I briven,

$$f(z) = \log_e(1+z) \text{ where } z = x^T x, x \in \mathbb{R}^d$$

If,
$$\chi = \begin{bmatrix} y \\ \chi z \end{bmatrix}$$
 then, $\chi T = \begin{bmatrix} y \\ \chi z \end{bmatrix}$

Applying chain rule,

2|f(z) =
$$e^{-z/2}$$
; where $z = g(y)$, $g(y) = y^{-1}s^{-1}y$, $y = h(x)$, $h(x) = x - y$.

Voling chain rule,

$$\frac{1f}{dx} = \frac{1}{dz} \cdot \frac{dz}{dy} \cdot \frac{dy}{dx}$$
here, $\frac{1}{dz} = \frac{1}{dz} \cdot (e^{-z/2}) = -\frac{e^{(-z/2)}}{2}$

$$\frac{dz}{dy} = \frac{1}{dy} \cdot (y^{T}S^{-1}y)$$

$$= \lim_{h \to 0} \frac{(y^{T} + h)S'(y + h) - y^{T}S^{-1}y}{h}$$

$$= \lim_{h \to 0} \frac{(y^{T}S^{-1} + hS^{-1})(y + h) - y^{T}S^{-1}y}{h}$$

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