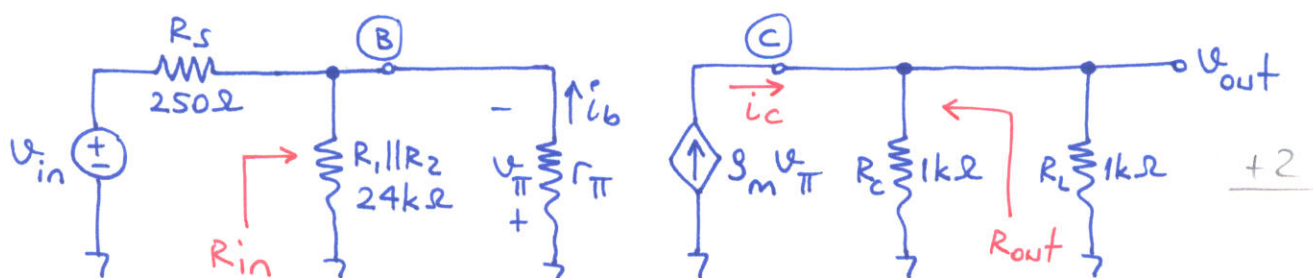
3. (20 points) For the following BJT amplifier circuit, let $\beta = 200$ and $V_{EB(on)} = 0.7V$, and the transistor is biased at $I_{CQ} = 2.4887 \text{ mA}$. Assume that the capacitors are very large.

- (6 points) Draw the small-signal ac equivalent circuit and calculate the small-signal transistor parameters, r_π and g_m .
- (6 points) Determine the input resistance (R_{in}) and the output resistance (R_{out}).
- (8 points) Determine the voltage gain, $A_v = V_{out} / V_{in}$



SOLUTION:

(a) $r_\pi = \frac{\beta V_T}{I_{CQ}} = 2.0894 \text{ k}\Omega$ and $g_m = \frac{I_{CQ}}{V_T} = 95.7192 \text{ mA/V}$



(b) $R_{in} = R_1 \parallel R_2 \parallel r_\pi = 1.9221 \text{ k}\Omega$

To find R_{out} , we set $V_{in} = 0$. Then $V_\pi = 0$ and $i_b = i_c = 0$.

Therefore, $R_{out} = R_C = 1 \text{ k}\Omega$

(c) $V_{out} = g_m V_\pi (R_C \parallel R_L)$ and $V_\pi = \frac{-R_{in}}{R_s + R_{in}} V_{in}$

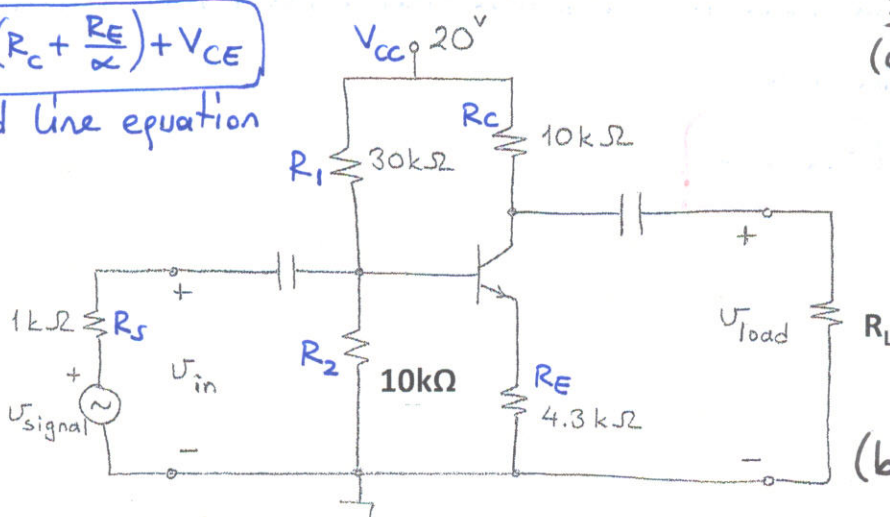
$A_v = \frac{V_{out}}{V_{in}} = -g_m (R_C \parallel R_L) \left(\frac{R_{in}}{R_s + R_{in}} \right) = -42.35$

4. (30 points) For the following BJT amplifier circuit, let $\beta = 100$, and $V_{BE(on)} = 1.0V$, and $V_{CE(sat)} = 0.2V$. Assume that the capacitors are very large.

- (4 points) Find the DC base current.
- (6 points) Draw the small-signal ac equivalent circuit and calculate the small-signal transistor parameters, r_π and g_m .
- (12 points) Find the value of R_L to obtain the maximum possible undistorted symmetric voltage swing across the load resistor (v_{load}). What is the value of the peak-to-peak swing?
- (8 points) Assume $R_L = 30k\Omega$. What is the value of the peak-to-peak undistorted symmetric Collector-Emitter voltage swing (v_{ce}).

$$V_{CC} = I_C(R_C + \frac{R_E}{\alpha}) + V_{CE}$$

dc load line equation



SOLUTION:

$$(a) V_{TH} = \frac{R_2}{R_1 + R_2} V_{CC} = 5V$$

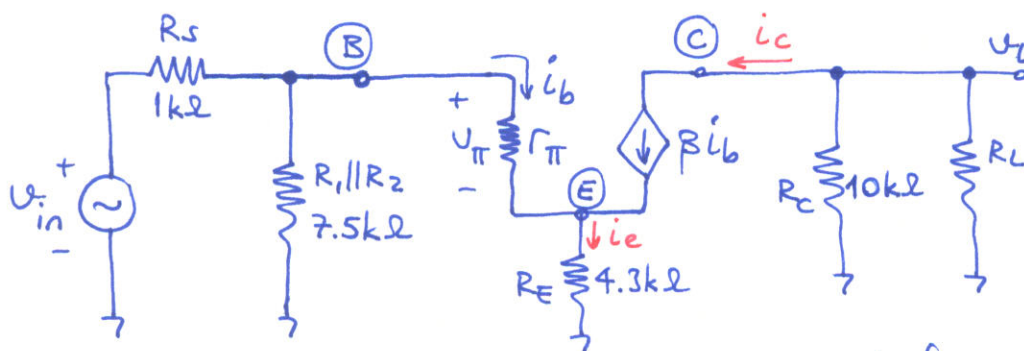
$$R_{TH} = R_1 || R_2 = 7.5k\Omega$$

$$I_{BA} = \frac{V_{TH} - V_{BE(on)}}{R_{TH} + (\beta + 1)R_E}$$

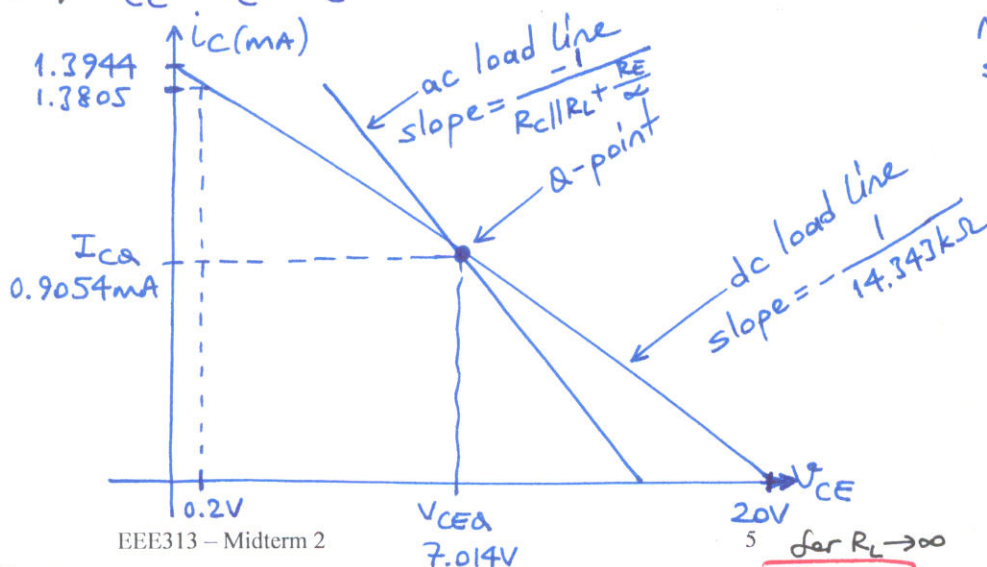
$$I_{BA} = 9.0539\mu A$$

$$(b) r_\pi = \frac{V_T}{I_{BA}} = 2.8717k\Omega$$

$$g_m = \frac{I_{CQ}}{V_T} = 34.8227 \frac{mA}{V}$$



$$(c) v_{ce} = v_c - v_e = -i_c(R_C || R_L) - i_e R_E = -i_c \left[R_C || R_L + \frac{R_E}{\alpha} \right] : \text{ac load line}$$



Max. possible undistorted symmetric v_{ce} swing is

$$V_{CEQ} - V_{CE(sat)} = 6.814V$$

Peak value of collector current (i_c) swing is $0.9054mA$

$$\text{Then } R_C || R_L + \frac{R_E}{\alpha} = 7.526k\Omega$$

$$\text{Thus } V_{pp} = 5.7638V$$

$$R_L = 4.669k\Omega \text{ For } v_{load}$$

Max. undistorted symmetric swing across the load is obtained when $R_L = \infty$

$$\text{For } v_{load} : V_{pp} = 2(1.3805 - 0.9054)(10) = 9.502V$$

(d) For $R_L = 30k\Omega$, the slope of ac load line is

$$-\frac{1}{R_C \parallel R_L + \frac{R_E}{\alpha}} = \frac{-1}{11.843k\Omega}$$

Positive peak of ac collector-emitter voltage can be at most

$$(R_C \parallel R_L + \frac{R_E}{\alpha}) I_{CQ} = 10.7222V$$

Negative peak of v_{ce} can be at most

$$V_{CEQ} - V_{CE(sat)} = 6.814V.$$

Therefore, max. possible undistorted symmetric voltage swing

is $V_p = 6.814V$

$$V_{pp} = 13.628V$$

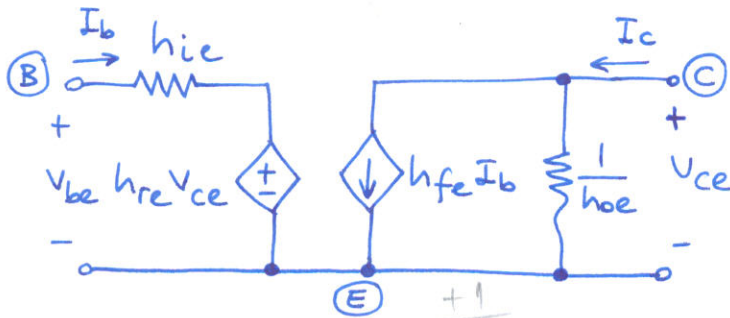


5. (12 points) For two-port network representation of a single n-p-n Bipolar Junction Transistor (BJT), express the following h-parameters in terms of the small-signal hybrid- π model parameters (include r_π , g_m and r_o only) of the transistor. Explain your work.

a. (6 points) h_{fe}

b. (6 points) h_{oe}

SOLUTION:



h-parameter model of BJT

$$V_{be} = h_{ie}I_b + h_{re}V_{ce} \quad +2$$

$$I_c = h_{fe}I_b + h_{oe}V_{ce}$$

(a) $h_{fe} = \left. \frac{I_c}{I_b} \right|_{V_{ce}=0} \quad +2$

Now, set $V_{ce}=0$ in the hybrid- π model.

$$I_c = g_m V_\pi \text{ where } V_\pi = I_b r_\pi$$

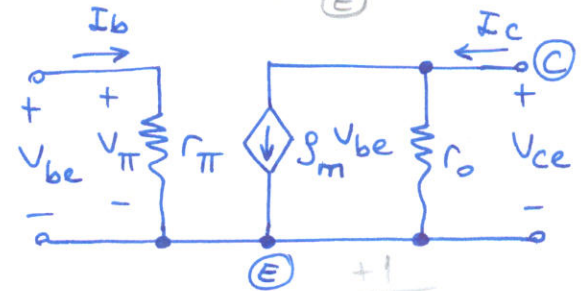
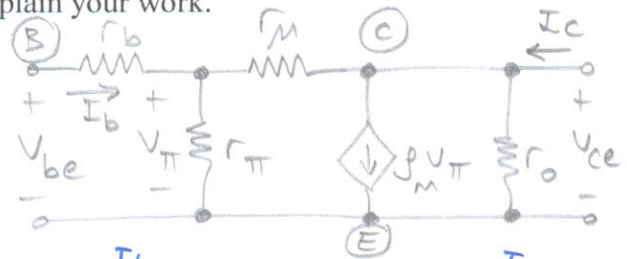
Therefore, $h_{fe} = g_m r_\pi = \beta \quad +2$

(b) $h_{oe} = \left. \frac{I_c}{V_{ce}} \right|_{I_b=0} \quad +2$

Now, set $I_b=0$ in the hybrid- π model.

$$V_\pi = 0 \text{ and } g_m V_\pi = 0.$$

Therefore, $h_{oe} = \frac{1}{r_o} \quad +2$



Hybrid- π model of BJT

$$h_{fe} = \frac{\beta r_\pi - r_\pi}{r_\pi + r_\pi} = \beta - (\beta + 1) \frac{r_\pi}{r_\pi + r_\pi}$$

$$h_{oe} = \frac{1}{r_o} + \frac{\beta + 1}{r_\pi + r_\pi}$$