



# AHSANIA MISSION UNIVERSITY OF SCIENCE & TECHNOLOGY

## Lab Report-5

**Lab No: 05**

**Course Code: CSE 2202**

**Course Title: Computer Algorithm Sessional.**

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1<sup>st</sup> Batch, 2<sup>nd</sup> Year, 2<sup>nd</sup> Semester

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Task No.: 01

Problem Statement: Merge Sort : Counting Inversions

Sample Input    STDIN Function

-----	-----
2	d = 2
5	arr[] size n = 5 for the first dataset
1 1 1 2 2	arr = [1, 1, 1, 2, 2]
5	arr[] size n = 5 for the second dataset
2 1 3 1 2	arr = [2, 1, 3, 1, 2]

Sample Output

0  
4

Source Code:

```
#include
<iostream> using
namespace std;
int Merge(int arr[], int le , int mid, int right)
{
    int n1 = mid - le + 1;
    int n2 = right - mid;
    int le Arr[n1],
    rightArr[n2];
    for (int i = 0; i < n1; i++)
    {
        le Arr[i] = arr[le + i];
    }
    for (int i = 0; i < n2; i++)
    {
        rightArr[i] = arr[mid + 1 + i];
    }
    int i = 0, j = 0, k = le , invCount = 0;
    while (i < n1 && j < n2)
    {
        if (le Arr[i] <= rightArr[j])
        {
            arr[k] = le
Arr[i];
```

```

i++;    }
else
    {
        arr[k] = rightArr[j];
        invCount += (n1
- i);    j++;

    }
k++;
;
    }
    while (i < n1)
    {
        arr[k] = le
Arr[i];
i++;    k++;
    }

    while (j < n2)
    {
        arr[k] = rightArr[j];

j++;
k++;
    }
    return invCount;
}
int mergeAndCount(int arr[], int le , int right)
{
    if (le >= right)
    {
        return 0;
    }
    int mid = le + (right - le ) / 2;
    int invCount = 0;    invCount +=
mergeAndCount(arr, le , mid);    invCount
+= mergeAndCount(arr, mid + 1, right);
invCount += Merge(arr, le , mid, right);
return invCount;
}
int main()
{
    int t;
    cin>
>t;
    while
(t--)

```

```

    {      int n;
cin>>n;      int
arr[n];
for(int i=0; i<n;
i++)
    {
cin>>arr[i];
    }

    cout<< mergeAndCount(arr,0,n-1)<<endl;
    }
}

```

Output:

```

| 2
5
1 1 1 2 2
0
5

```

Task No.: 02

Problem Statement:

D. Merge  
Sort  
limit per test  
2 seconds  
memory limit  
per test  
256 megabytes

Merge sort is a well-known sorting algorithm. The main function that sorts the elements of array  $a$  with indices from  $[l, r)$  can be implemented as follows:

1. If the segment  $[l, r)$  is already sorted in non-descending order (that is, for any  $i$  such that  $l \leq i < r - 1$   $a[i] \leq a[i + 1]$ ), then end the function call;
2. Let ;  $mid = \lfloor \frac{l+r}{2} \rfloor$
3. Call `mergesort(a, l, mid)`;
4. Call `mergesort(a, mid, r)`;
5. Merge segments  $[l, mid)$  and  $[mid, r)$ , making the segment  $[l, r)$  sorted in non-descending order. The merge algorithm doesn't call any other functions.

The array in this problem is 0-indexed, so to sort the whole array, you need to call mergesort(a, 0, n).

The number of calls of func on mergesort is very important, so Ivan has decided to calculate it while sorting the array. For example, if  $a = \{1, 2, 3, 4\}$ , then there will be 1 call of mergesort — mergesort(0, 4), which will check that the array is sorted and then end. If  $a = \{2, 1, 3\}$ , then the number of calls is 3: first of all, you call mergesort(0, 3), which then sets  $mid = 1$  and calls mergesort(0, 1) and mergesort(1, 3), which do not perform any recursive calls because segments (0, 1) and (1, 3) are sorted.

Ivan has implemented the program that counts the number of mergesort calls, but now he needs to test it. To do this, he needs to find an array  $a$  such that  $a$  is a permutation of size  $n$  (that is, the number of elements in  $a$  is  $n$ , and every integer number from  $[1, n]$  can be found in this array), and the number of mergesort calls when sorting the array is exactly  $k$ .

Help Ivan to find an array he wants!

#### Input

The first line contains two numbers  $n$  and  $k$  ( $1 \leq n \leq 100000$ ,  $1 \leq k \leq 200000$ ) — the size of a desired permutation and the number of mergesort calls required to sort it.

#### Output

If a permutation of size  $n$  such that there will be exactly  $k$  calls of mergesort while sorting it doesn't exist, output -1. Otherwise output  $n$  integer numbers  $a[0], a[1], \dots, a[n-1]$  — the elements of a permutation that would meet the required conditions. If there are multiple answers, print any of them.

#### Examples

Input

3 3

Output

2 1 3

Input

4 1

Output

1 2 3 4

Input

5 6

Output

-1

#### Source Code:

```
#include
<bits/stdc++.h> using
namespace std;
int n, k;
int a[100010];
```

```

void dfs(int l, int r)
{
    if (k == 1 || l
+ 1 == r)
    {
        return;
    }
    k -= 2;
    int
mid = (l + r)/2;
swap(a[mid], a[mid
- 1]);
    dfs(l, mid);
    dfs(mid, r);
}

int main()
{
    cin >> n
>> k;
    if
(k % 2 ==
0)
    {
        cout << -1;
        return 0;
    }
    for (int i = 0; i < n; i++)
    {
a[i] = i +
1;
    }

    dfs(0,
n);
    if (k !=
1)
    {
        cout << -1;
    }
    else
    {
        for (int i = 0; i < n; i++)
        {
            prin ("%d ", a[i]);
        }
    }
}

```

Output:

```

3 3
2 1 3
Process returned 0 (0x0)   execution time : 16.709 s
Press any key to continue.
|

```

Task No.: 03

Problem Statement:

#### E. Binary Search

time limit per  
test  
2 seconds  
memory limit  
per test  
256 megabytes

Anton got bored during the hike and wanted to solve something. He asked Kirill if he had any new problems, and of course, Kirill had one.

You are given a permutation  $p$  of size  $n$ , and a number  $x$  that needs to be found. A permutation of length  $n$  is an array consisting of  $n$  distinct integers from 1 to  $n$  in arbitrary order. For example,  $[2, 3, 1, 5, 4]$  is a permutation, but  $[1, 2, 2]$  is not a permutation (2 appears twice in the array), and  $[1, 3, 4]$  is also not a permutation ( $n=3$  but there is 4 in the array).

You decided that you are a cool programmer, so you will use an advanced algorithm for the search — binary search. However, you forgot that for binary search, the array must be sorted.

You did not give up and decided to apply this algorithm anyway, and in order to get the correct answer, you can perform the following operation no more than 22 times before running the algorithm: choose the indices  $i, j$  ( $1 \leq i, j \leq n$ ) and swap the elements at positions  $i$  and  $j$ .

After that, the binary search is performed. At the beginning of the algorithm, two variables  $l=1$  and  $r=n+1$  are declared. Then the following loop is executed:

1. If  $r=l$ , end the loop
2.  $m = \lfloor \frac{r+l}{2} \rfloor$
3. If  $p_m \leq x$ , assign  $l=m$ , otherwise  $r=m$ .

The goal is to rearrange the numbers in the permutation before the algorithm so that after the algorithm is executed,  $p_l$  is equal to  $x$ . It can be shown that 22 operations are always sufficient.

Input

Each test consists of multiple test cases. The first line contains a single integer  $t$  ( $1 \leq t \leq 2 \cdot 10^5$ ) — the number of test cases. Then follow the descriptions of the test cases.

The first line of each test case contains two integers  $n$  and  $x$  ( $1 \leq x \leq n \leq 2 \cdot 10^5$ ) — the length of the permutation and the number to be found. The second line contains the permutation  $p$  separated by spaces ( $1 \leq p_i \leq n$ ). It is guaranteed that the sum of the values of  $n$  for all test cases does not exceed  $2 \cdot 10^6$ .

Output

For each test case, output an integer  $k$  ( $0 \leq k \leq 22$ ) on the first line — the number of operations performed by you. In the next  $k$  lines, output 2 integers  $i, j$  ( $1 \leq i, j \leq n$ ) separated by a space, indicating that you are swapping the elements at positions  $i$  and  $j$ .

Note that you do not need to minimize the number of operations.

Source Code:

```
#include <iostream>
#include <vector>
#include <algorithm> // For sort()

using namespace std;

int main() {
    int testCases;
    cout << "Enter number of test cases: ";
    cin >> testCases;

    while (testCases--> {
        int n, x;
        cout << "\nEnter size of array (n) and the target number (x): ";
        cin >> n >> x;

        vector<int> arr(n);
        cout << "Enter " << n << " elements of the array: ";
        for (int i = 0; i < n; i++) {
            cin >> arr[i];
        }

        // Find the index of x in the array
        int indexOfX = -1;
        for (int i = 0; i < n; i++) {
            if (arr[i] == x) {
                indexOfX = i;
                break;
            }
        }

        if (indexOfX == -1) {
            cout << "Output: -1 (x is not in the array)\n";
            continue;
        }

        // Sorted array to find correct position of x
        vector<int> sortedArr = arr;
        sort(sortedArr.begin(), sortedArr.end());

        int targetPosition = -1;
        for (int i = 0; i < n; i++) {
            if (sortedArr[i] == x) {
                targetPosition = i;
                break;
            }
        }
    }
}
```



```

    }
}

// Case 1: x is already at correct position
if (arr[targetPosition] == x && indexOfX == targetPosition) {
    cout << "Output: 0 (x is already at the correct position)\n";
}
// Case 2: One swap can fix it
else if (arr[targetPosition] == x) {
    cout << "Output:\n1\n";
    cout << indexOfX + 1 << " " << targetPosition + 1 << "\n";
}
// Case 3: Try two swaps
else {
    bool foundTwoSwap = false;
    for (int i = 0; i < n; i++) {
        if (arr[i] == x) continue;

        swap(arr[i], arr[indexOfX]);

        if (arr[targetPosition] == x) {
            cout << "Output:\n2\n";
            cout << indexOfX + 1 << " " << i + 1 << "\n";
            cout << i + 1 << " " << targetPosition + 1 << "\n";
            foundTwoSwap = true;
            break;
        }

        swap(arr[i], arr[indexOfX]); // Undo
    }

    if (!foundTwoSwap) {
        cout << "Output: -1 (Not possible even with two swaps)\n";
    }
}

return 0;
}

```

Output:

Enter number of test cases: 2

Enter size of array (n) and the target number (x): 5 2

Enter 5 elements of the array: 1 2 3 5 4

Output: 0 (x is already at the correct position)

Enter size of array (n) and the target number (x): 3 10

Enter 3 elements of the array: 1 2 3

Output: -1 (x is not in the array)

Process returned 0 (0x0) execution time : 55.921 s

Press any key to continue.