

Artificial Intelligence
ICS461
Fall 2010

Nancy E. Reed

nreed@hawaii.edu

Lecture #10A – Classical Planning
Outline

- The Planning problem
- Classical planning
- STRIPS
- Partial Order Planning
- Chapter 10

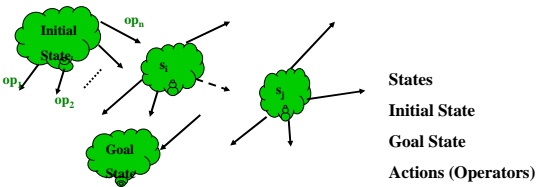
What is Planning?

- Generate sequences of actions to perform tasks and achieve objectives.
 - States, actions and goals
- Search for solution over abstract space of plans.
- Assists humans in practical applications
 - design and manufacturing
 - military operations
 - games
 - space exploration

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Search or Planning Agent?

- State Space Search: (Problem solving agent)



- Planning (Planning agent) – computes several steps of problem solving procedure before executing them.
Plan: sequence of actions.

Previous Agent Limitations

- Ch 3 model-based agent
 - Uses an atomic representation of states
 - With good domain-specific heuristics
 - can find a goal state not too large
- Ch 7 hybrid propositional logic agent
 - may be swamped with large search spaces having many actions and/or states

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Planning: Example

- Goal: *Get a bunch of bananas, a cordless drill, and a quart of milk*
 - Initial State: $\text{At Home} \wedge \text{No milk} \wedge \text{No cordless drill} \wedge \text{No bananas}$
 - Goal State: $\text{At Home} \wedge \text{milk} \wedge \text{cordless drill} \wedge \text{bananas}$

Problem: Many actions and many states to consider; sequence of actions could become too long

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$PlanResult(p, s)$ is the situation resulting from executing p in s

$PlanResult([], s) = s$
 $PlanResult([a|p], s) = PlanResult(p, Result(a, s))$

Initial state $At(Home, S_0) \wedge \neg Have(Milk, S_0) \wedge \dots$

Actions as Successor State axioms
 $Have(Milk, Result(a, s)) \Leftrightarrow [(a = Buy(Milk) \wedge At(Supermarket, s)) \vee (Have(Milk, s) \wedge a \neq \dots)]$

Query
 $s = PlanResult(p, S_0) \wedge At(Home, s) \wedge Have(Milk, s) \wedge \dots$

Solution
 $p = [Go(Supermarket), Buy(Milk), Buy(Bananas), Go(HWS), \dots]$

Principal difficulty: unconstrained branching, hard to apply heuristics

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Tidily arranged actions descriptions, restricted language

ACTION: $Buy(x)$
PRECONDITION: $At(p), Sells(p, x)$
EFFECT: $Have(x)$

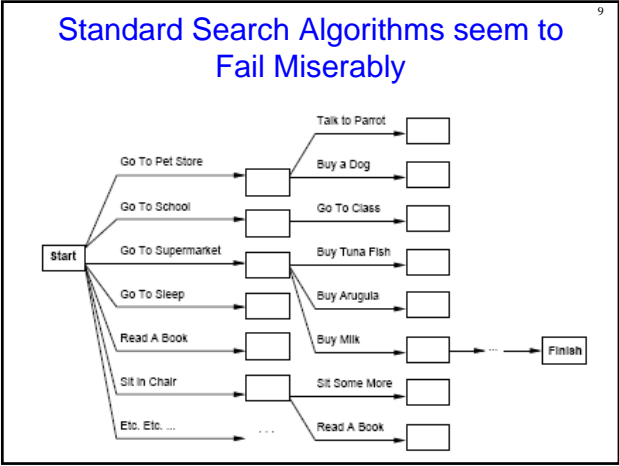
[Note: this abstracts away many important details!]

Restricted language \Rightarrow efficient algorithm
Precondition: conjunction of positive literals
Effect: conjunction of literals

$At(p) \quad Sells(p, x)$

Buy(x)

$Have(x)$



Forward vs. Backward Search

- Forward search may not succeed.
 - Starting at initial state.
 - Forces agent's hand.
 - Example: Since agent is at home, and the things he needs are not at home, he must go somewhere. But where?
- Backward search may be better.
 - One way to have milk is to buy it.
 - Milk can be purchased at the grocery store. Therefore,

Planning

- Determine possible next states by applying evaluation function.
 - Only select states closer to goal.
- Problem: Too many states!**
 - Goal and evaluation function are black boxes, therefore, cannot really eliminate a number of actions from consideration.
- Note: Evaluation function is being applied after the fact
- After the fact goal evaluation isn't enough

Search vs. Planning

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Planning systems do the following:

- open up action and goal representation to allow selection
- divide-and-conquer by subgoaling
- relax requirement for sequential construction of solutions

	Search	Planning
States	Lisp data structures	Logical sentences
Actions	Lisp code	Preconditions/outcomes
Goal	Lisp code	Logical sentence (conjunction)
Plan	Sequence from S_0	Constraints on actions

Planning: Classical Approach

- Considers environments that are:
 - Fully observable
 - Deterministic
 - Finite
 - Static
 - Only change is via the agent's actions
 - And are discrete in time, action, objects, and effects.

Planning Languages

- What is a good language?
 - **Expressive** enough to describe a wide variety of problems.
 - **Restrictive** enough to allow efficient algorithms to operate on it.
 - Planning algorithm should be able to take advantage of the **logical structure** of the problem.
- STRIPS and ADL

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General Language Features

- Representation of states
- Decompose the world in logical conditions and represent a state as a *conjunction of positive literals*.
 - Propositional literals: *Poor* \wedge *Unknown*
 - FO-literals (grounded and function-free): *At(Plane1, Melbourne)* \wedge *At(Plane2, Sydney)*
 - Closed world assumption
- Representation of goals
- Partially specified state and represented as a *conjunction of positive ground literals*
 - A goal is *satisfied* if the state contains all literals in goal.

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General Language Features

- Representations of actions
- Action = PRECOND + EFFECT
 - Action(Fly(p,from, to),*
PRECOND: At(p,from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)
EFFECT: \neg At(p,from) \wedge At(p,to)
= action schema (p, from, to need to be instantiated)
 - Action name and parameter list
 - Precondition (conj. of function-free literals)
 - Effect (conj of function-free literals and P is True and not P is false)
 - Add-list vs. delete-list in Effect

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How Do Actions Affect States?

- An action is applicable in any state that satisfies the precondition.
- For FO action schema applicability involves a substitution θ for the variables in the PRECOND.
 - *At(P1,JFK) \wedge At(P2,SFO) \wedge Plane(P1) \wedge Plane(P2) \wedge Airport(JFK) \wedge Airport(SFO)*
 - Satisfies : *At(p,from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)*
 - With $\theta = \{p/P1, from/JFK, to/SFO\}$
 - Thus the action is applicable.

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STRIPS

- (STanford Research Institute Problem Solver) language
 - Relies on representing states, goals and actions.
 - Uses Closed World Assumption in state representation.

STRIPS

- **States:** Conjunction of grounded function free predicates
 - States are always represented with positive literals (no negations).

Initial State:

$At(Home) \wedge \neg Want(Milk) \wedge \neg Want(Bananas) \wedge \neg Want(Drill)$

- **Goals:** A partially specified State.

$At(Home) \wedge Have(Milk) \wedge Have(Bananas) \wedge Have(Drill)$

STRIPS Actions: Represented by

- **Precondition:** conjunction of function free positive literals that must be true before the action is applied.
- **Add list:** A set of function free literals that will be added to the current state.
- **Delete List:** A set of function free literals that will be deleted from the current state.
- **Effect:** Conjunction of function free literals representing how the state changed when the action is applied.
 - Negations in Effect list represent items to be deleted.

STRIPS Operators

- **Restricted Language**

Action: $Buy(x)$
Precondition: $At(p) \wedge Sells(p,x) \wedge Want(x)$
Add List: $Have(x)$
Delete List: $Want(x)$
Effect: $\neg Want(x) \wedge Have(x)$

- abstracts away many important details \Rightarrow search algorithm to generate efficient plan.

STRIPS

STRIPS action consists of three parts

1. *PC: preconditions*
2. *D: delete list (negative literals)*
3. *A: add list (positive literals)*
4. *Ef: Effect*
 - *After-action* state description generated by deleting all literals in *D* from the *before-action* state description, and then add the literals in *A*.
 - **Strips Assumption:** All literals not mentioned in *D* carry over from the *before-action* to the *after-action* state (Effect). -- Important: **Frame Problem**.

Executing Actions

The result of executing **action a** in **state s** is the state **s'**

- **s'** is same as **s** except
 - Any positive literal *P* in the effect of *a* is added to **s'**
 - Any negative literal $\neg P$ is removed from **s'**

$At(P1,SFO) \wedge At(P2,SFO) \wedge Plane(P1) \wedge Plane(P2) \wedge Airport(JFK) \wedge Airport(SFO)$

- STRIPS assumption: (avoids representational frame problem)
every literal NOT in the effect remains unchanged

Expressiveness and Extensions

- STRIPS is simplified
 - Important limit: function-free literals
 - Allows for propositional representation
- Function symbols lead to infinitely many states and actions
- Recent extension: Action Description language (ADL)
 $Action(Fly(p:Plane, from: Airport, to: Airport),$
 $PRECOND: At(p,from) \wedge (from \neq to)$
 $EFFECT: \neg At(p,from) \wedge At(p,to))$

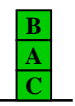
Standardization : *Planning domain definition language (PDDL)*

STRIPS applied to the Blocks World

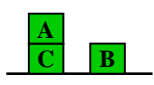
State Description:

$On(B,A) \wedge On(A,C) \wedge On(C,Fl) \wedge Clear(B) \wedge Clear(Fl)$

STRIPS operator:

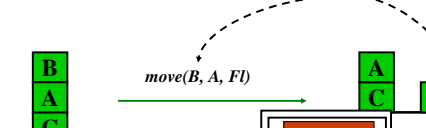


$move(x,y,z)$
 $PC: On(x,y) \wedge Clear(x) \wedge Clear(z)$
 $D: Clear(z) \wedge On(x,y)$
 $A: On(x,z) \wedge Clear(y) \wedge Clear(fl)$
 $EF: \neg Clear(z) \wedge \neg On(x,y) \wedge On(x,z) \wedge Clear(y) \wedge Clear(fl)$
 $x,y, \text{ and } z \text{ are free variables.}$



Apply it to given state: $move(B,A,Fl)$
Then, $move(A,C,Fl)$ or $move(A,C,B)$, etc.

STRIPS Applied to the Blocks World



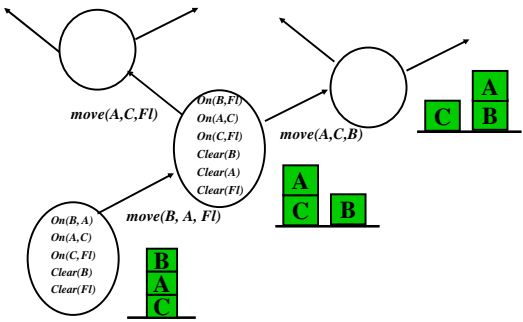
$move(B,A,Fl)$

$On(B,A)$	Delete List
$On(A,C)$	Add List
$On(C,Fl)$	Effect
$Clear(B)$	Unchanged
$Clear(Fl)$	New State

Substitute: $B|x,A|y,Fl|z$

$move(x,y,z)$
 $PC: On(x,y) \wedge Clear(x) \wedge Clear(z)$
 $D: Clear(z) \wedge On(x,y)$
 $A: On(x,z) \wedge Clear(y) \wedge Clear(Fl)$
 $EF: \neg Clear(z) \wedge \neg On(x,y) \wedge On(x,z) \wedge Clear(y) \wedge Clear(Fl)$
 $x,y, \text{ and } z \text{ are free variables.}$

STRIPS Algorithm: Forward Search

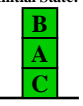


STRIPS Algorithm

- Forward search (progression planning) with a divide-and conquer heuristic.
 - Solve conjunctive goal literals, one at a time.
 - Based on the *General Problem Solver (GPS)* developed by Newell, Shaw, and Simon in 1959
 - Technique to solve goal literal called *Means-end analysis*.

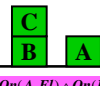
Apply STRIPS Algorithm

Initial State:



$On(B,A) \wedge On(A,C) \wedge On(C,Fl) \wedge Clear(B) \wedge Clear(Fl)$

Goal State:



$On(A,Fl) \wedge On(B,Fl) \wedge On(C,B)$

No initial state description meets goal constructs.

Divide and conquer: choose $On(A,Fl)$ as initial goal.

$move(A,x,Fl)$ has $On(A,Fl)$ in its add list.

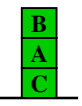
Call STRIPS recursively to achieve its preconditions: $Clear(A) \wedge Clear(Fl) \wedge On(A,x)$

Make substitution C/x , which makes all but $Clear(A)$ satisfied by initial state

$move(x,y,z)$
 $PC: On(x,y) \wedge Clear(x) \wedge Clear(z)$
 $D: Clear(z) \wedge On(x,y)$
 $A: On(x,z) \wedge Clear(y) \wedge Clear(Fl)$
 $EF: \neg Clear(z) \wedge \neg On(x,y) \wedge On(x,z) \wedge Clear(y) \wedge Clear(Fl)$
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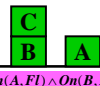
Apply STRIPS Algorithm

Initial State:



$On(B,A) \wedge On(A,C) \wedge On(C,Fl) \wedge Clear(B) \wedge Clear(Fl)$

Goal State:



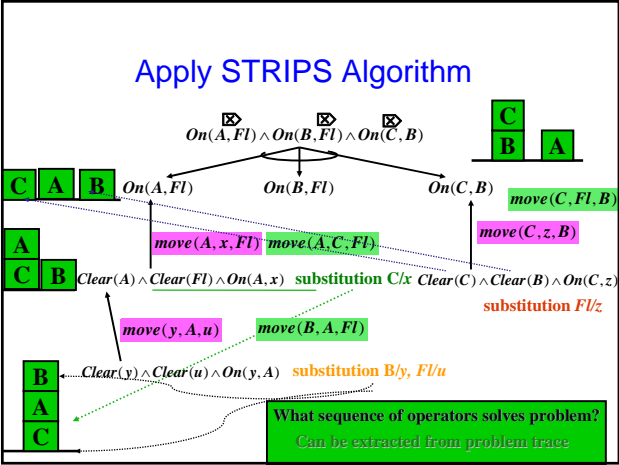
$On(A,Fl) \wedge On(B,Fl) \wedge On(C,B)$

Call STRIPS again (recursively) to solve $Clear(A)$

Use operator $move(y,A,u)$ $On(A,Fl)$

Precondition: $Clear(y) \wedge Clear(u) \wedge On(y,A)$

Continue this process and solve the problem.



STRIPS Algorithm

STRIPS (γ) -- γ is conjunctive goal formula
Uses global data structure, S , consisting of a set of ground literals – **initial state description**.

1. Repeat (iterative main loop continues till state description = γ) Termination in step 9 produces a substitution σ , such that some conjuncts (possibly none) of $\gamma\sigma$ appear in S . Several substitutions can be tried in performing the test, so this is *possible backtracking point*.
2. $g \leftarrow$ an element of $\gamma\sigma$, such that $S \not\models g$. In means-end analysis terms g is regarded as “difference” that must be “reduced” to achieve the goal. (*Backtracking point*).
3. $f \leftarrow$ STRIPS rule whose add list contains the literal, λ , that unifies with g using unifier s . f is an operator that is relevant to reducing the difference. More than one choice of f : *backtracking point*.
4. $f' \leftarrow fs$. This is an instance of f after substitution s . f' can contain variables (is not a ground instance).
5. $p \leftarrow$ precondition formula for f' (instantiated with the substitution s).
6. STRIPS(p). **Recursive call with new sub-goal.**
7. $f'' \leftarrow$ a ground instance of f' applicable in S
8. $S \leftarrow$ result of applying f'' to S .
9. until $S \models \gamma$. (**This test is always against the entire goal γ .**)

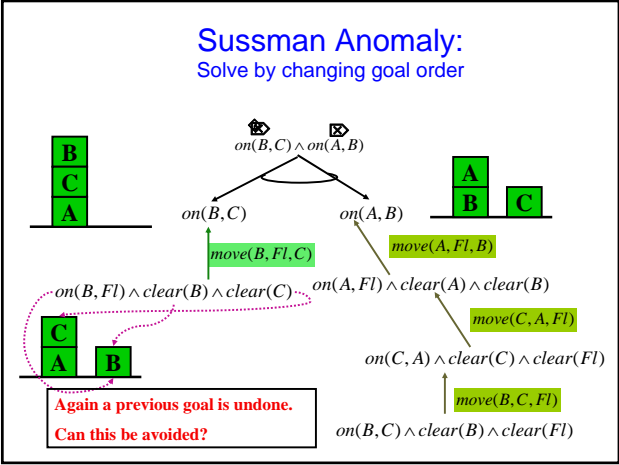
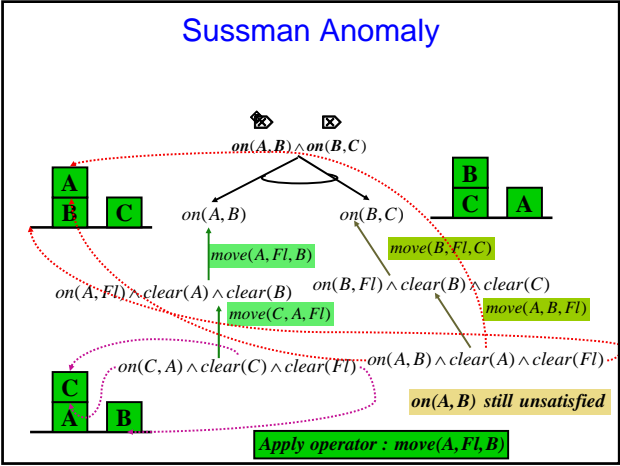
STRIPS Plans can Have Problems

Example: Sussman Anomaly

Initial State: $on(C, A) \wedge on(B, FI) \wedge on(A, FI)$ Goal condition: $on(A, B) \wedge on(B, C)$

Question: Can STRIPS solve this problem?
If not why not?
Divide and conquer approach:
First solve: $on(A, B)$ then $on(B, C)$
What happens?

Problem of focusing narrowly on one conjunct at a time



Sussman Anomaly (notes)

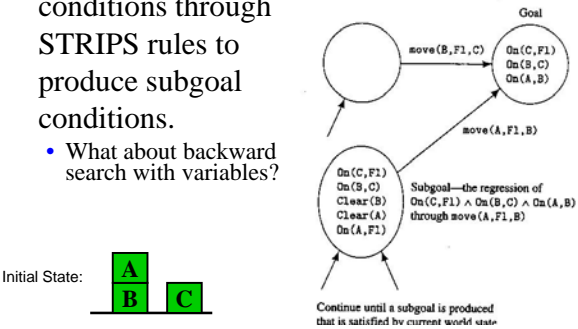
- STRIPS can generate a plan for Sussman anomaly situations but has to undo a goal condition to satisfy the other goal condition.
- There is **no way STRIPS can avoid this**, irrespective of which goal condition it starts of with first.

Backward Search

- Search backwards from goal states.
- Also known as **regression planning**
- Considers only **relevant** actions.
 - Asks: “What are the states from which applying a given action leads to the goal?”
 - What does this consideration imply about the search space?
- Any action that does not undo a desired literal is **consistent**
 - All actions must be consistent.

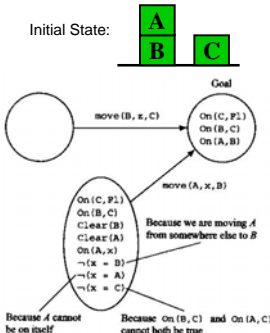
Regression Planning

- **Regress** goal conditions through STRIPS rules to produce subgoal conditions.
 - What about backward search with variables?

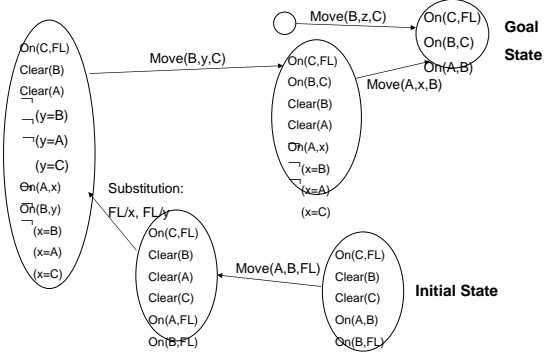


Regression Planning

- Why move A from floor to B?
- So why make commitment?
 - Principle: **Least Commitment Planning**
 - Regress goal through partially instantiated operators
 - Makes backward search complicated, but avoids problems, such as Sussman Anomaly



Regression Planning



Total Order Searches

- Forward and backward searches discussed are **Total Order searches**
- **Strictly linear sequence** of actions from start to goal states.
 - **Does not permit independent sub-goal problem solving**
 - **Is this realistic** for real world problems?
 - How can we deal with these issues?

Planning: Flexible Order

- Need representations for states, goals, and actions.
- Planner can add actions to the plan in any order as needed.
 - Do not have to start at initial state and incrementally (sequentially) progress.

Partial Order Plans

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Partially ordered collection of steps with

- Start step* has the initial state description as its effect
- Finish step* has the goal description as its precondition
- causal links from outcome of one step to precondition of another
- temporal ordering between pairs of steps

Open condition = precondition of a step not yet causally linked

A plan is complete iff every precondition is achieved

A precondition is *achieved* iff it is the effect of an earlier step and no possibly intervening step undoes it

Partial Order Plans (2)

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Operators on partial plans:

- add a link from an existing action to an open condition
- add a step to fulfill an open condition
- order one step wrt another to remove possible conflicts

Gradually move from incomplete/vague plans to complete, correct plans

Backtrack if an open condition is unachievable or if a conflict is unresolvable

Planning: Problem Decomposition

- Many parts of the world are independent of others.
- Use *divide and conquer*.
 - Create sub-problems and solve them one by one.
 - Many planners assume subgoals can be solved independently.
 - Will this approach always work?

Partial Order Planning

- Allows *planning for multiple independent sub-goals*.
- The sub-plans are then combined to form a complete plan.
- Allows one to *solve obvious and important decisions first*
- “Any planner that can place two actions into a plan without specifying which comes first is a partial order planner.”

Partial Order Planning Components

Each POP has four components

- The plan **action** steps.
- The **ordering constraints** determine in what order steps are to be executed.
 - Ordering constraints that create cycles are **not** added to plans.
 - Fewer ordering constraints simplify plan construction.

POP Components (cont)

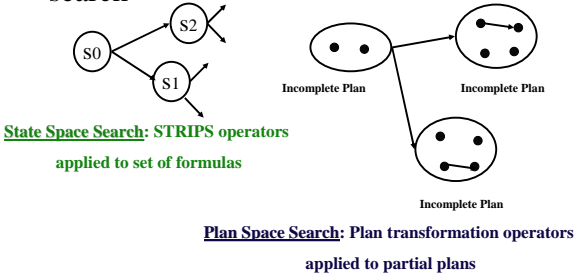
- A set of **causal links** indicates what assertions must be true between two actions.
 - “A achieves p for B.” $A \xrightarrow{p} B$
 - p must be true from the time A is completed and B starts.
- The set of **open preconditions** contains all preconditions that have not yet been achieved by an action in the plan.
 - Planners attempt to empty the set while not introducing contradictions.

Consistency

- A **consistent** plan contains no cycles in the ordering constraints and no conflicts with the causal links.
- A **solution** is a consistent plan with an empty precondition set.

Plan Spaces

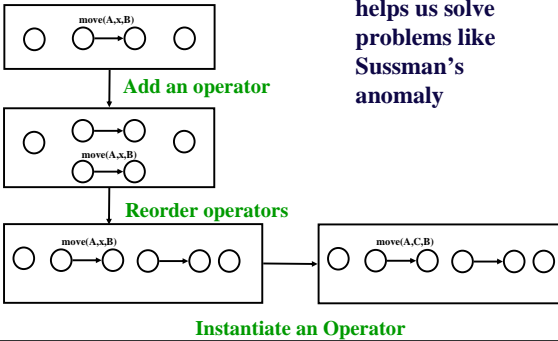
- Introduce the notion of plan space search



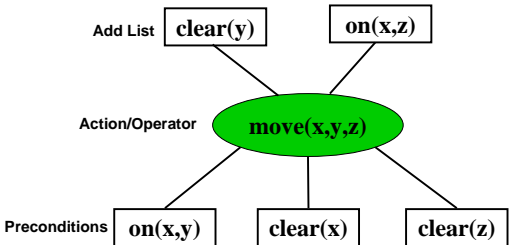
Plan Transformations

- Potential plan transformations
 - Adding steps to the plan.
 - Reordering existing plan steps.
 - Changing a POP into a fully-ordered plan.
 - Changing the plan schema (with instantiated variables) into some instance of that schema.
- Plan Transformations are considered actions in the search, NOT actions on the world.

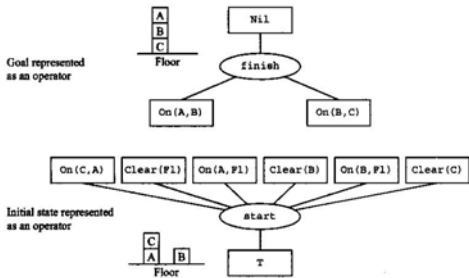
Plan Transformation



STRIPS Rule: Graphical Representation

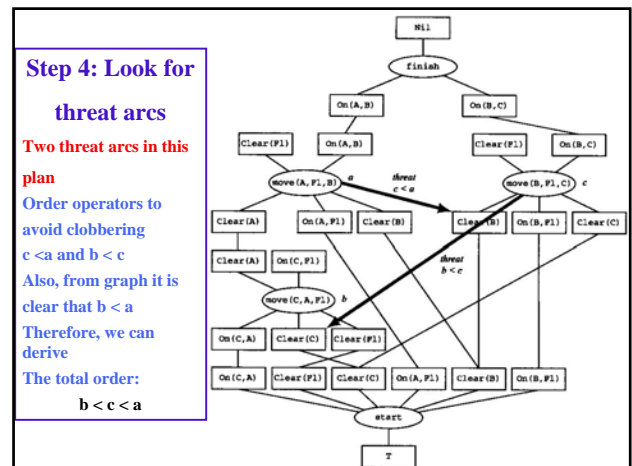
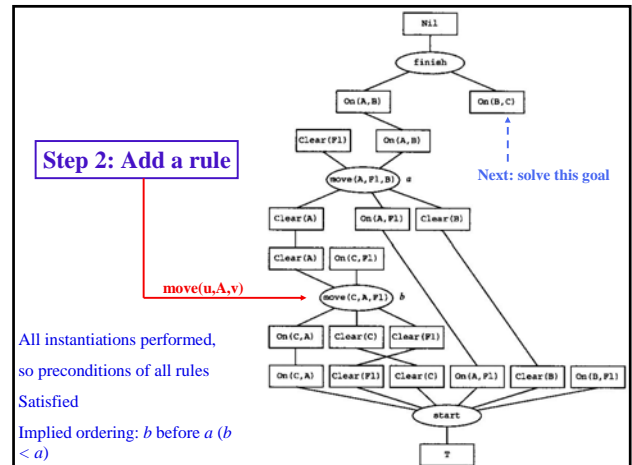


Partial Order Planning (POP)



Start with the start and finish rules

Plan incomplete: apply plan transformation operators



- Continuation of classical planning in next set of slides