Body Kalman Filtering Body center point location

State vector s:

$$s = \begin{bmatrix} x \\ y \\ z \\ v_x \\ v_y \\ v_z \end{bmatrix}$$

where

(x, y, z) = location of the body center point (v_x, v_y, v_z) = velocity of the body

State equation in differential form:

State equation in difference form:

$$A = \begin{bmatrix} 1 & 0 & 0 & \Delta & 0 & 0 \\ 0 & 1 & 0 & 0 & \Delta & 0 \\ 0 & 0 & 1 & 0 & 0 & \Delta \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

where Δ is the time increment and ε Gaussian noise with covariance R:

Measurement equation:

$$z(k) = C * s(k) + \delta(k)$$

$$C = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \end{bmatrix}$$

Where δ is Gaussian noise with covariance matrix Q:

$$Q = \begin{bmatrix} 200 & 0 & 0 \\ 0 & 200 & 0 \\ 0 & 0 & 200 \end{bmatrix}$$

Kalman filter initialization:

$$\mu(0) = \begin{bmatrix} x(0) \\ y(0) \\ z(0) \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

where x(0), y(0), z(0) is the first location measurement.

$$\Sigma(0) = \begin{bmatrix} 100\,000 & 0 & 0 & 0 & 0 & 0 \\ 0 & 100\,000 & 0 & 0 & 0 & 0 \\ 0 & 0 & 100\,000 & 0 & 0 & 0 \\ 0 & 0 & 0 & 100\,000 & 0 & 0 \\ 0 & 0 & 0 & 0 & 100\,000 & 0 \\ 0 & 0 & 0 & 0 & 0 & 100\,000 \end{bmatrix}$$

Kalman filter update:

$$\begin{split} \mu_1(k) &= A * \mu(k-1) \\ \Sigma_1(k) &= A * \Sigma(k-1) * A^T + R \\ K(k) &= \Sigma_1(k) * C^T(C * \Sigma_1(k) * C^T + Q)^{-1} \\ \mu(k) &= \mu_1(k) + K(k) * (z(k) - C * \mu_1(k)) \\ \Sigma(k) &= (I - K(k) * C) * \Sigma_1(k) \end{split}$$