Image Object Kalman Filtering

Bounding box line location

State vector s:

$$S = egin{bmatrix} x_{min} \ v_{xmin} \ a_{xmin} \ x_{max} \ v_{xmax} \ a_{xmax} \ y_{min} \ v_{ymin} \ a_{ymin} \ y_{max} \ v_{ymax} \ a_{ymax} \ a_{ym$$

where

 $(x_{min}, x_{max}, y_{min}, y_{max})$ = location of the bounding box corner lines in the image $(v_{xmin}, v_{xmax}, v_{ymin}, v_{ymax})$ = velocity of the bounding box corner line in the image $(a_{xmin}, a_{xmax}, a_{ymin}, a_{ymax})$ = acceleration of the bounding box corner line in the image

State equation in differential form:

State equation in difference form:

$$s(k+1) = (I + \Delta * A_1) * s(k) + \epsilon(k)$$

where Δ is the time increment and ε Gaussian noise with covariance R.

Measurement equation

Where δ is Gaussian noise with covariance matrix Q.

Kalman filter initialization:

$$\mu(0) = \begin{bmatrix} x_{min}(0) \\ 0 \\ 0 \\ x_{max}(0) \\ 0 \\ 0 \\ y_{min}(0) \\ 0 \\ 0 \\ y_{max}(0) \\ 0 \\ 0 \end{bmatrix}$$

where x(0) is the first location measurement.

where α , β and γ are believed variances of location, velocity and acceleration, for example 1.0.

where r_1 , r_2 and r_3 are believed variances of location, velocity and acceleration, for example 1.0.

$$Q = \begin{bmatrix} q & 0 & 0 & 0 \\ 0 & q & 0 & 0 \\ 0 & 0 & q & 0 \\ 0 & 0 & 0 & q \end{bmatrix}$$

Where q is the believed measurement variance, for example 1.0.

Kalman filter update:

$$\begin{split} \mu_1(k) &= A * \mu(k-1) \\ \Sigma_1(k) &= A * \Sigma(k-1) * A^T + R \\ K(k) &= \Sigma_1(k) * C^T(C * \Sigma_1(k) * C^T + Q)^{-1} \\ \mu(k) &= \mu_1(k) + K(k) * (z(k) - C * \mu_1(k)) \\ \Sigma(k) &= (I - K(k) * C) * \Sigma_1(k) \end{split}$$