

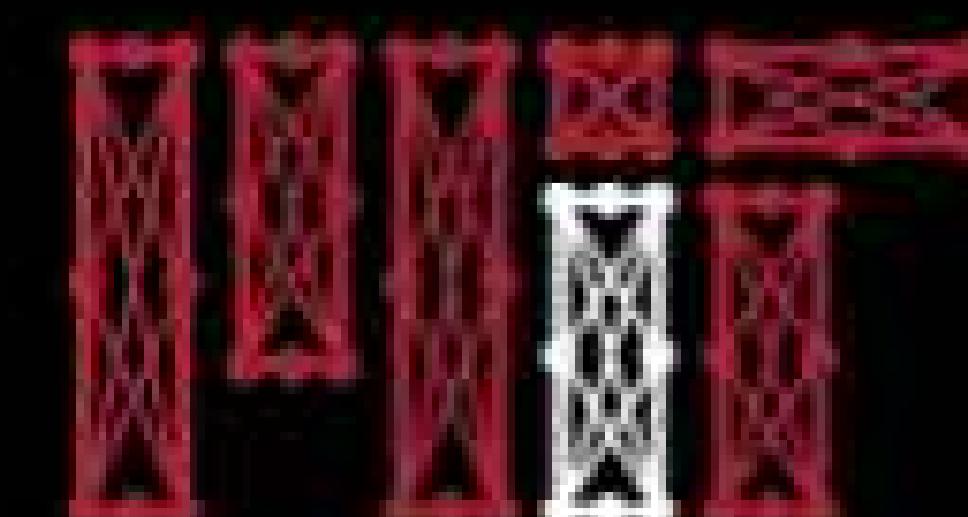


# Deep Computer Vision

Alexander Amini

MIT 6.S191


January 25, 2022





**“To know what is  
where by looking.”**

To discover from images what is present in the world, where things are, what actions are taking place, to predict and anticipate events in the world



# The rise and impact of computer vision

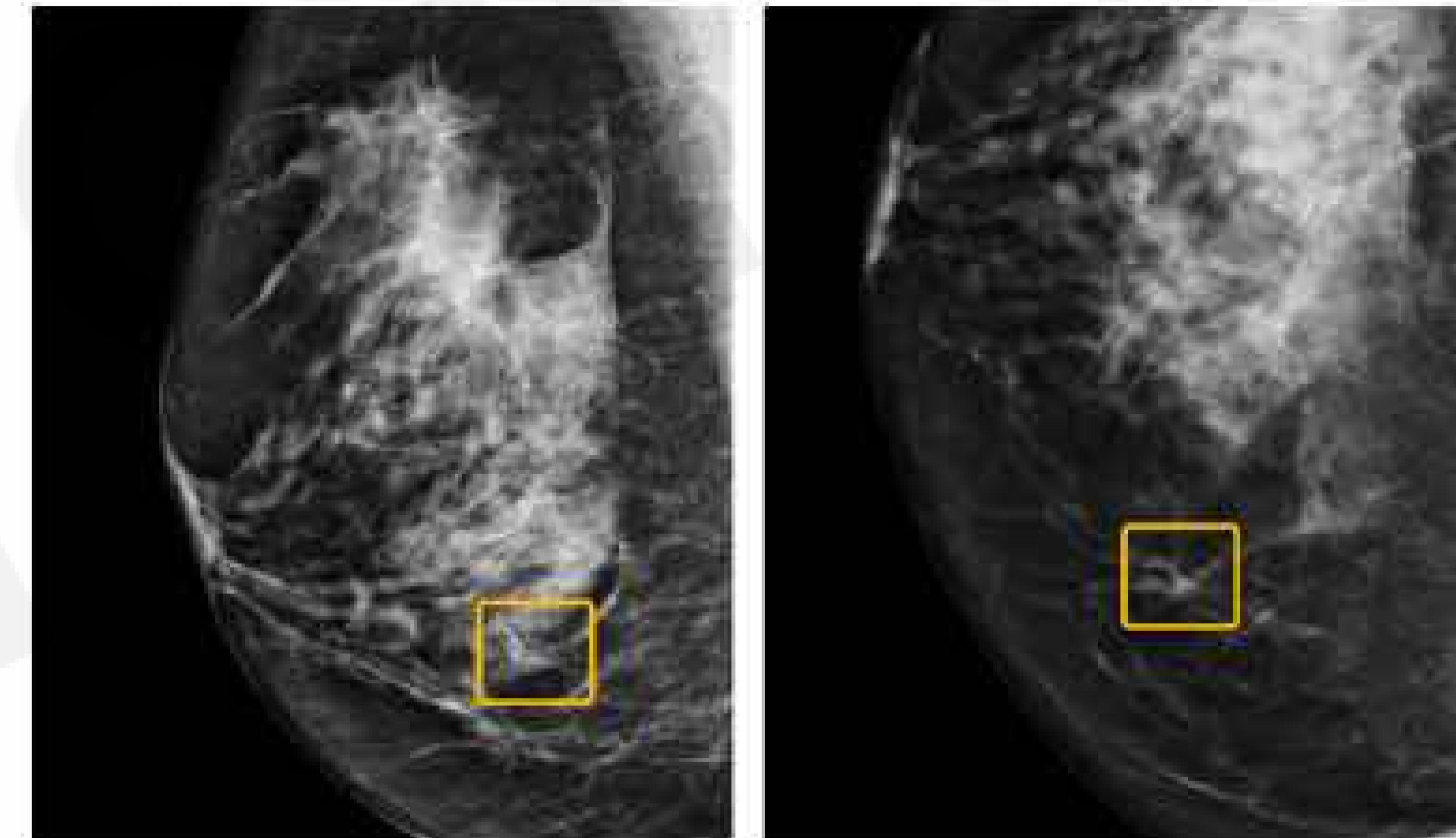
Robotics



Accessibility



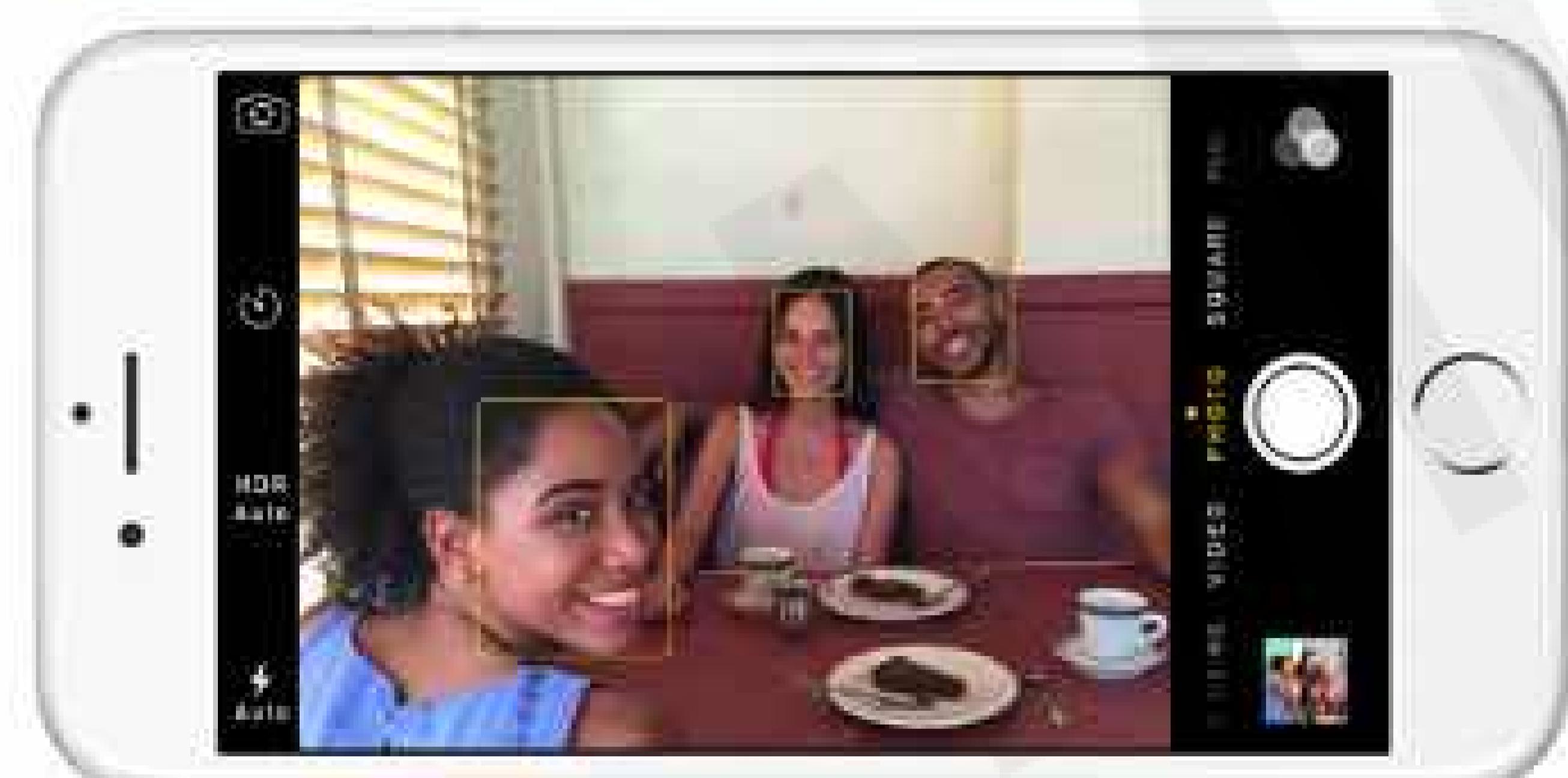
Biology & Medicine



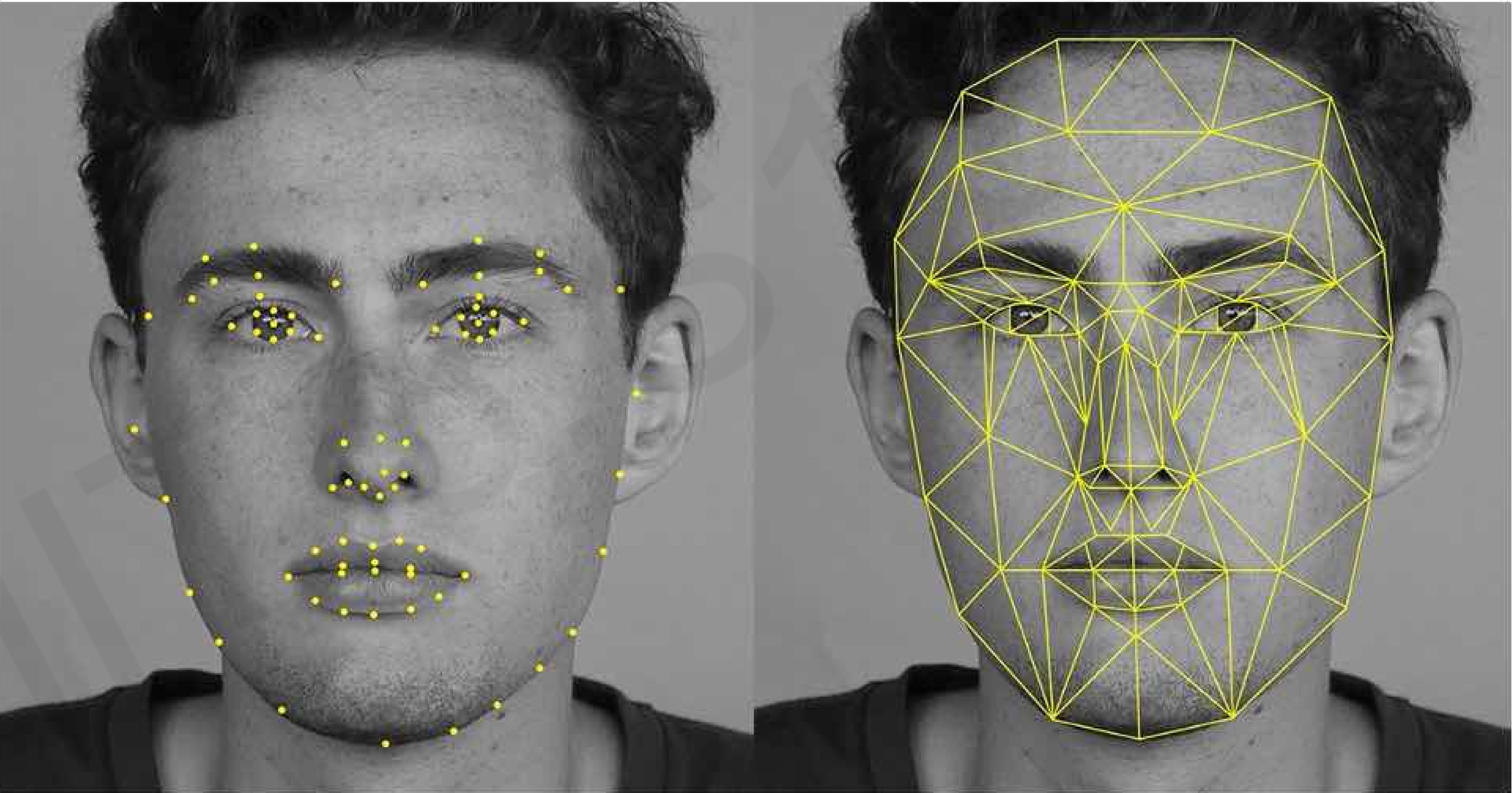
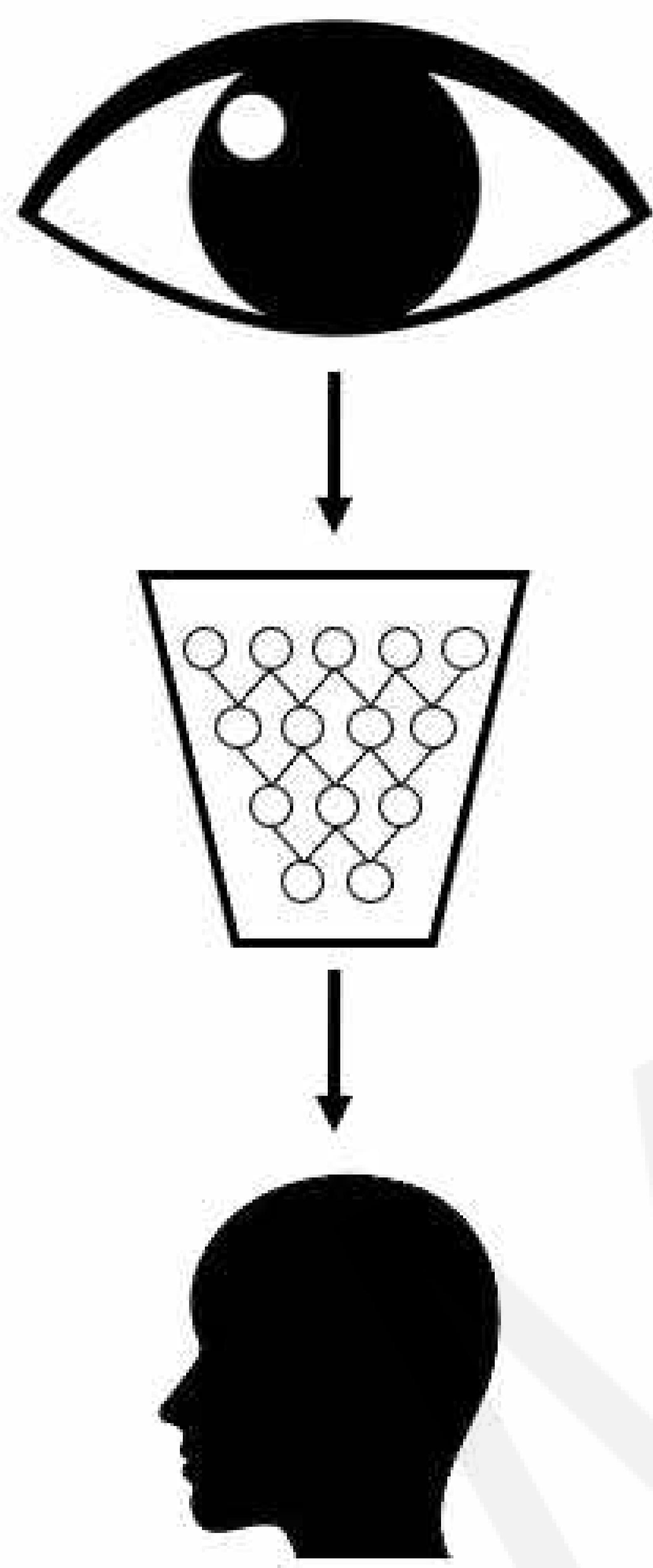
Autonomous driving



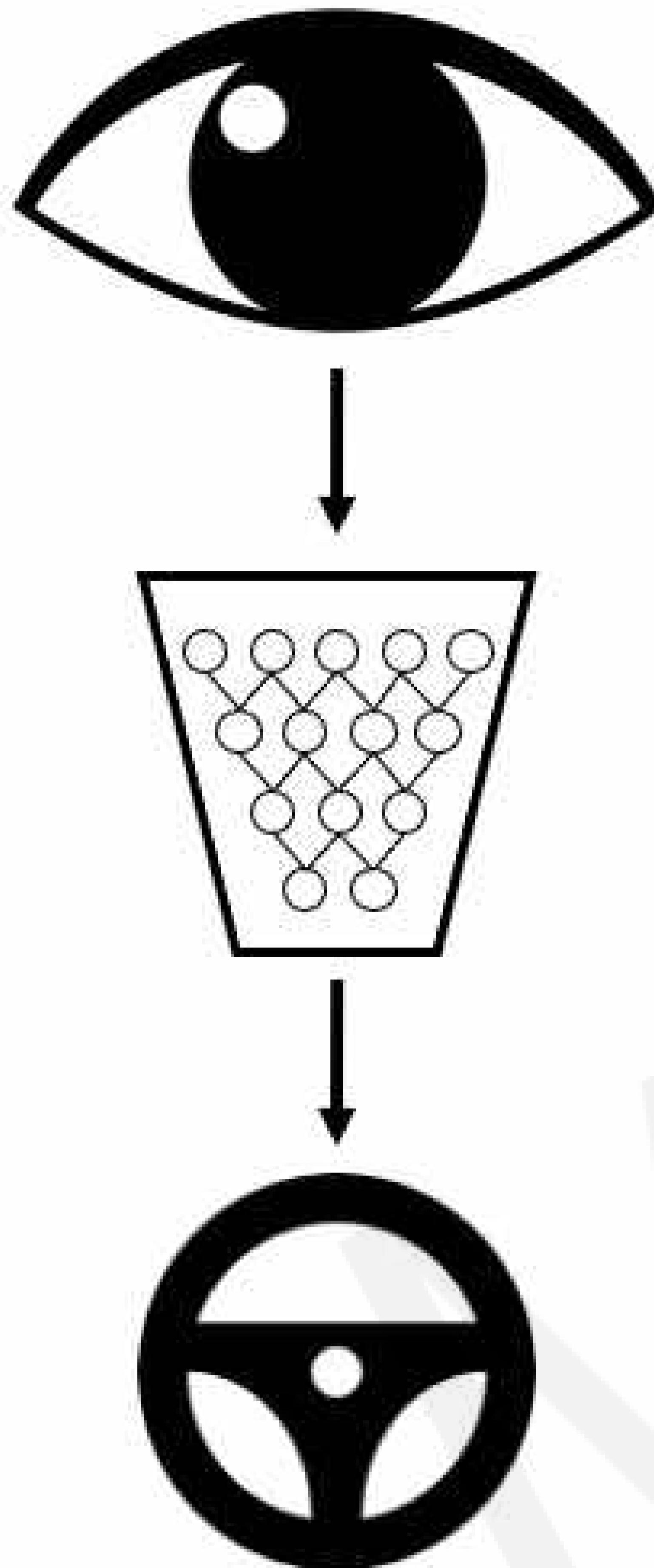
Mobile computing



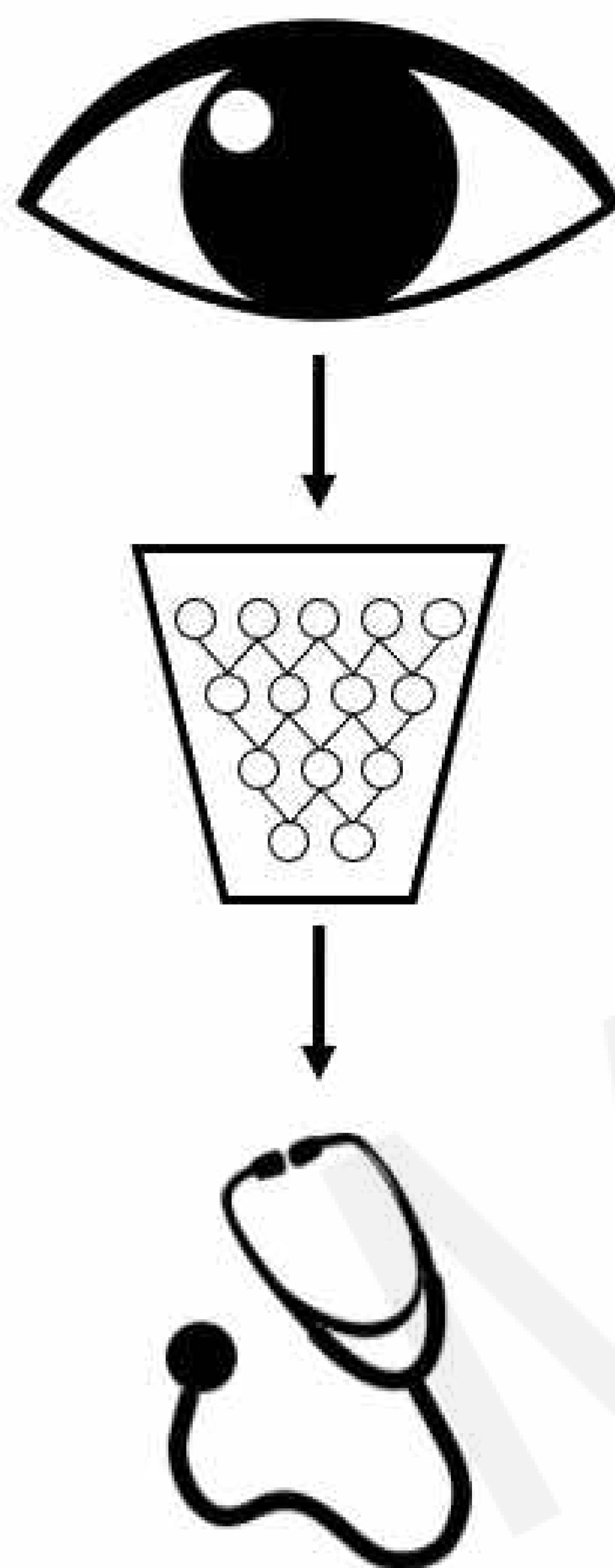
# Impact: Facial Detection & Recognition



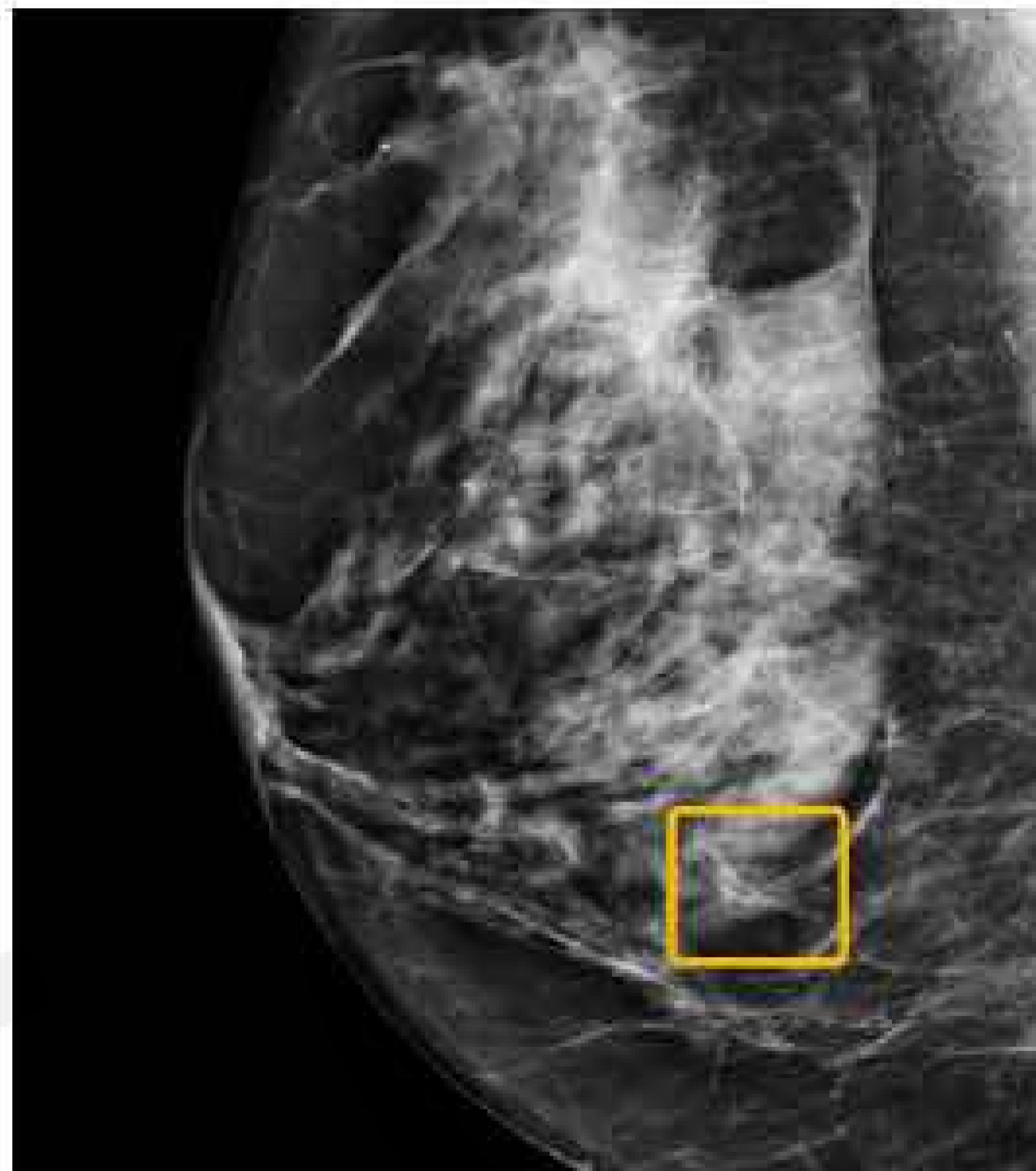
# Impact: Self-Driving Cars



# Impact: Medicine, Biology, Healthcare



Breast cancer



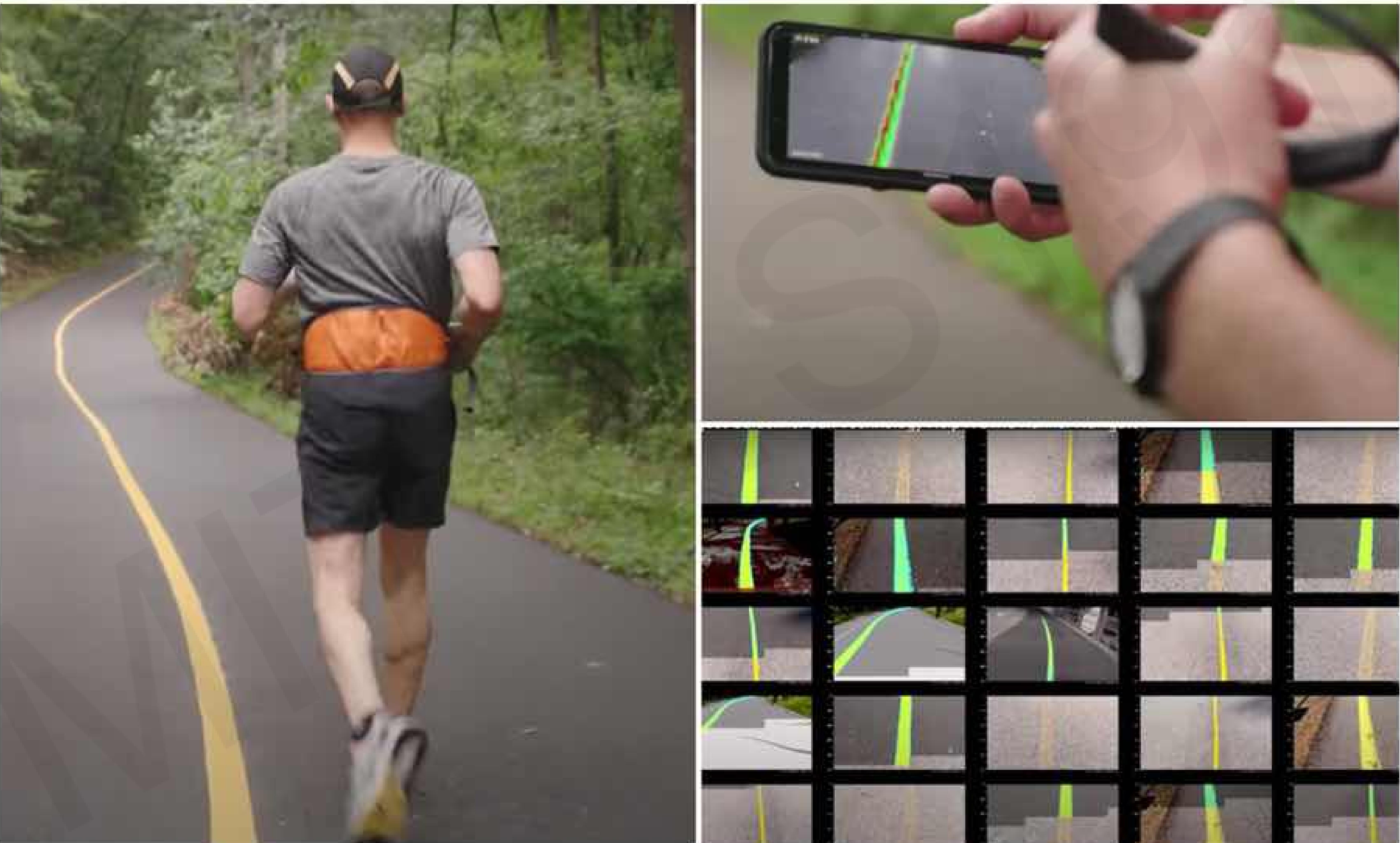
COVID-19



Skin cancer

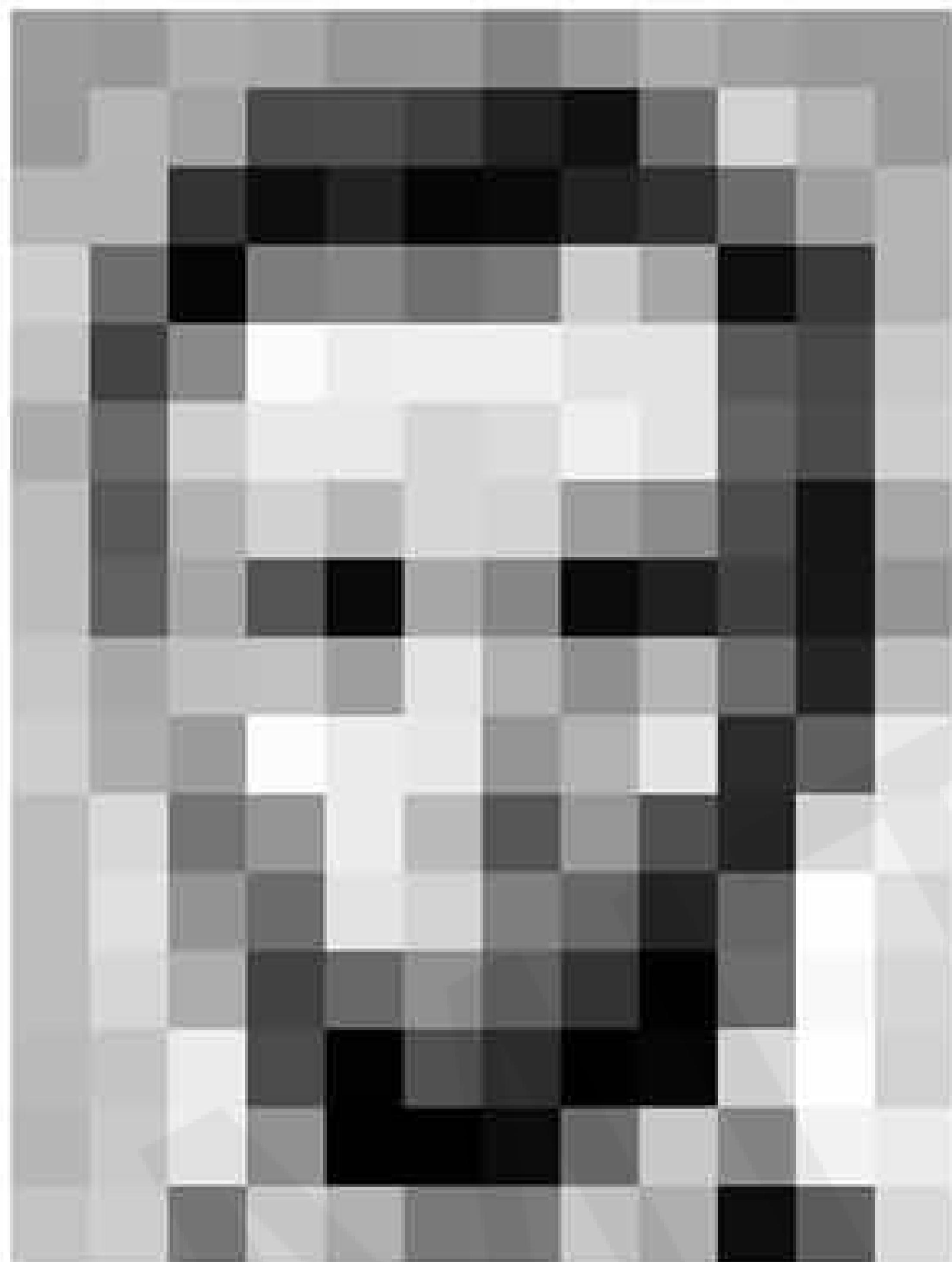


# Impact: Accessibility



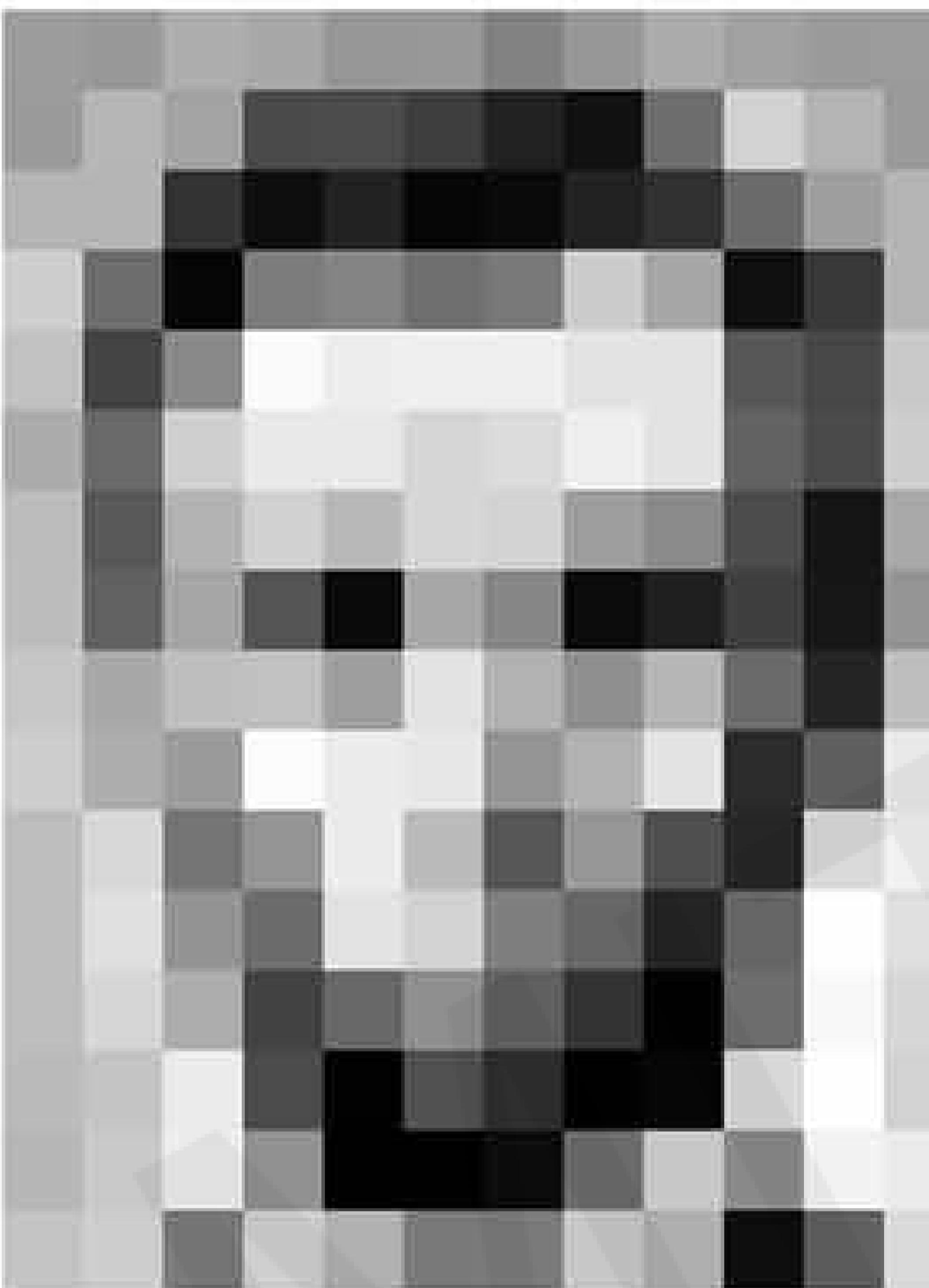
# What Computers “See”

# Images are Numbers



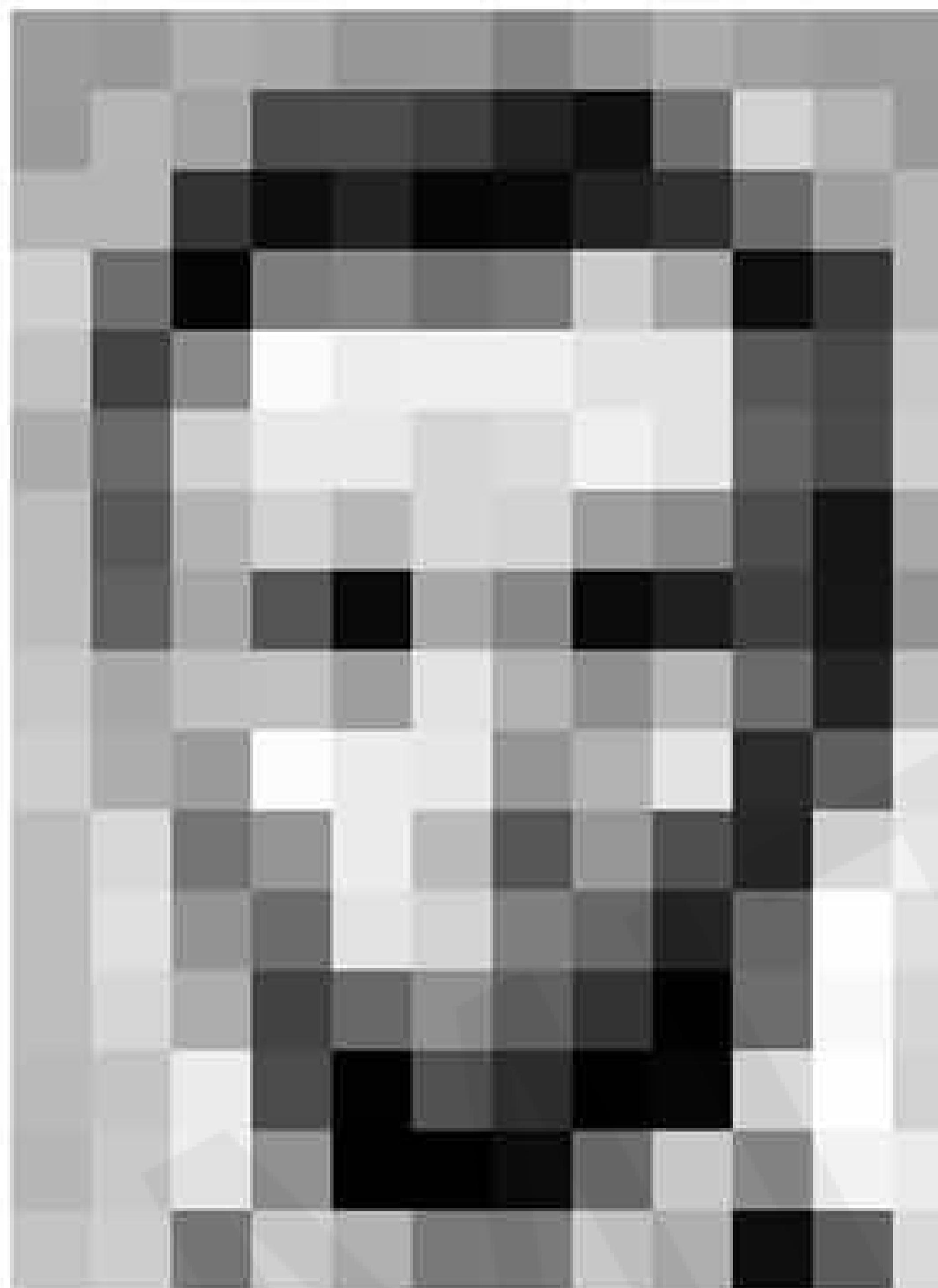
6.S191

# Images are Numbers



167	153	174	168	160	162	129	151	172	161	155	166
165	162	169	74	76	62	33	17	110	210	180	154
180	180	50	14	54	6	10	33	45	106	159	181
206	109	5	124	131	111	120	204	166	15	56	180
194	33	137	251	237	239	239	228	227	37	71	201
172	159	297	233	233	214	220	239	228	98	74	206
188	83	179	229	185	215	211	158	139	75	20	169
189	97	165	64	10	168	134	11	31	62	22	148
199	168	151	163	158	227	178	143	182	106	36	190
205	174	155	252	236	231	149	178	228	43	63	234
190	216	116	149	236	187	56	150	79	35	218	241
190	224	147	168	227	210	127	102	36	101	255	224
190	214	173	65	163	143	96	50	2	109	249	215
187	196	235	75	1	61	47	0	6	217	255	211
183	202	237	145	0	0	12	108	200	138	243	236
196	206	123	207	177	121	123	200	175	13	96	218

# Images are Numbers



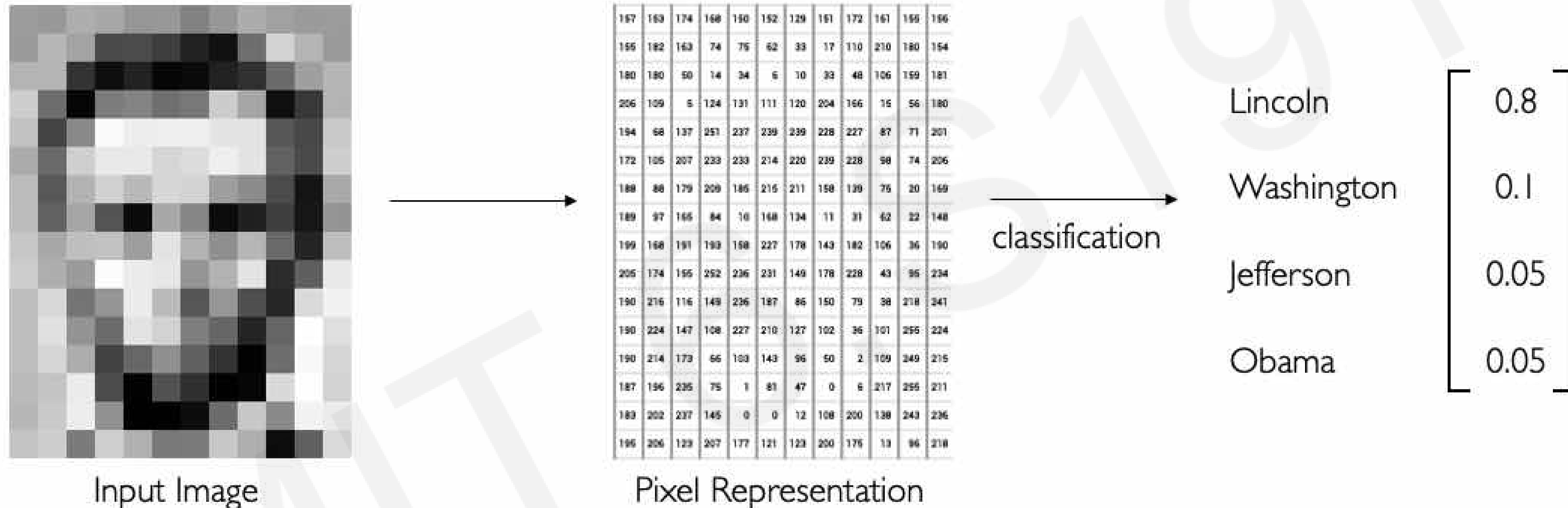
157	153	174	168	160	162	129	151	172	161	155	166
165	162	163	74	76	62	33	17	110	210	180	154
180	180	50	14	34	6	10	33	48	106	159	181
206	109	5	124	131	111	120	204	166	15	56	180
194	68	137	251	237	239	239	228	227	87	71	201
172	106	207	233	233	214	220	239	228	98	74	206
188	88	179	209	186	215	211	158	139	75	20	169
189	97	165	64	10	168	134	11	31	62	22	148
199	168	191	193	158	227	178	143	182	106	36	190
205	174	155	252	236	231	149	178	228	43	63	234
190	216	116	149	236	187	66	150	79	38	218	241
190	224	147	168	227	210	127	102	36	101	255	224
190	214	173	65	103	143	96	56	2	109	249	216
187	196	235	75	1	61	47	0	6	217	255	211
183	202	237	145	0	0	12	108	200	138	243	236
196	206	123	207	177	121	123	200	175	13	96	218

What the computer sees

157	153	174	168	150	152	129	151	172	161	155	156
156	162	163	74	76	62	33	17	110	210	180	154
180	180	50	14	34	6	10	33	48	106	159	181
206	109	5	124	131	111	120	204	166	15	56	180
194	68	137	251	237	239	239	228	227	87	71	201
172	106	207	233	233	214	220	239	228	98	74	206
188	88	179	209	186	215	211	158	139	75	20	169
189	97	165	64	10	168	134	11	31	62	22	148
199	168	191	193	158	227	178	143	182	106	36	190
205	174	155	252	236	231	149	178	228	43	63	234
190	216	116	149	236	187	66	150	79	38	218	241
190	224	147	168	227	210	127	102	36	101	255	224
190	214	173	65	103	143	96	56	2	109	249	216
187	196	235	75	1	61	47	0	6	217	255	211
183	202	237	145	0	0	12	108	200	138	243	236
196	206	123	207	177	121	123	200	175	13	96	218

An image is just a matrix of numbers [0,255]!  
i.e., 1080x1080x3 for an RGB image

# Tasks in Computer Vision



- **Regression:** output variable takes continuous value
- **Classification:** output variable takes class label. Can produce probability of belonging to a particular class

# High Level Feature Detection

Let's identify key features in each image category



Nose,  
Eyes,  
Mouth



Wheels,  
License Plate,  
Headlights



Door,  
Windows,  
Steps

# Manual Feature Extraction

Domain knowledge

Define features

Detect features  
to classify

Problems?

# Manual Feature Extraction

Domain knowledge

Define features

Detect features  
to classify

Viewpoint variation



Illumination conditions



Scale variation



Deformation



Background clutter



Occlusion



Intra-class variation



# Manual Feature Extraction

Domain knowledge

Define features

Detect features  
to classify

Viewpoint variation



Illumination conditions



Scale variation



Deformation



Background clutter



Occlusion



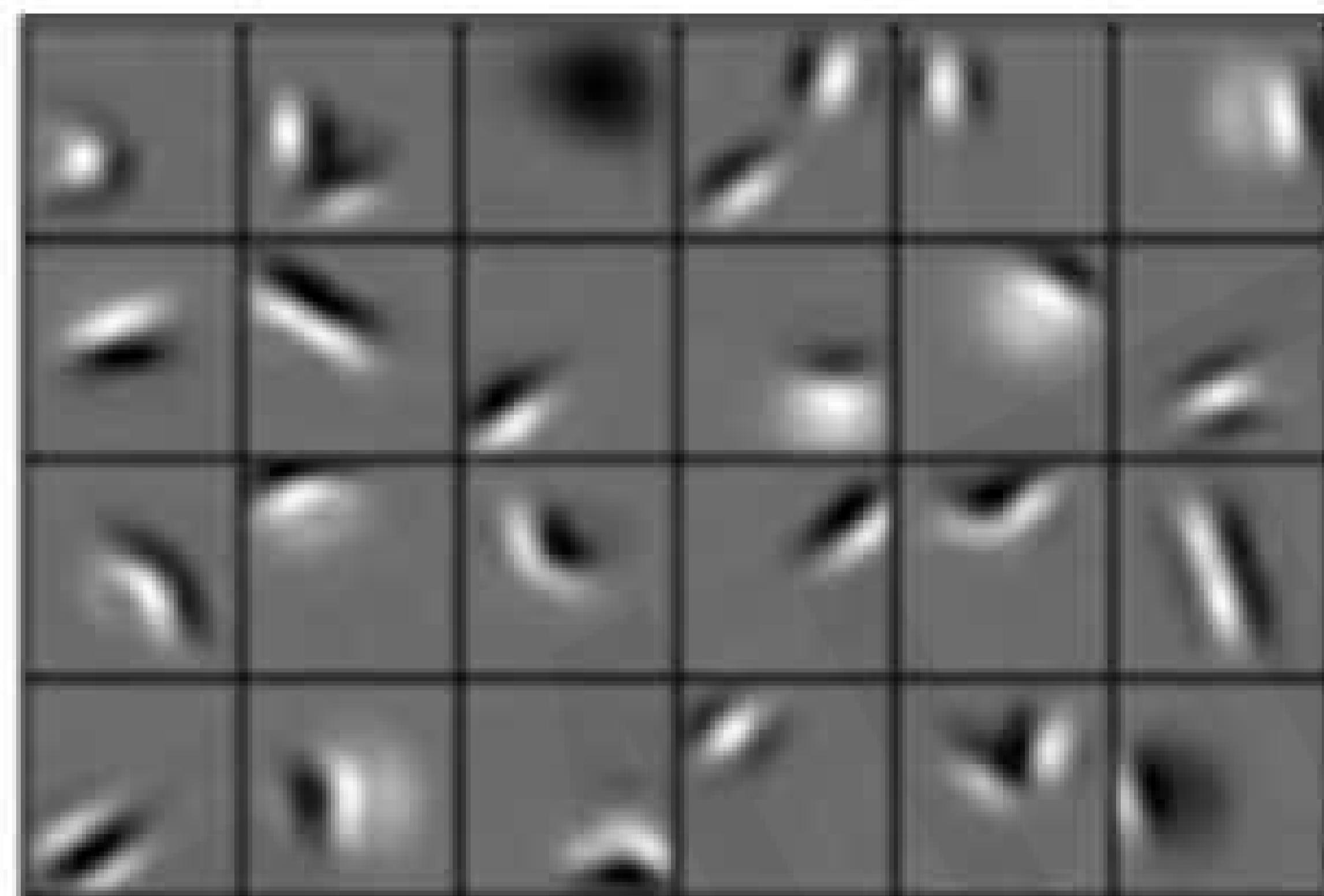
Intra-class variation



# Learning Feature Representations

Can we learn a **hierarchy of features** directly from the data instead of hand engineering?

Low level features



Edges, dark spots

Mid level features



Eyes, ears, nose

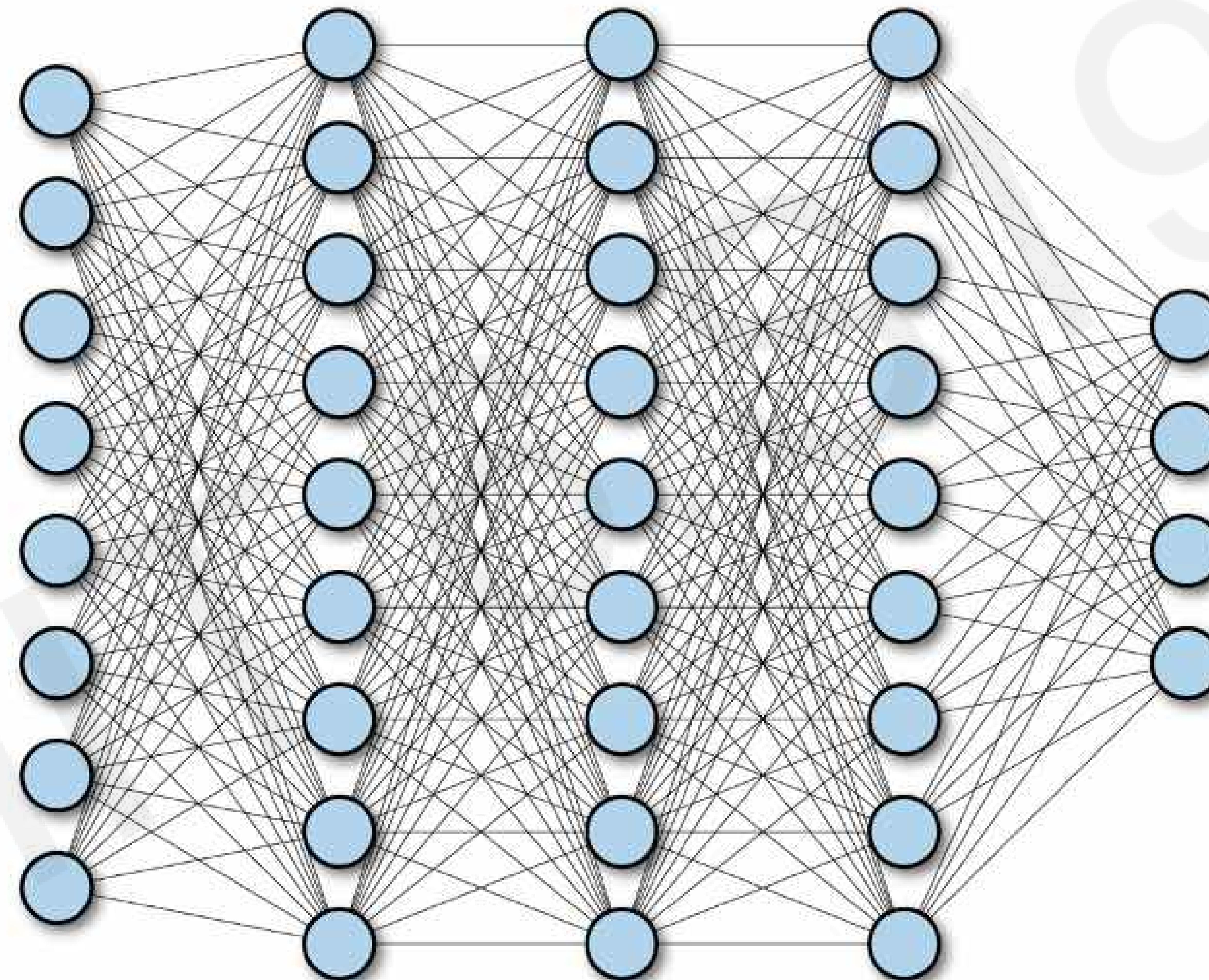
High level features



Facial structure

# Learning Visual Features

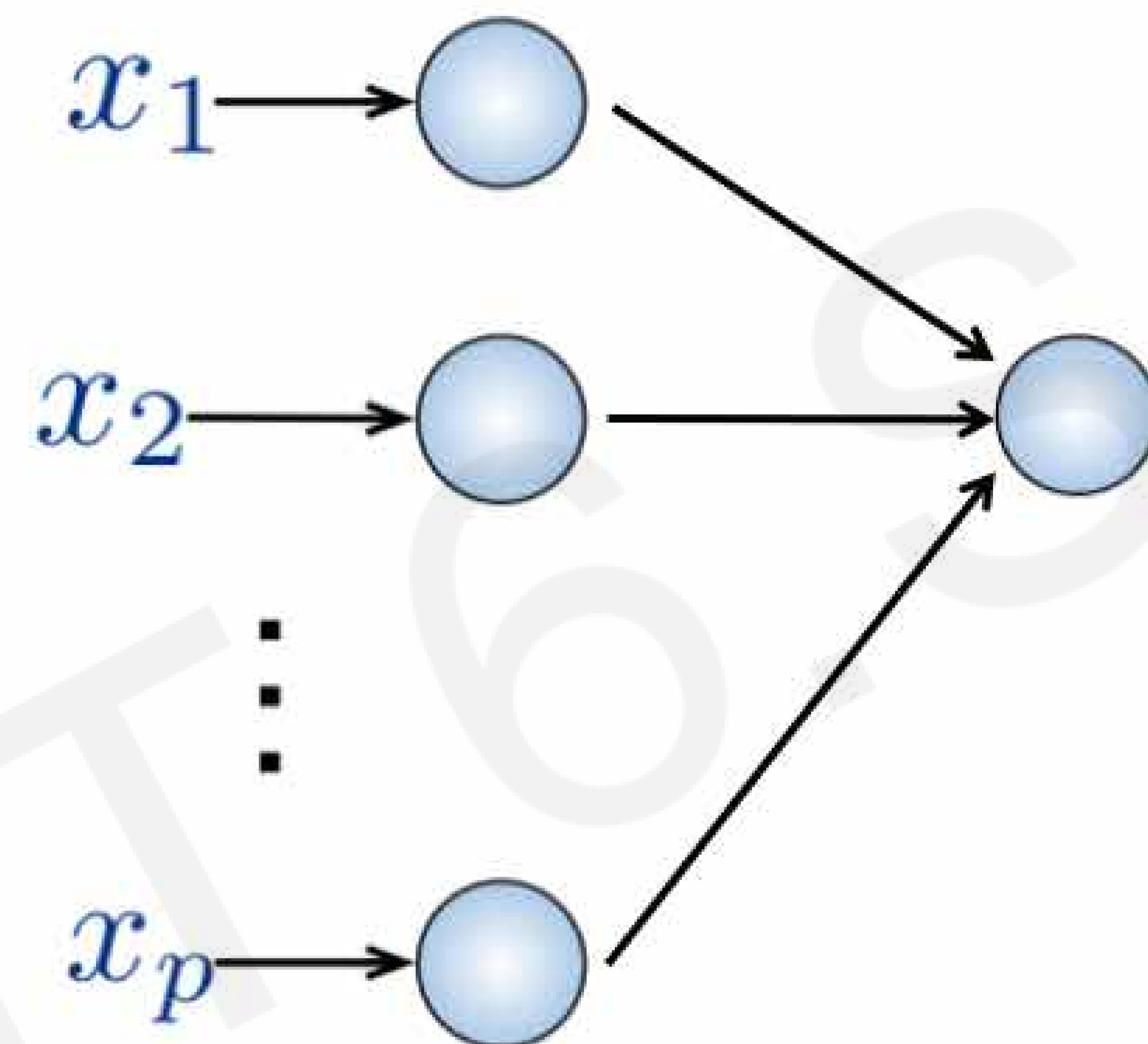
# Fully Connected Neural Network



# Fully Connected Neural Network

## Input:

- 2D image
- Vector of pixel values



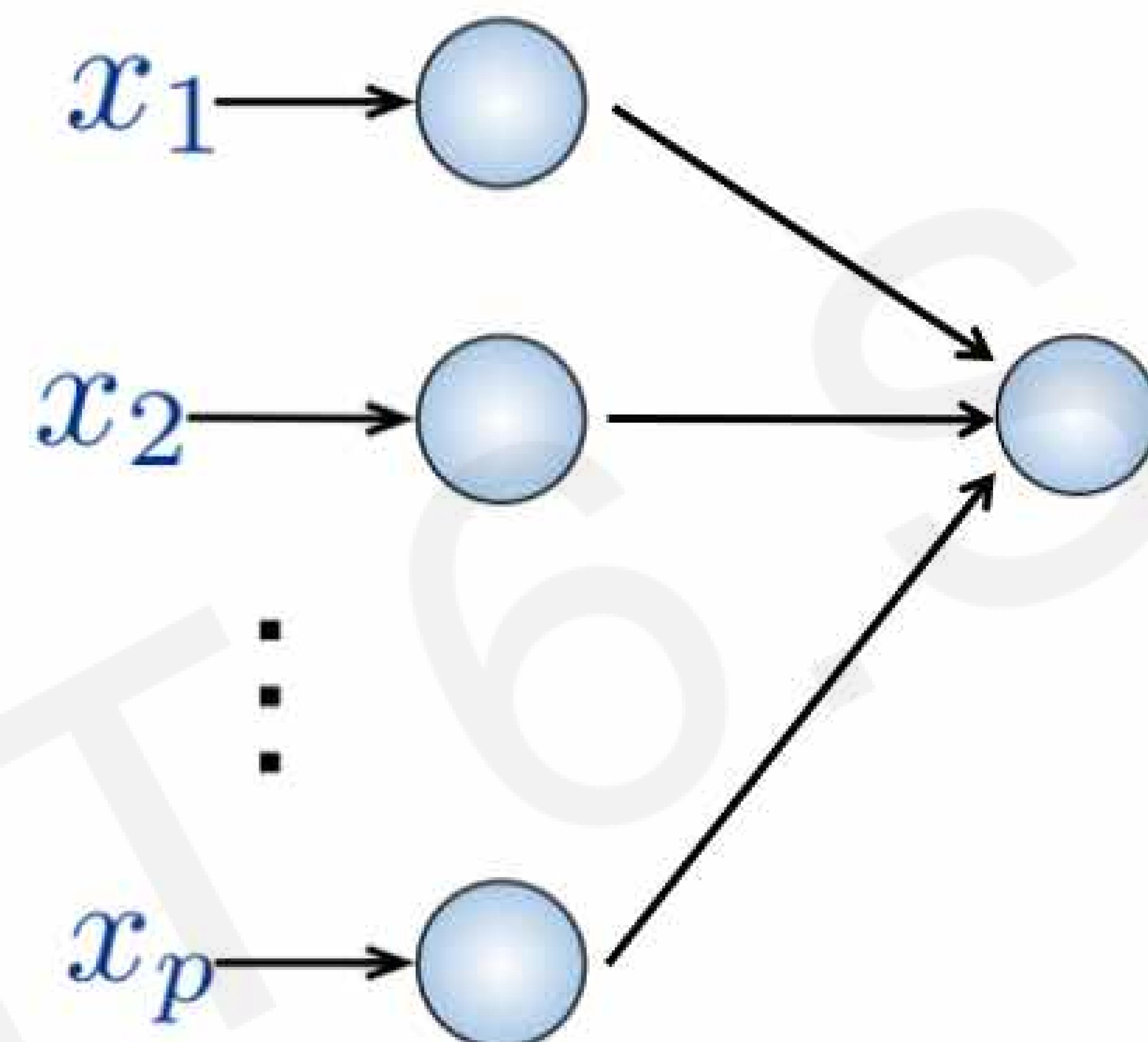
## Fully Connected:

- Connect neuron in hidden layer to all neurons in input layer
- No spatial information!
- And many, many parameters!

# Fully Connected Neural Network

## Input:

- 2D image
- Vector of pixel values



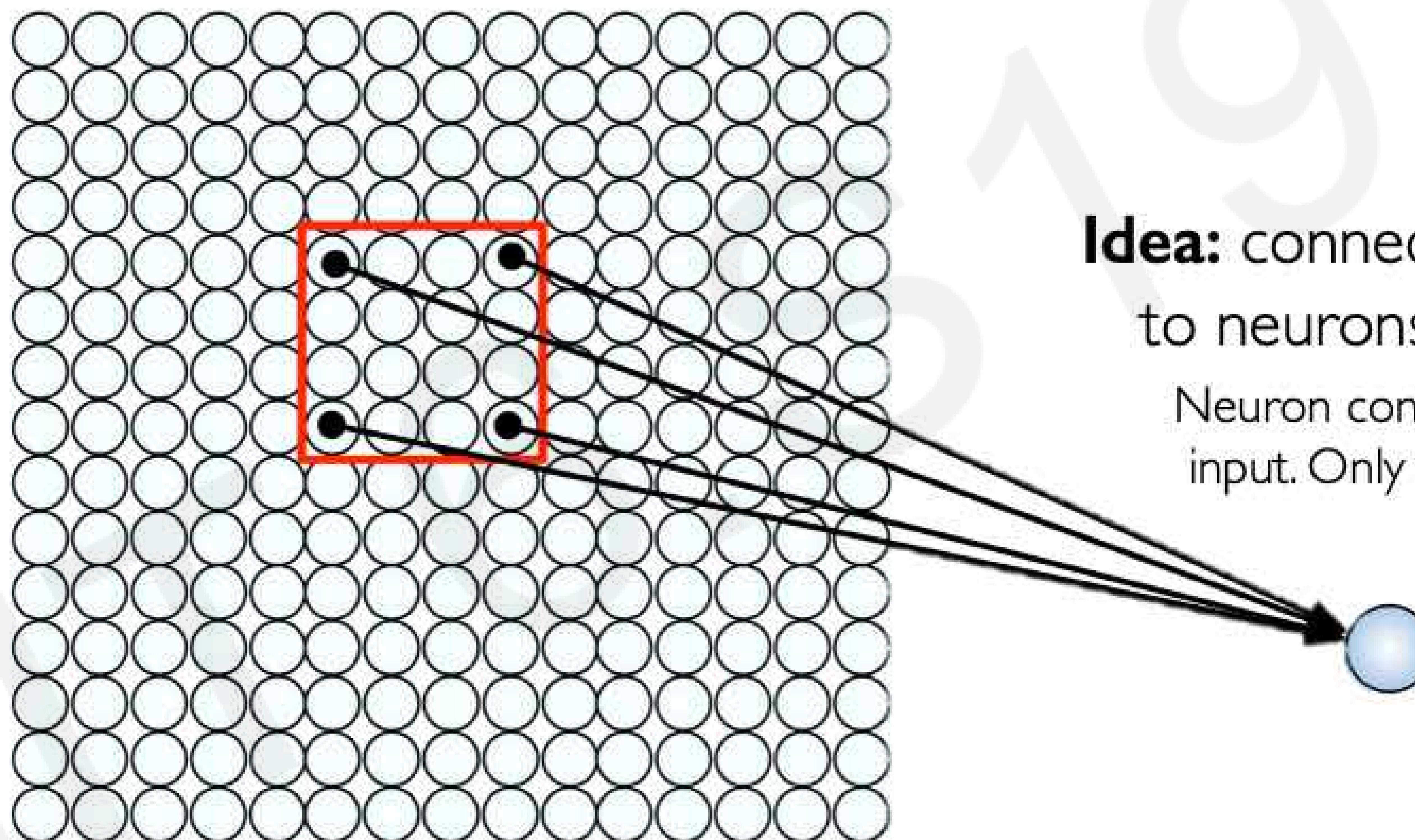
## Fully Connected:

- Connect neuron in hidden layer to all neurons in input layer
- No spatial information!
- And many, many parameters!

How can we use **spatial structure** in the input to inform the architecture of the network?

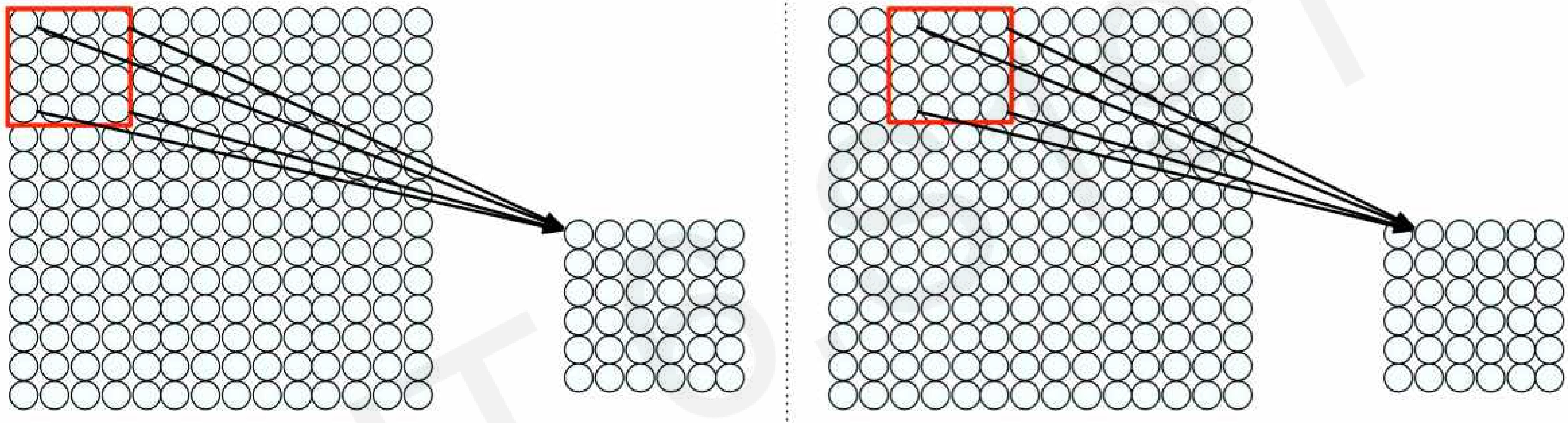
# Using Spatial Structure

**Input:** 2D image.  
Array of pixel values



**Idea:** connect patches of input  
to neurons in hidden layer.  
Neuron connected to region of  
input. Only "sees" these values.

# Using Spatial Structure

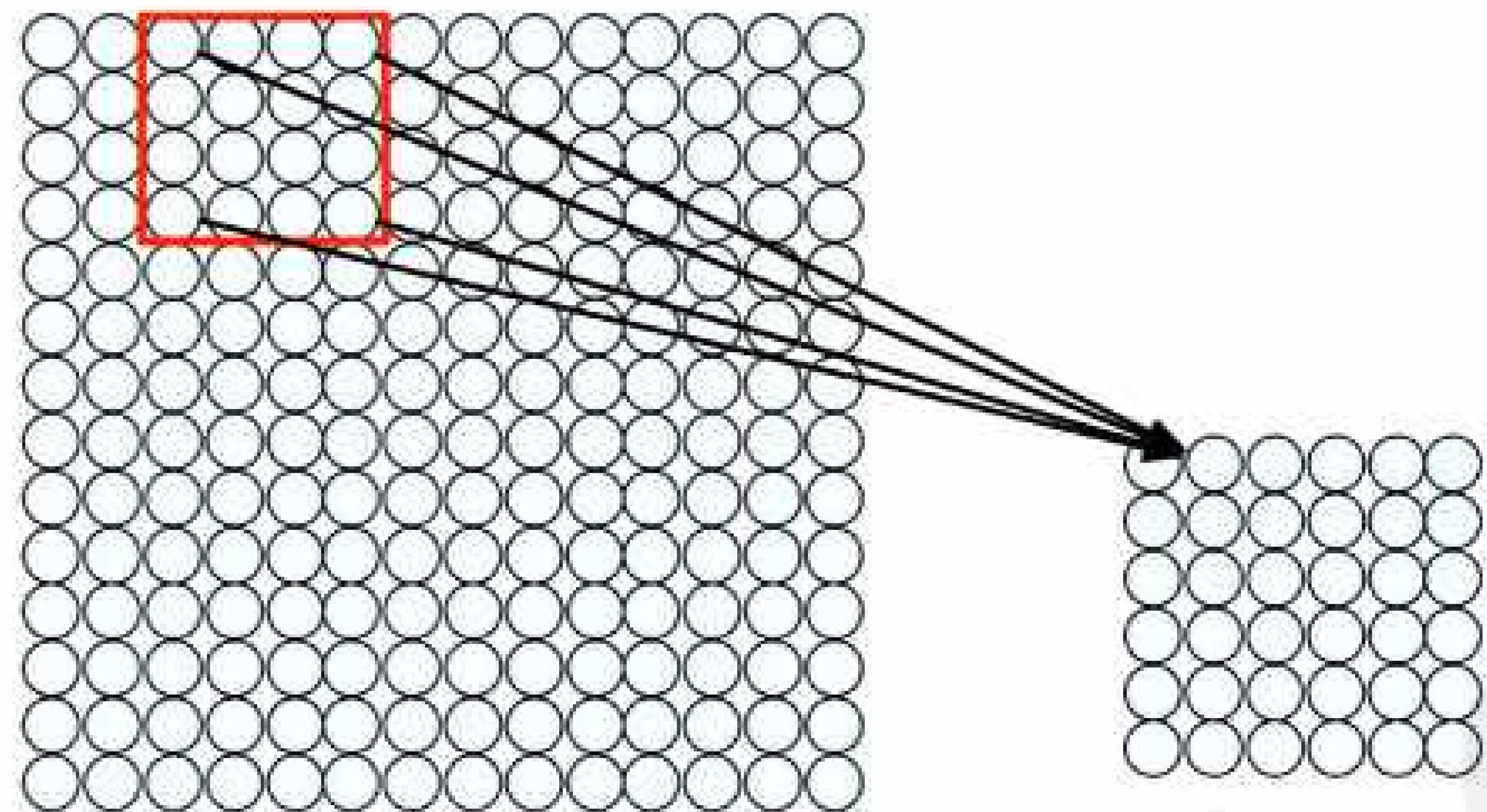


Connect patch in input layer to a single neuron in subsequent layer.  
Use a sliding window to define connections.  
How can we **weight** the patch to detect particular features?

# Applying Filters to Extract Features

- 1) Apply a set of weights – a filter – to extract **local features**
- 2) Use **multiple filters** to extract different features
- 3) Spatially **share** parameters of each filter  
(features that matter in one part of the input should matter elsewhere)

# Feature Extraction with Convolution



- Filter of size  $4 \times 4$  : 16 different weights
- Apply this same filter to  $4 \times 4$  patches in input
- Shift by 2 pixels for next patch

This “patchy” operation is **convolution**

- 1) Apply a set of weights – a filter – to extract **local features**
- 2) Use **multiple filters** to extract different features
- 3) **Spatially share** parameters of each filter

# Feature Extraction and Convolution

## A Case Study

# X or X?

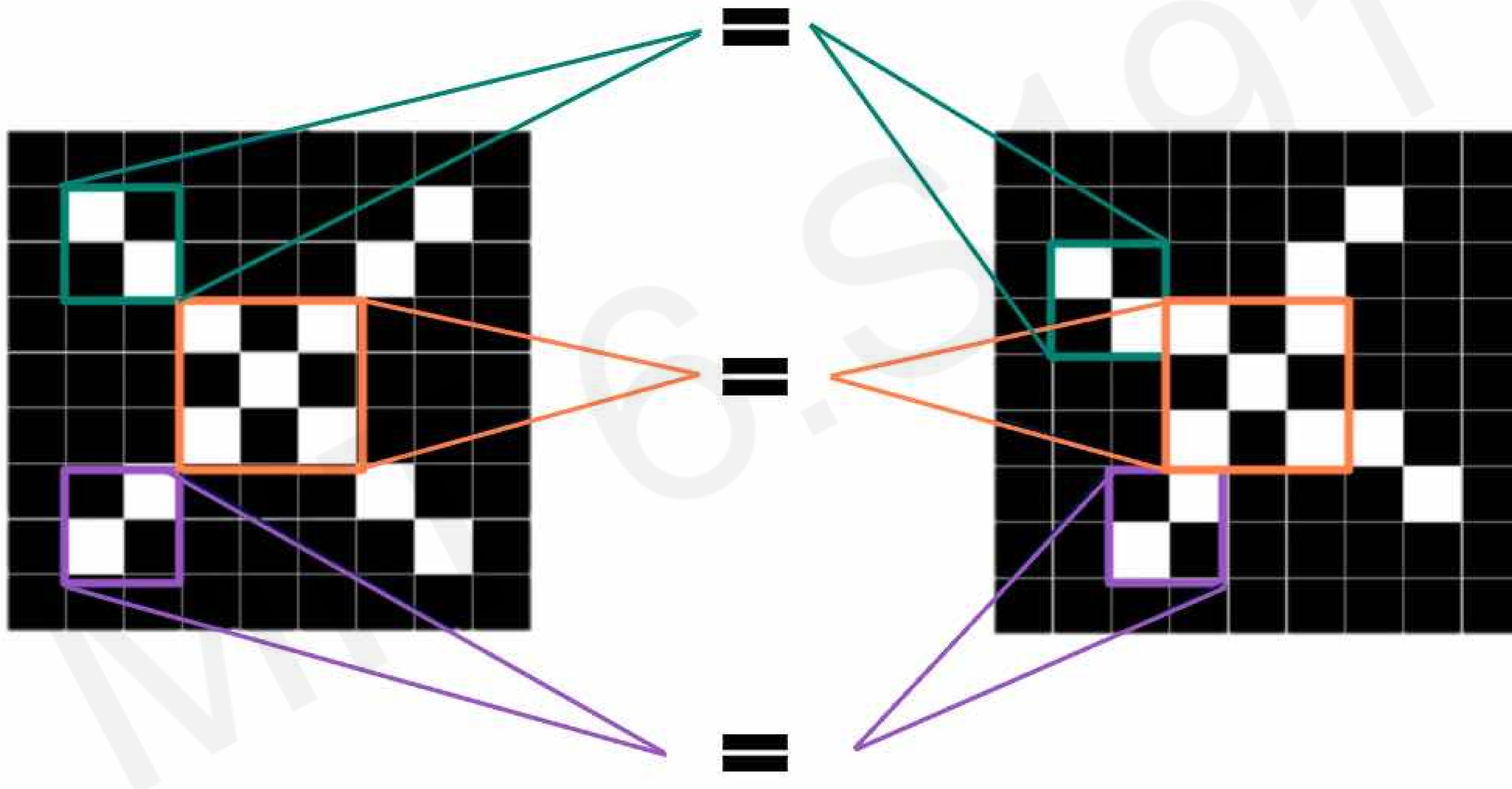
-1	-1	-1	-1	-1	-1	-1	-1	-1
-1	1	-1	-1	-1	-1	-1	1	-1
-1	-1	1	-1	-1	-1	1	-1	-1
-1	-1	-1	1	-1	1	-1	-1	-1
-1	-1	-1	-1	1	-1	-1	-1	-1
-1	-1	-1	-1	1	-1	-1	-1	-1
-1	-1	-1	1	-1	1	-1	-1	-1
-1	-1	1	-1	-1	-1	1	-1	-1
-1	1	-1	-1	-1	-1	1	-1	-1
-1	-1	-1	-1	-1	-1	-1	-1	-1



-1	-1	-1	-1	-1	-1	-1	-1	-1
-1	-1	-1	-1	-1	-1	-1	1	-1
-1	1	-1	-1	-1	-1	1	-1	-1
-1	-1	1	1	-1	-1	-1	-1	-1
-1	-1	-1	-1	1	-1	-1	-1	-1
-1	-1	-1	-1	1	-1	-1	-1	-1
-1	-1	-1	1	-1	1	-1	-1	-1
-1	-1	-1	1	-1	1	-1	-1	-1
-1	-1	1	-1	-1	-1	1	-1	-1
-1	1	-1	-1	-1	-1	1	-1	-1
-1	-1	-1	-1	-1	-1	-1	-1	-1

Image is represented as matrix of pixel values... and computers are literal!  
We want to be able to classify an X as an X even if it's shifted, shrunk, rotated, deformed.

# Features of X



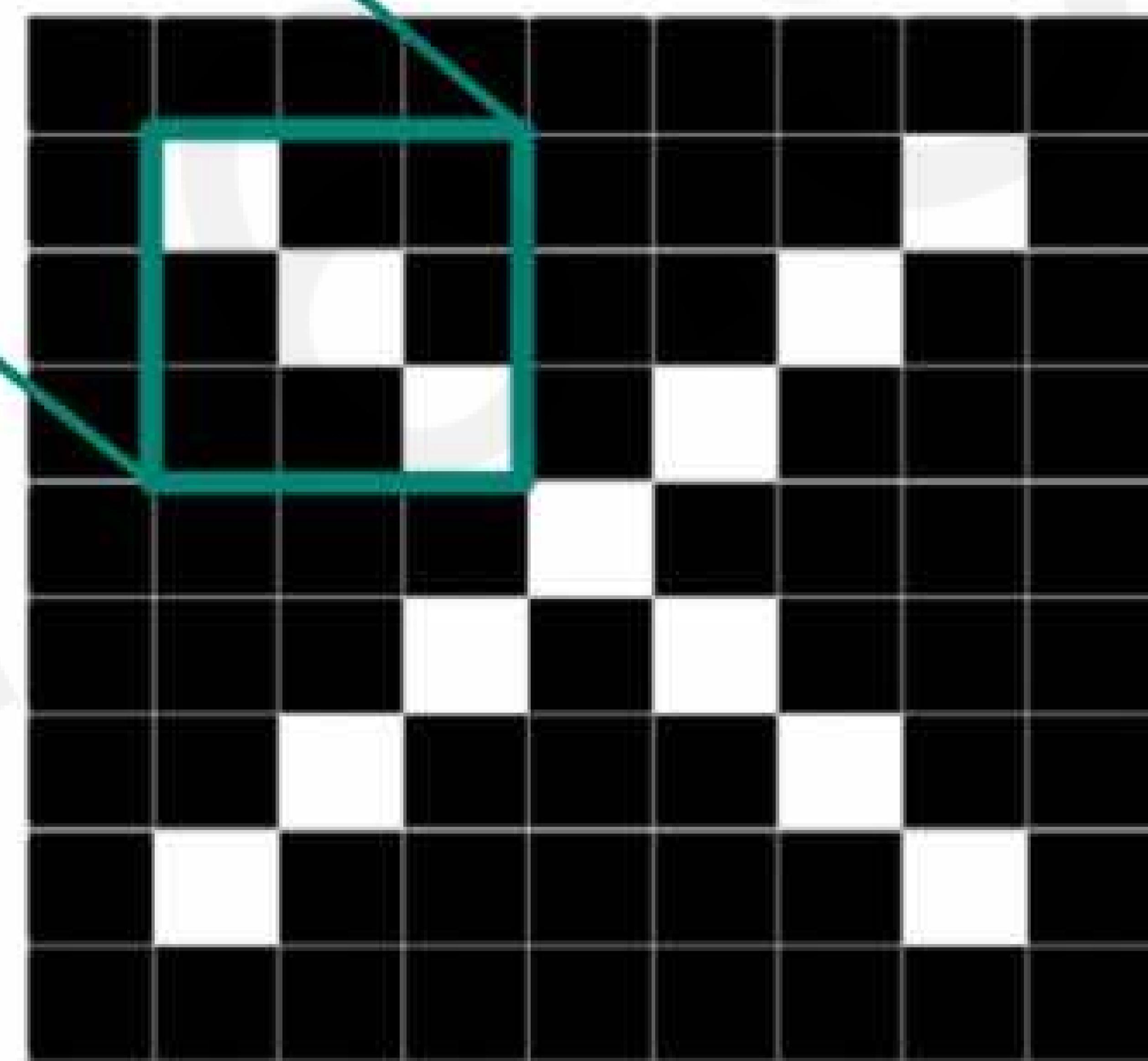
# Filters to Detect X Features

filters

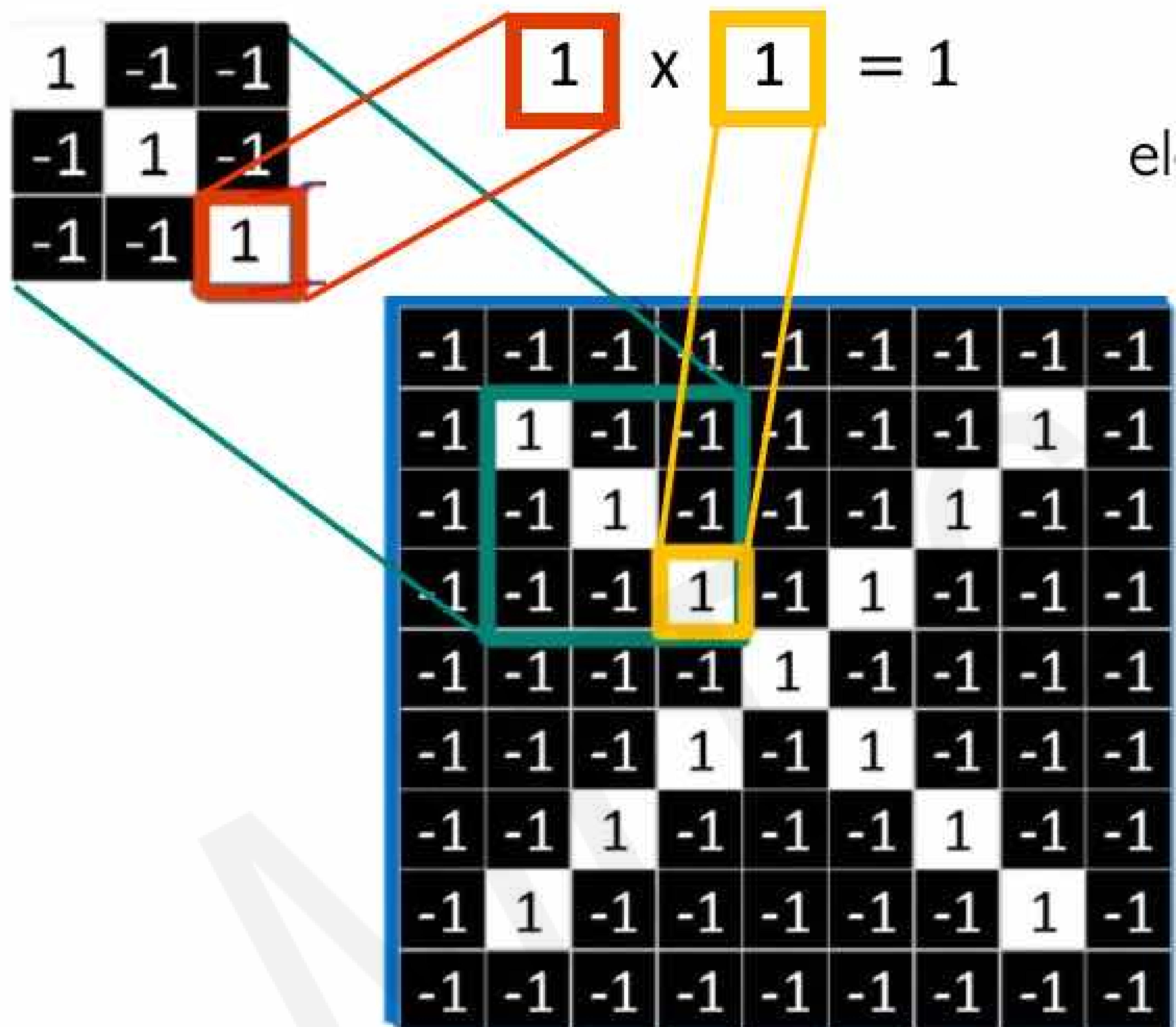
$$\begin{matrix} 1 & -1 & -1 \\ -1 & 1 & -1 \\ -1 & -1 & 1 \end{matrix}$$

$$\begin{matrix} 1 & -1 & 1 \\ -1 & 1 & -1 \\ 1 & -1 & 1 \end{matrix}$$

$$\begin{matrix} -1 & -1 & 1 \\ -1 & 1 & -1 \\ 1 & -1 & -1 \end{matrix}$$



# The Convolution Operation

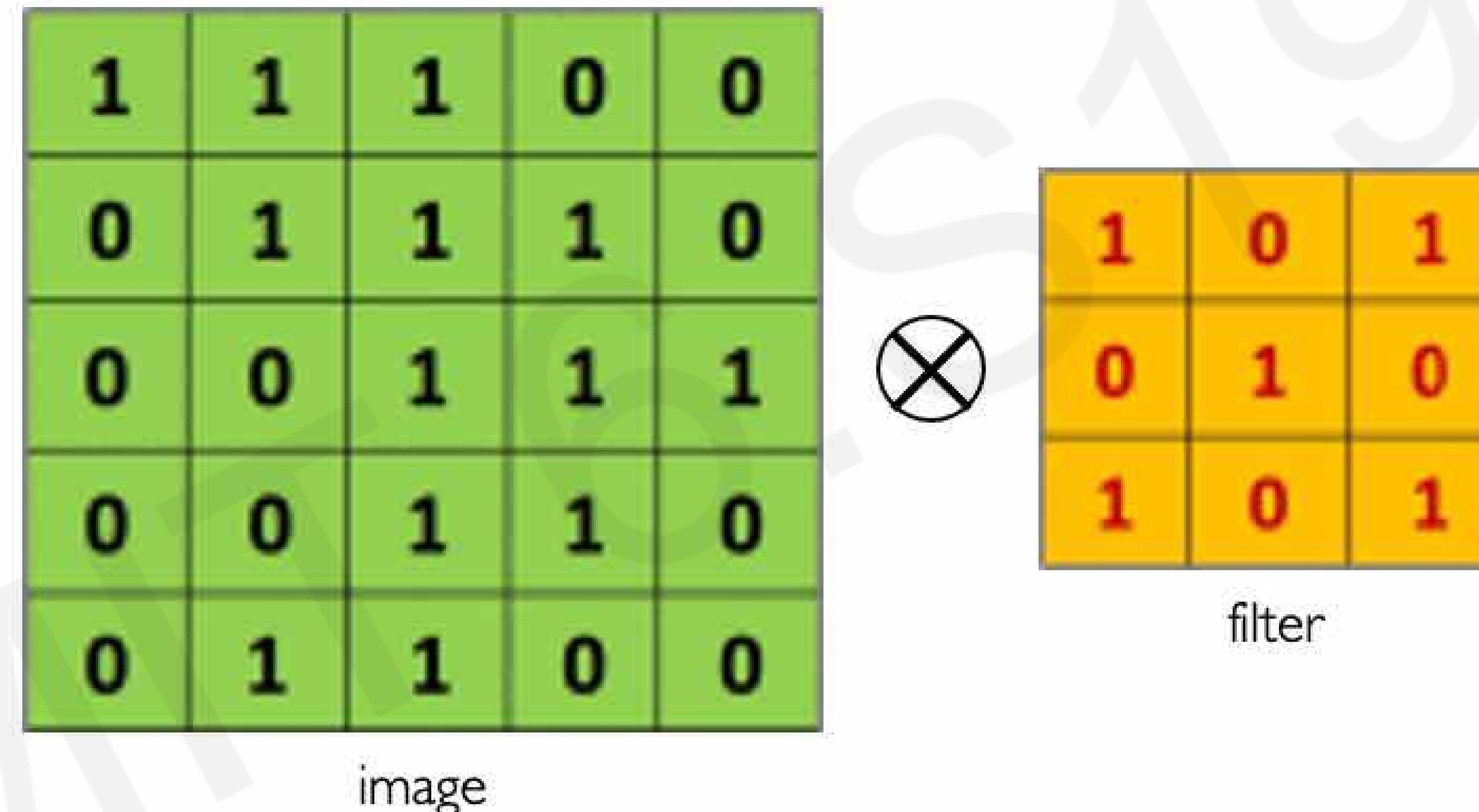


element wise multiply

add outputs

# The Convolution Operation

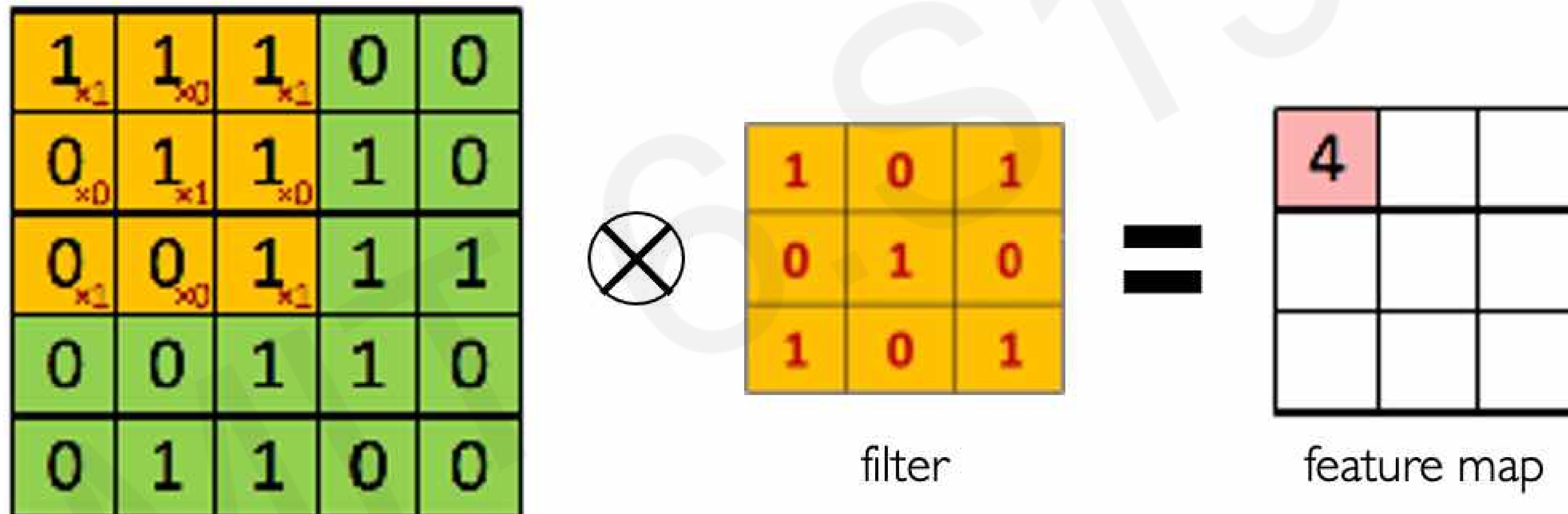
Suppose we want to compute the convolution of a 5x5 image and a 3x3 filter:



We slide the 3x3 filter over the input image, element-wise multiply, and add the outputs...

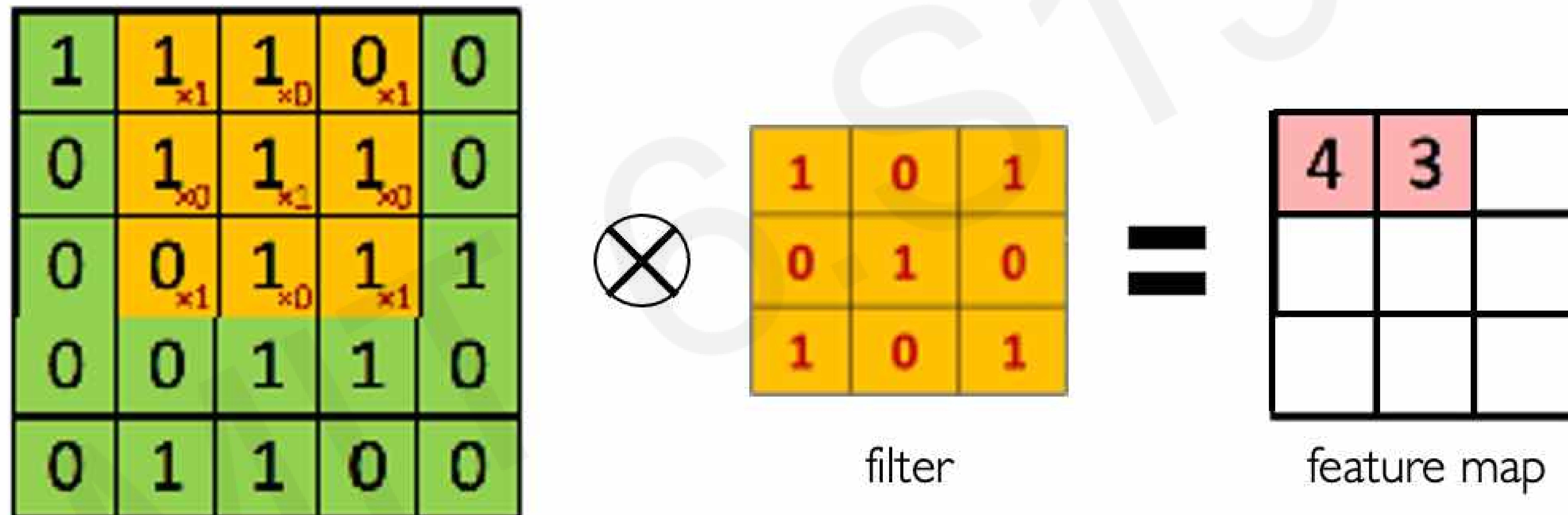
# The Convolution Operation

We slide the  $3 \times 3$  filter over the input image, element-wise multiply, and add the outputs:



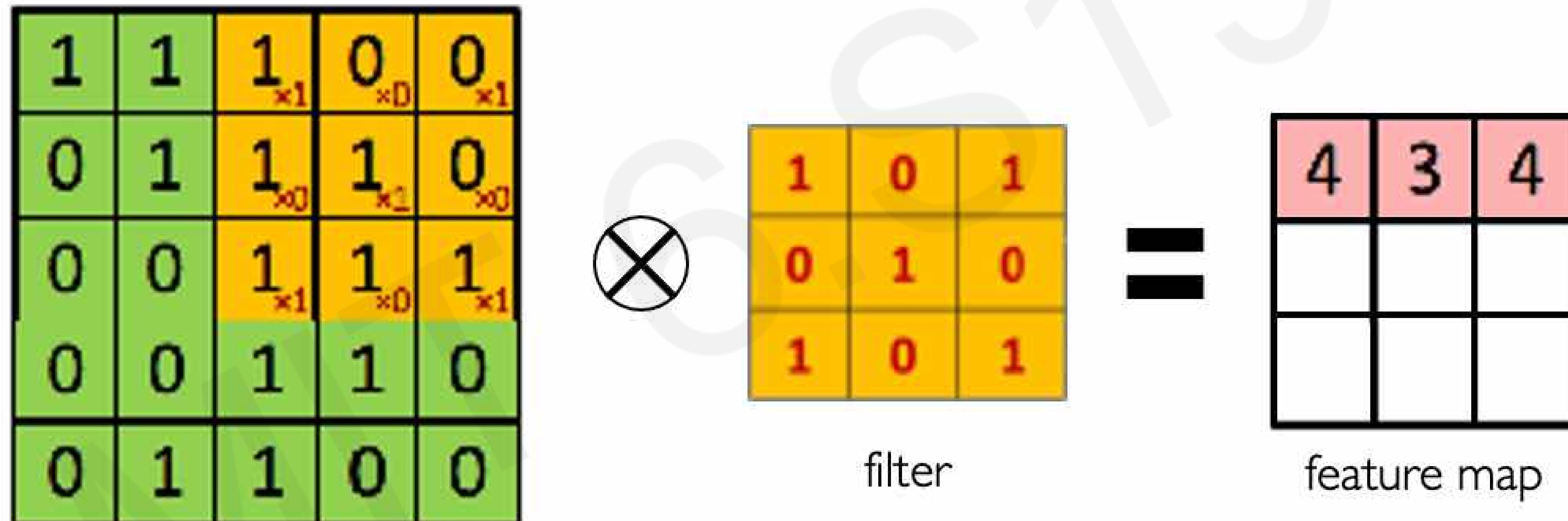
# The Convolution Operation

We slide the  $3 \times 3$  filter over the input image, element-wise multiply, and add the outputs:



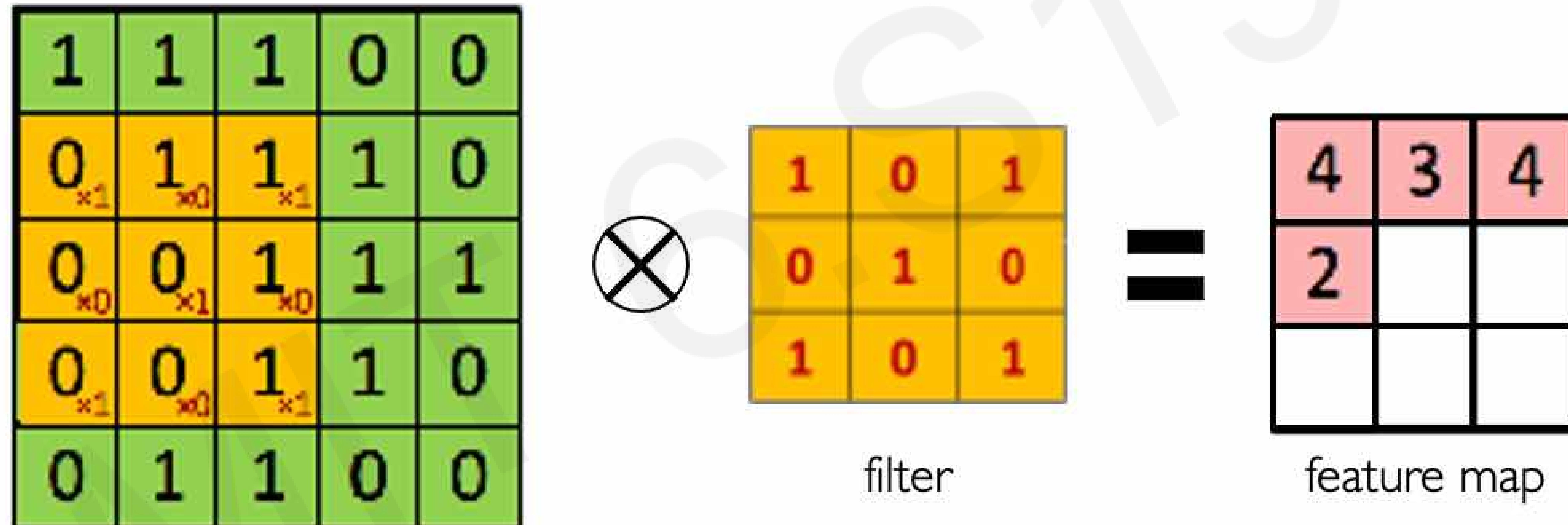
# The Convolution Operation

We slide the 3x3 filter over the input image, element-wise multiply, and add the outputs:



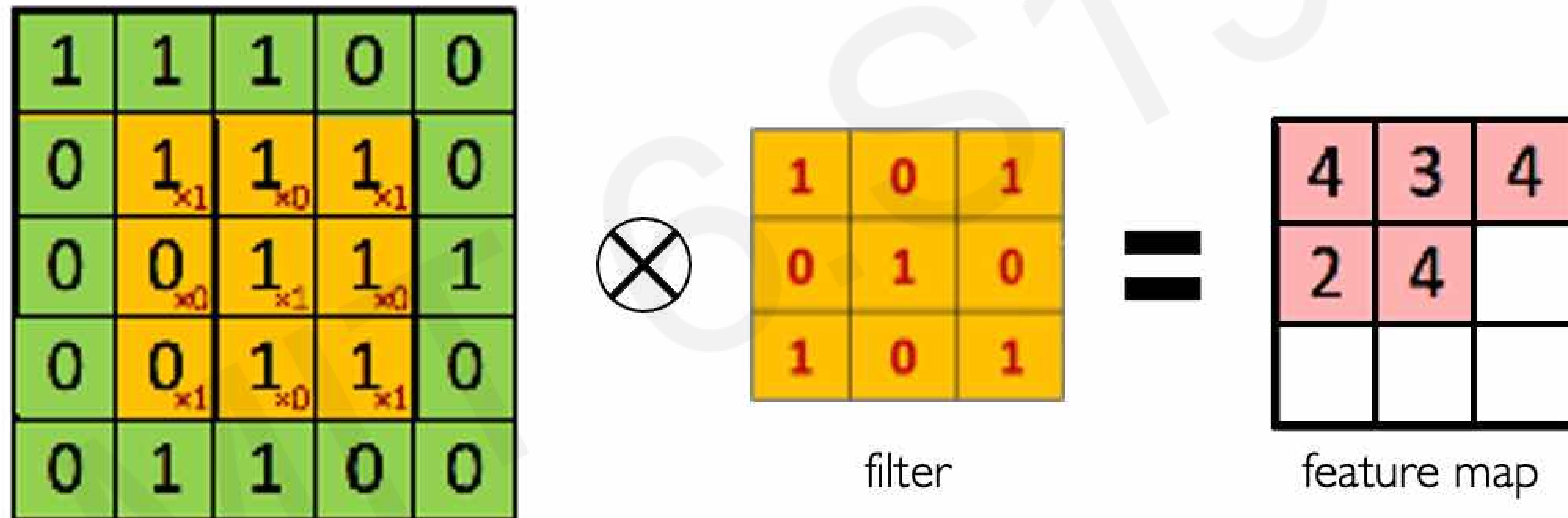
# The Convolution Operation

We slide the  $3 \times 3$  filter over the input image, element-wise multiply, and add the outputs:



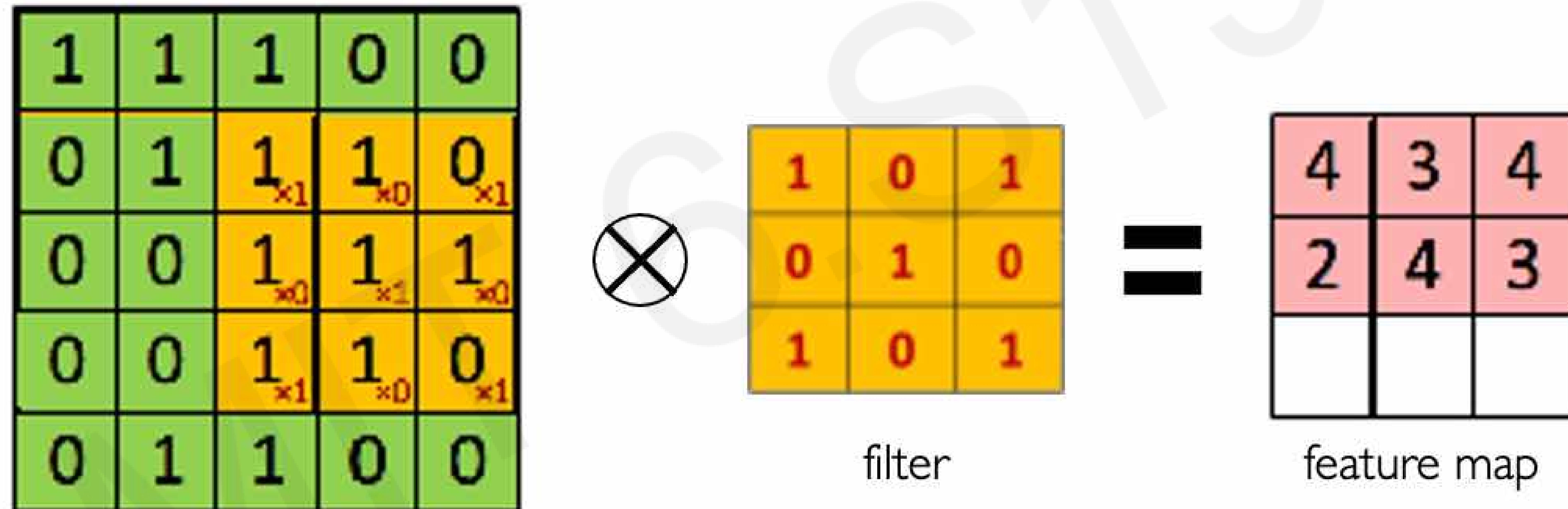
# The Convolution Operation

We slide the 3x3 filter over the input image, element-wise multiply, and add the outputs:



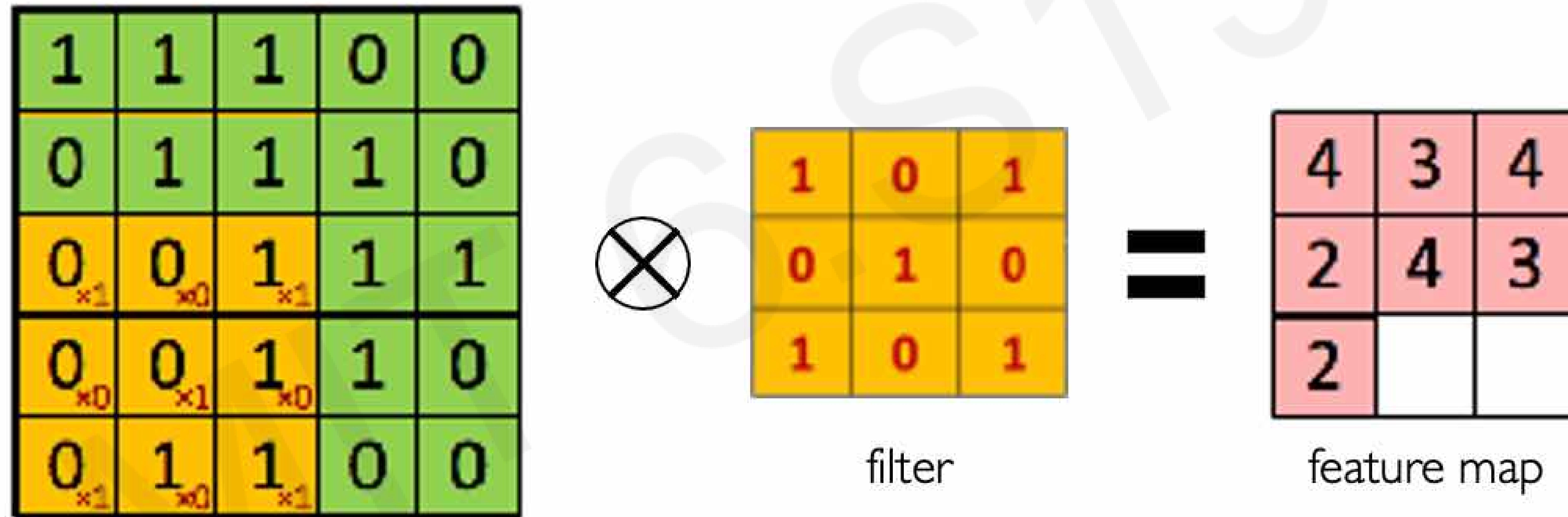
# The Convolution Operation

We slide the 3x3 filter over the input image, element-wise multiply, and add the outputs:



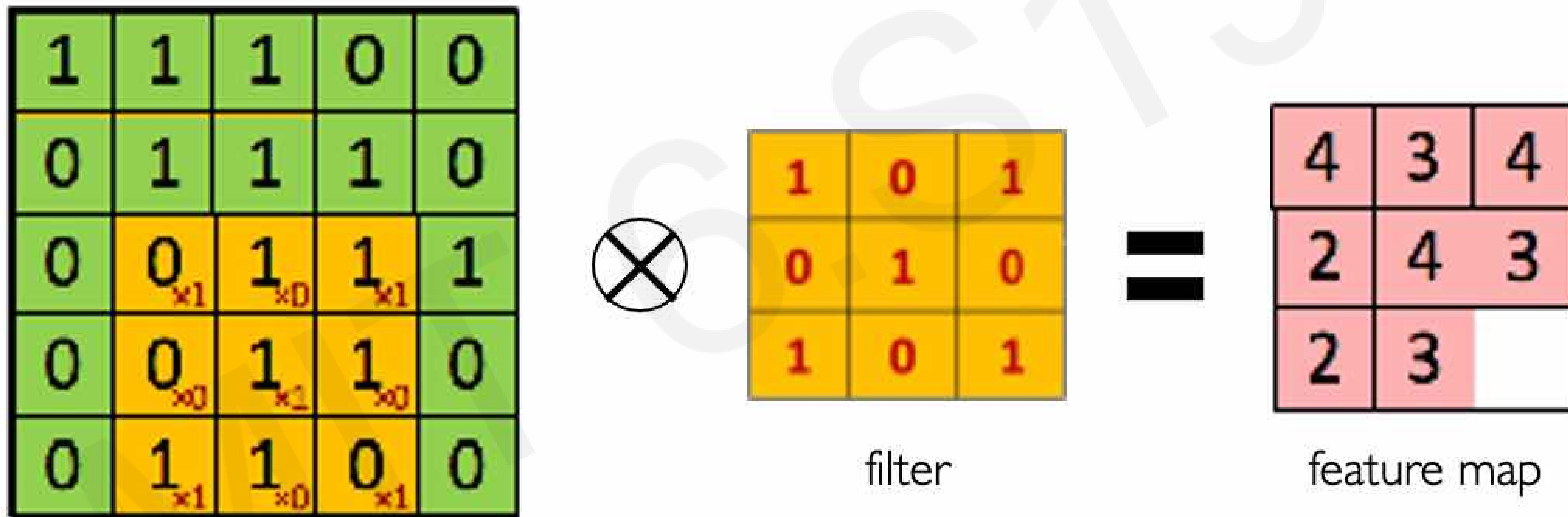
# The Convolution Operation

We slide the 3x3 filter over the input image, element-wise multiply, and add the outputs:



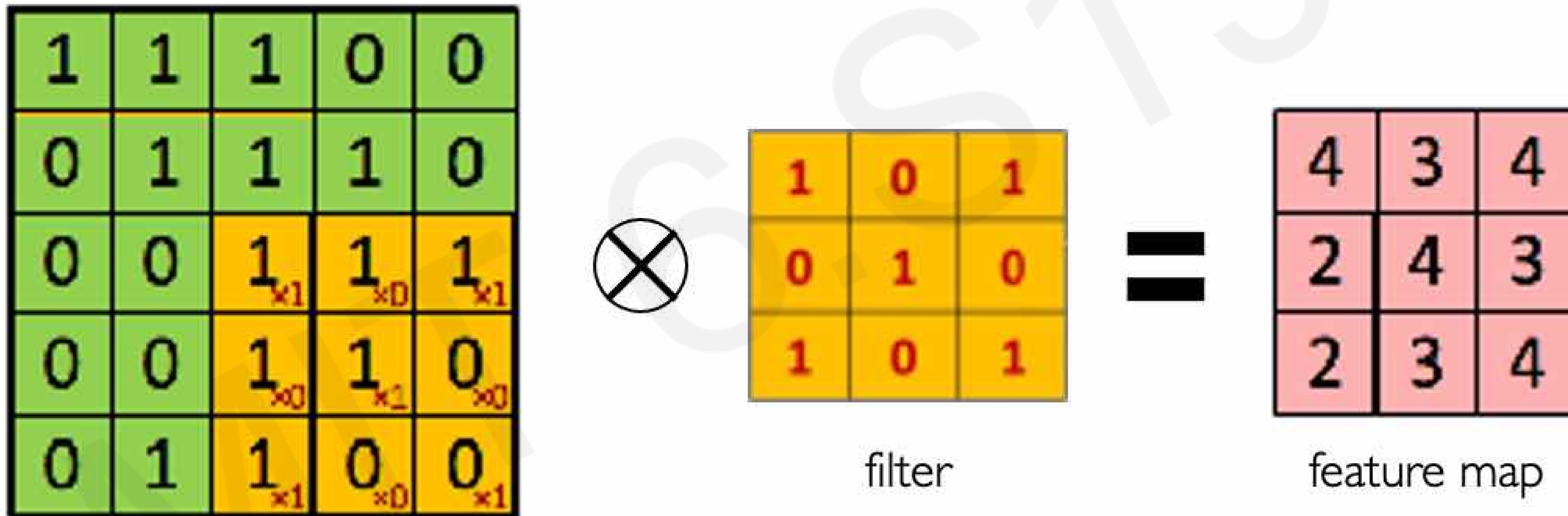
# The Convolution Operation

We slide the 3x3 filter over the input image, element-wise multiply, and add the outputs:



# The Convolution Operation

We slide the 3x3 filter over the input image, element-wise multiply, and add the outputs:



# Producing Feature Maps



Original



Sharpen

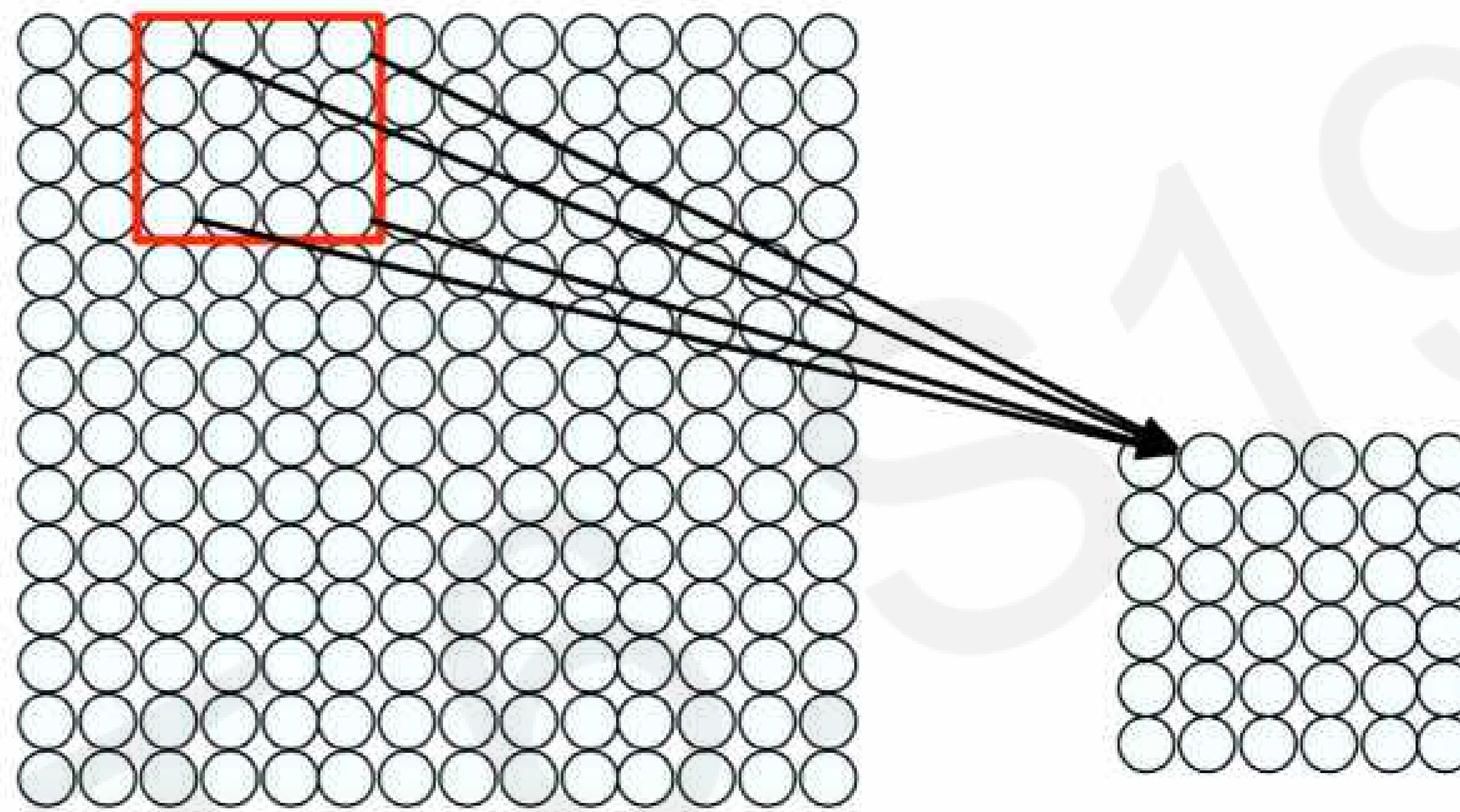


Edge Detect



"Strong" Edge  
Detect

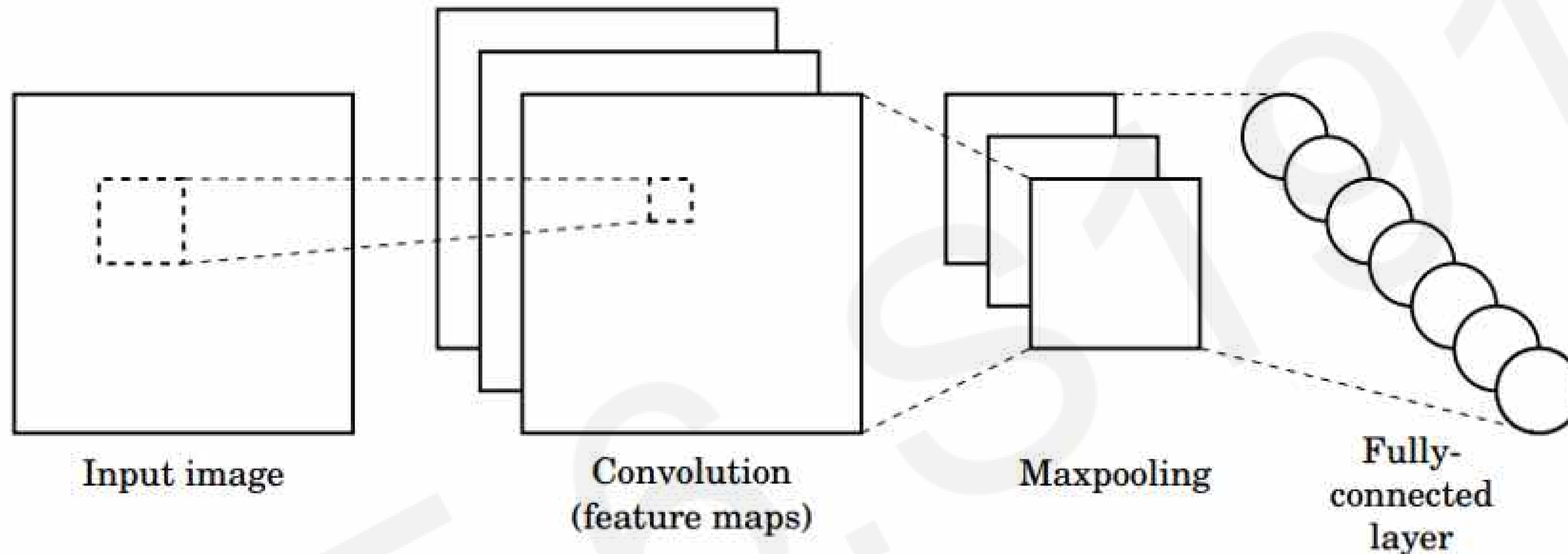
# Feature Extraction with Convolution



- 1) Apply a set of weights – a filter – to extract **local features**
- 2) Use **multiple filters** to extract different features
- 3) **Spatially share** parameters of each filter

# Convolutional Neural Networks (CNNs)

# CNNs for Classification



- 1. Convolution:** Apply filters to generate feature maps.
- 2. Non-linearity:** Often ReLU.
- 3. Pooling:** Downsampling operation on each feature map.

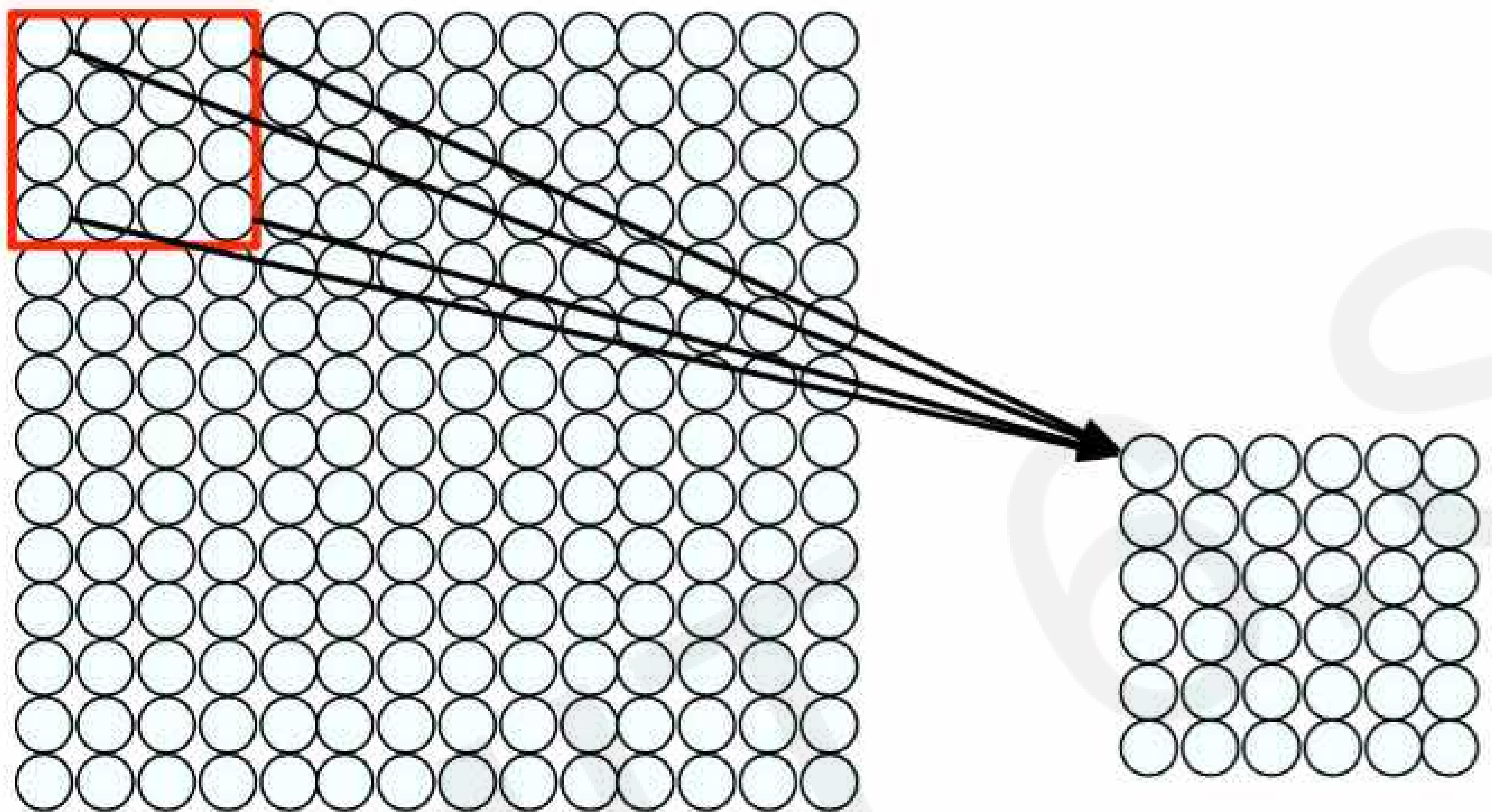
 `tf.keras.layers.Conv2D`

 `tf.keras.activations.*`

 `tf.keras.layers.MaxPool2D`

**Train model with image data.**  
**Learn weights of filters in convolutional layers.**

# Convolutional Layers: Local Connectivity

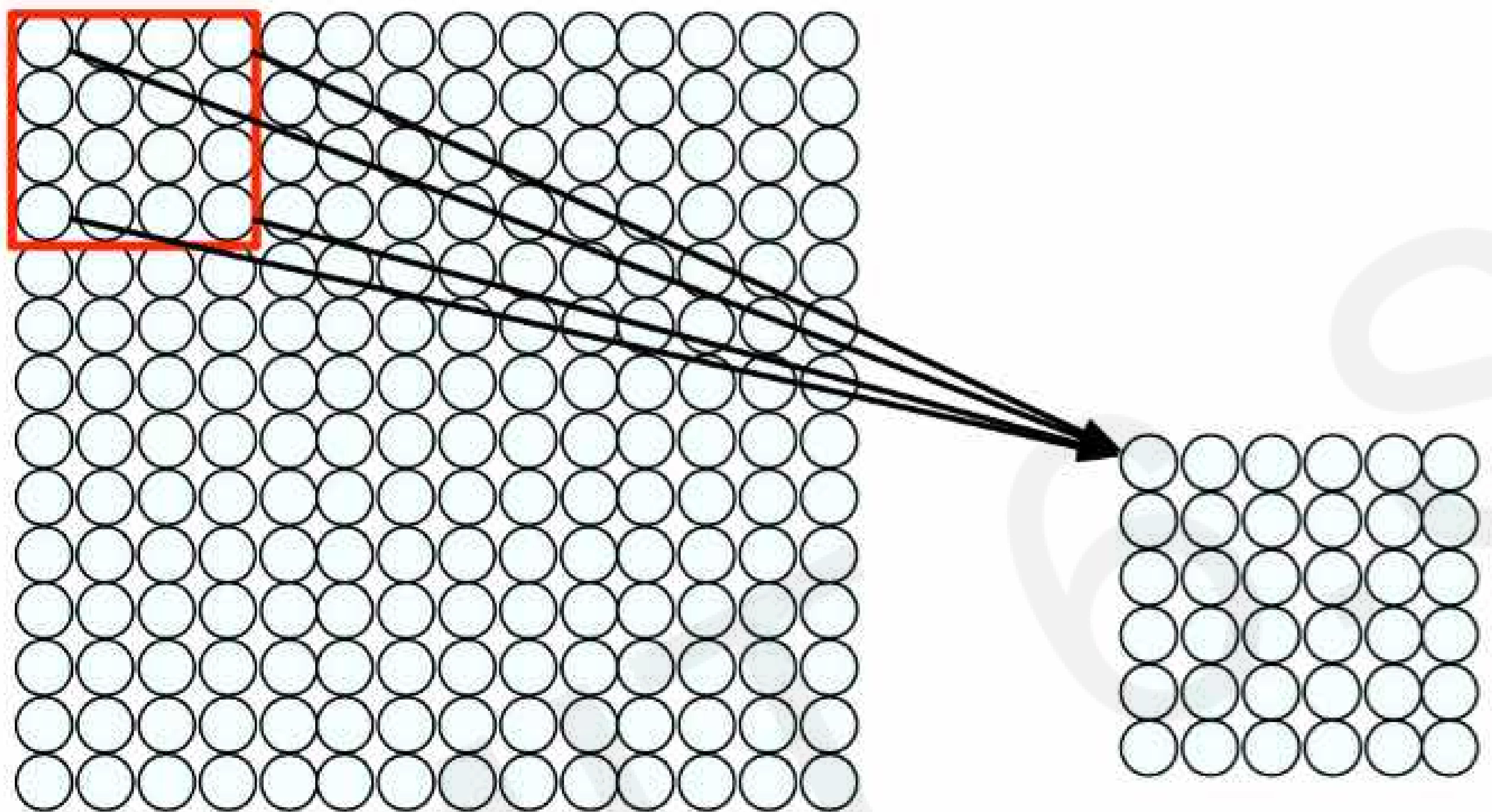


 `tf.keras.layers.Conv2D`

**For a neuron in hidden layer:**

- Take inputs from patch
- Compute weighted sum
- Apply bias

# Convolutional Layers: Local Connectivity



4x4 filter: matrix of weights  $w_{ij}$

$$\sum_{i=1}^4 \sum_{j=1}^4 w_{ij} x_{i+p,j+q} + b$$

for neuron  $(p,q)$  in hidden layer



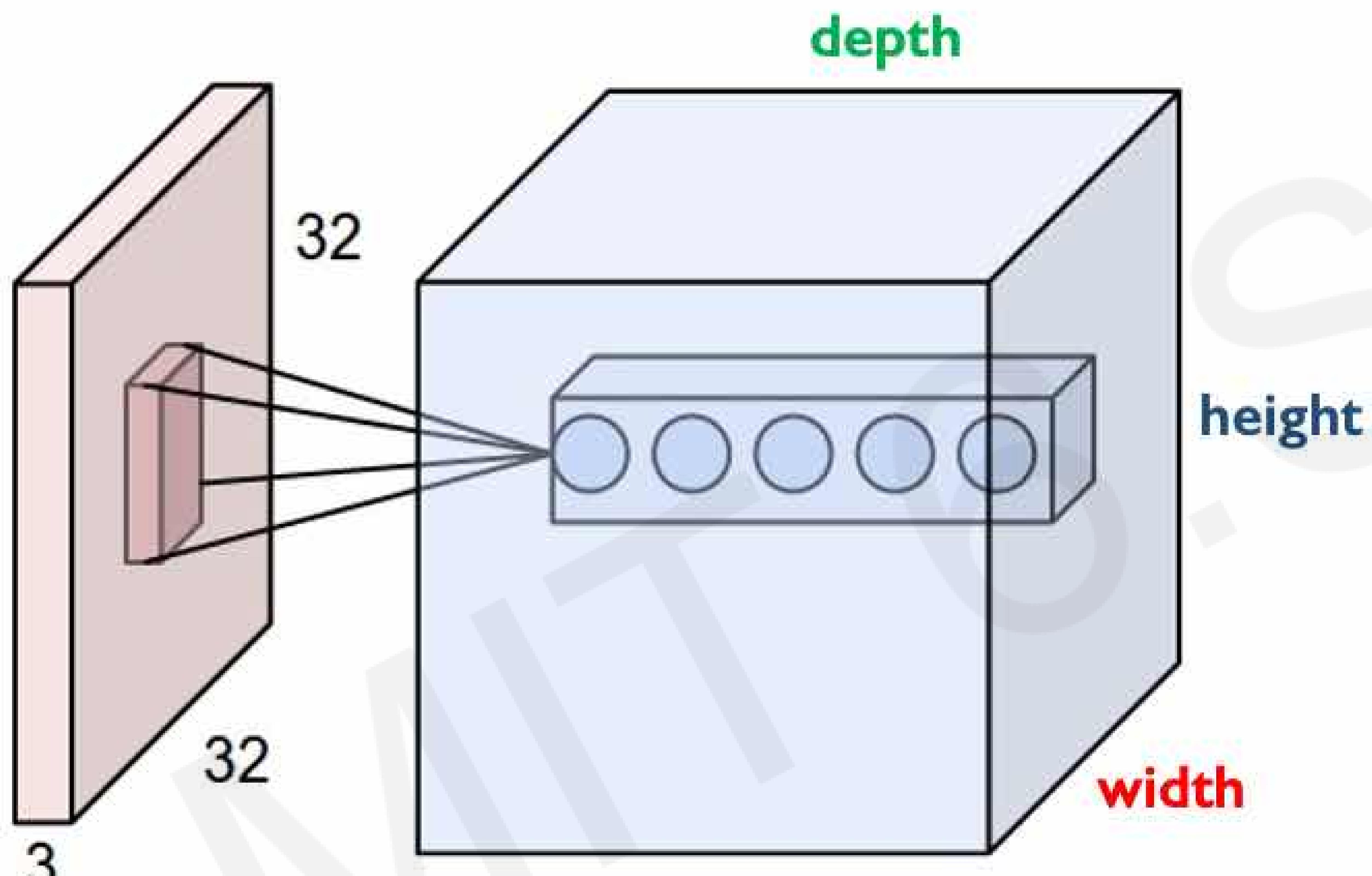
`tf.keras.layers.Conv2D`

**For a neuron in hidden layer:**

- Take inputs from patch
- Compute weighted sum
- Apply bias

- 1) applying a window of weights
- 2) computing linear combinations
- 3) activating with non-linear function

# CNNs: Spatial Arrangement of Output Volume



**Layer Dimensions:**

$h \times w \times d$

where  $h$  and  $w$  are spatial dimensions  
 $d$  (depth) = number of filters

**Stride:**

Filter step size

**Receptive Field:**

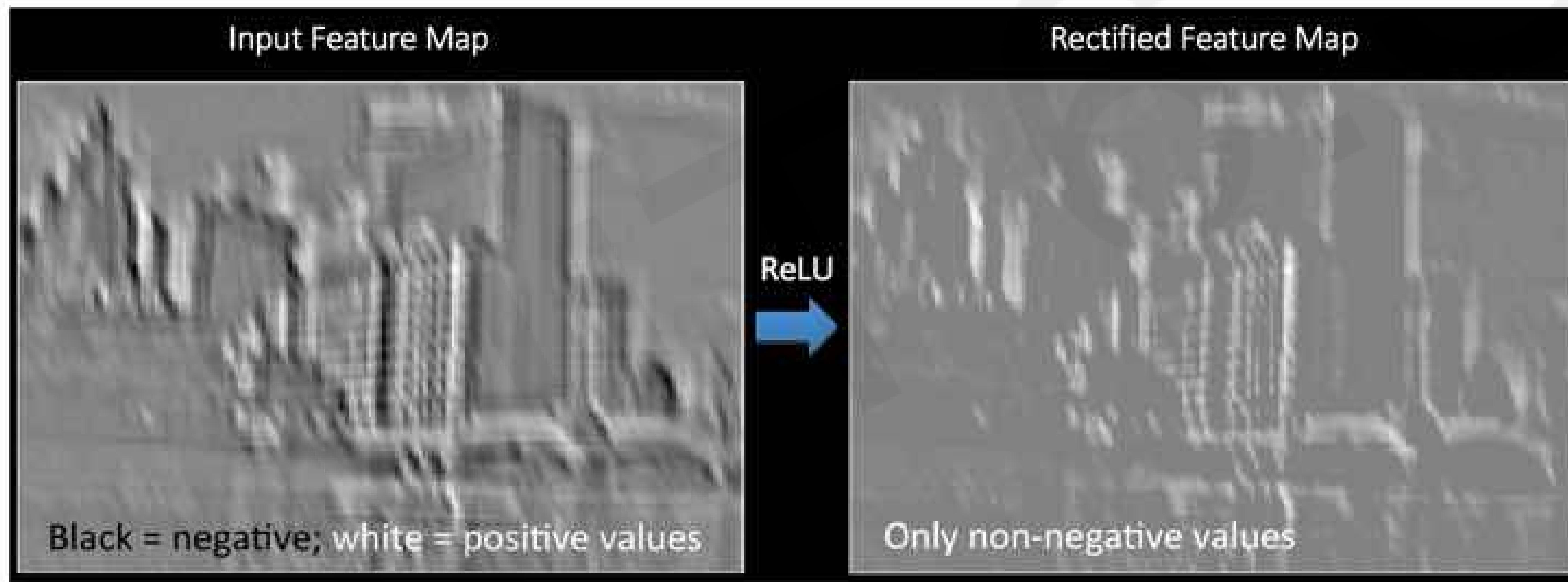
Locations in input image that  
a node is path connected to



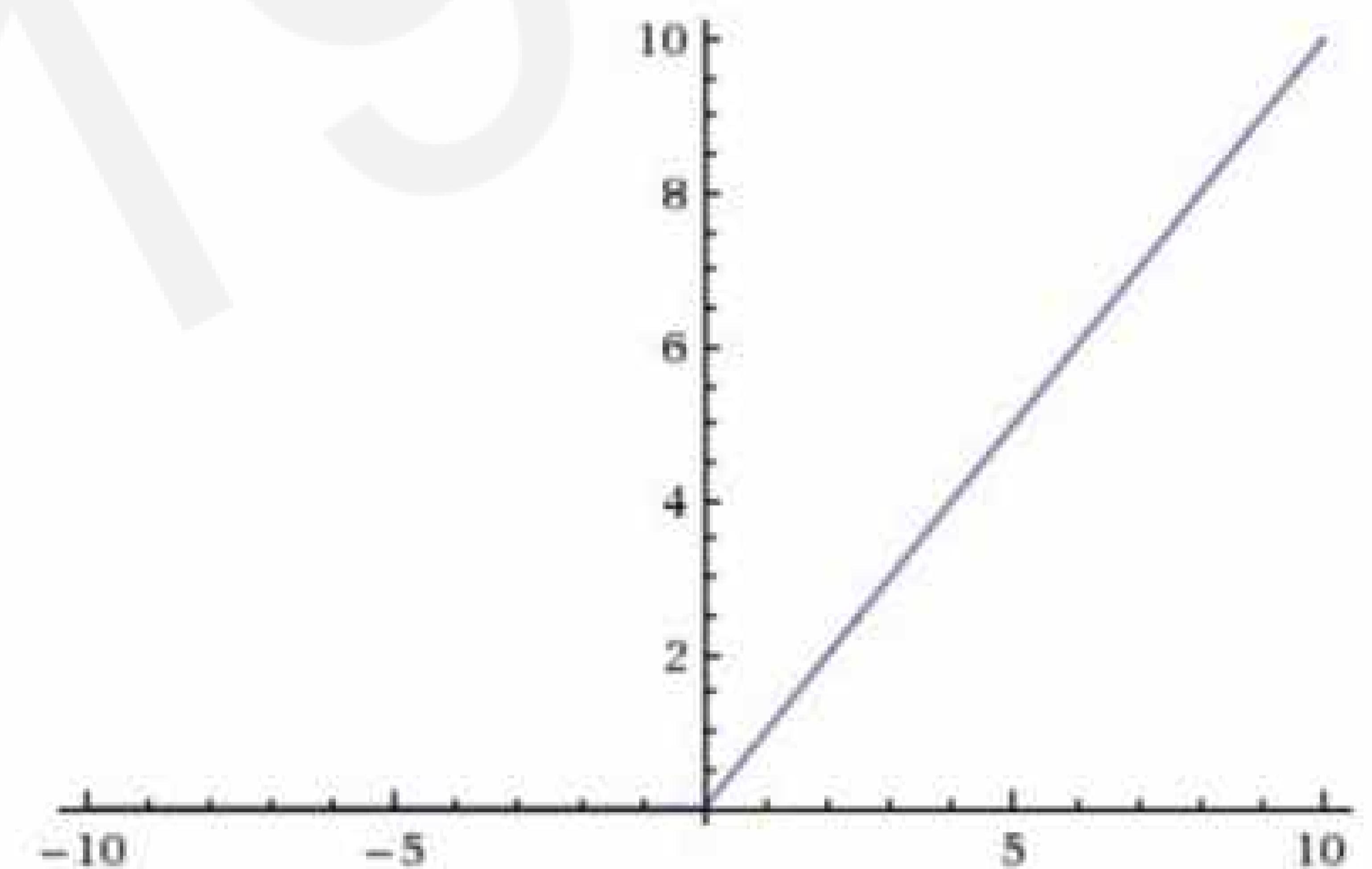
`tf.keras.layers.Conv2D( filters=d, kernel_size=(h,w), strides=s )`

# Introducing Non-Linearity

- Apply after every convolution operation (i.e., after convolutional layers)
- ReLU: pixel-by-pixel operation that replaces all negative values by zero. **Non-linear operation!**

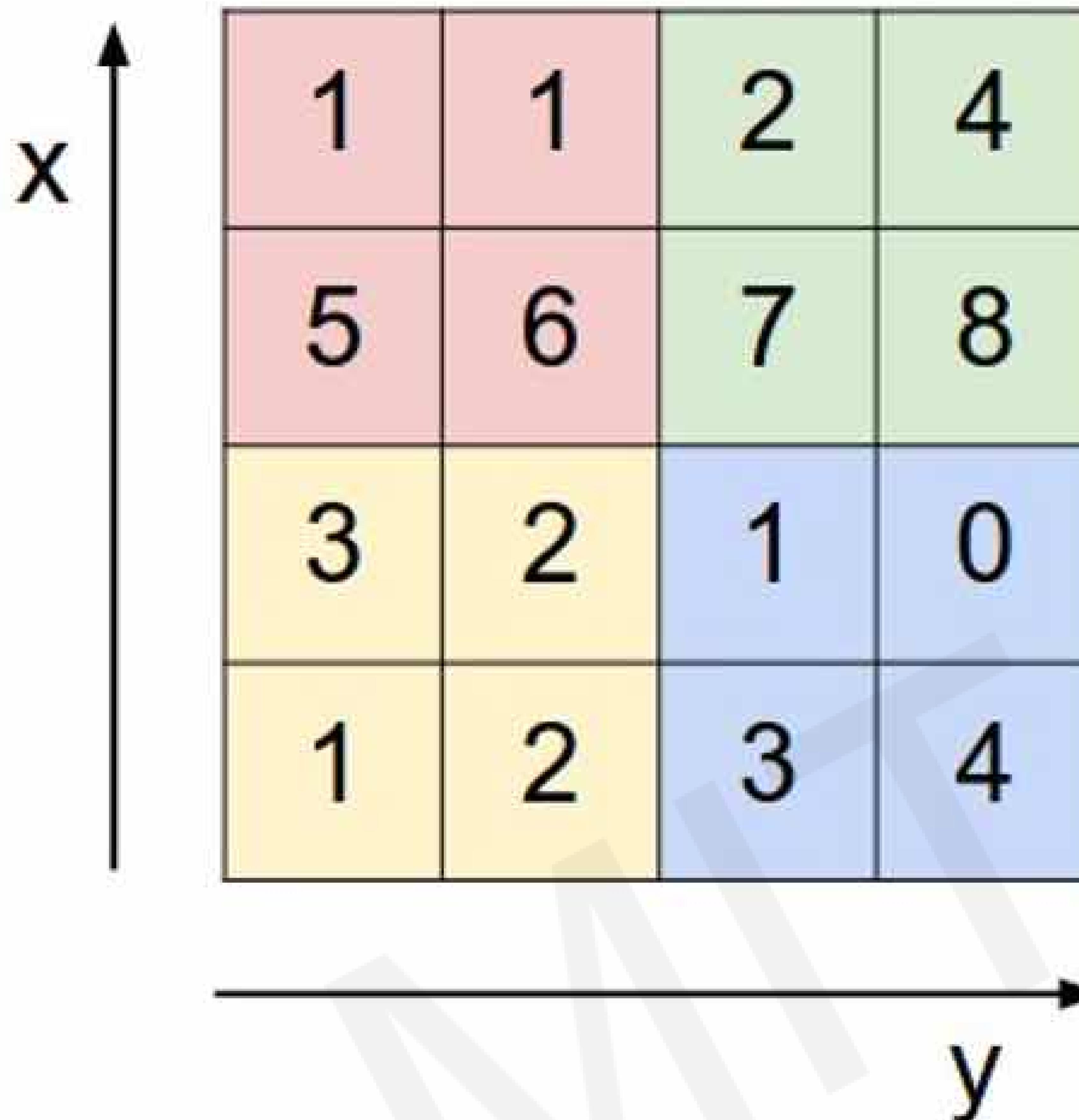


## Rectified Linear Unit (ReLU)



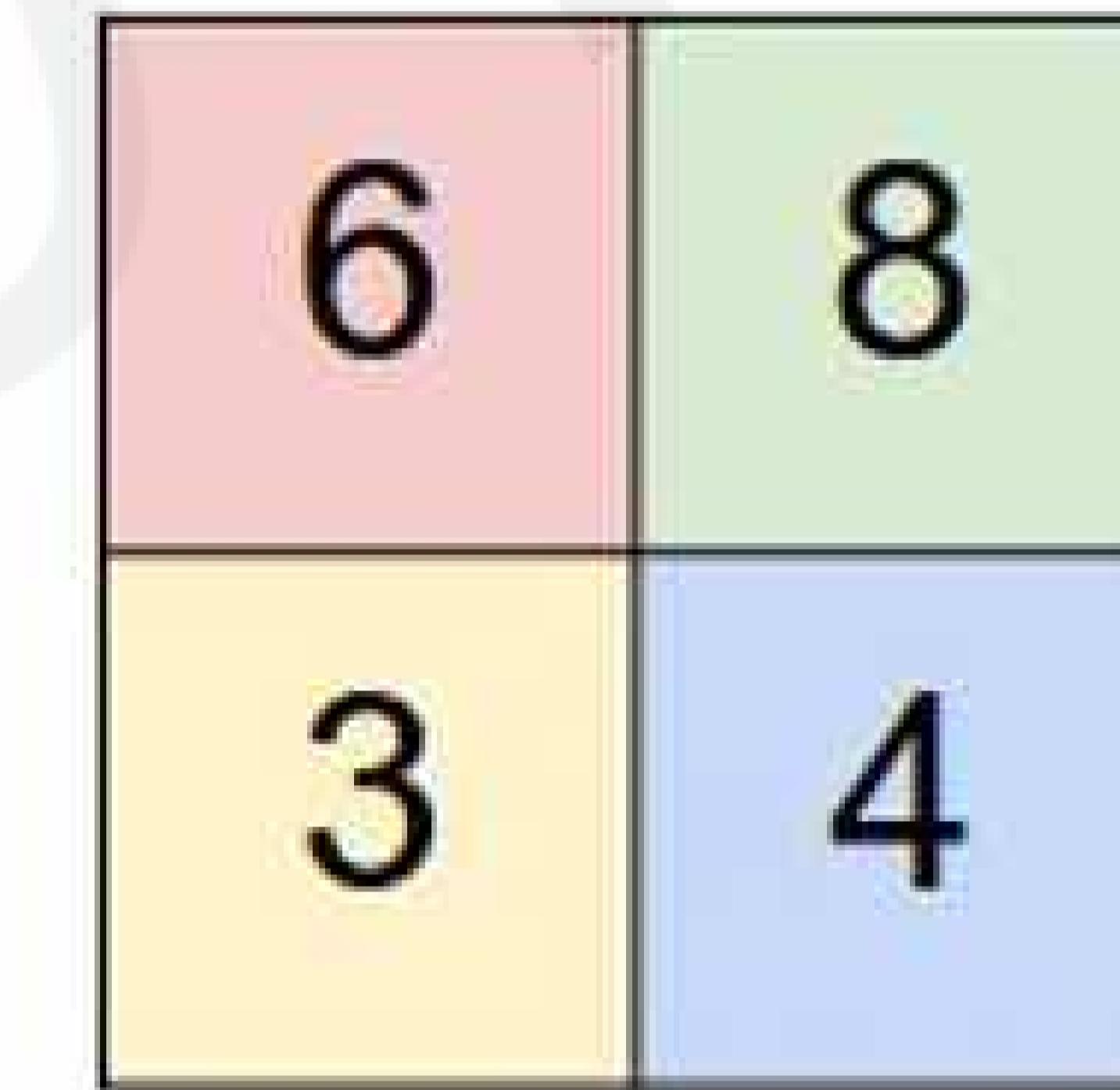
 `tf.keras.layers.ReLU`

# Pooling



max pool with 2x2 filters  
and stride 2

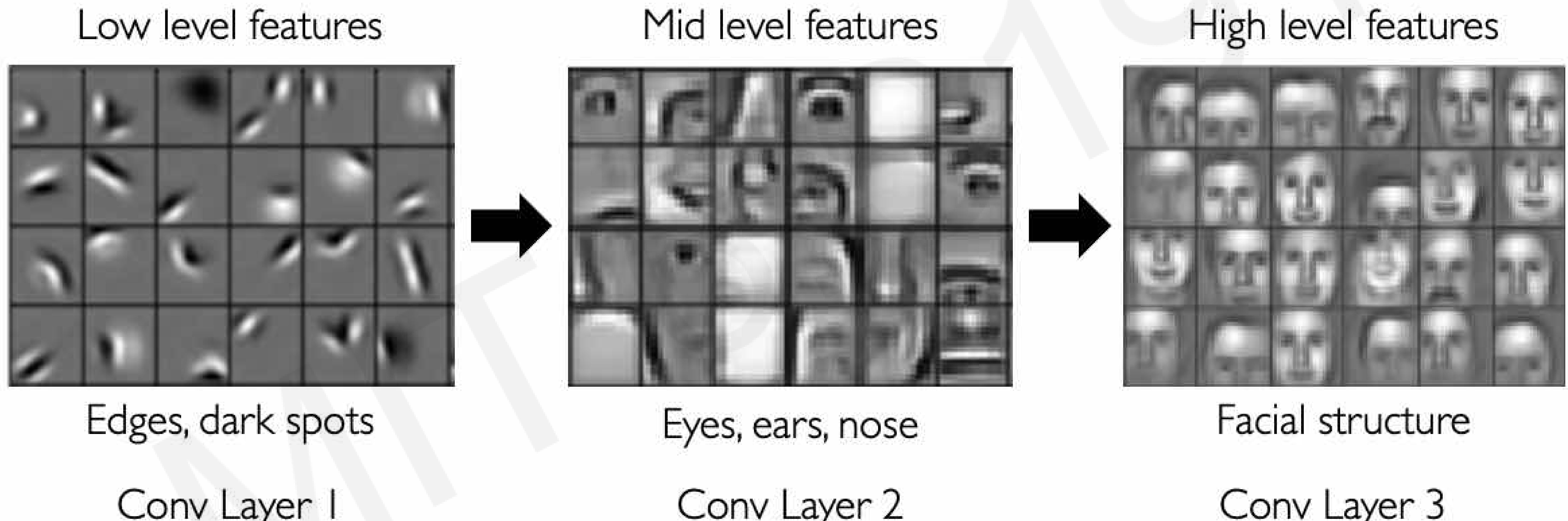
```
tf.keras.layers.MaxPool2D(  
    pool_size=(2,2),  
    strides=2  
)
```



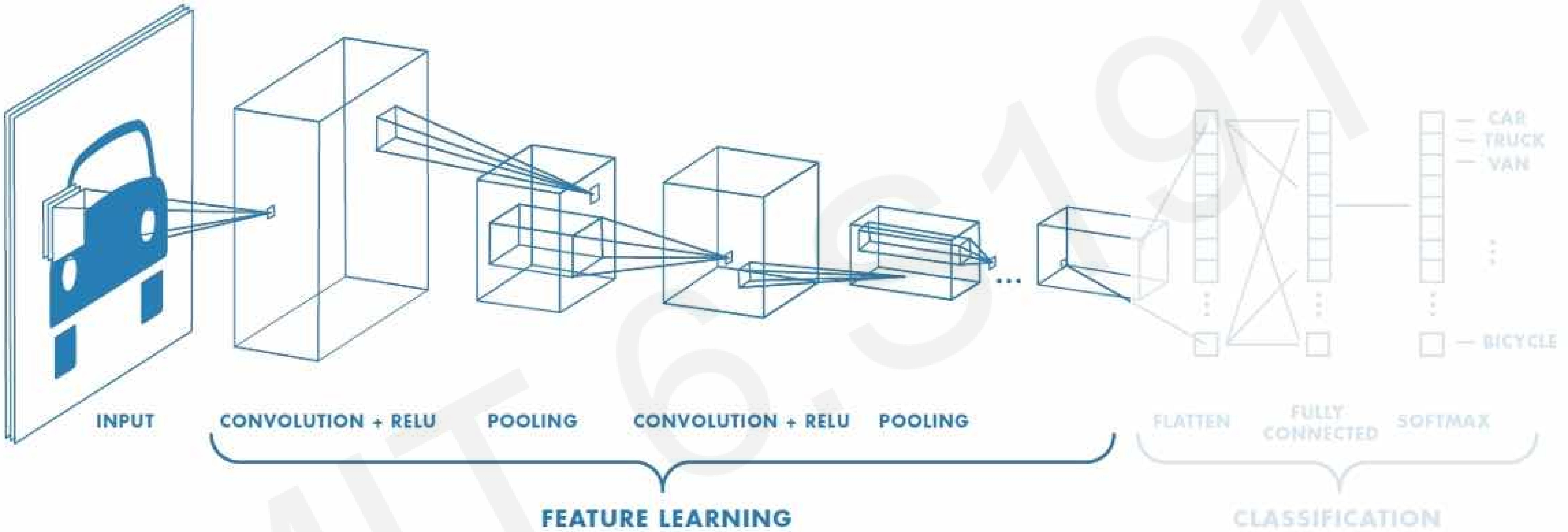
- 1) Reduced dimensionality
- 2) Spatial invariance

How else can we downsample and preserve spatial invariance?

# Representation Learning in Deep CNNs

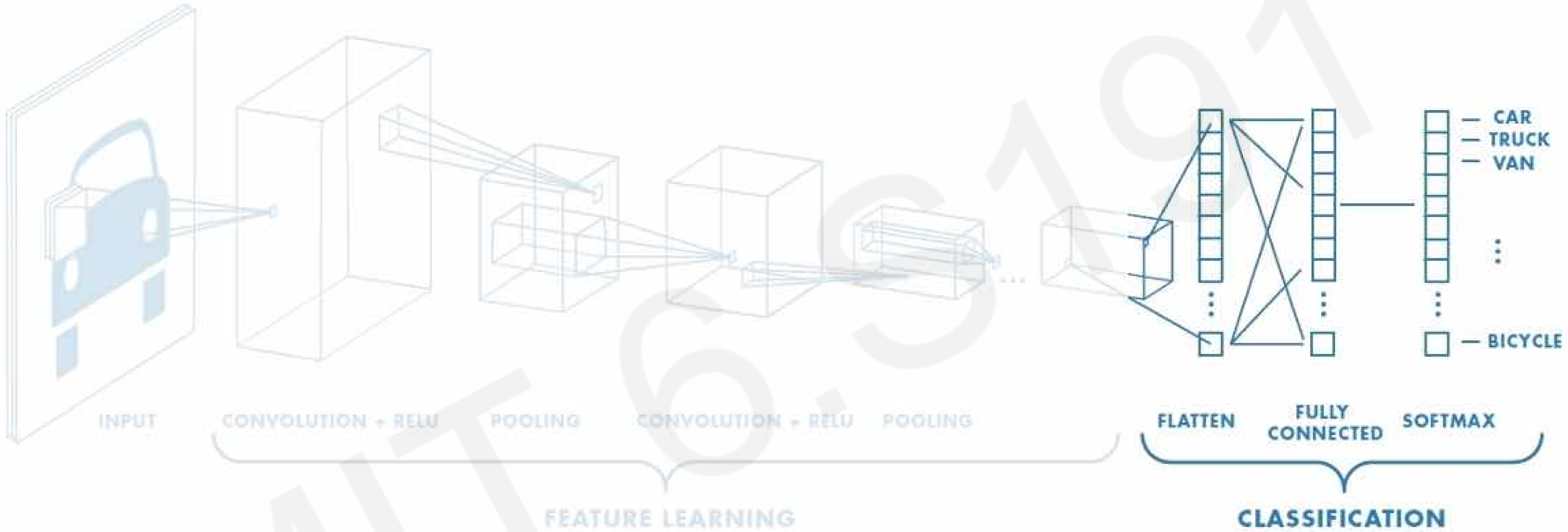


# CNNs for Classification: Feature Learning



1. Learn features in input image through **convolution**
2. Introduce **non-linearity** through activation function (real-world data is non-linear!)
3. Reduce dimensionality and preserve spatial invariance with **pooling**

# CNNs for Classification: Class Probabilities



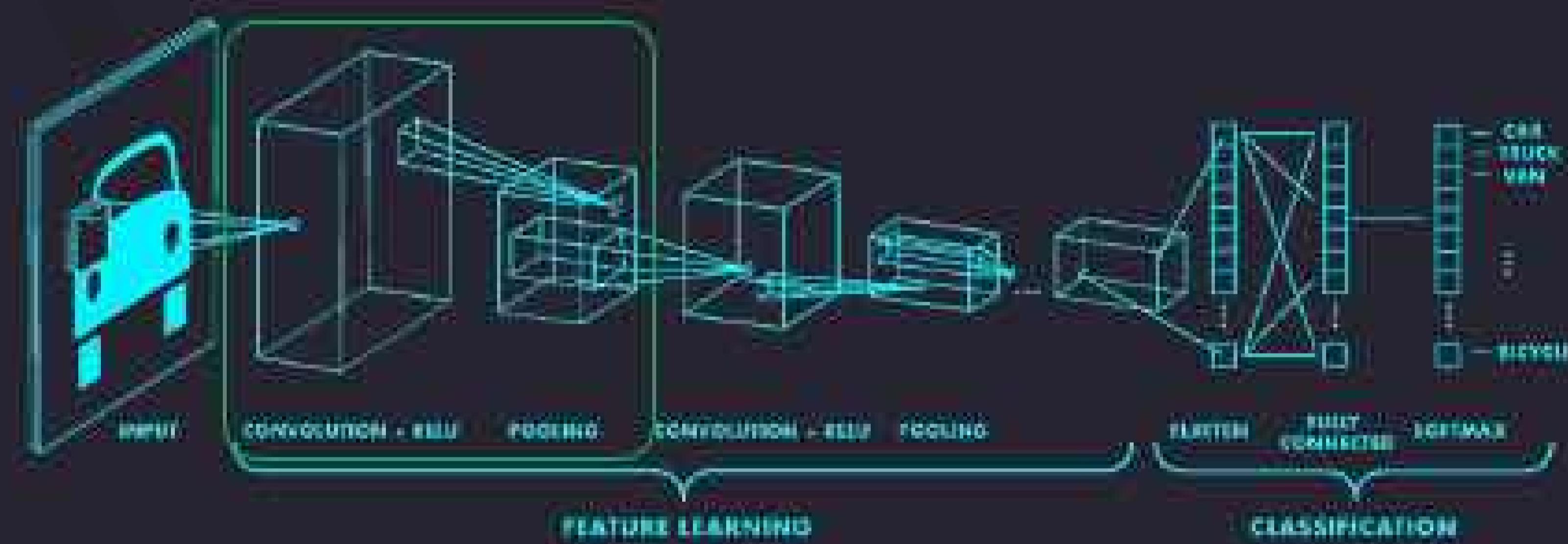
- CONV and POOL layers output high-level features of input
- Fully connected layer uses these features for classifying input image
- Express output as **probability** of image belonging to a particular class

$$\text{softmax}(y_i) = \frac{e^{y_i}}{\sum_j e^{y_j}}$$

# Putting it all together

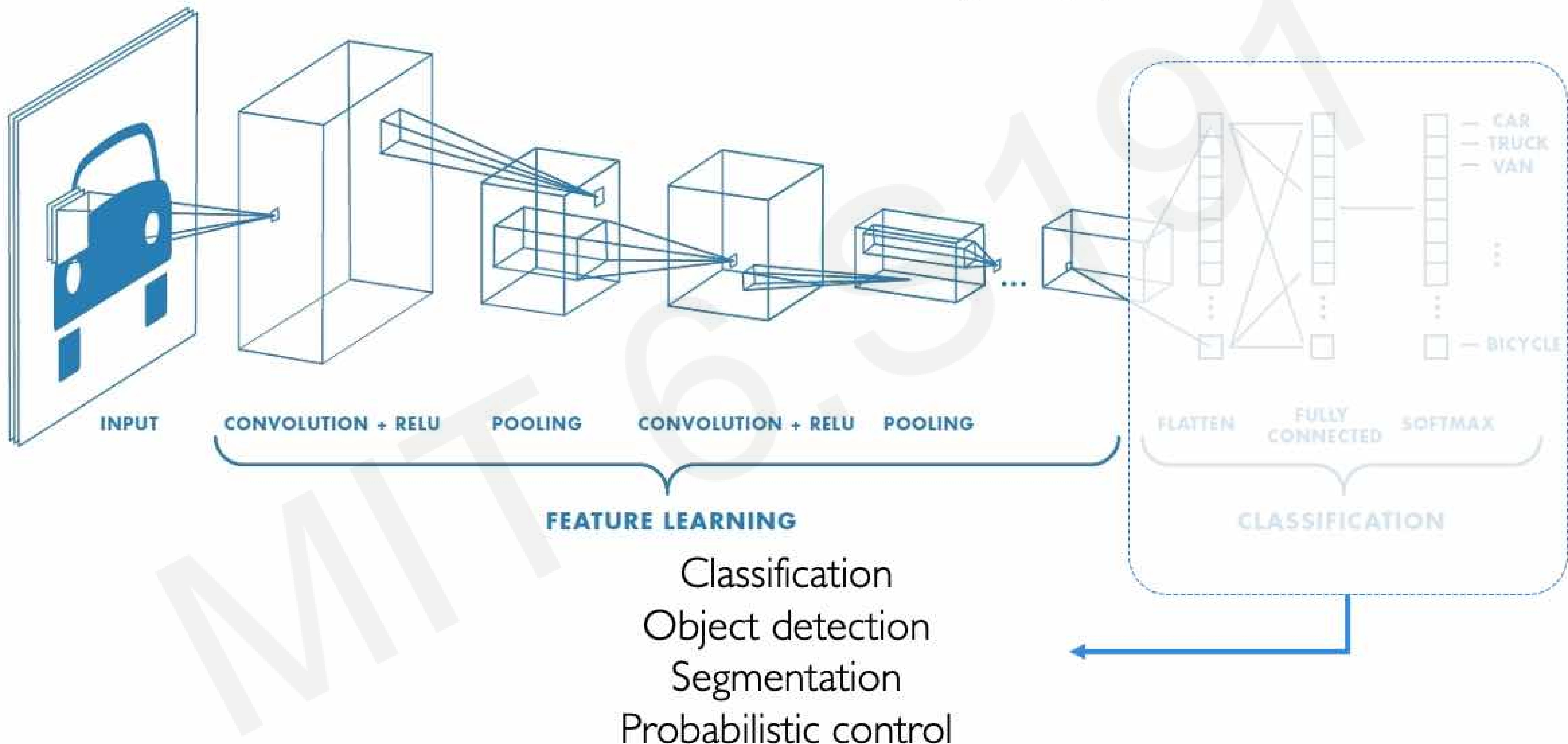
```
import tensorflow as tf

def generate_model():
    model = tf.keras.Sequential([
        # first convolutional layer
        tf.keras.layers.Conv2D(32, filter_size=3, activation='relu'),
        tf.keras.layers.MaxPool2D(pool_size=2, strides=2),
        # second convolutional layer
        tf.keras.layers.Conv2D(64, filter_size=3, activation='relu'),
        tf.keras.layers.MaxPool2D(pool_size=2, strides=2),
        # fully connected classifier
        tf.keras.layers.Flatten(),
        tf.keras.layers.Dense(1024, activation='relu'),
        tf.keras.layers.Dense(10, activation='softmax') # 10 outputs
    ])
    return model
```



# An Architecture for Many Applications

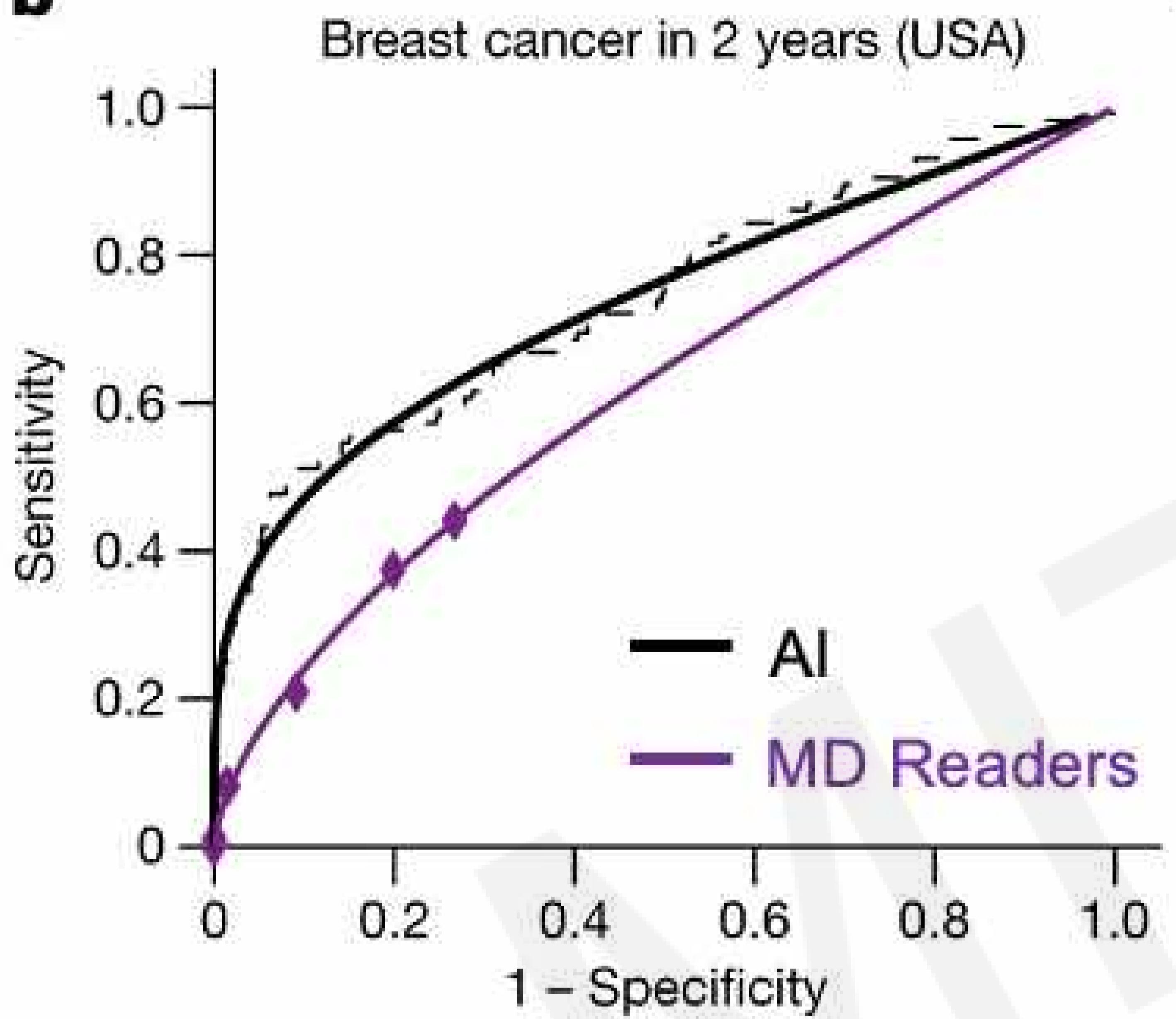
# An Architecture for Many Applications



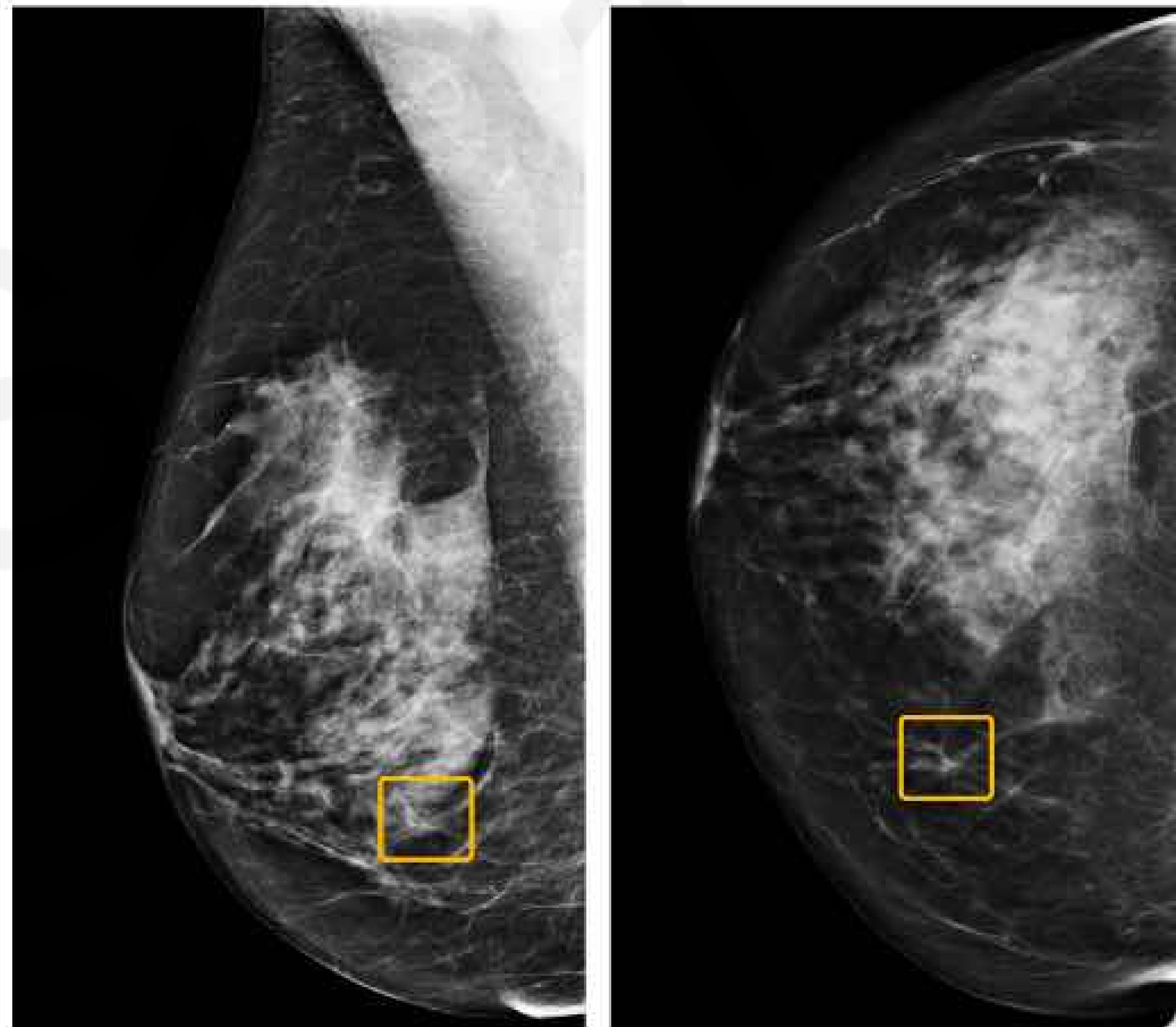
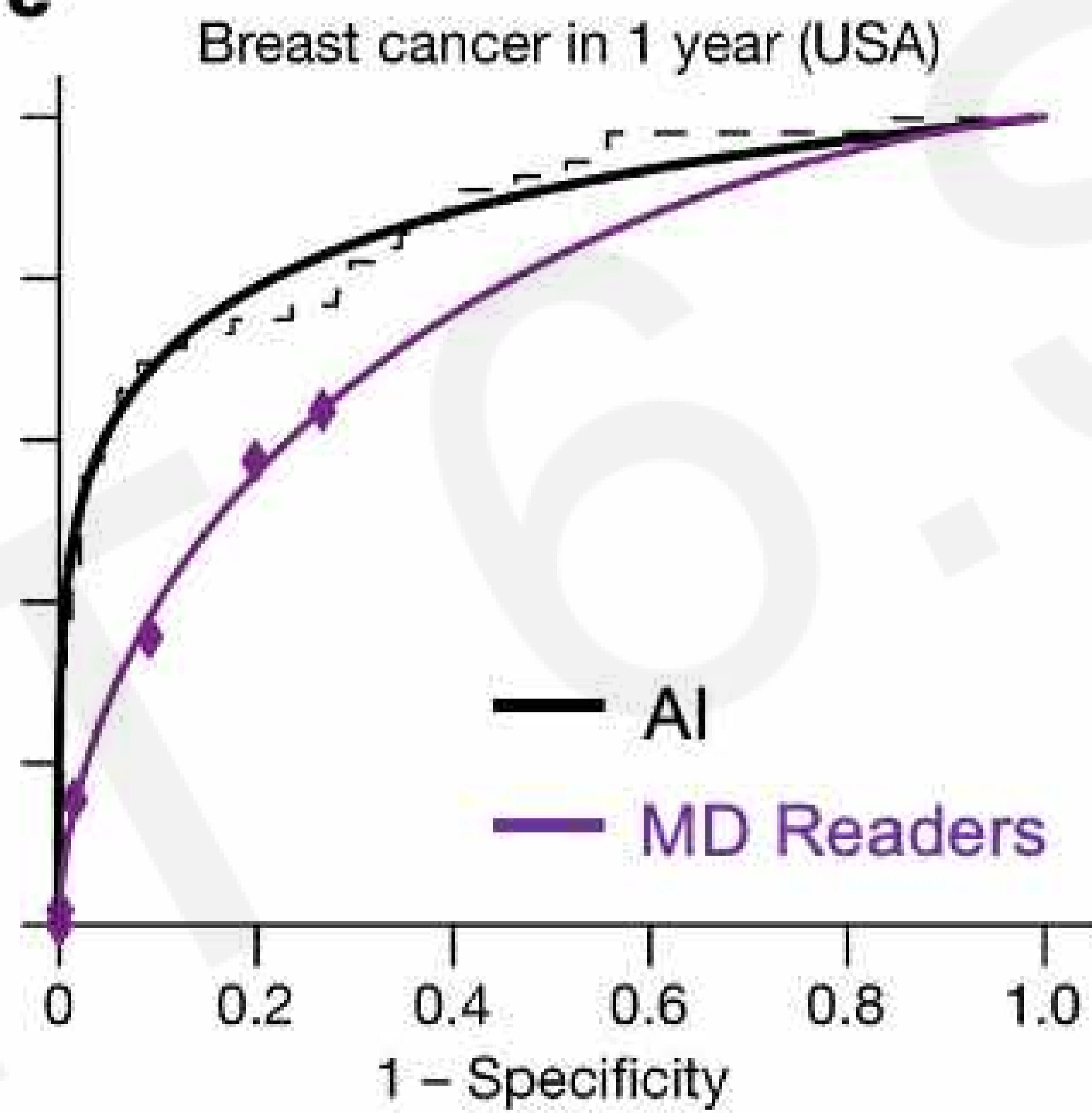
# Classification: Breast Cancer Screening

## International evaluation of an AI system for breast cancer screening

b



c



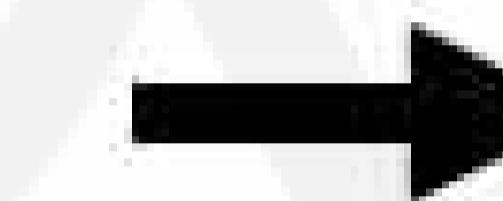
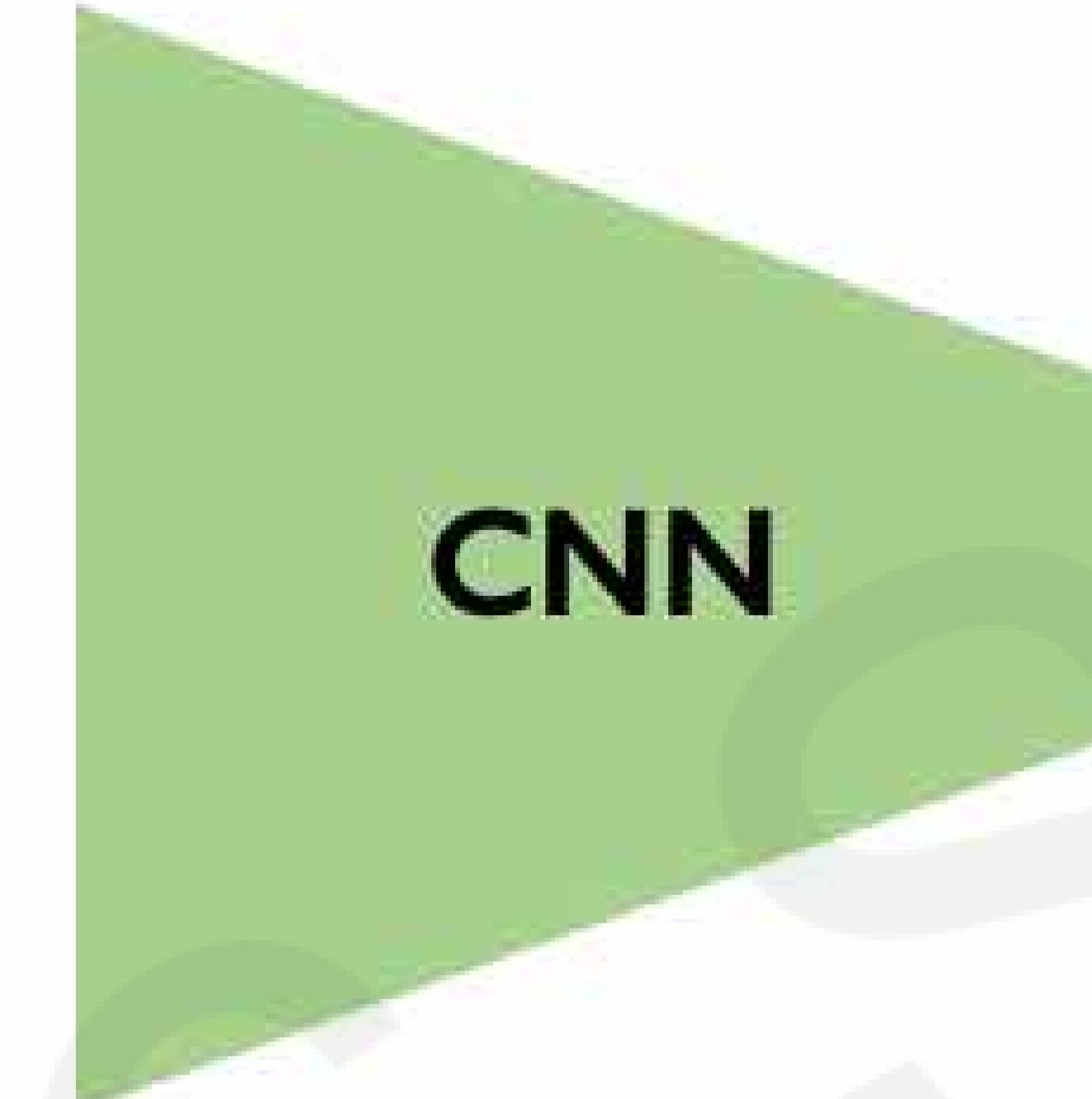
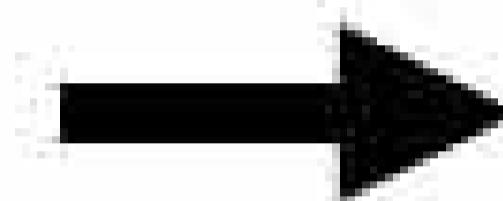
CNN-based system outperformed expert radiologists at detecting breast cancer from mammograms

Breast cancer case missed by radiologist but detected by AI

# Object Detection



Image X

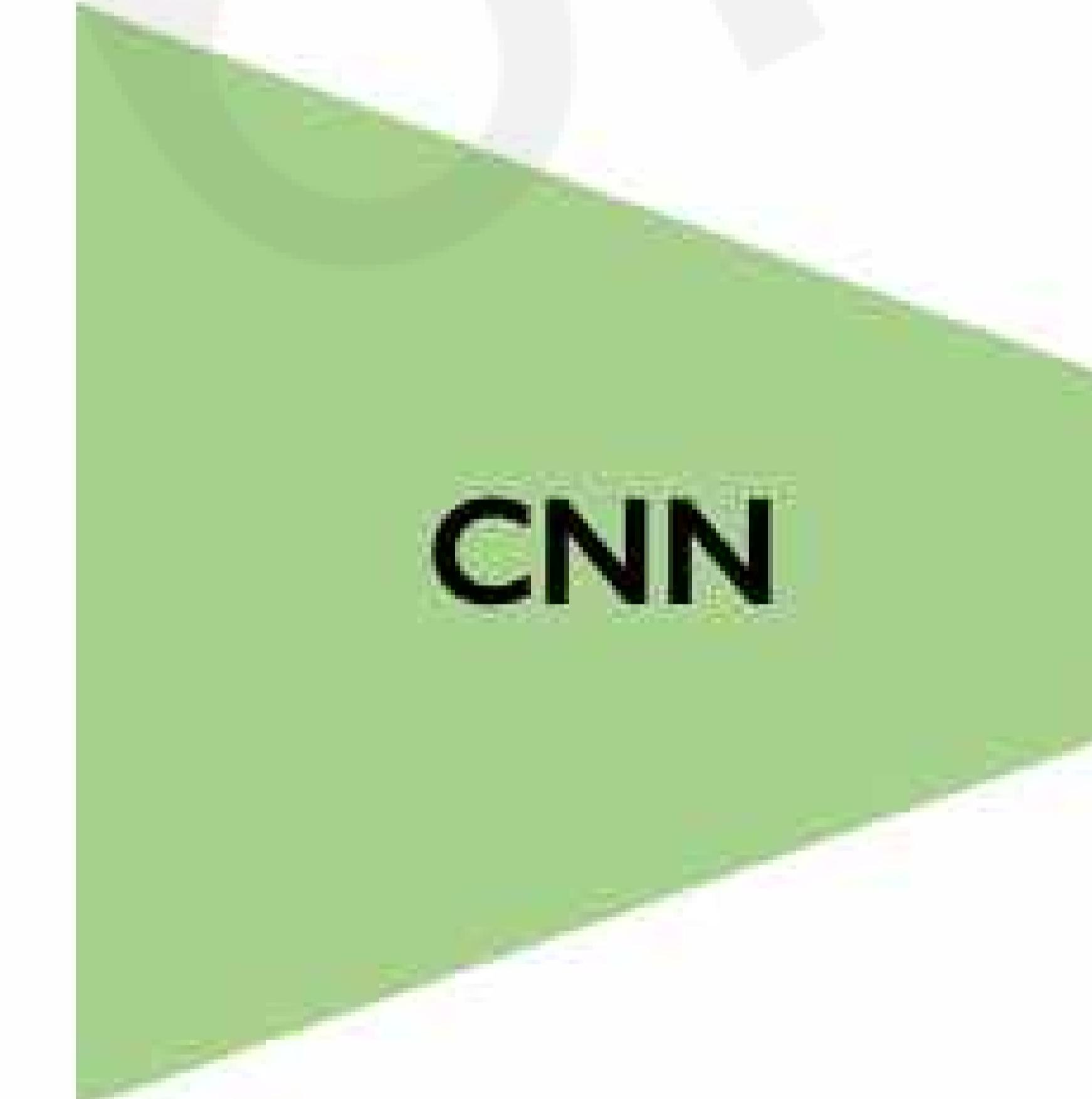
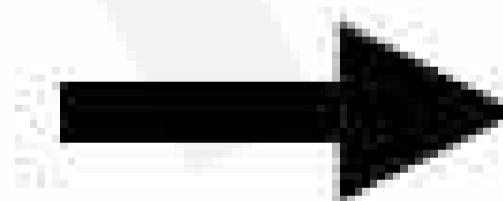


Taxi

Class label y



Image X

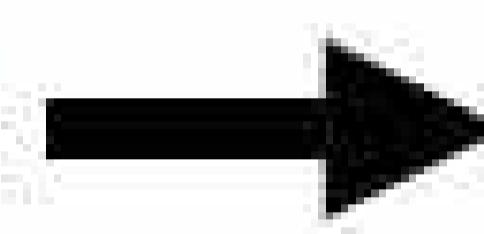


Label  $(x, y, w, h)$

# Object Detection



Image X

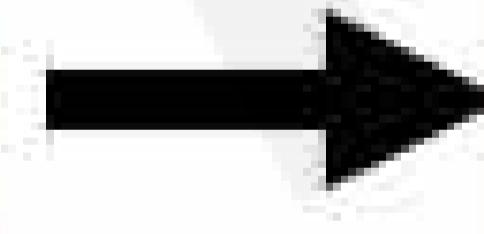


**Output:**

**taxi**:  $(x_l, y_l, w_l, h_l)$



Image X



**Output:**

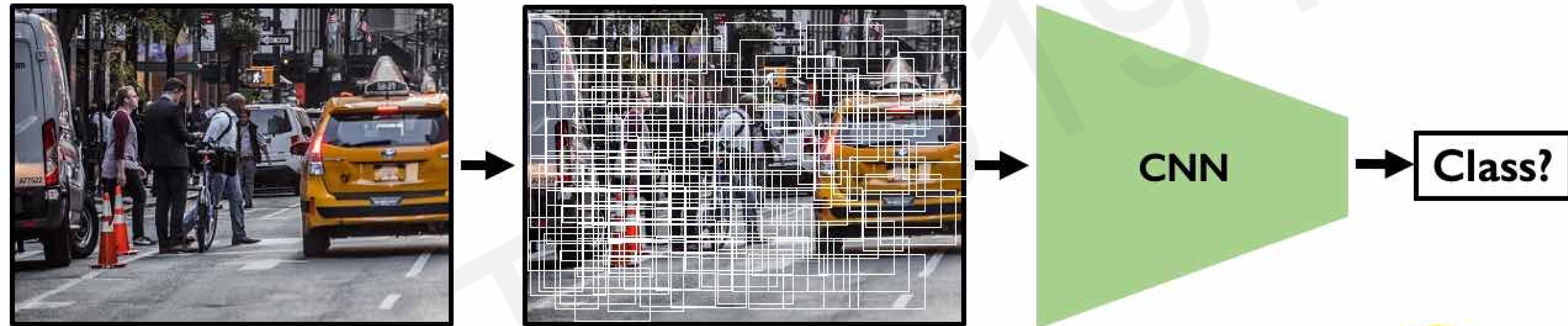
**taxi**:  $(x_l, y_l, w_l, h_l)$

**person**:  $(x_2, y_2, w_2, h_2)$

**person**:  $(x_3, y_3, w_3, h_3)$

...

# Naïve Solution to Object Detection



**Problem:** Way too many inputs! This results in too many scales, positions, sizes!



# Object Detection with R-CNNs

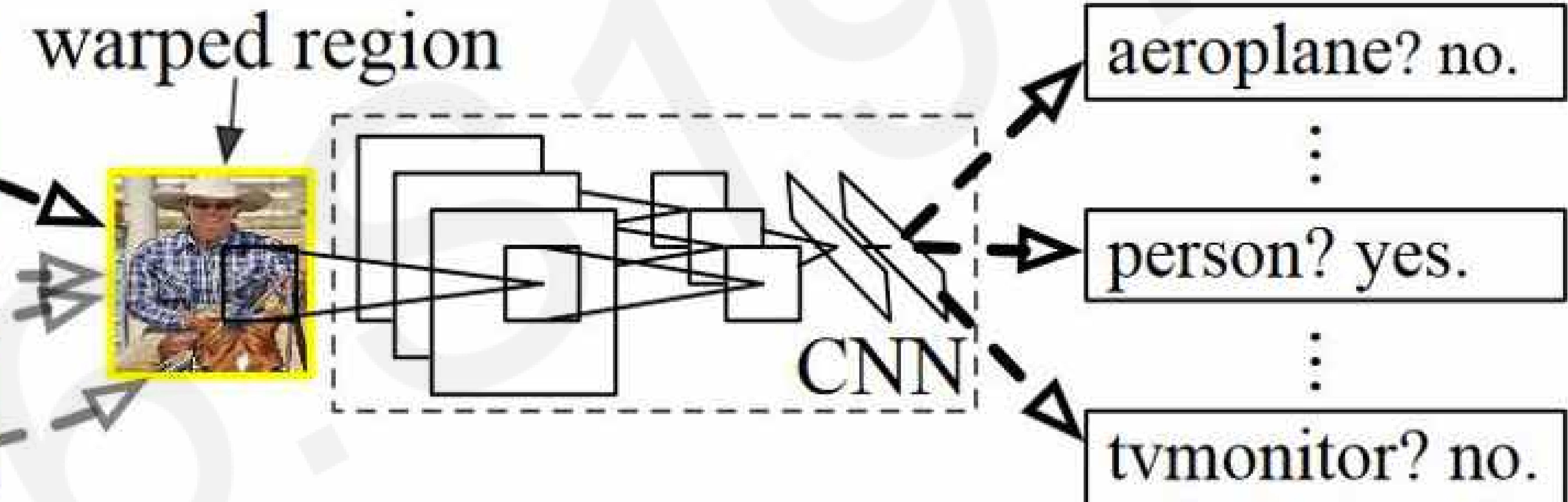
R-CNN algorithm: Find regions that we think have objects. Use CNN to classify.



1. Input image



2. Extract region proposals (~2k)



3. Compute CNN features

4. Classify regions

**Problems:** 1) Slow! Many regions; time intensive inference.  
2) Brittle! Manually defined region proposals.

# Faster R-CNN Learns Region Proposals

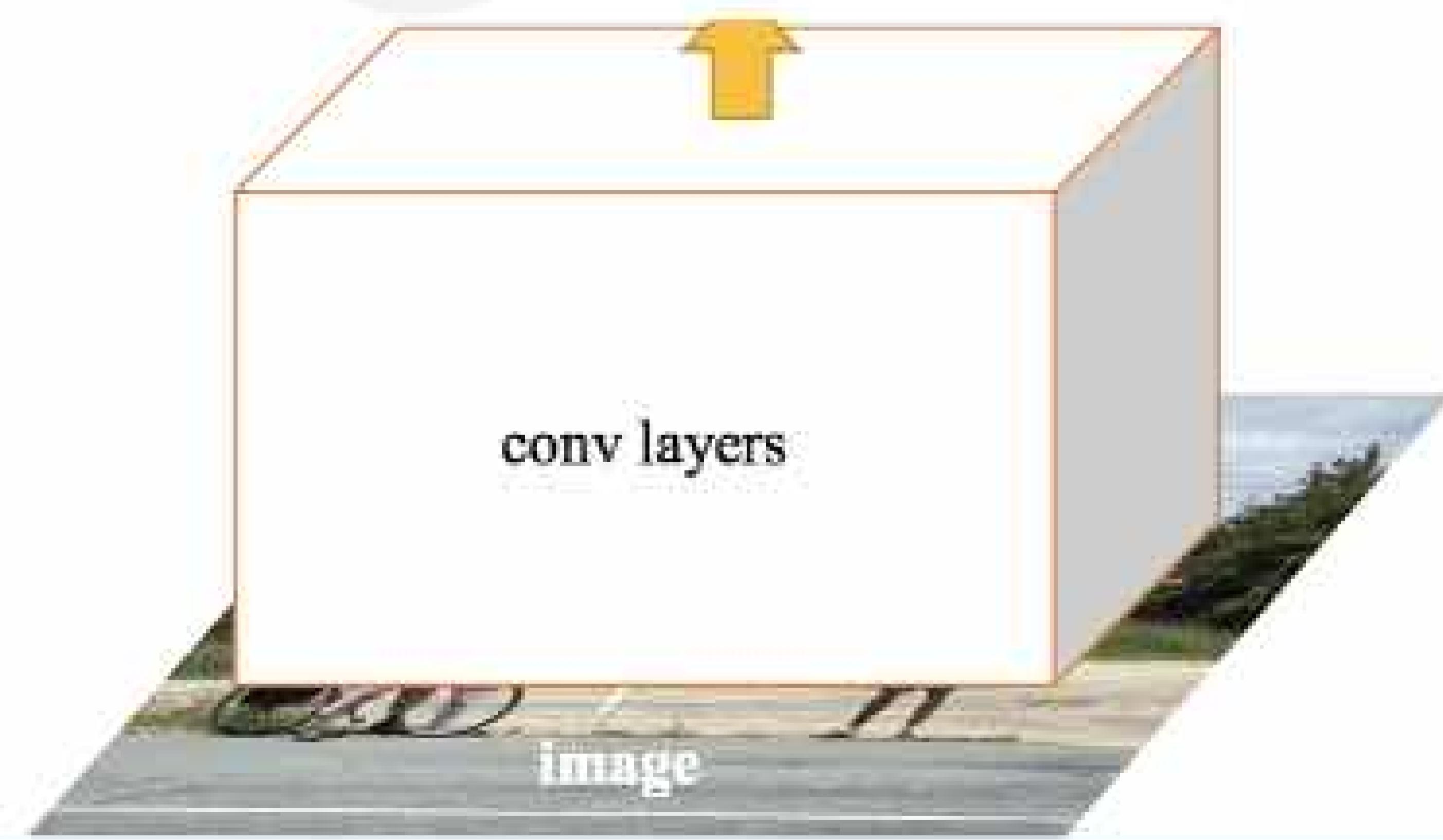
Classification of regions →  
object detection

Feature extraction over  
proposed regions

Region proposal network  
to learn candidate regions

**Learned, data-driven**

Image input directly into  
convolutional feature extractor  
**Fast! Only input image once!**



# Semantic Segmentation: Fully Convolutional Networks

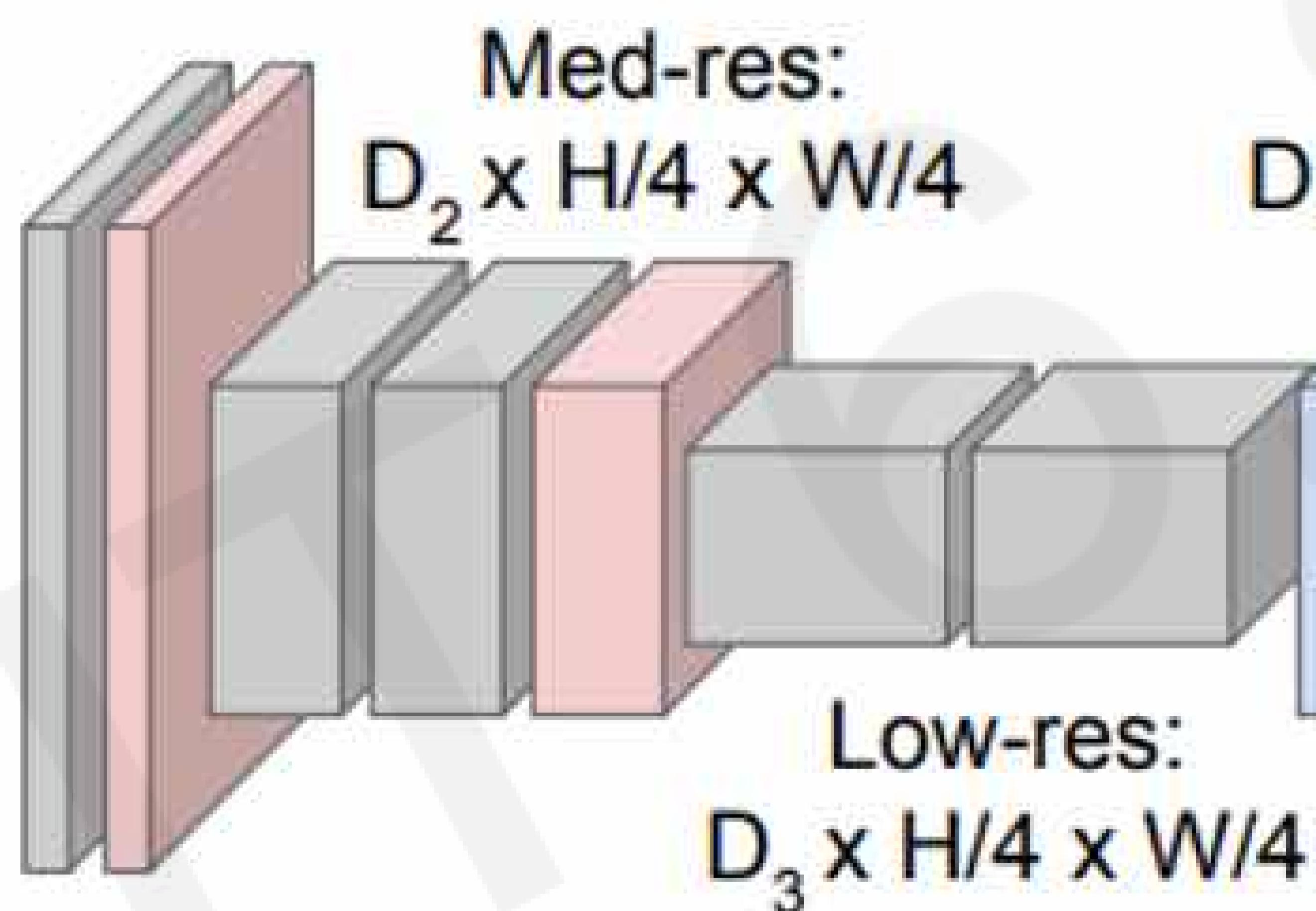
FCN: Fully Convolutional Network.

Network designed with all convolutional layers,  
with **downsampling** and **upsampling** operations



Input:  
 $3 \times H \times W$

High-res:  
 $D_1 \times H/2 \times W/2$



High-res:  
 $D_1 \times H/2 \times W/2$

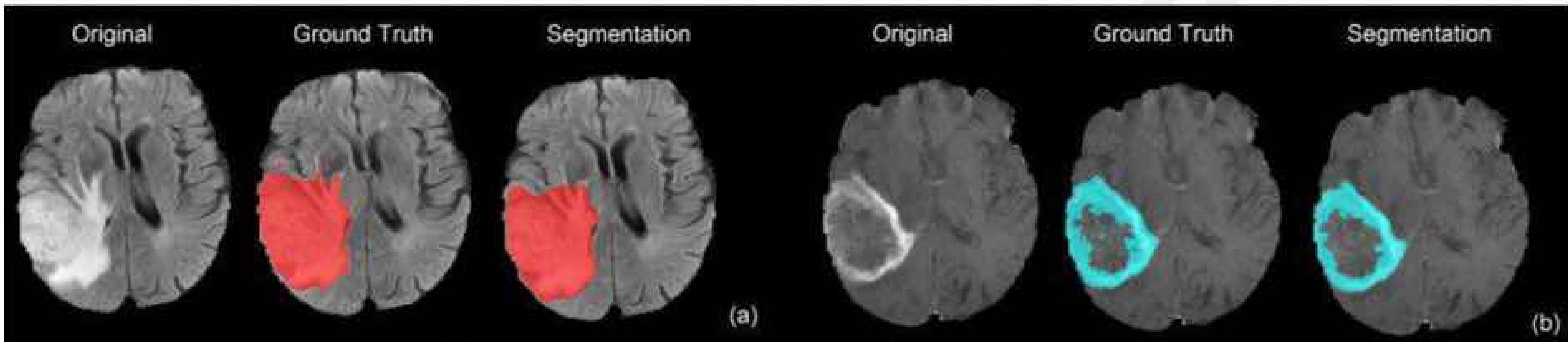


Predictions:  
 $H \times W$

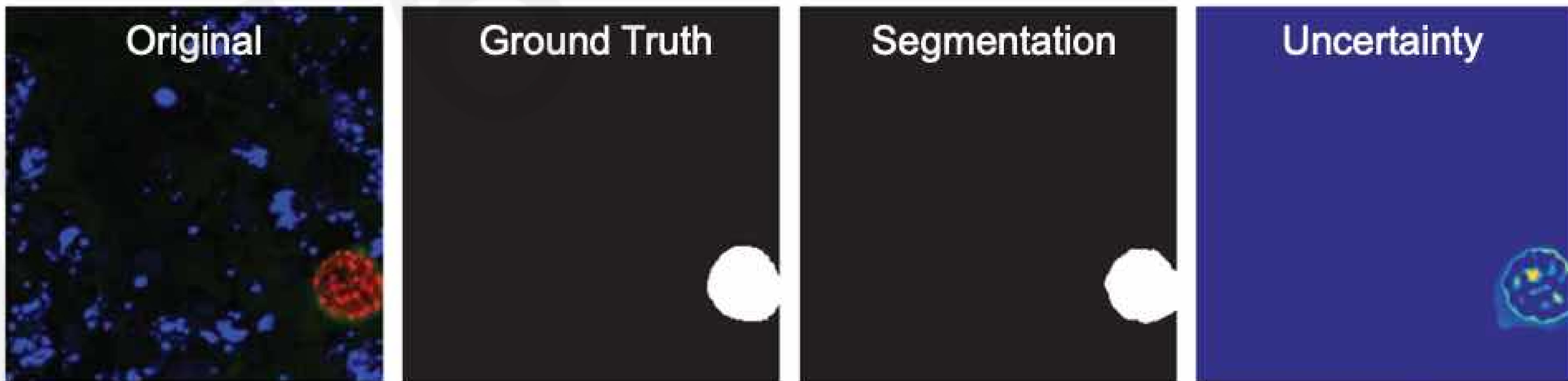
`tf.keras.layers.Conv2DTranspose`

# Semantic Segmentation: Biomedical Image Analysis

Brain Tumors  
Dong+ MIUA 2017.



Malaria Infection  
Soleimany+ arXiv 2019.



# Continuous Control: Navigation from Vision

Raw Perception

*I*

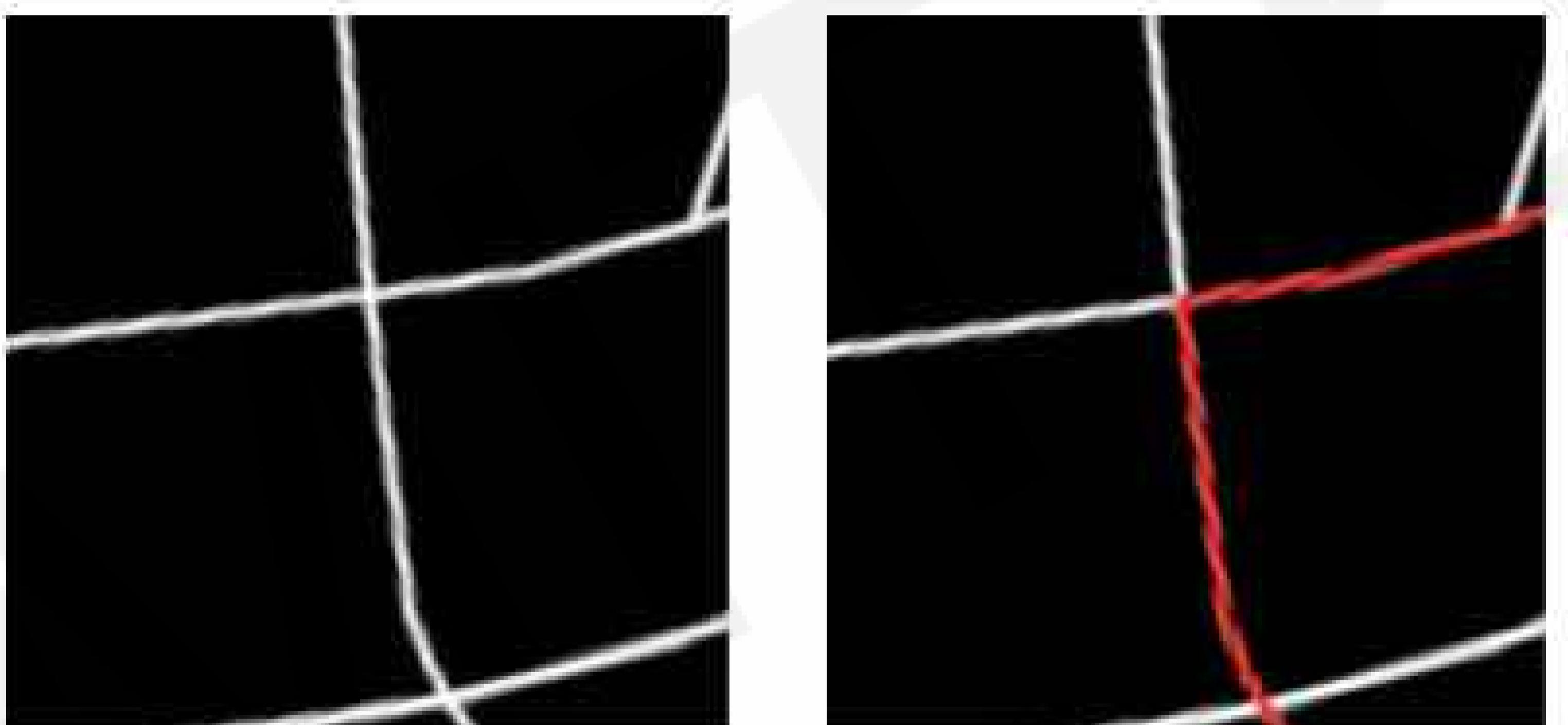
(ex. camera)



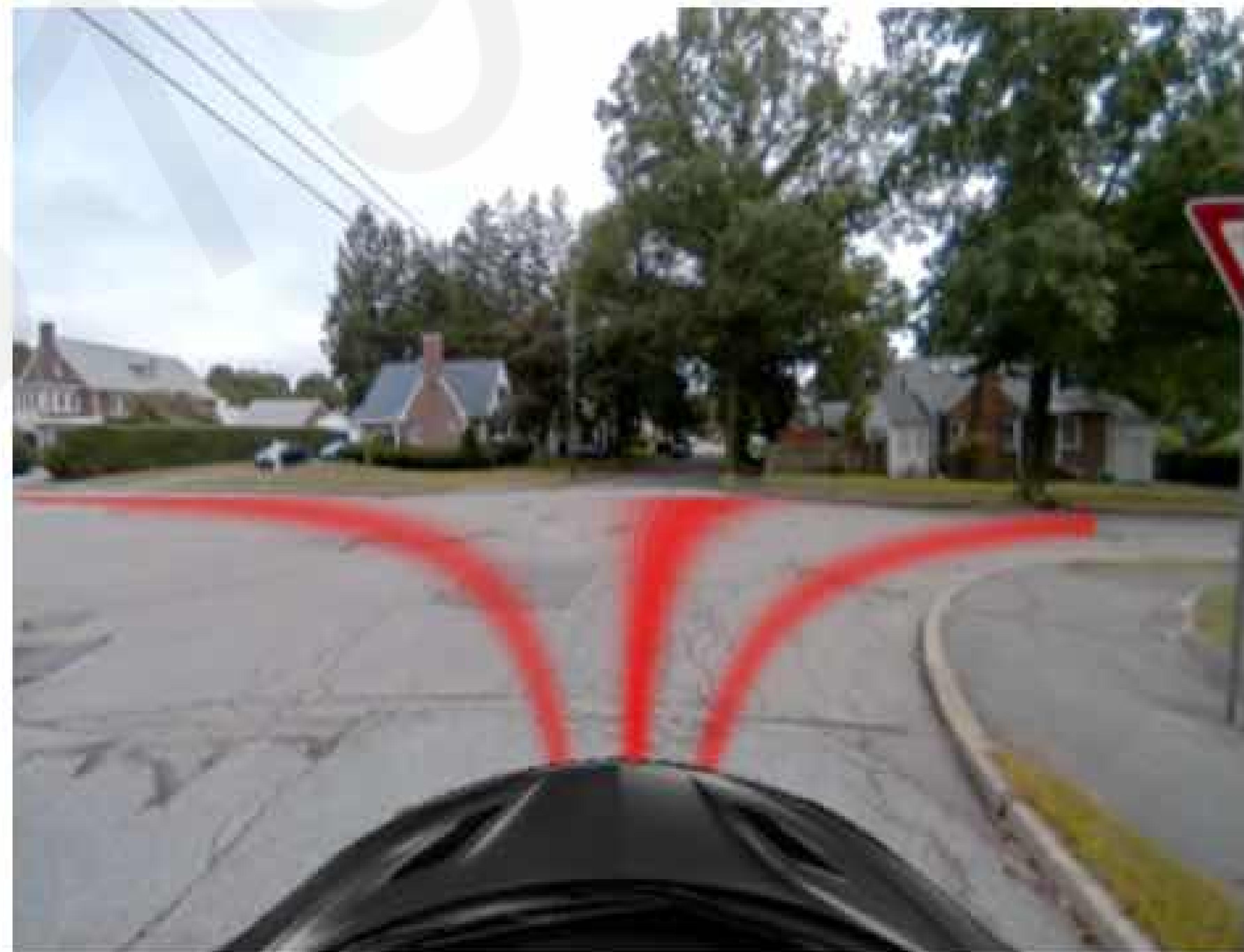
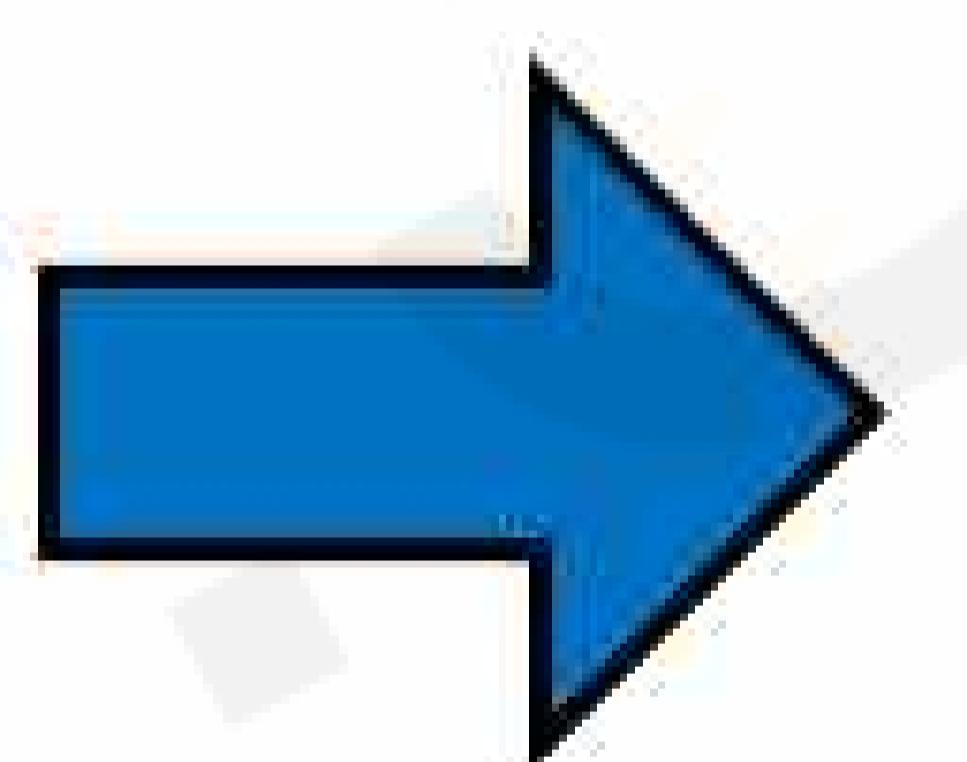
Coarse Maps

*M*

(ex. GPS)

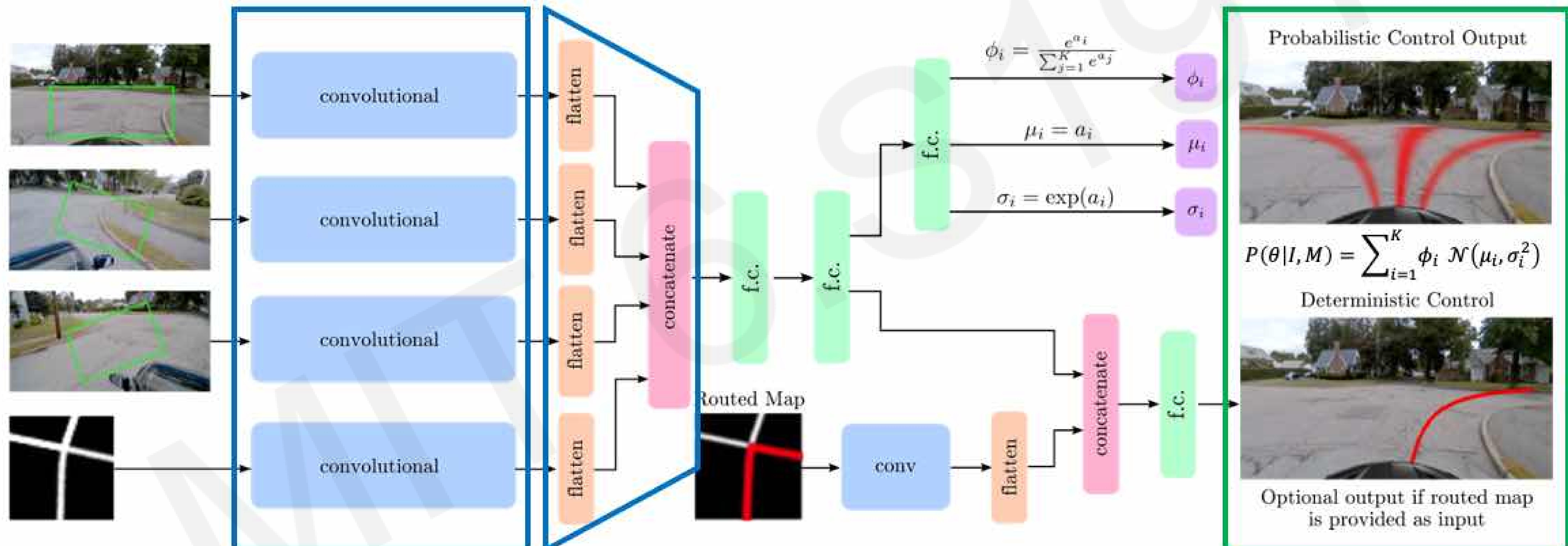


Possible Control Commands



# End-to-End Framework for Autonomous Navigation

Entire model is trained end-to-end **without any human labelling or annotations**



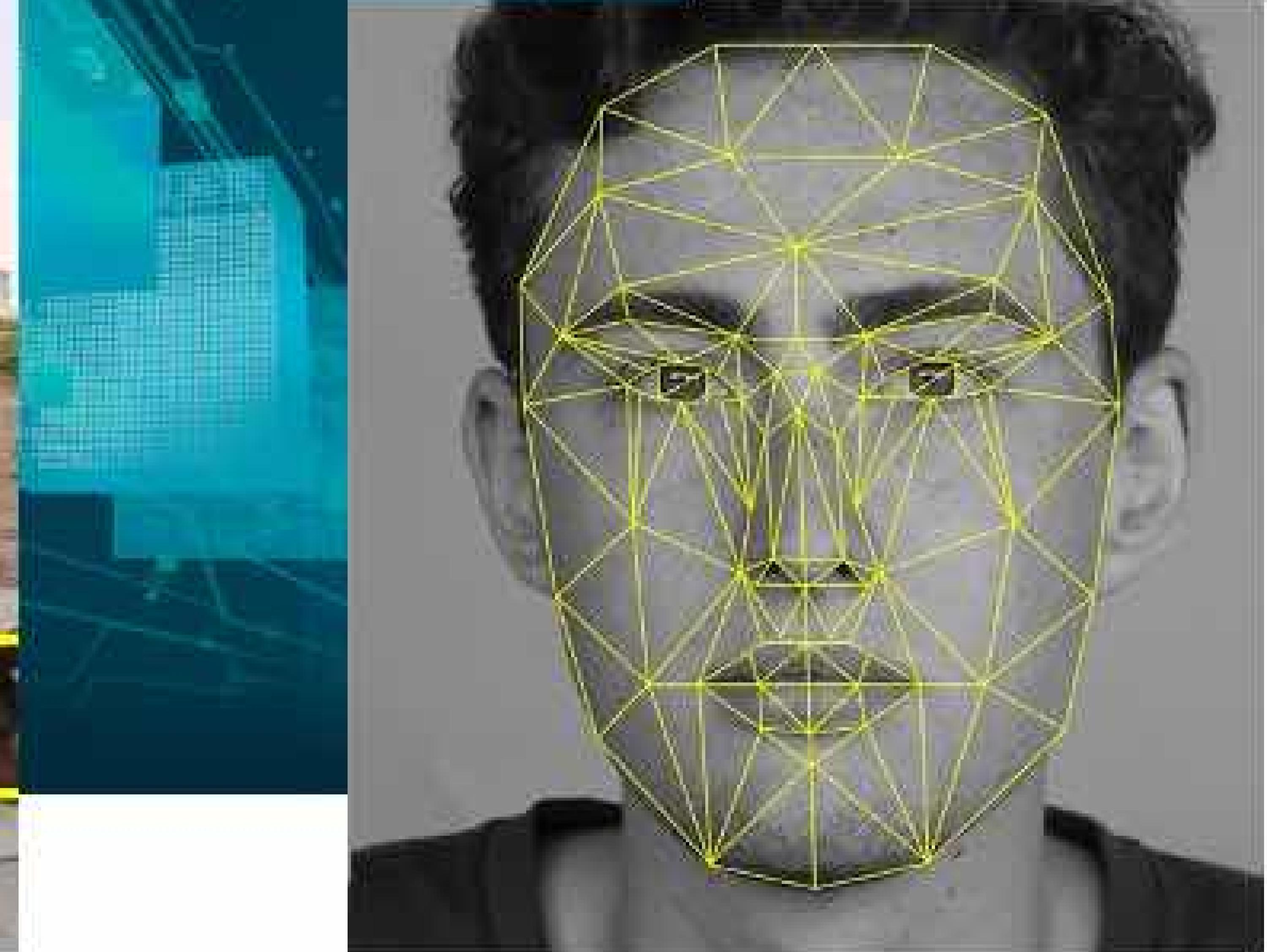
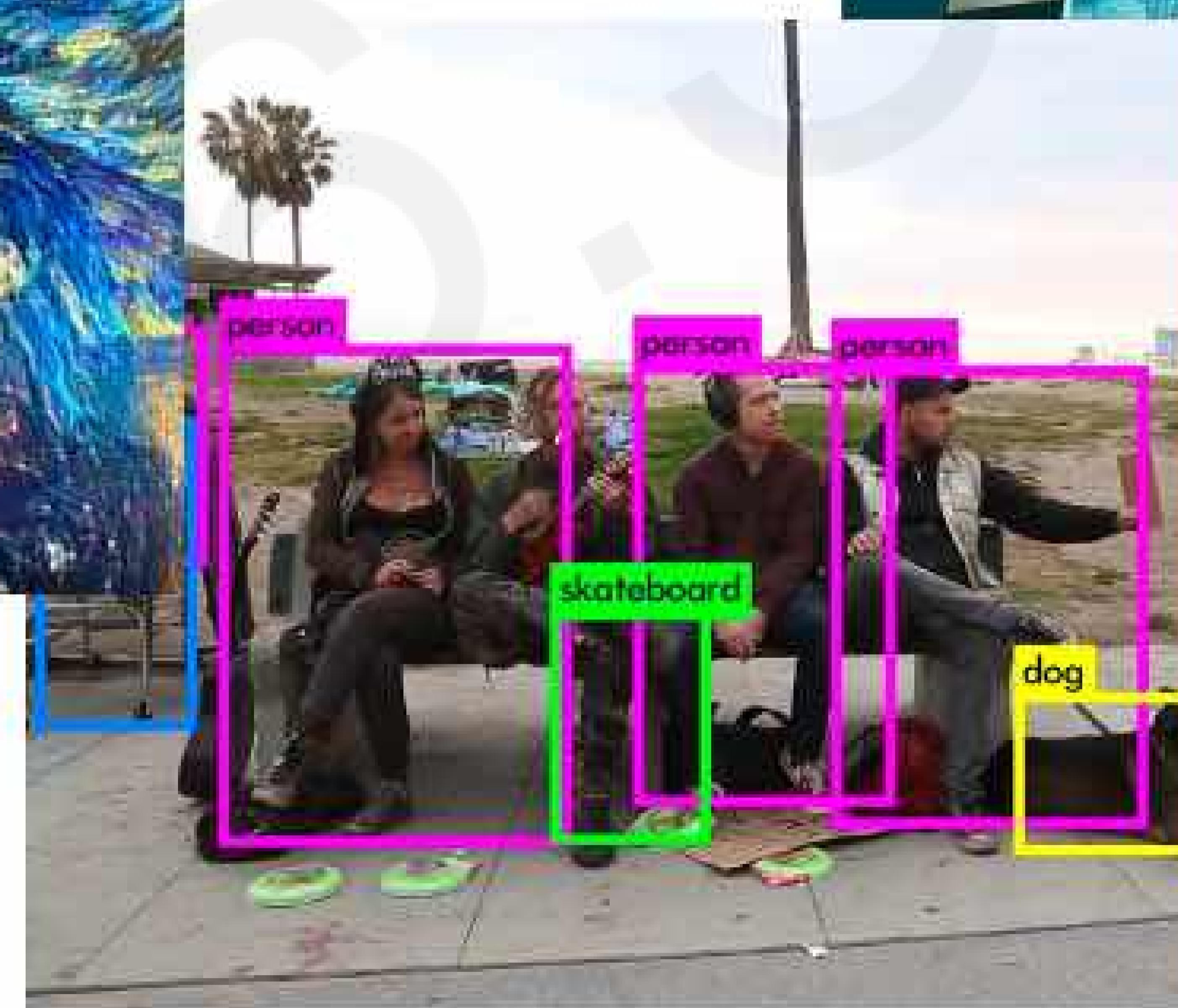
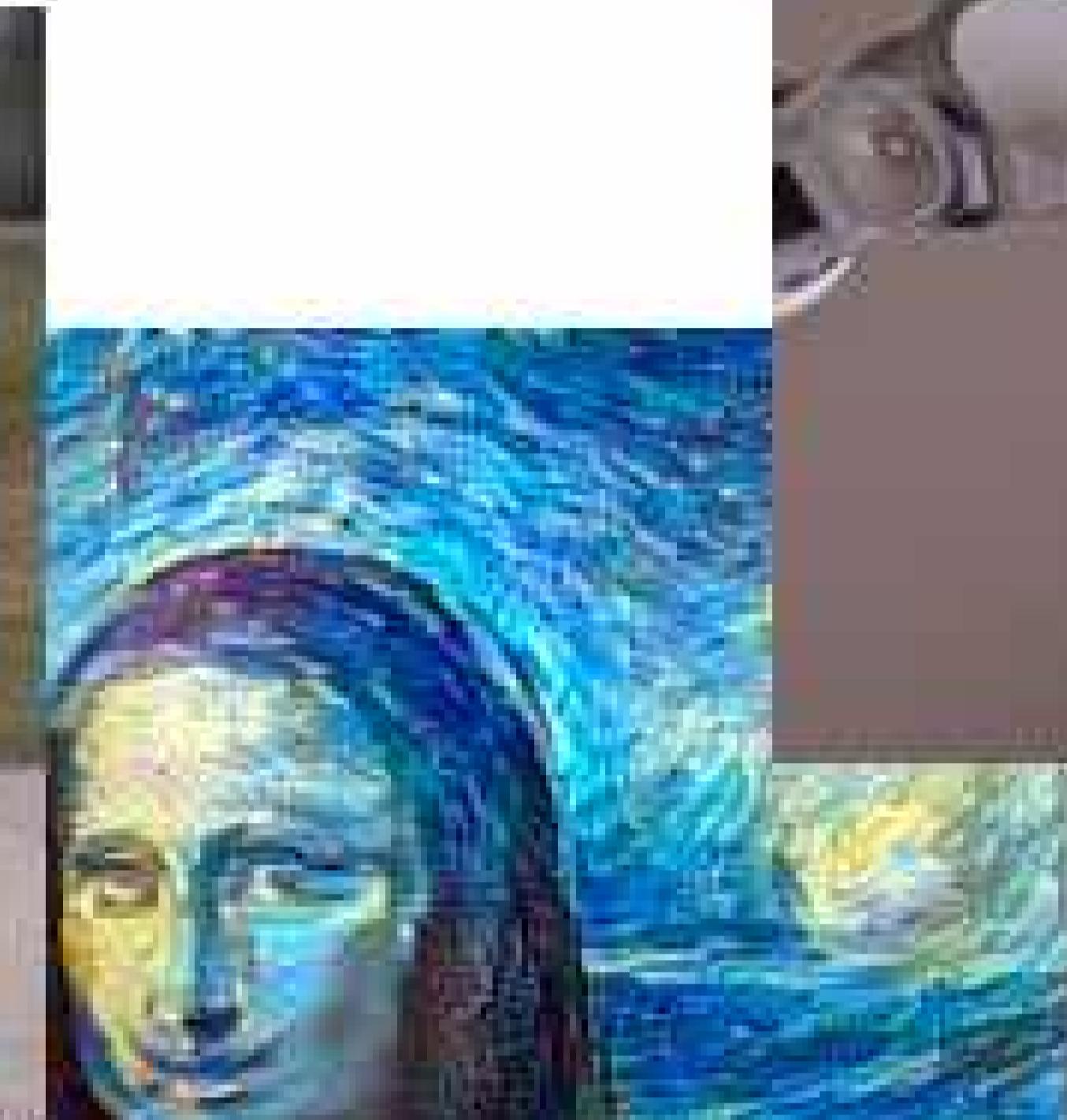
$$L = -\log(P(\theta|I, M))$$



**Auto ON**  
Navigation and Localization



# Deep Learning for Computer Vision: Impact



# Deep Learning for Computer Vision: Summary

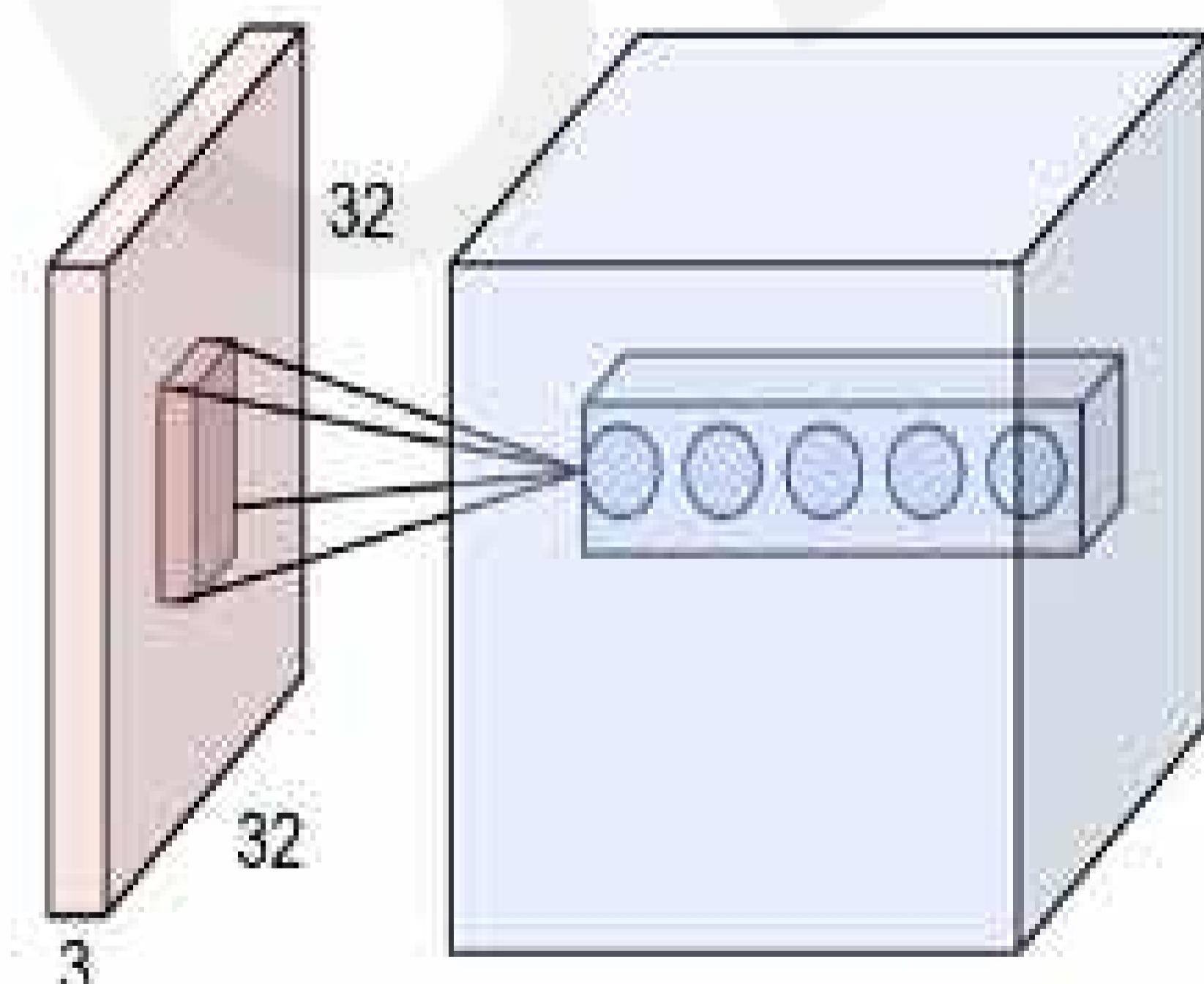
## Foundations

- Why computer vision?
- Representing images
- Convolutions for feature extraction



## CNNs

- CNN architecture
- Application to classification
- ImageNet



## Applications

- Segmentation, image captioning, control
- Security, medicine, robotics





# 6.S191:

## Introduction to Deep Learning

### Lab 2: Computer Vision

Link to download labs:  
<http://introtodeeplearning.com#schedule>

1. Open the lab in Google Colab
2. Start executing code blocks and filling in the #TODOs
3. Need help? Come to the class Gather.Town!