

## Pattern Kalman Filtering

### Bounding box corner location

State vector  $s$ :

$$s = \begin{bmatrix} l \\ v \end{bmatrix}$$

where

$l$  = location coordinate ( $x_{\min}$ ,  $x_{\max}$ ,  $y_{\min}$ ,  $y_{\max}$ ) of the bounding box corner in the image

$v$  = velocity ( $vx_{\min}$ ,  $vx_{\max}$ ,  $vy_{\min}$ ,  $vy_{\max}$ ) of the bounding box corner in the image

State equation in differential form:

$$\frac{ds(t)}{dt} = \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix} * s(t) + \epsilon(t) = A_1 * s$$

State equation in difference form:

$$\begin{aligned} s(k+1) &= (I + \Delta * A_1) * s(k) + \epsilon(k) \\ &= \begin{bmatrix} 1 & \Delta \\ 0 & 1 \end{bmatrix} * s(k) + \epsilon(k) = A * s(k) + \epsilon(k) \end{aligned}$$

where  $\Delta$  is the time increment and  $\epsilon$  Gaussian noise with covariance  $R$ .

Measurement equation

$$z(k) = \begin{bmatrix} 1 & 0 \end{bmatrix} * s(k) + \delta(k) = C * s(k) + \delta(k)$$

Where  $\delta$  is Gaussian noise with covariance matrix  $Q$ .

Kalman filter initialization:

$$\mu(0) = \begin{bmatrix} l(0) \\ 0 \end{bmatrix}$$

where  $l(0)$  is the first location measurement.

$$\Sigma(0) = \begin{bmatrix} 10.0 & 0 \\ 0 & 10000.0 \end{bmatrix}$$

where 10.0 and 10000.0 are believed initial error variances of location and velocity.

$$R = \begin{bmatrix} 1.0 & 0 \\ 0 & 1.0 \end{bmatrix}$$

where diagonal elements are believed state equation variances of location and velocity.

$$Q = [10.0]$$

Where 10.0 is the believed measurement variance.

Kalman filter update:

$$\begin{aligned} \mu_1(k) &= A * \mu(k-1) \\ \Sigma_1(k) &= A * \Sigma(k-1) * A^T + R \end{aligned}$$

$$K(k) = \Sigma_1(k) * C^T * (C * \Sigma_1(k) * C^T + Q)^{-1}$$

$$\mu(k) = \mu_1(k) + K(k) * (z(k) - C * \mu_1(k))$$

$$\Sigma(k) = (I - K(k) * C) * \Sigma_1(k)$$