# COL341: Assignment 3

Note: random\_state has been set to 0 for consistent results

# Single-state

Faces at 1, Rest at 0

|                    | 3.1A (IG)     | 3.1A (GINI) | 3.1B (GINI) | 3.1B (IG)   |  |
|--------------------|---------------|-------------|-------------|-------------|--|
| Training Time      | 139.0977933   | 162.330637  | 3.567991257 | 2.245169163 |  |
|                    |               | On          | Train       |             |  |
| Accuracy           | 0.8555        | 0.8635      | 0.9885      | 0.999       |  |
| Precision of state |               |             |             |             |  |
| 1                  | 0.903935957   | 0.897602074 | 0.988749173 | 1           |  |
| Precision of state |               |             |             |             |  |
| 0                  | 0.710578842   | 0.748358862 | 0.987730061 | 0.996015936 |  |
| Recall of state 1  | 0.903333333   | 0.923333333 | 0.996       | 0.998666667 |  |
| Recall of state 0  | 0.712         | 0.684       | 0.966       | 1           |  |
|                    | On Validation |             |             |             |  |
| Accuracy           | 0.825         | 0.8175      | 0.9275      | 0.9425      |  |
| Precision of state |               |             |             |             |  |
| 1                  | 0.888513514   | 0.874587459 | 0.935691318 | 0.969491525 |  |
| Precision of state |               |             |             |             |  |
| 0                  | 0.644230769   | 0.639175258 | 0.898876404 | 0.866666667 |  |
| Recall of state 1  | 0.876666667   | 0.883333333 | 0.97        | 0.953333333 |  |
| Recall of state 0  | 0.67          | 0.62        | 0.8         | 0.91        |  |

|                    |                | 3.1C         | 3.1D         |                | 3.1E         |
|--------------------|----------------|--------------|--------------|----------------|--------------|
|                    | 3.1C (Default) | (GridSearch) | (BestPruned) | 3.1E (Default) | (GridSearch) |
| Training Time      | 0.015074968    | 0.01129365   | -            | 5.681501865    | 6.592205048  |
|                    |                | On           | Train        |                |              |
| Accuracy           | 0.9295         | 0.8775       | 0.9755       | 1              | 1            |
| Precision of state |                |              |              |                |              |
| 1                  | 0.974842767    | 0.928327645  | 0.972638436  | 1              | 1            |
| Precision of state |                |              |              |                |              |
| 0                  | 0.815465729    | 0.738317757  | 0.984946237  | 1              | 1            |
| Recall of state 1  | 0.93           | 0.906666667  | 0.995333333  | 1              | 1            |
| Recall of state 0  | 0.928          | 0.79         | 0.916        | 1              | 1            |
|                    |                | On           | Validation   |                |              |
| Accuracy           | 0.885          | 0.8775       | 0.935        | 0.9725         | 0.9825       |
| Precision of state |                |              |              |                |              |
| 1                  | 0.934931507    | 0.93728223   | 0.936305732  | 0.964630225    | 0.977198697  |
| Precision of state |                |              |              |                |              |
| 0                  | 0.75           | 0.725663717  | 0.930232558  | 1              | 1            |
| Recall of state 1  | 0.91           | 0.896666667  | 0.98         | 1              | 1            |
| Recall of state 0  | 0.81           | 0.82         | 0.8          | 0.89           | 0.93         |

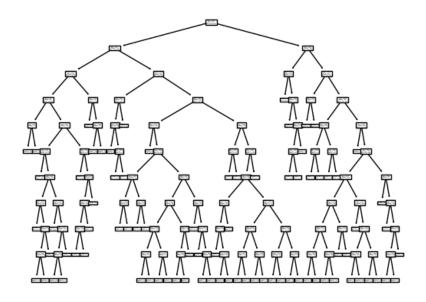
|                    |                 | 3.1F         |                | 3.1F        |
|--------------------|-----------------|--------------|----------------|-------------|
|                    | 3.1F (Gradient) | (GradientGS) | 3.1F (XGBoost) | (XGBoostGS) |
| Training Time      | 116.5799448     | Too long*    | 5.303102255    | 4.706798553 |
|                    |                 | On Train     |                |             |
| Accuracy           | 1               | -            | 1              | 1           |
| Precision of state |                 |              |                |             |
| 1                  | 1               | -            | 1              | 1           |
| Precision of state |                 |              |                |             |
| 0                  | 1               | -            | 1              | 1           |
| Recall of state 1  | 1               | -            | 1              | 1           |
| Recall of state 0  | 1               | -            | 1              | 1           |
|                    | On Validation   |              |                |             |
| Accuracy           | 0.98            | -            | 0.9875         | 0.9775      |
| Precision of state |                 |              |                |             |
| 1                  | 0.980263158     | -            | 0.983606557    | 0.97704918  |
| Precision of state |                 |              |                |             |
| 0                  | 0.979166667     | -            | 1              | 0.978947368 |
| Recall of state 1  | 0.993333333     | -            | 1              | 0.993333333 |
| Recall of state 0  | 0.94            | -            | 0.95           | 0.93        |

<sup>\*-</sup> Insufficient processing power to compute under 8 hours

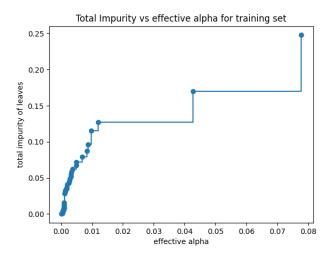
# Analysis of Sections

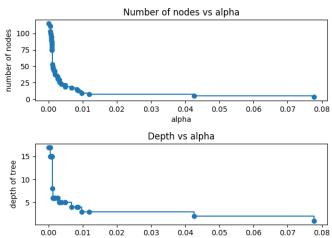
#### 3.1c

Visualised tree for SelectKBest



3.1d Required graphs





0.00

0.01

0.02

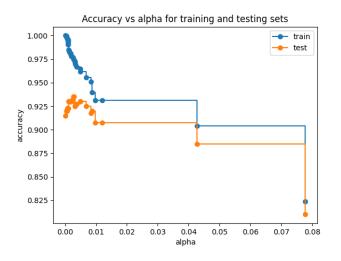
0.03

0.04

alpha

0.07

0.08

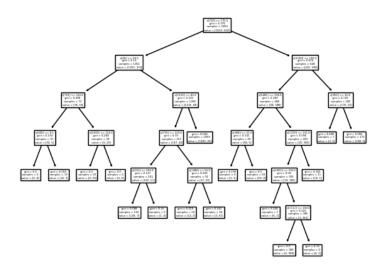


On training data, accuracy decreases with increase in alpha. We cannot conclude anything substantial from this. However, on testing data, accuracy first increases then decreases.

This clearly shows that post-pruning using ccp\_alpha can correct overfitting to some extent (for ideal selection of ccp\_alpha), however on increasing beyond this point accuracy is compromised.

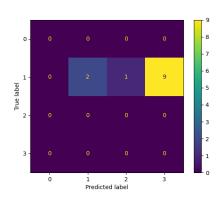
ccp\_alpha controls a trade-off between complexity of a subtree and how well it fits to training data. With increase in alpha, effect of complexity becomes more prominent and in turn tree is pruned, thus reducing accuracy on training data.

Cost function is penalised by adding a term + ccp\_alpha\*|Complexity measure of tree|, similar to addition of penalty in linear regression to make ridge regression.



Visualisation of best-pruned tree tree on validation split

3.2g
Model used: XGBClassifier() with best parameters as learned by Grid-Search
Images are variations of completely in frame, zoomed or misaligned (9 of my own, 3 of another).

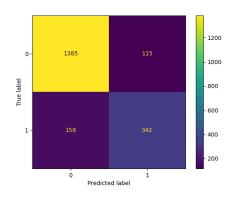


Despite good performance of classifier on validation set, it classifies these images poorly (2 correctly, 1 incorrectly as airplane, 9 incorrectly as dogs). This could be due to bias in the selection of images for training and validation purposes.

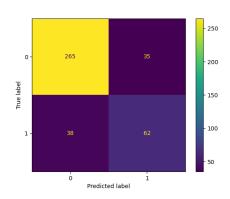
## Confusion Matrix and Parameters (3.1g)

• Decision tree from scratch (3.1a)

#### **GINI Index**

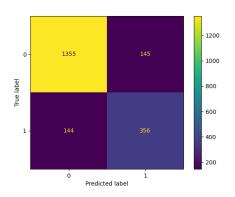


Confusion Matrix on Train data

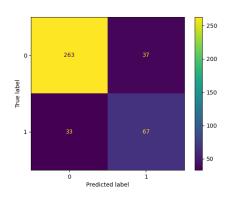


Confusion Matrix on Validation data

IG



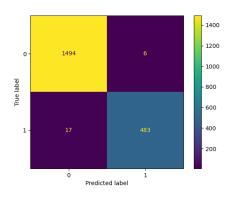
Confusion Matrix on Train data



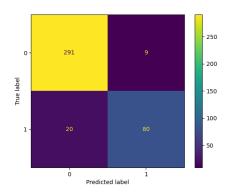
Confusion Matrix on Validation data

• Decision Tree sklearn (3.1b)

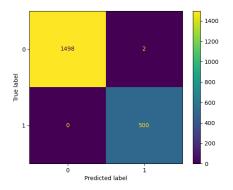
#### **GINI Index**

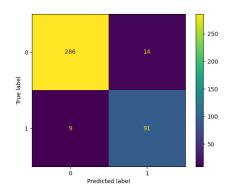


Confusion Matrix on Train data



Confusion Matrix on Validation data



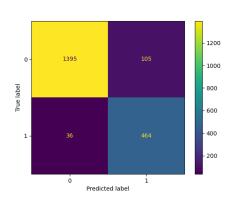


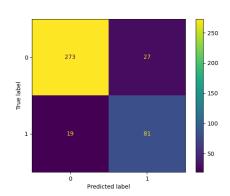
Confusion Matrix on Train data

Confusion Matrix on Validation data

• Decision Tree Grid-Search (3.1c)

#### Default

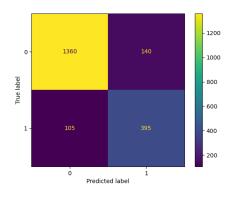


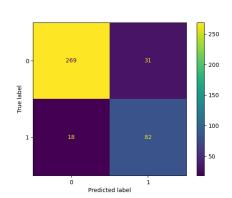


Confusion Matrix on Train data

Confusion Matrix on Validation data

Best parameters: {'criterion': 'entropy', 'max\_depth': 5, 'min\_samples\_split': 4}



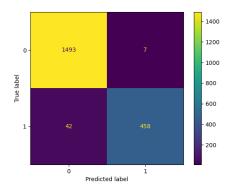


Confusion Matrix on Train data

Confusion Matrix on Validation data

• Decision Tree Post Pruning with Cost Complexity Pruning (3.1d)

Best-performing tree on validation split



1 - 20 80 - 50

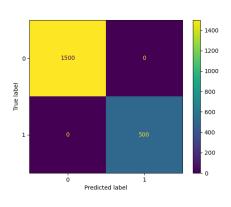
Predicted label

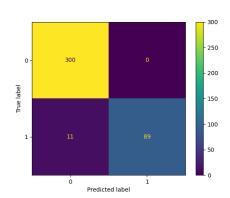
Confusion Matrix on Train data

Confusion Matrix on Validation data

Random forests (3.1e)

#### Default



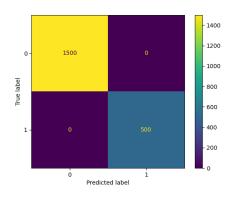


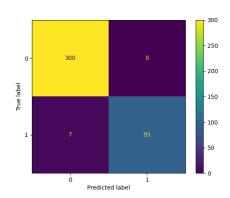
Confusion Matrix on Train data

Confusion Matrix on Validation data

#### **Grid-Search Best Parameters**

Best parameters: {'criterion': 'entropy', 'max\_depth': None, 'min\_samples\_split': 7, 'n\_estimators': 150}



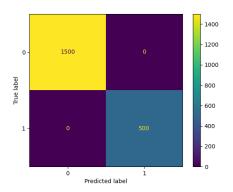


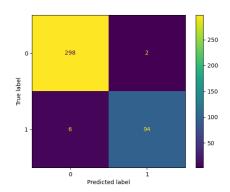
Confusion Matrix on Train data

Confusion Matrix on Validation data

• Gradient Boosted Trees and XGBoost (3.1f)

**Gradient Boosted with Default** 





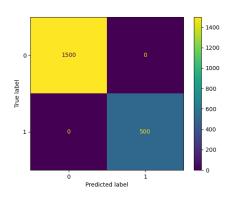
Confusion Matrix on Train data

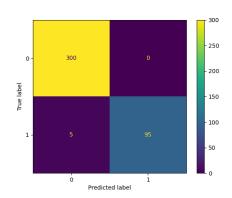
Confusion Matrix on Validation data

Gradient Boosted with Grid-Search Best Parameters

Note: Unable to complete regular, took ~8 hours.

XGBoost with Default



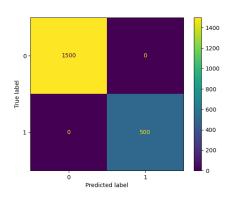


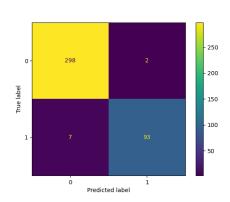
Confusion Matrix on Train data

Confusion Matrix on Validation data

XGBoost with Grid-Search Best Parameters

Best parameters: {'max\_depth': 6, 'n\_estimators': 40, 'subsample': 0.6}





Confusion Matrix on Train data

Confusion Matrix on Validation data

#### Multi-state

Cars at 0, Faces at 1, Airplanes at 2, Dogs at 3

|               | 3.2A (GINI) | 3.2A (IG)   | 3.2B (Default) | 3.2B<br>(GridSearch) |
|---------------|-------------|-------------|----------------|----------------------|
| Training Time | 3.27023983  | 4.622252703 | 0.013673067    | 0.014748335          |
|               |             | On          | Train          |                      |
| Accuracy      | 0.969       | 0.971       | 0.8105         | 0.669                |
|               |             | On          | Validation     |                      |
| Accuracy      | 0.7425      | 0.7225      | 0.6325         | 0.6025               |

|               | 3.2C (BestPruned) | 3.2D (Default) | 3.2D (GridSearch) | 3.2E (Gradient) |
|---------------|-------------------|----------------|-------------------|-----------------|
| Training Time | -                 | 9.960266113    | 9.01617837        | 704.1730013     |
|               | On                | Train          |                   |                 |
| Accuracy      | 0.957             | 1              | 0.9985            | 1               |
|               | On                | Validation     |                   |                 |
| Accuracy      | 0.7425            | 0.8725         | 0.8775            | 0.8925          |

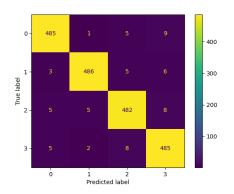
|               | 3.2E         |                | 3.2E        |
|---------------|--------------|----------------|-------------|
|               | (GradientGS) | 3.2E (XGBoost) | (XGBoostGS) |
| Training Time | Too long*    | 28.95156932    | 27.03962278 |
|               | On           | Train          |             |
| Accuracy      | -            | 1              | 1           |
|               | On           | Validation     |             |
| Accuracy      | -            | 0.9025         | 0.91        |

<sup>\*-</sup> Insufficient processing power to compute under 8 hours

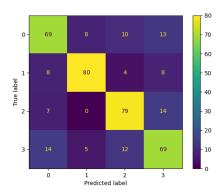
# Confusion Matrix and Parameters (3.2f)

• Decision Tree sklearn (3.2a)

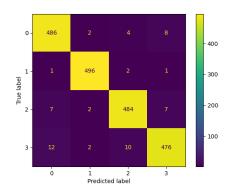
#### **GINI Index**







Confusion Matrix on Validation data



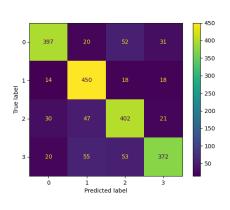
0 - 65 4 11 20 - 80 - 70 1 - 6 65 4 11 20 - 80 1 - 70 1 - 6 65 1 - 6 60 1 - 70 1 - 6 60 1 - 7

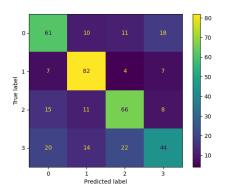
Confusion Matrix on Train data

Confusion Matrix on Validation data

• Decision Tree Grid-Search (3.2b)

#### Default:

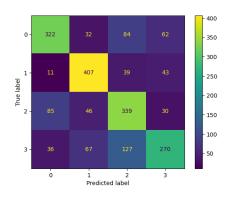


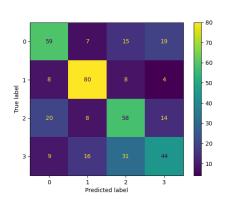


Confusion Matrix on Train data

Confusion Matrix on Validation data

Best parameters: {'criterion': 'entropy', 'max\_depth': 5, 'min\_samples\_split': 4}



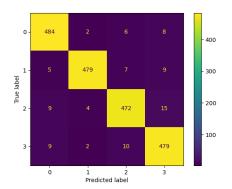


Confusion Matrix on Train data

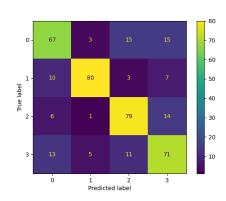
Confusion Matrix on Validation data

• Decision Tree Post Pruning with Cost Complexity Pruning (3.2c)

Best-performing tree



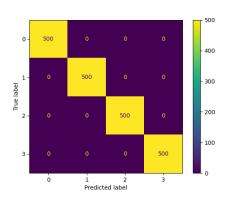
Confusion Matrix on Train data



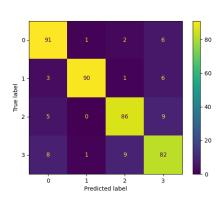
Confusion Matrix on Validation data

• Random forests (3.2d)

#### Default



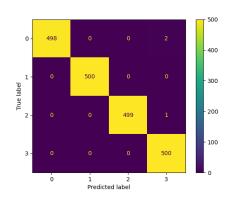
Confusion Matrix on Train data



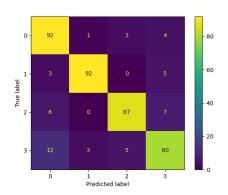
Confusion Matrix on Validation data

**Grid-Search Best Parameters** 

Best parameters: {'criterion': 'entropy', 'max\_depth': 10, 'min\_samples\_split': 10, 'n\_estimators': 100}



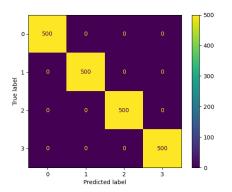
Confusion Matrix on Train data

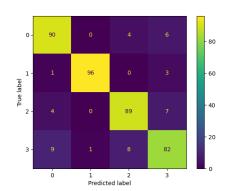


Confusion Matrix on Validation data

• Gradient Boosted Trees and XGBoost (3.2e)

Default





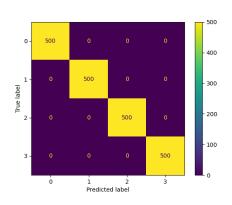
Confusion Matrix on Train data

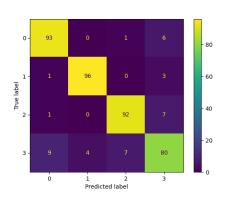
Confusion Matrix on Validation data

Gradient Boosted with Grid-Search Best Parameters

Note: Unable to complete, took ~8 hours

Default



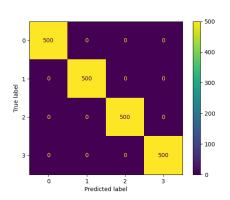


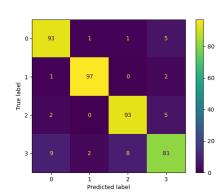
Confusion Matrix on Train data

Confusion Matrix on Validation data

XGBoost with Grid-Search Best Parameters

Best parameters: {'max\_depth': 10, 'n\_estimators': 50, 'subsample': 0.6}





Confusion Matrix on Train data

Confusion Matrix on Validation data

## Glossary

$$Accuracy = \frac{True\ Positive + True\ Negative}{Total}$$
 
$$Precision = \frac{True\ Positive}{True\ Positive + False\ Positive}$$
 
$$Recall = \frac{True\ Positive}{True\ Positive + False\ Negative}$$