# Homework Report

CONTROL IN ROBOTICS COURSE FATEMEH HEIRAN

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## The Robot Model

#### **3-Dof Articulated Robot Structure**

In an articulated robot, joints are all revolute, similar to a human's arm. They are the most common configuration for industrial robots. The selected articulated robot is the same as PUMA's robot first part which yields to the robot end effector position (simplified PUMA). The robot configuration is showed in right side of fig. 1. Accordingly, the robot consist of three revolute joint which implied 3 Dof in task space.

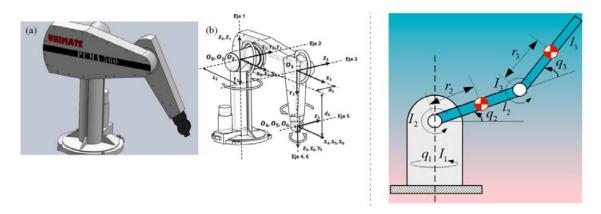


Figure 1- the left side picture is PUMA robot and the right side picture is the simplified PUMA robot [1]

#### **Direct Kinematics**

If we state the end effector coordinates of manipulator based on the angles of the joints, it means the forward kinematics. In other word, in forward kinematics, the measures of the joint space are available and we want to determine the measures of coordinate space. In reality, forward kinematics analyzing is a mapping from joint space to the coordinate space. The direct kinematics of this robot comes as follows [2]:

$$P_x = (l_2 \cos \theta_2 + l_3 \cos(\theta_2 + \theta_3)) * \sin \theta_1 \tag{1}$$

$$P_{\nu} = (l_2 \cos \theta_2 + l_3 \cos(\theta_2 + \theta_3)) * \cos \theta_1 \tag{2}$$

$$P_{z} = l_{2} \sin \theta_{2} + l_{3} \sin(\theta_{2} + \theta_{3}) + l_{1}$$
(3)

## **Jacobian Matrix**

The Jacobian matrix concluded from velocity analysis for the robot and is defined as [2]:

$$\dot{x} = \begin{bmatrix} C_1(l_3C_{23} + l_2C_2) & -S_1(l_3S_{23} + l_2S_2) & -l_3S_{23}S_1 \\ -S_1(l_3C_{23} + l_2C_2) & -C_1(l_3S_{23} + l_2S_2) & -l_3S_{23}C_1 \\ 0 & l_3C_{23} + l_2C_2 & l_3C_{23} \end{bmatrix} \dot{\theta} = J\dot{\theta}$$
(4)

Also in some analysis the derivative of Jacobian is needed, therefore it defined as:

$$\dot{J}_{11} = -S_1 \dot{\theta}_1 (l_3 C_{23} + l_2 C_2) + C_1 (-l_3 S_{23} (\dot{\theta}_2 + \dot{\theta}_3) - l_2 S_2 \dot{\theta}_2) \tag{5}$$

$$\dot{J}_{12} = -C_1 \dot{\theta}_1 (l_3 S_{23} + l_2 S_2) - S_1 (l_3 C_{23} (\dot{\theta}_2 + \dot{\theta}_3) + l_2 C_2 \dot{\theta}_2) \tag{6}$$

$$\dot{J}_{13} = -l_3 C_{23} (\dot{\theta}_2 + \dot{\theta}_3) S_1 - l_3 S_{23} C_1 \dot{\theta}_1 \tag{7}$$

$$\dot{J}_{21} = -C_1 \dot{\theta}_1 (l_3 C_{23} + l_2 C_2) - S_1 (-l_3 S_{23} (\dot{\theta}_2 + \dot{\theta}_3) - l_2 S_2 \dot{\theta}_2) \tag{8}$$

$$\dot{J}_{22} = S_1 \dot{\theta}_1 (l_3 S_{23} + l_2 S_2) - C_1 (l_3 C_{23} (\dot{\theta}_2 + \dot{\theta}_3) + l_2 C_2 \dot{\theta}_2) \tag{9}$$

$$\dot{J}_{23} = -l_3 C_{23} (\dot{\theta}_2 + \dot{\theta}_3) C_1 + l_3 S_{23} S_1 \dot{\theta}_1 \tag{10}$$

$$j_{31} = 0 (11)$$

$$\dot{J}_{32} = -l_3 S_{23} (\dot{\theta}_2 + \dot{\theta}_3) C_1 - l_2 S_2 \dot{\theta}_2 \tag{12}$$

$$\dot{J}_{33} = -l_3 S_{23} (\dot{\theta}_2 + \dot{\theta}_3) \tag{13}$$

#### **Direct Dynamics**

According to [1], in the simplified PUMA560,  $m_1$ ,  $m_2$ ,  $m_3$  are the mass of the turntable, the boom and the arm, respectively. The mass of the turntable can be ignored,  $l_2$ ,  $l_3$  are the length of the boom and the length of the arm, respectively,  $r_2$ ,  $r_3$  are the distance from the center of mass of the boom to the axis of rotation and the distance from the center of mass of the arm to the axis of rotation.  $l_1$ ,  $l_2$ ,  $l_3$  are the moment of inertia about the rotation of each axis. Let:

$$a_1 = m_2 r_2^2 + m_3 l_2^2$$
,  $a_2 = m_3 r_3^2$ ,  $a_3 = m_3 r_3 l_2$   $b_1 = (m_2 r_2 + m_3 l_2)g$ ,  $b_2 = m_3 r_3 g$ 

Establishing the dynamic equation based on the D-H rule:

$$M(q)\ddot{q} + b(q,\dot{q})\dot{q} + f(q) = \tau \tag{14}$$

Where,

$$M(\mathbf{q}) = \begin{bmatrix} m_{11} & m_{12} & m_{13} \\ m_{21} & m_{22} & m_{23} \\ m_{31} & m_{32} & m_{33} \end{bmatrix} b(\mathbf{\theta}, \dot{\mathbf{\theta}}) = \begin{bmatrix} b_{11} & b_{12} & b_{13} \\ b_{21} & b_{22} & b_{23} \\ b_{31} & b_{32} & b_{33} \end{bmatrix} f(\mathbf{q}) = \begin{bmatrix} 0 \\ b_{1}\cos q_{2} + b_{2}\cos(q_{2} + q_{3}) \\ b_{2}\cos(q_{2} + q_{3}) \end{bmatrix}$$

```
\begin{split} &m_{11} = a_1 \cos^2 q_2 + a_2 \cos^2 \left(q_2 + q_3\right) + 2a_3 \cos q_2 \cos \left(q_2 + q_3\right) + I_1, \ m_{22} = a_1 + a_2 + 2a_3 \cos q_3 + I_2 \\ &m_{33} = a_2 + I_3, \ m_{23} = m_{32} = a_2 + a_3 \cos q_3, \ m_{12} = m_{21} = m_{13} = m_{31} = 0 \\ &b_{11} = -\frac{1}{2}a_1\dot{q}_2\sin(2q_2) - \frac{1}{2}a_2\left(\dot{q}_2 + \dot{q}_3\right)\sin(2q_2 + 2q_3) - a_3\dot{q}_2\sin(2q_2 + q_3) - a_3\dot{q}_3\cos q_2\sin\left(q_2 + q_3\right) \\ &b_{12} = -\frac{1}{2}a_1\dot{q}_1\sin(2q_2) - \frac{1}{2}a_2\dot{q}_1\sin(2q_2 + 2q_3) - a_3\dot{q}_1\sin(2q_2 + q_3) \\ &b_{13} = -\frac{1}{2}a_2\dot{q}_1\sin(2q_2 + 2q_3) - a_3\dot{q}_1\cos q_2\sin(q_2 + q_3), \ b_{21} = -b_{12}, \ b_{22} = -a_3\dot{q}_3\sin q_3, \\ &b_{23} = -a_3(\dot{q}_2 + \dot{q}_3)\sin q_3, \ b_{31} = -b_{13}, \ b_{32} = a_3\dot{q}_2\sin q_3, \ b_{33} = 0 \end{split}
```

## **Regressor Matrix**

```
M = [\cos(q(2))^2*ddq(1), \cos(q(2) + q(3))^2*ddq(1), 2*\cos(q(2))*\cos(q(2) + q(3))^2*ddq(1), 2*\cos(q(2))*\cos(q(2))
q(3))*ddq(1), ddq(1), 0, 0, 0, 0; ...
                 ddq(2), ddq(2) + ddq(3), 2*cos(q(3))*ddq(2) + ddq(3)*cos(q(3)), 0, ddq(2),
0, 0, 0, 0; ...
                  0, ddq(2) + ddq(3), ddq(2)*cos(q(3)), 0, 0, ddq(3), 0, 0, 0];
C = [-0.5*dq(2)*sin(2*q(2))*dq(1) - 0.5*dq(2)*dq(1)*sin(2*q(2)), - 0.5*(dq(2) + (2))]
dq(3))*sin(2*q(2) + 2*q(3))*dq(1)...
                   -\ 0.5*dq(2)*dq(1)*sin(2*q(2) + 2*q(3)) - 0.5*dq(3)*dq(1)*sin(2*q(2) + 2*q(3)) - 0.5*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*dq(3)*
2*q(3)), -dq(2)*sin(2*q(2) + q(3))*dq(1)...
                   - dq(1)*dq(3)*cos(q(2))*sin(q(2) + q(3)) - dq(2)*dq(1)*sin(2*q(2) + q(3)) -
dq(3)*dq(1)*cos(q(2))*sin(q(2) + q(3))...
                   , 0, 0, 0, 0, 0, 0; ...
                  0.5*dq(1)*dq(1)*sin(2*q(2)), 0.5*dq(1)*dq(1)*sin(2*q(2) + 2*q(3)),
dq(1)*dq(1)*sin(2*q(2) + q(3)) - dq(2)*dq(3)...
                   sin(q(3)) - dq(3)*(dq(2) + dq(3))*sin(q(3)), 0, 0, 0, 0, 0;...
                  0, 0.5*dq(1)*dq(1)*sin(2*q(2) + 2*q(3)), dq(1)*dq(1)*cos(q(2))*sin(q(2) + 2*q(3)), dq(1)*dq(1)*dq(1)*sin(q(2) + 2*q(3)), dq(1)*dq(1)*sin(q(2))*sin(q(2)) + 2*q(3)), dq(1)*dq(1)*cos(q(2))*sin(q(2)) + 2*q(3)), dq(1)*dq(1)*cos(q(2))*sin(q(2)) + 2*q(3)), dq(1)*dq(1)*cos(q(2))*sin(q(2)) + 2*q(3)), dq(1)*dq(1)*cos(q(2)) + 2*q(3)), dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq(1)*dq
q(3)) + dq(2)*dq(2)*sin(q(3)),...
                  0, 0, 0, 0, 0, 0];
G = [0, 0, 0, 0, 0, 0, 0, 0, 0; ...
                   0, 0, 0, 0, 0, 0, \sin(q(2))*g/2, -\sin(q(2) + q(3))*g/2, -\sin(q(2))*g; \dots
                   0, 0, 0, 0, 0, 0, 0, -\sin(q(2) + q(3))*q/2, 0];
Y = M + C + G;
```

#### **Parameters Vector**

```
theta = [a1; a2; a3; I1; I2; I3; m2*12; m3*13; m3*12]
```

## **Controller Design and Simulation**

## **Trajectory Planning**

The trajectory planning for the robot joint angles has been take place with assuming the initial and final position, velocity and acceleration between time 0 to 5 second as follows.

$$x_{1} = \begin{bmatrix} \theta_{1i} & \dot{\theta}_{1i} & \ddot{\theta}_{1i} & \theta_{1f} & \dot{\theta}_{1f} & \ddot{\theta}_{1f} \end{bmatrix} = \begin{bmatrix} 0, 0, pi/12, 2pi/3, 0, 0 \end{bmatrix}$$

$$x_{2} = \begin{bmatrix} \theta_{2i} & \dot{\theta}_{2i} & \ddot{\theta}_{2i} & \theta_{2f} & \dot{\theta}_{2f} \end{bmatrix} = \begin{bmatrix} 0, 0, pi/12, pi/3, 0, 0 \end{bmatrix}$$

$$x_{3} = \begin{bmatrix} \theta_{3i} & \dot{\theta}_{3i} & \ddot{\theta}_{3i} & \theta_{3f} & \dot{\theta}_{3f} & \ddot{\theta}_{3f} \end{bmatrix} = \begin{bmatrix} 0, 0, pi/12, 5pi/6, 0, 0 \end{bmatrix}$$

Which yields to the trajectory planning as follows:

```
theta1 = 0.1309*t^2 + 0.0147*t^3 - 0.0085*t^4 + 0.0007*t^5;
theta2 = 0.1309*t^2 - 0.0188*t^3 - 0.001*t^4 + 0.0002*t^5;
theta3 = 0.1309*t^2 + 0.0314*t^3 - 0.0123*t^4 + 0.001*t^5;
```

- Hint 1: there is a m file named trajectoryPlanning to obtain the trajectory.
- ➤ Hint 2: in the case of impedance and parallel control because of singularity in above trajectory, the simulation doesn't work well. Therefore, we changed the trajectory as follows:

```
theta1 = 2*exp(-0.1*t);
theta2 = 1 + exp(-0.15*t);
theta3 = 0.5 + 2*exp(-0.2*t);
```

## **Assumptions**

The robot parameters are considered as follows:

```
m1 = 1;

m2 = 1;

m3 = 1;

11 = 1;

12 = 1;

13 = 1;

r1 = 11/2;

r2 = 12/2;

r3 = 13/2;

R1 = 0.05;

R2 = 0.05;

R3 = 0.05;
```

## **PD Controller**

## PD

In this controller the terms including gravity (g) were omitted. Fig. 2 show the controller designed in Simulink.

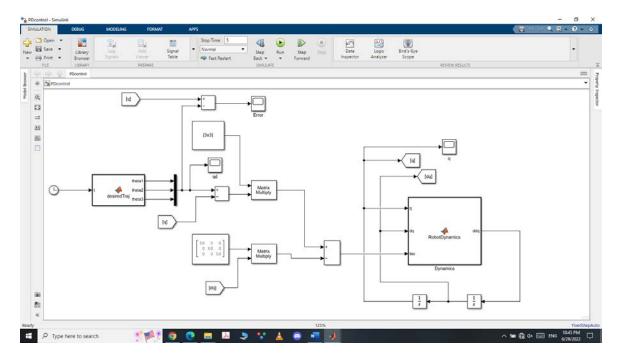


Figure 2- Simulation of PD Controller

According to the simulation, the error is revealed in fig. 3.

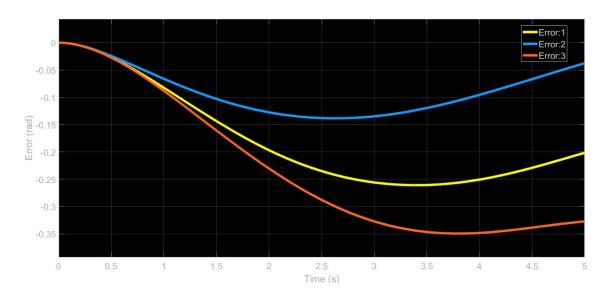


Figure 3- PD controller simulation results

## **PD + Gravity Controller**

This controller is PD type with considering gravity in designing controller. Fig. 4 show the controller designed in Simulink.

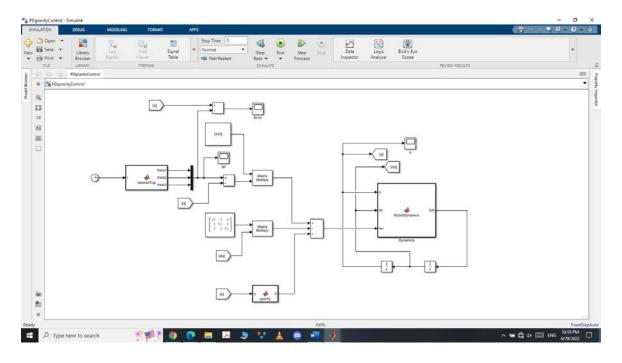


Figure 4- Simulation of PD + gravity Controller

According to the simulation, the error is revealed in fig. 5.

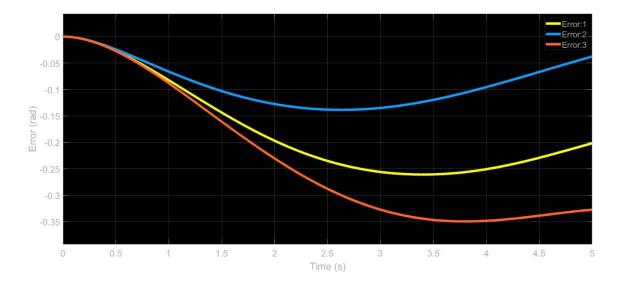


Figure 5- PD + gravity controller simulation results

## **Inverse Dynamics Control**

## **PD Inverse Dynamics**

The fig. 6 shows the simulations of the controller. The control design assumptions are defined as follows:

```
Kp = [1 0 0; 0 1 0; 0 0 1];
Kd = [1 0 0; 0 1 0; 0 0 1];
```

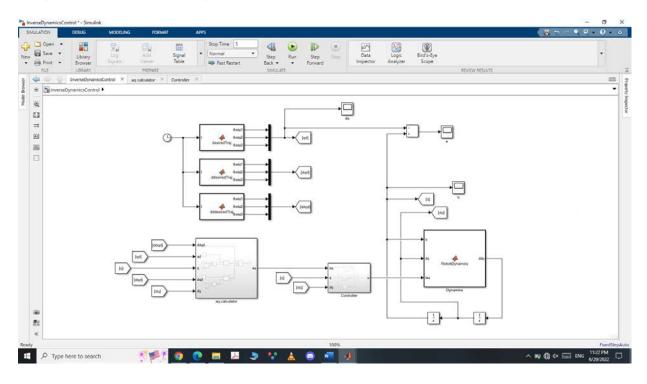


Figure 6- Simulation of PD inverse dynamics Controller

According to the simulation, the error is revealed in fig. 7.

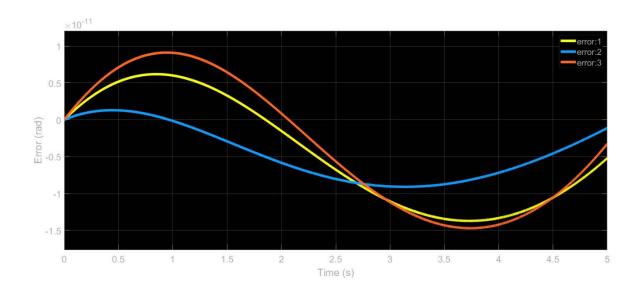


Figure 7- PD inverse dynamics controller simulation results

## **Robust Inverse Dynamics**

The fig. 8 shows the simulations of the controller. The control design assumptions are defined as follows:

```
kd1 = 100; kd2 = 100; kd3 = 100;
kp1 = 100; kp2 = 100; kp3 = 100;
P = [-49 0 0 53 0 0; 0 -49 0 0 53 0; 0 0 -49 0 0 53; 53 0 0 -59 0 0; 0 53 0 0 -
59 0; 0 0 53 0 0 -59];
Rho = 0.01;
Mhat = [3.5 0 0; 0 3.5 0.75; 0 0.75 1.25];
Chat = [2 1.25 1; -1.25 0.5 0.5; -1 0.5 0];
Ghat = [0; 20; 5];
epsilon = 0.1;
```

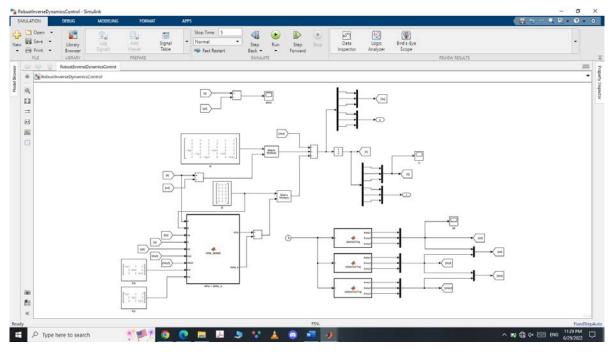


Figure 8- Simulation of robust inverse dynamics Controller

According to the simulation, the error is revealed in fig. 9.

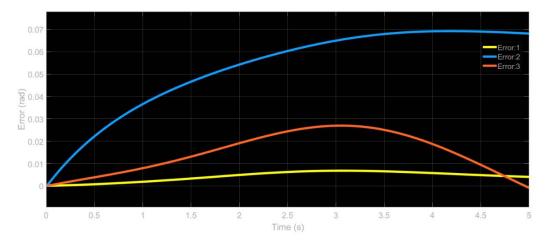


Figure 9- Robust inverse dynamics controller simulation results

#### **Adaptive Inverse Dynamics**

The fig. 10 shows the simulations of the controller. The control design assumptions are defined as follows:

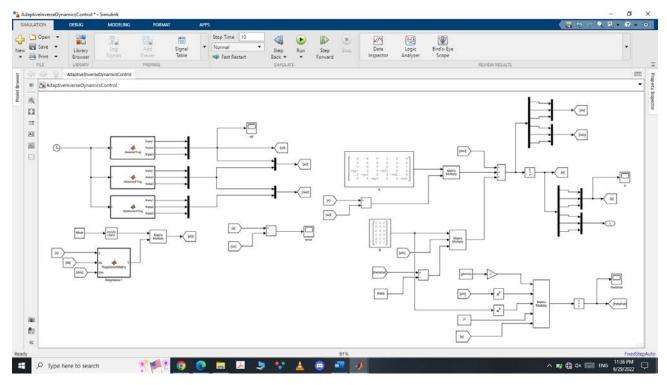


Figure 10- Simulation of adaptive inverse dynamics Controller

According to the simulation, the error is revealed in fig. 11.

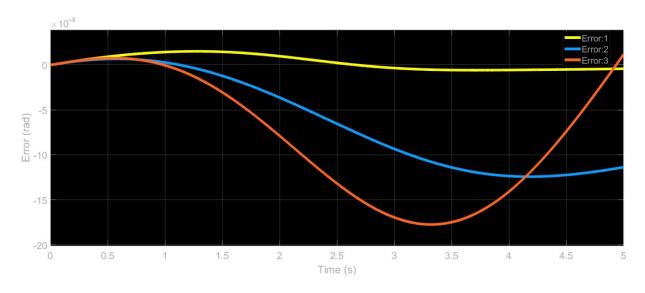


Figure 11- Adaptive inverse dynamics controller simulation results

# **Passivity Based Control**

## **PD Passivity Based**

The fig. 12 shows the simulations of the controller. The control design assumptions are defined as follows:

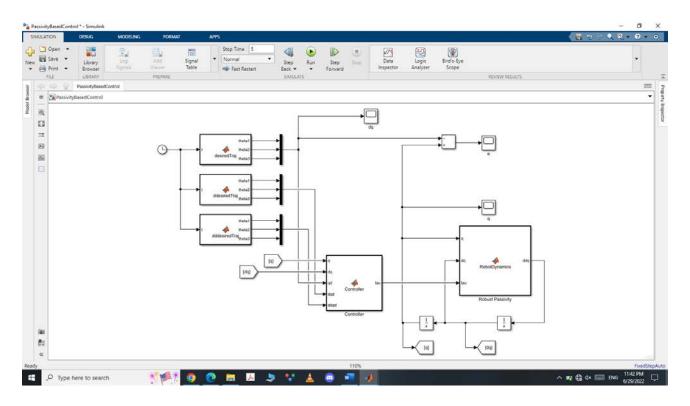


Figure 12- Simulation of PD passivity based Controller

According to the simulation, the error is revealed in fig. 13.

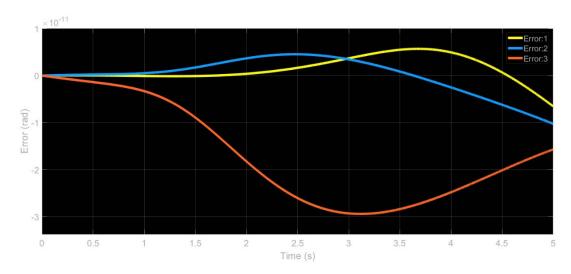


Figure 13- PD passivity based controller simulation results

## **Robust Passivity Based**

The fig. 14 shows the simulations of the controller. The control design assumptions are defined as follows:

```
theta = [1.25; 0.25; 0.5; 1; 1; 1; 1; 1; 1];
theta0 = theta.*3;
K = 100.*[1 0 0; 0 1 0; 0 0 1];
gamma = 1.*[1 0 0; 0 1 0; 0 0 1];
Rho = 10;
epsilon = 0.1;
```

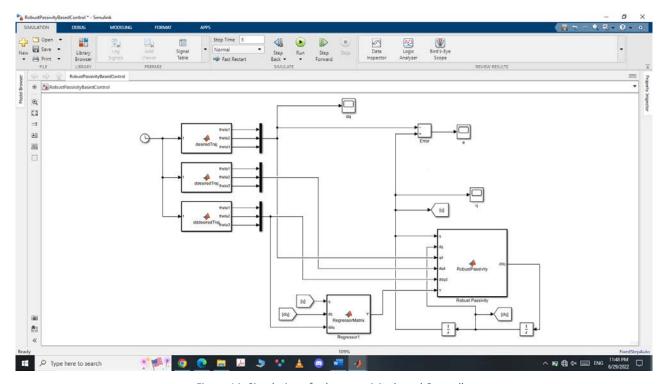


Figure 14- Simulation of robust passivity based Controller

According to the simulation, the error is revealed in fig. 15.

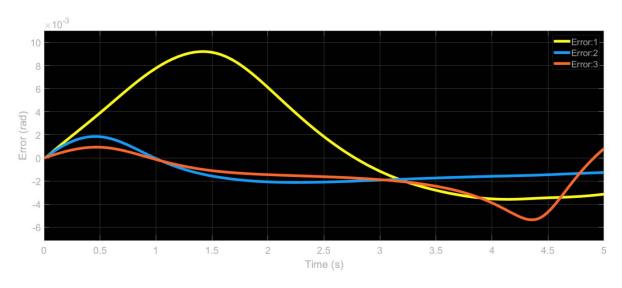


Figure 15- Robust passivity based controller simulation results

## **Adaptive Passivity Based**

The fig. 16 shows the simulations of the controller. The control design assumptions are defined as follows:

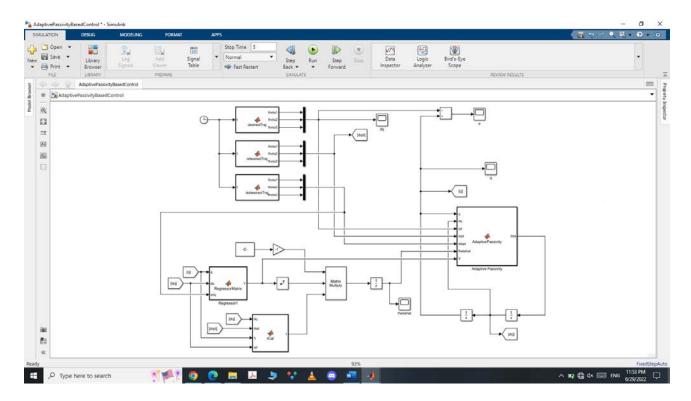


Figure 16- Simulation of adaptive passivity based Controller

According to the simulation, the error is revealed in fig. 17.

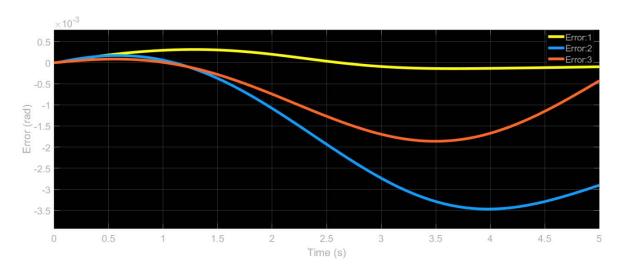


Figure 17- Adaptive passivity based controller simulation results

## **Impedance Control**

The fig. 18 shows the simulations of the controller. The control design assumptions are defined as follows:

```
Cd = [2 \ 1.25 \ 1; -1.25 \ 0.5 \ 0.5; -1 \ 0.5 \ 0];
Kd = [0 \ 0 \ 0; \ 0 \ 20 \ 0; \ 0 \ 0 \ 5];
Md = 5.*[3.5 \ 0 \ 0; \ 0 \ 3.5 \ 0.75; \ 10 \ 30 \ 15];
```

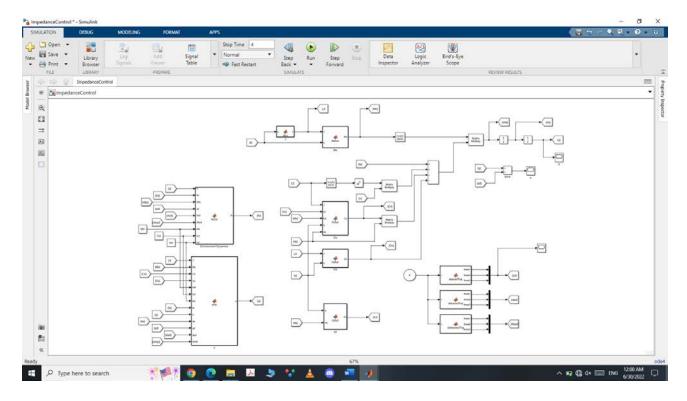


Figure 18- Simulation of impedance Controller

According to the simulation, the error is revealed in fig. 19.

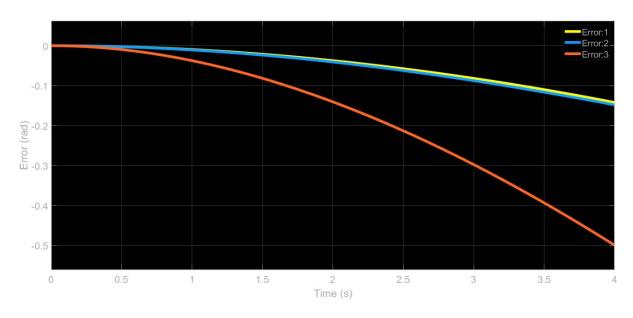


Figure 19- Impedance controller simulation results

## **Parallel Control**

The fig. 20 shows the simulations of the controller. The control design assumptions are defined as follows:

```
Ki = 80.*[1 0 0; 0 1 0; 0 0 10];

Kf = 80.*[1 0 0; 0 1 0; 0 0 1];

Cd = [2 1.25 1; -1.25 0.5 0.5; -3 2 0];

Kd = [0 0 0; 0 20 0; 0 0 50];

Md = 5.*[3.5 0 0; 0 3.5 0.75; 10 30 15];
```

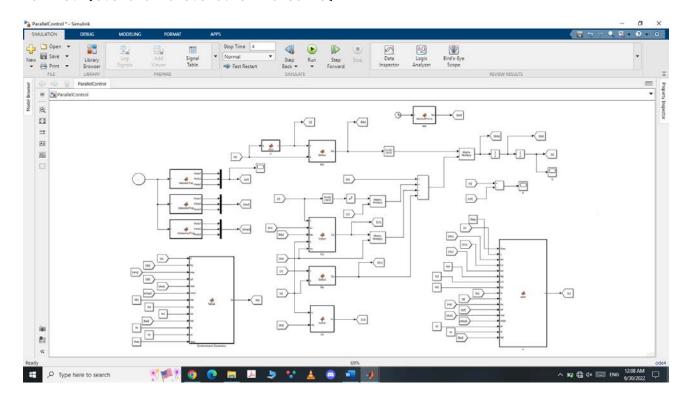


Figure 20- Simulation of parallel Controller

According to the simulation, the error is revealed in fig. 21.

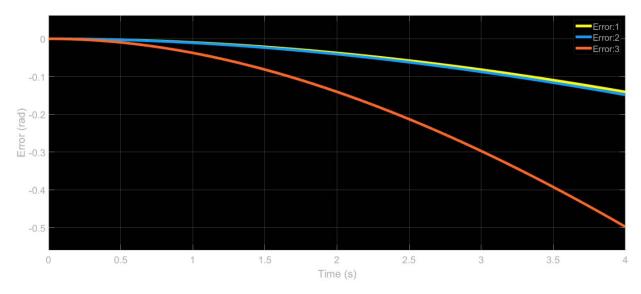


Figure 21- Parallel controller simulation results

## **Tele-robotics Force-Force Using ISS Approach**

The fig. 22 shows the simulations of the controller. The considered system contains two 3-Dof articulated robots one as master and another one as slave. The operator force defined as:

```
Fh = [t; 2*t; 3*t];
```

Also the environment force is defined as:

```
Fe = [0.5*t; 0.6*t; 0.7*t];
```

The delay time between master and slave considered 1 second and parameters of ISS approach are defined as follow:

```
gammaM = [1 0 0; 0 1 0; 0 0 1];
gammaS = [1 0 0; 0 1 0; 0 0 1];
Km = 300.*[1 0 0; 0 1 0; 0 0 1];
Ks = 300.*[1 0 0; 0 1 0; 0 0 1];
```

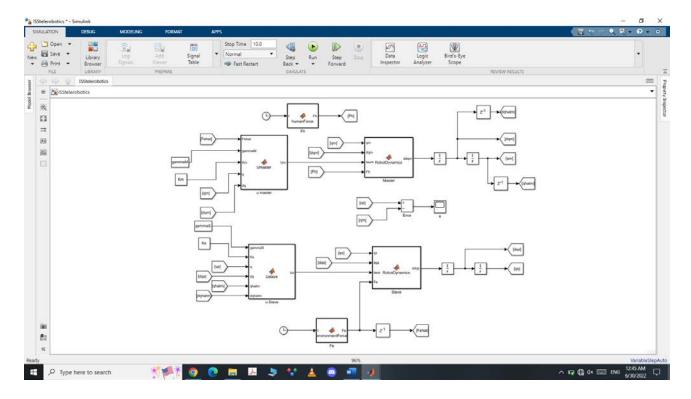


Figure 22- Simulation of tele-robotics system

According to the simulation, the error is revealed in fig. 23.

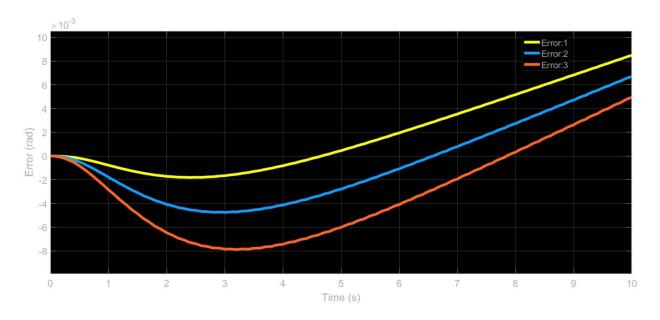


Figure 23- tele-robotics system simulation results