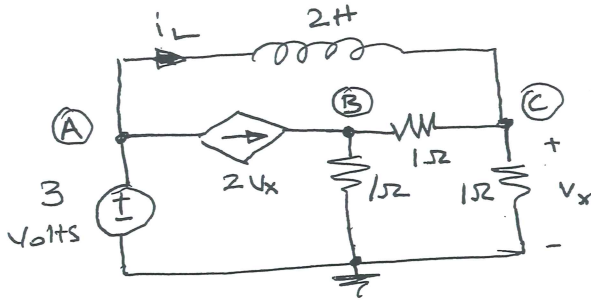


EEE 202 CIRCUIT THEORY
Second Midterm, Spring 2013-14

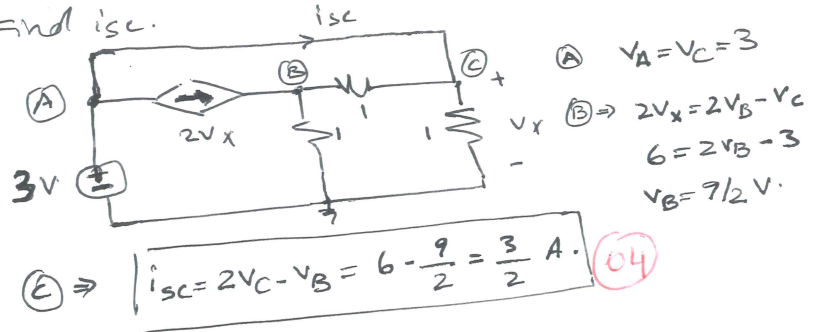
No credits will be given for unjustified answers. Good luck.

Prob. 1 : (30 pt.s)

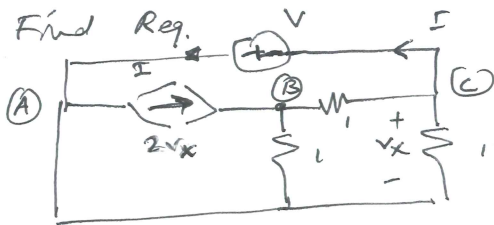
i : Consider the following circuit. Let $i_L(0) = 1$ Amps. Find $i_L(t)$ and $v_x(t)$.



Find i_{sc} .



Find R_{eq} .



$V_A = 0 \quad V_C = -V = V_x$
 $\textcircled{B} \Rightarrow 2V_x = 2V_B - V_C \Rightarrow -3V = 2V_B \Rightarrow V_B = -\frac{3}{2}V$
 $\textcircled{C} \Rightarrow I + V_C - V_B = 0 \Rightarrow I - 2V + \frac{3}{2}V = 0 \Rightarrow I = \frac{1}{2}V$
 $R_{eq} = \frac{V}{I} = 2\Omega$

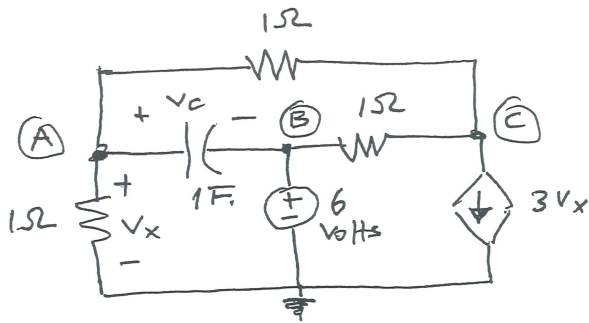
$\Rightarrow \tau = \frac{L_{eq}}{R_{eq}} = 1 \text{ sec.}$

$\Rightarrow i_L(t) - \frac{3}{2} = \left[1 - \frac{3}{2}\right] e^{-t}$

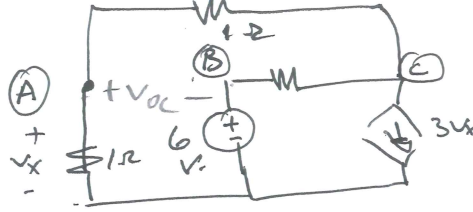
$\Rightarrow i_L(t) = \frac{3}{2} - \frac{1}{2} e^{-t} \text{ Amp.}$

$\Rightarrow v_L = L \frac{di_L}{dt} = 2 \cdot \left(-\frac{1}{2} \cdot (-1)\right) e^{-t} = e^{-t} \text{ V.}$
 $\Rightarrow v_x = v_L + V_x \Rightarrow v_x = 3 - v_L = 3 - e^{-t} \text{ V.}$

ii : Consider the following circuit. Let $v_C(0) = 1$ Volts. Find $v_C(t)$ and $v_x(t)$.



Find v_{OC}



$$\textcircled{A} \Rightarrow v_A = \frac{v_C}{2}$$

$$\textcircled{B} \Rightarrow v_B = 6$$

$$\textcircled{C} \Rightarrow 3v_A + \frac{v_C}{2} + (v_C - 6) = 0$$

$$\frac{3}{2}v_C + \frac{v_C}{2} + v_C - 6 = 0$$

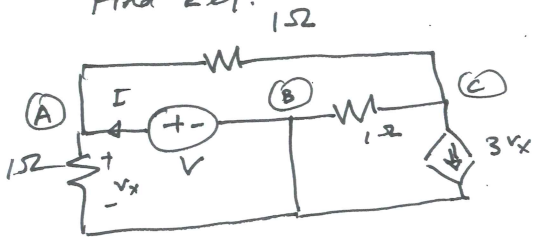
$$\boxed{v_C = 2V}$$

$$\Rightarrow v_A = 1V = \frac{v_C}{2}$$

$$\Rightarrow \boxed{v_{OC} = v_A - 6 = -5V.}$$

(04)

Find R_{eq} .



$$v_B = 0, v_A = v, \textcircled{C} \quad v_x = v_A$$

$$v_C + 3v_A + (v_C - v_A) = 0$$

$$\boxed{v_C = -v_A = -V}$$

(04)

$$\textcircled{A} \quad (v_C - v_A) + I = v_A$$

$$\Rightarrow -V - V + I = V \Rightarrow I = 3V$$

$$I = 3V \Rightarrow \boxed{R_{eq} = \frac{V}{I} = \frac{1}{3}\Omega}$$

$$\Rightarrow \tau = R_{eq}C = \frac{1}{3} \text{ sec}$$

$$\Rightarrow v_C(t) + 5 = [1 + 5] e^{-3t}$$

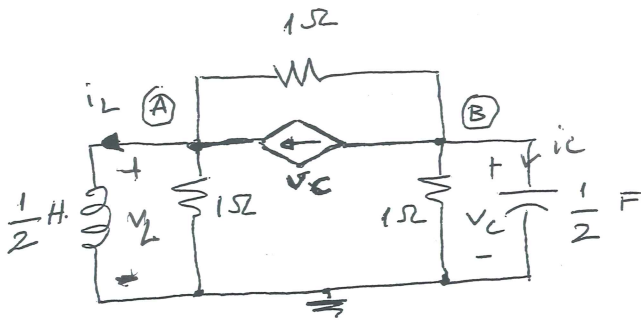
$$\Rightarrow \boxed{v_C(t) = -5 + 6e^{-3t} \text{ Volts.}}$$

(04)

$$v_x = v_C + 6 \Rightarrow \boxed{v_x = 1 + 6e^{-3t} \text{ Volts.}}$$

(03)

Prob. 2 : (20 pt.s) Consider the following circuit. Let $v_C(0) = 1$ Volts and $i_L(0) = 1$ Amps. Find $v_C(t)$.



$$\begin{aligned} & \boxed{v_B = v_C} \quad \boxed{v_A = v_L} \\ & \text{(B)} \quad i_C + v_C + v_C + v_C - v_A = 0 \Rightarrow \boxed{i_C + 3v_C - v_A = 0} \\ & \text{(A)} \quad i_L + v_A + v_A - v_B - v_B = 0 \Rightarrow \boxed{i_L + 2v_L - 2v_C = 0} \\ & \Rightarrow \boxed{v_L = v_C - \frac{1}{2}i_L} \Rightarrow \boxed{\frac{1}{2}\dot{i}_L = v_C - \frac{1}{2}i_L} \\ & \Rightarrow \boxed{\dot{i}_L = 2v_C - i_L} \quad (1) \end{aligned}$$

$$\begin{aligned} \rightarrow i_C + 3v_C - (v_C - \frac{1}{2}i_L) &= 0 \Rightarrow \boxed{i_C = -2v_C - \frac{1}{2}i_L} \Rightarrow \boxed{\frac{1}{2}\dot{v}_C = -2v_C - \frac{1}{2}i_L} \\ &\Rightarrow \boxed{\dot{v}_C = -4v_C - i_L} \quad (2) \end{aligned}$$

$$\begin{aligned} (1) \& (2) \Rightarrow \begin{bmatrix} \dot{v}_C \\ \dot{i}_L \end{bmatrix} &= \begin{bmatrix} -4 & -1 \\ 2 & -1 \end{bmatrix} \begin{bmatrix} v_C \\ i_L \end{bmatrix} \Rightarrow \boxed{\ddot{v}_C + 5\dot{v}_C + 6v_C = 0} \quad (03) \\ & \boxed{v_C(0) = 1 \quad \dot{v}_C(0) = -4 - 1 = -5} \quad (02) \end{aligned}$$

$$\Rightarrow \boxed{s^2 + 5s + 6 = 0} \Rightarrow \boxed{s_1 = -2, s_2 = -3} \quad (02)$$

$$\Rightarrow \boxed{v_C(t) = C_1 e^{-2t} + C_2 e^{-3t}} \Rightarrow$$

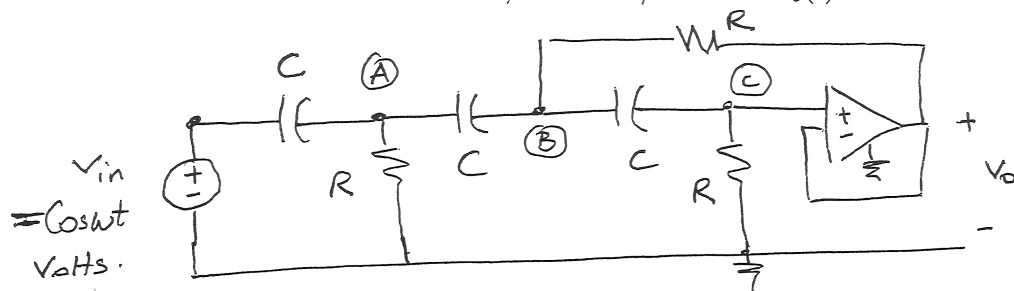
$$\begin{aligned} & \boxed{C_1 + C_2 = 1} \\ & \boxed{-2C_1 - 3C_2 = -5} \quad (02) \\ & C_1 = -2 \quad C_2 = 3 \end{aligned}$$

$$\Rightarrow \boxed{v_C(t) = -2e^{-2t} + 3e^{-3t}} \quad (02)$$

Prob. 3 : (24 pt.s) Consider the following circuit. Assume that the op-amp is linear and operates in the linear region. Assume that the circuit is in sinusoidal steady state.

i : Find the transfer function $H(j\omega) = \frac{V_o}{V_{in}}$.

ii : Let $R = 1 \Omega$ and $C = 1 \text{ F}$, $\omega = 1 \text{ rad/sec}$. Find $v_o(t)$.



$$V_{in} = \cos \omega t \text{ Volts}$$

Prob. 4 : (26 pt.s) Consider the following circuit. Assume that the circuit is in sinusoidal steady state. Here Z_L represents an arbitrary load impedance.

i : Draw the circuit in sinusoidal steady state by using the phasor values of $i_s(t)$ and indicate the impedance values of all relevant elements.

ii : Assume that Z_L is replaced by an open circuit. Find the open circuit voltage phasor V_{TH} between the nodes $A - B$, and evaluate $v_{TH}(t)$.

iii : Assume that Z_L is replaced by a short circuit. Find the short circuit current phasor I_N between the nodes $A - B$, and evaluate $i_N(t)$.

iv : Find an impedance Z_L so that the power transferred to the load is maximum.

