

**Graphs** 

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# **Graphs**

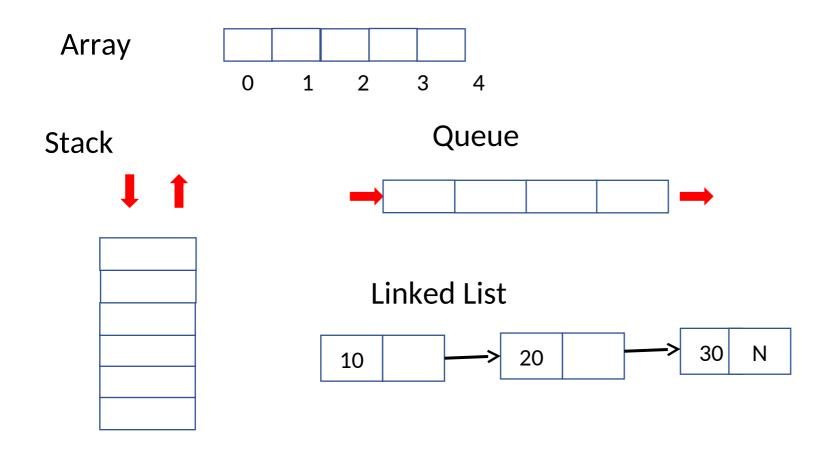
#### Saritha

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# **Introduction to graphs**



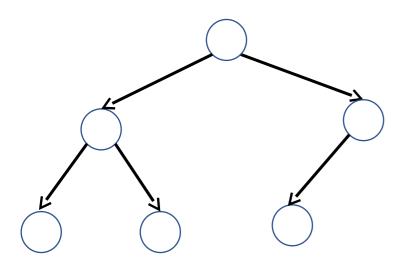
#### **Linear data structures**



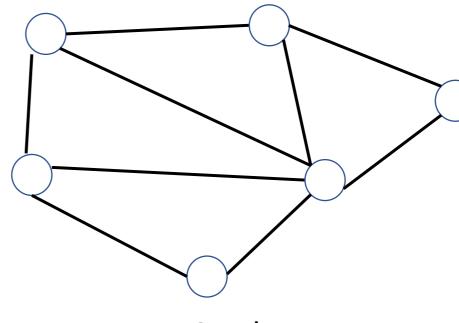
# DATA STRUCTURES AND ITS APPLICATIONS Introduction to Graphs

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#### **Non-Linear Data Structure**







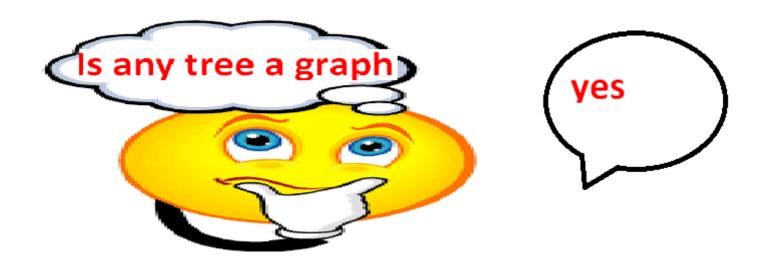
Tree

Graph

In a tree with N nodes there are N-1 edges

# Introduction to graph





# **Graphs**

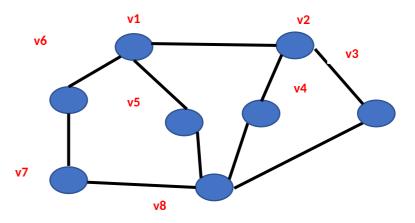


- A Graph is a data structure that consists of set of vertices and a set of edges that relate the node to each other.
- The set of edges represents the relationship among the vertices.
- A graph G is defined as

$$G=(V,E)$$

V: finite nonempty set of vertices

E: a set of edges



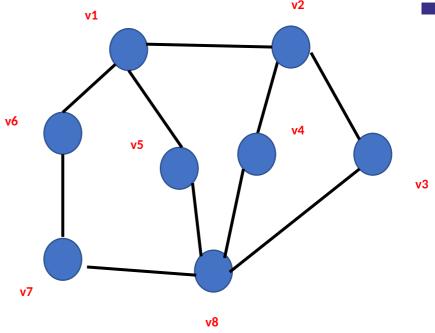
$$V = \{ v1, v2, v3, v4, v5, v6, v7, v8 \}$$

# **Representation of Edge**



$$V = \{ v1,v2,v3,v4,v5,v6,v7,v8 \}$$
  

$$E = \{ (v1,v2),(v2,v3),(v2,v4),(v4,v8),(v1,v5),(v1,v6),(v6,v7),(v5,v8) \}$$



# **Types of Graphs**



#### **Undirected Graph:**

• A graph is undirected, when the pair of vertices representing any edge is unordered.



# **Directed Graph:**

 A graph with all directed edges is called diagraph or directed graph.

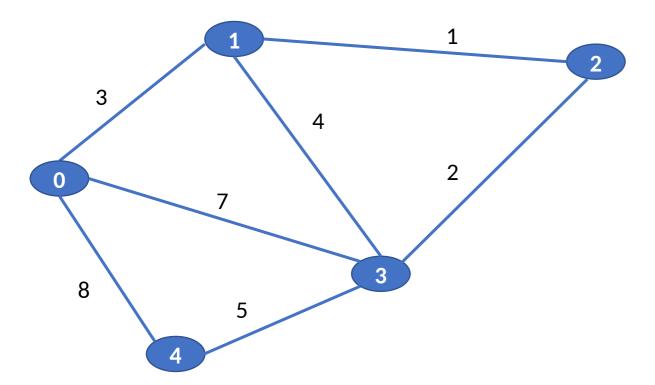


# **Types of Graphs**

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# Weighted Graph:

• A weighted graph is a graph where each edge has a numerical value called weight.



# **Graph terminologies**

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### **Adjacent Nodes:**

- •A node n is adjacent to node m if there is an edge from m to n.
- if n is adjacent to m, then n is called the **successor** of m and m is called the **predecessor** of n.



For example: a is adjacent to b

#### Path:

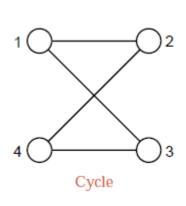
Path is a sequence of vertices that connect two nodes in a graph.

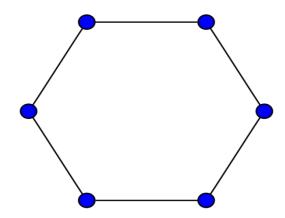
# **Graph terminologies**



### Cycle:

•A path from node to itself is called a cycle or cycle is path in which first and last vertices are same. A graph with at-least one cycle is called cyclic graph. For example the below graph are cyclic graphs



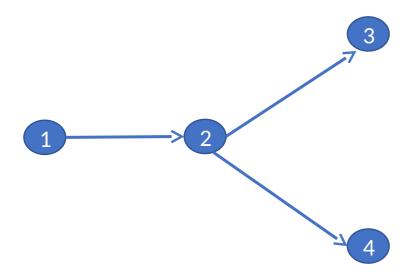


# **Graph terminologies**

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# Acylic:

•A graph with no cycles is called acyclic graph. A directed acyclic graph is called dag. For example below graph is a directed acylic graph



# **Graph terminologies**

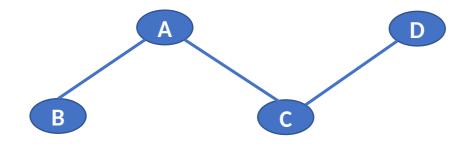


#### **Incident:**

A node n is incident to an edge x, if node is one of the two nodes the edge connects.

#### Degree:

The degree of vertex i is the number of edges incident on vertex i.



degree(A)=2, degree of(D)=1

# **Graph terminologies**

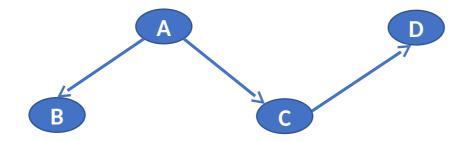
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### In-degree:

•In-degree of vertex i is the number of edges incident to i.

# **Out-degree:**

•Out-degree of vertex i is the number of edges incident from i.



Out-degree(A)=2,in-degree of(A)=0 Out-degree(c)=1,in-degree of (c)=1

# **Properties of Graph**

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# **Directed graph:**

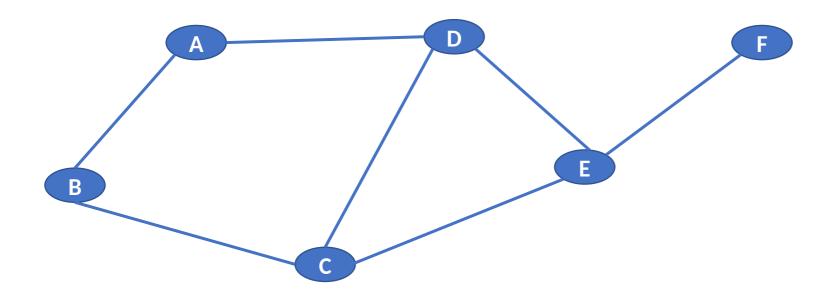
- •The number of possible pairs in an m vertex graph is m\*(m-1)
- •The number of edges in an directed graph is m\*(m-1) since the edge(u, v) is not the same as the edge(v, u)
- •The number of edges in an directed graph is<=m\*(m-1)

# **Properties of Graph**

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### **Undirected graph:**

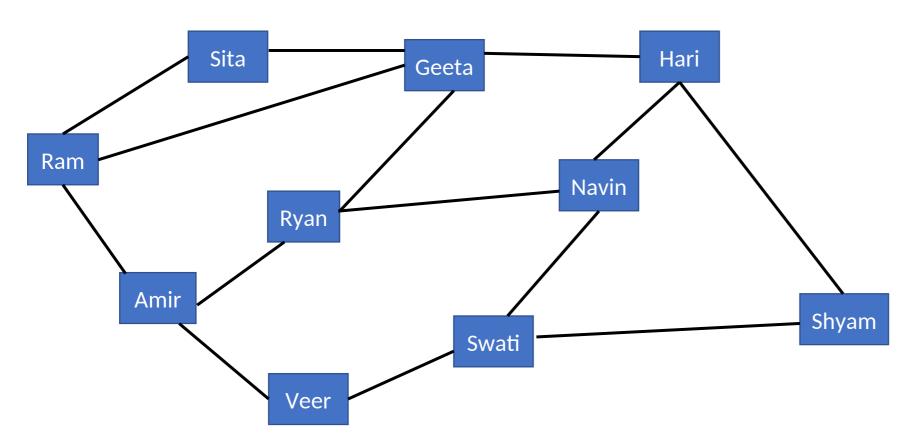
- •The number of possible pairs in an m vertex graph is m\*(m-1)
- •The number of edges in an undirected graph is  $m^*(m-1)/2$  since the edge(u, v) is same as the edge(v, u)



# **Applications of graph**

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# **Social Networking sites**





# **THANK YOU**

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