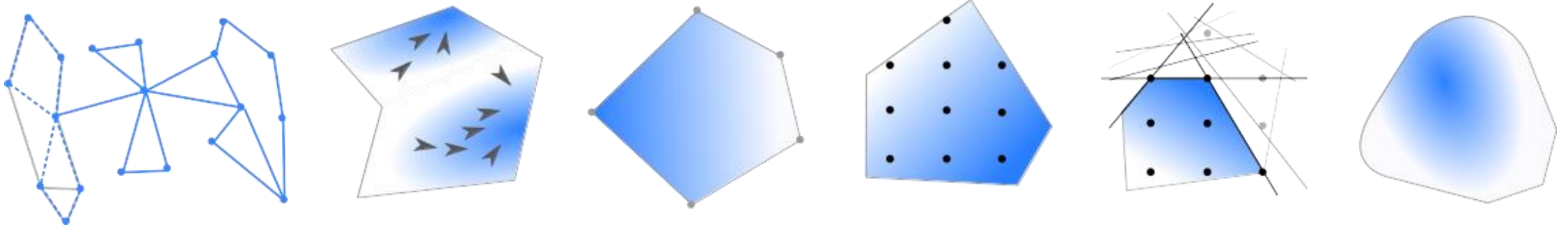
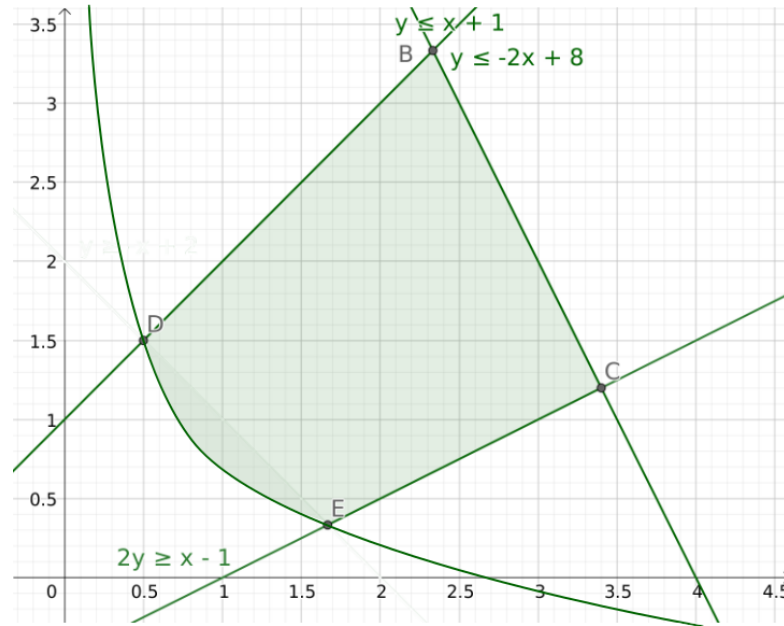


Meta-Heuristics 1

COMP4691 / 8691

↖
A2



Previously on COMP4691(8691)

- Construct \leftarrow TUE
- Improve
 - (Stochastic) Local Search
 - Simulated Annealing

MH

\leftarrow FLI

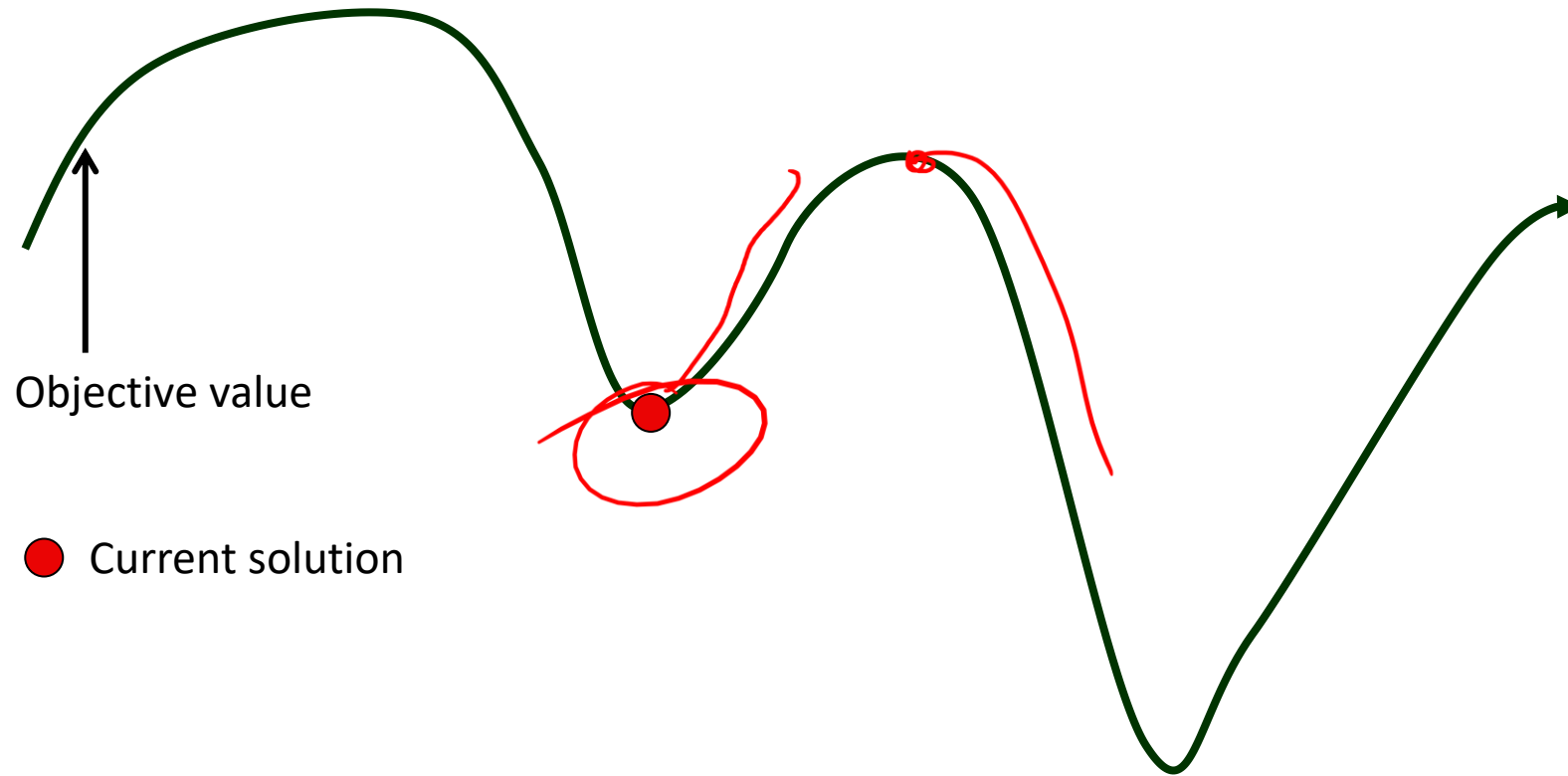
LOCAL SEARCH

Today:

- Other ways to escape local minima / search the solution space

Problems with Local Search I

Local minima



Meta-heuristics: Properties (1)

- can address both discrete- and continuous-domain optimisation problems
- are strategies that “guide” the search process LOCAL S.
- range from simple local search procedures to complex adaptive learning processes
- efficiently explore the search space to find good (near-optimal) feasible solutions
- provide no guarantee of global or local optimality B&B
- are agnostic to the unexplored feasible space (i.e., no “bound” information)
- lack a metric of “goodness” of solution (often stop due to an external time or iteration limit)

Meta-heuristics: Properties (2)

- are not based on some algebraic model (unlike exact methods)
- can be used in conjunction with an exact method
 - E.g., use meta-heuristic to provide upper bounds
 - E.g., use restricted MILP as “local heuristic” (== matheuristic)
- are usually non-deterministic
- are not problem specific (but their subordinate heuristics can be)
- may use some form of memory to better guide the search

← FEAS SOL

LNS

VRP 3-OPTs

Meta-heuristics: Overview

EXPLOITATION vs EXPLORATION

Exhibit Intensification and Diversification

- Need to do both 4-
- Can be explicitly controlled

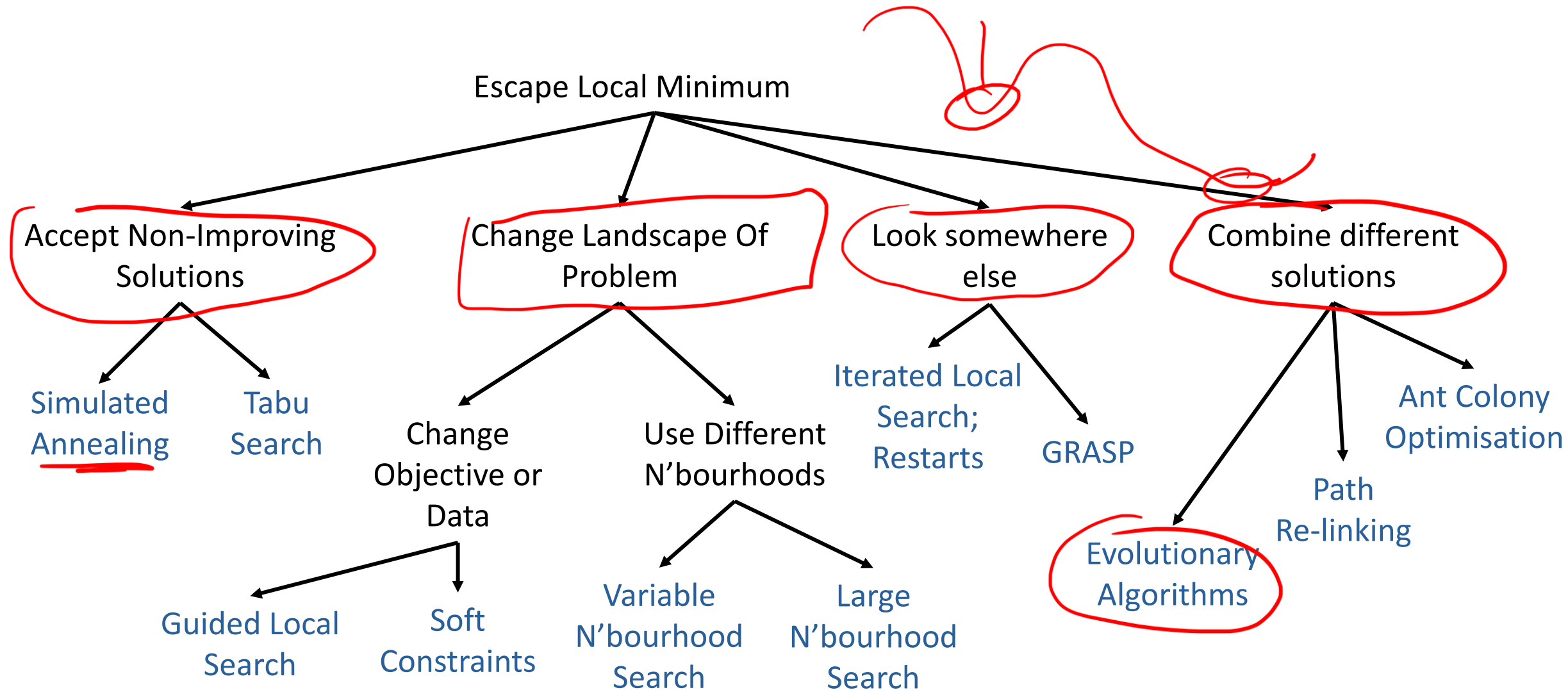
Intensification (Exploitation):

- Concentrate search around already-found “good” solutions
- Look harder in a smaller area

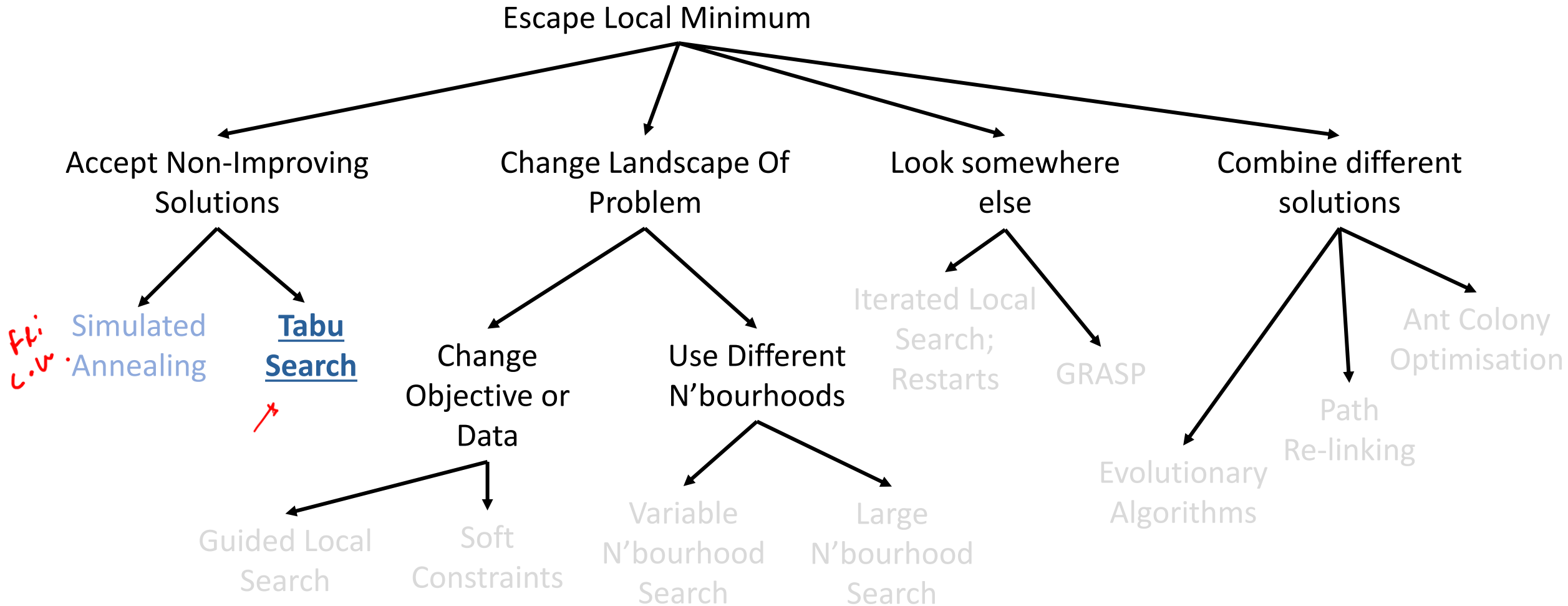
→ Diversification (Exploration):

- Expand the area being looked at
- Find new (promising?) areas to search
- Includes mechanisms to avoid getting trapped in confined areas of the search space

Meta-heuristics: An Incomplete Survey

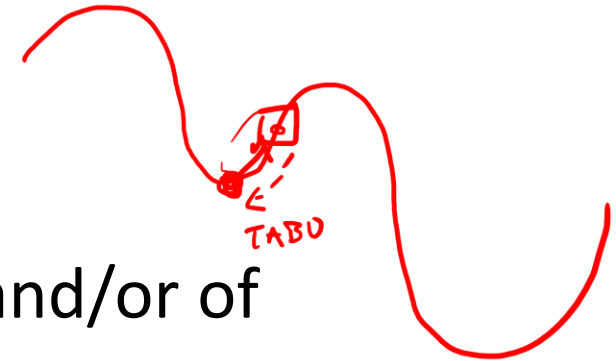


Meta-heuristics: An Incomplete Survey



Tabu Search

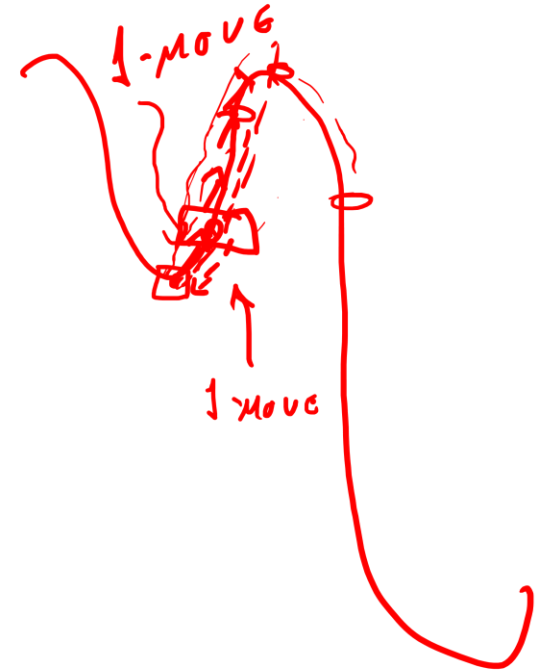
- Taboo (*English*): prohibited, disallowed, forbidden
- Tabu (*Fijian*): forbidden to use due to being sacred and/or of supernatural powers
- Starts with classic Local Search until a local minimum is found
- Choose an objective-increasing move
- Make undoing that move “tabu”
 - Place it on a “tabu list”
- Repeat



```
s ← GenerateInitialSolution() ✓
TabuList ← ∅ ✓
while termination conditions not met do
    s ← ChooseBestOf( $\mathcal{N}(s) \setminus \text{TabuList}$ )
    Update(TabuList)
endwhile
```

Tabu Search

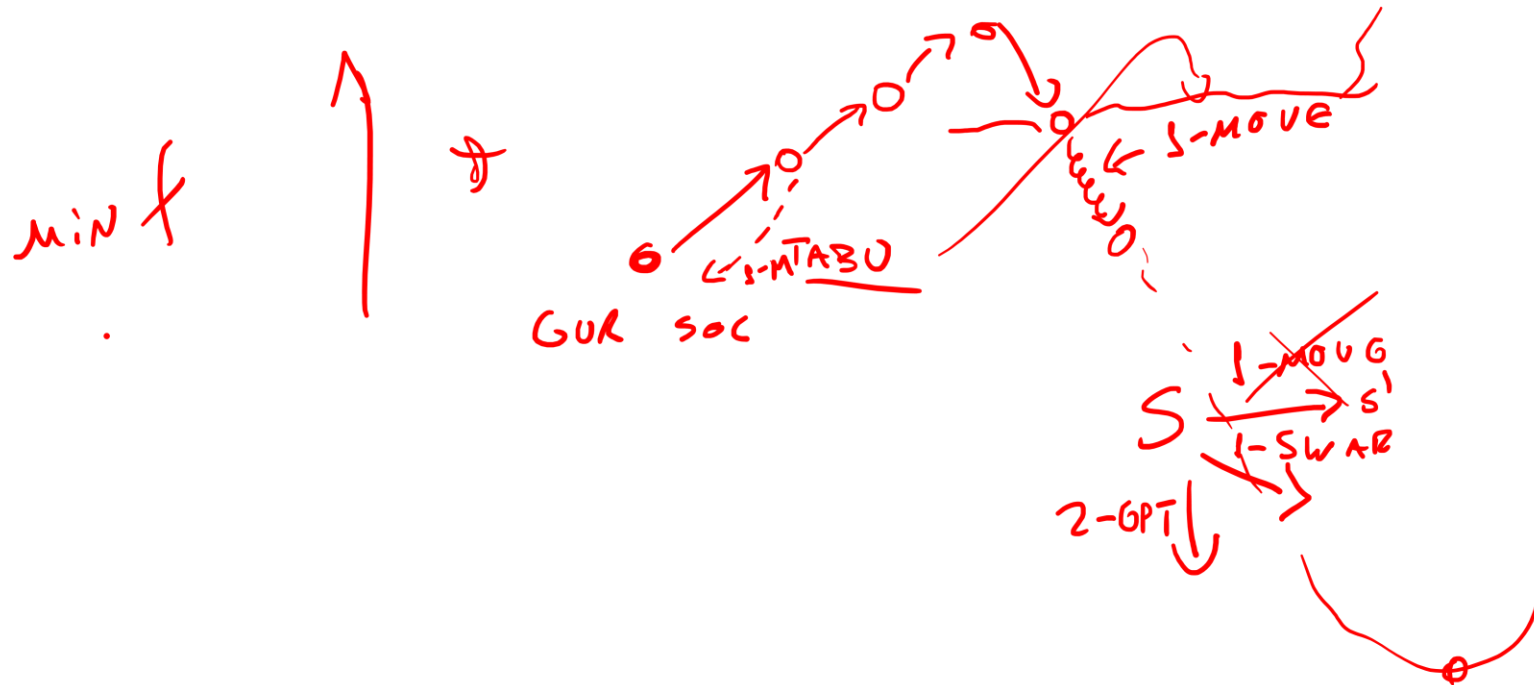
- Simple version: Tabu list has fixed length
 - Moves “fall off” the list after fixed number of iterations
- Length of the list is a critical parameter
 - Too small → Keep falling back into same local minimum
 - Too big → Not allowed to explore new space properly
- Dynamic list length
 - If you see the same solution, increase list length
 - Decrease when new incumbent found



Tabu Search

“Aspiration Criteria”

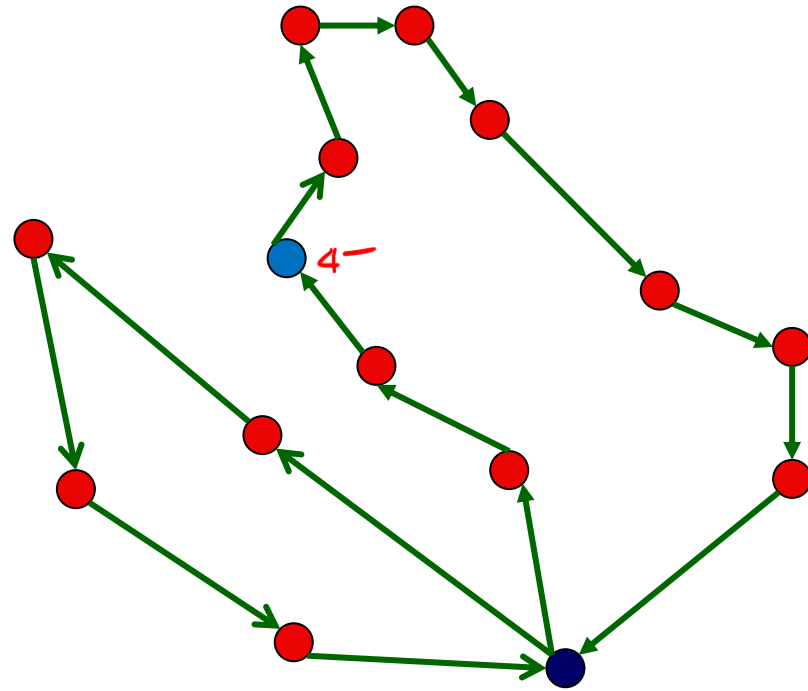
- Allowed to keep a solution if it meets certain criteria
- Most common: a new incumbent / best solution is kept



Tabu Search – VRP

E.g. VRP

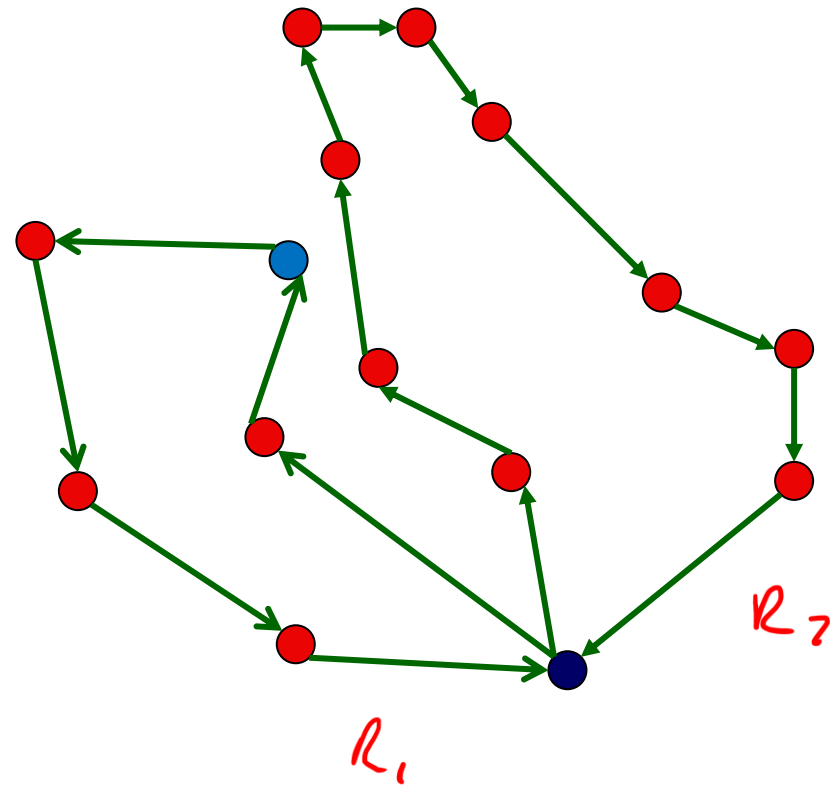
- 1-move



Tabu Search – VRP

E.g. VRP

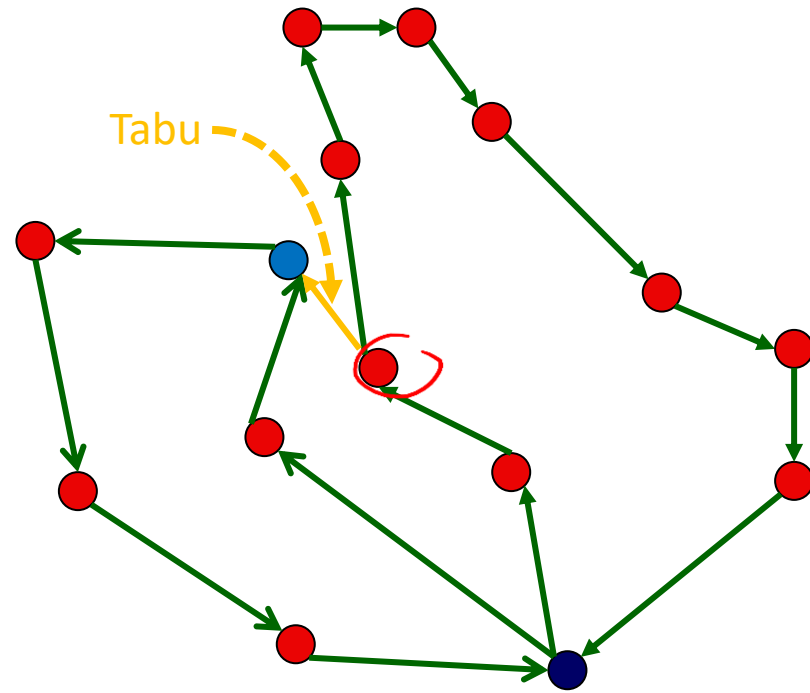
- 1-move



Tabu Search – VRP

E.g. VRP

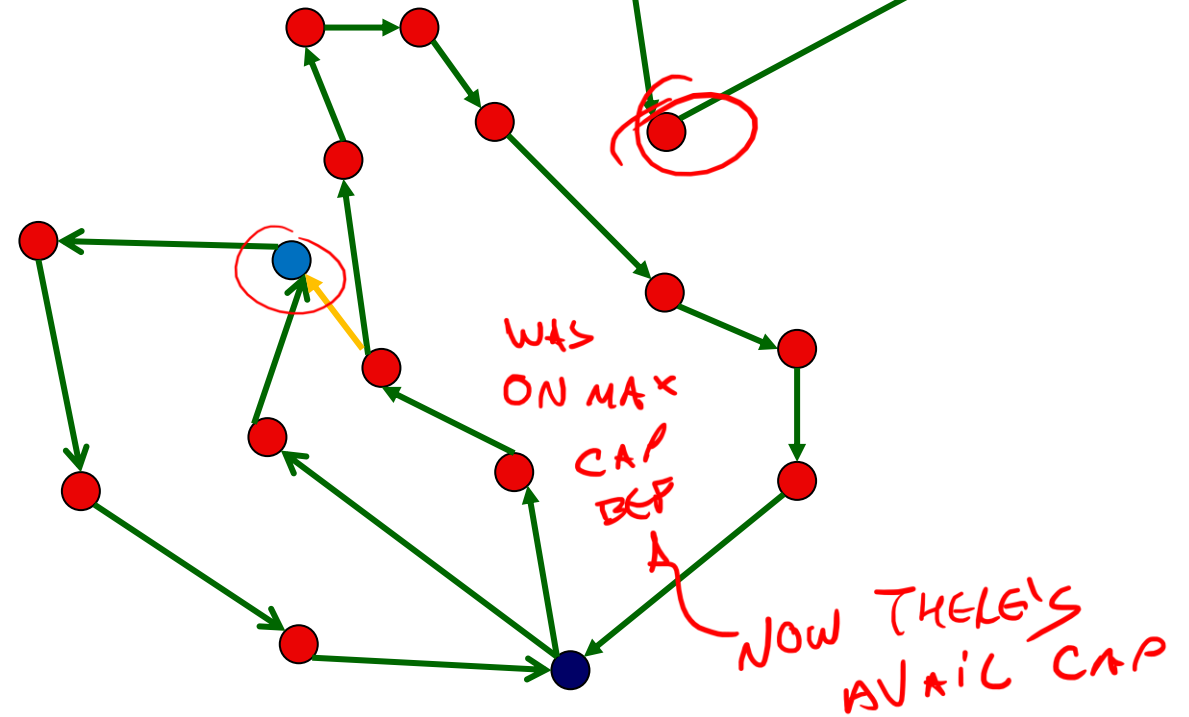
- 1-move



Tabu Search – VRP

E.g. VRP

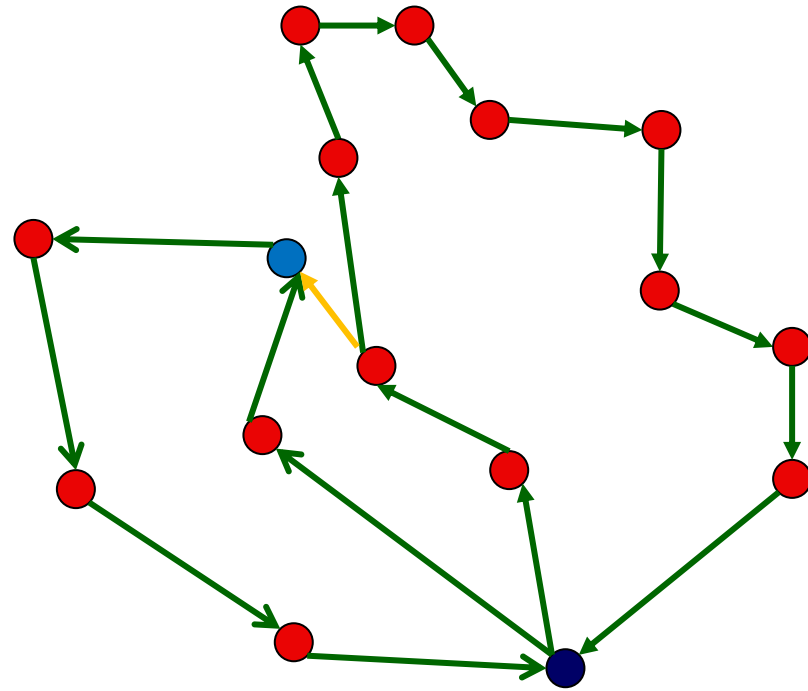
- 1-move



Tabu Search – VRP

E.g. VRP

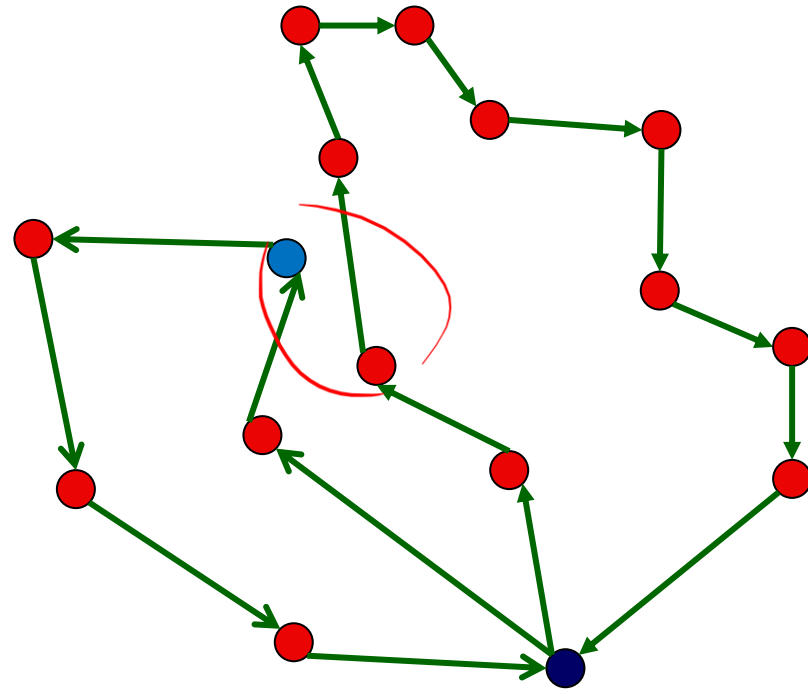
- 1-move



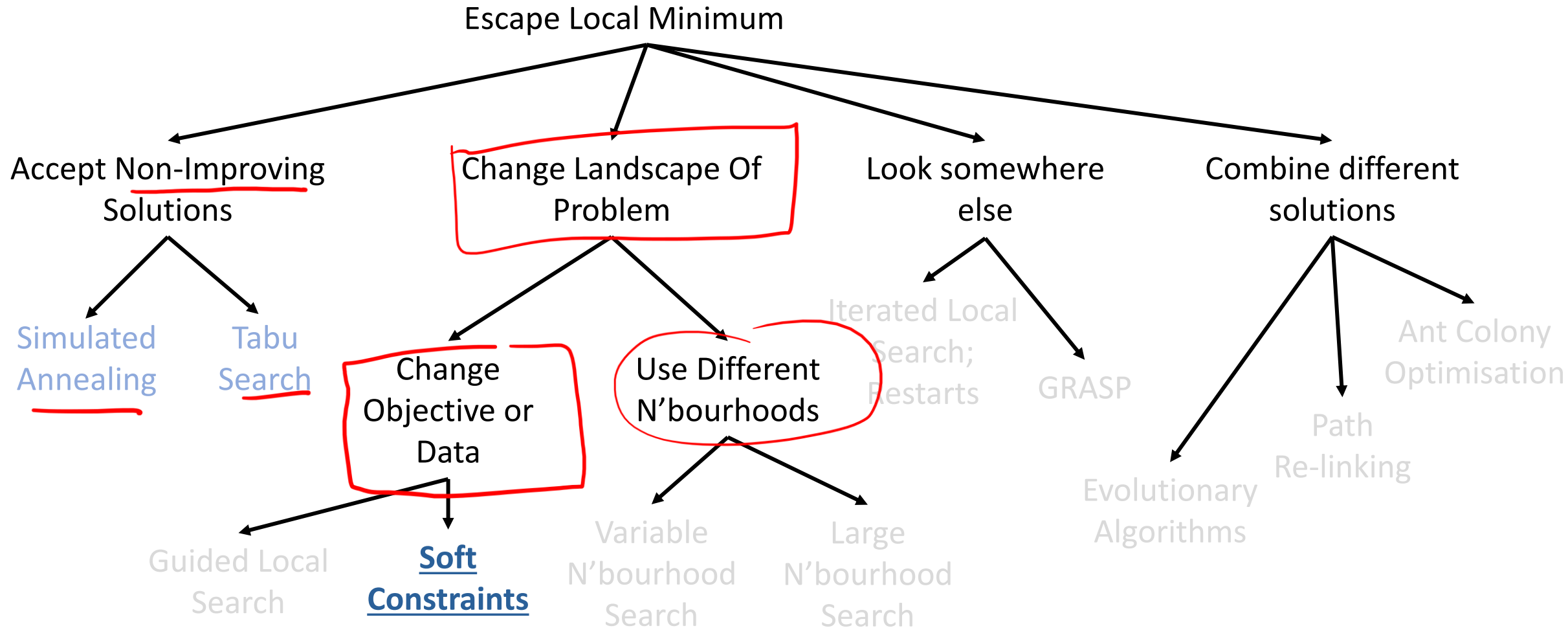
Tabu Search – VRP

E.g. VRP

- 1-move



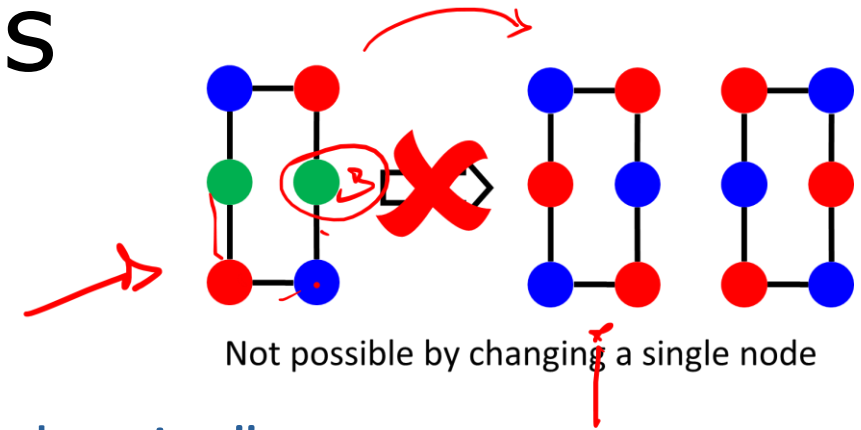
Meta-heuristics: An Incomplete Survey



Soft Constraints

General idea: Move constraints into the objective

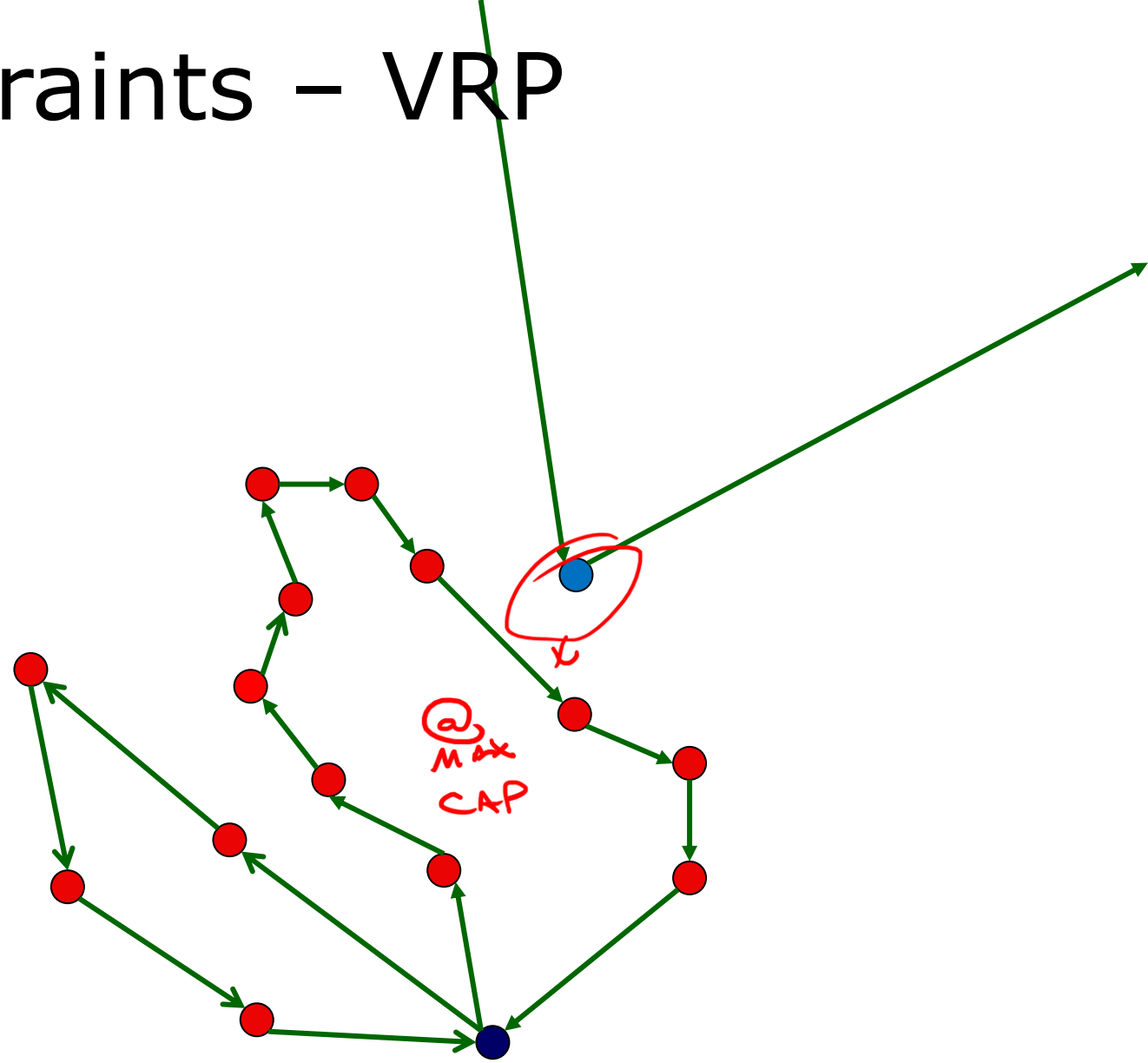
- Relax Constraints
 - Penalise degree of violation
 - Allows Local Search to move through “infeasibility barrier”
 - Opens new areas of search space
 - Maintain both best feasible solution, “best” infeasible solution
 - Increase penalty over time to force incumbent back to feasibility
 - Often used with Simulated Annealing or Tabu Search
 - Extensively used in practice, e.g., VRP
- Parameters:
 - Which constraints to relax
 - Penalty schedule



Soft Constraints – VRP

E.g. VRP

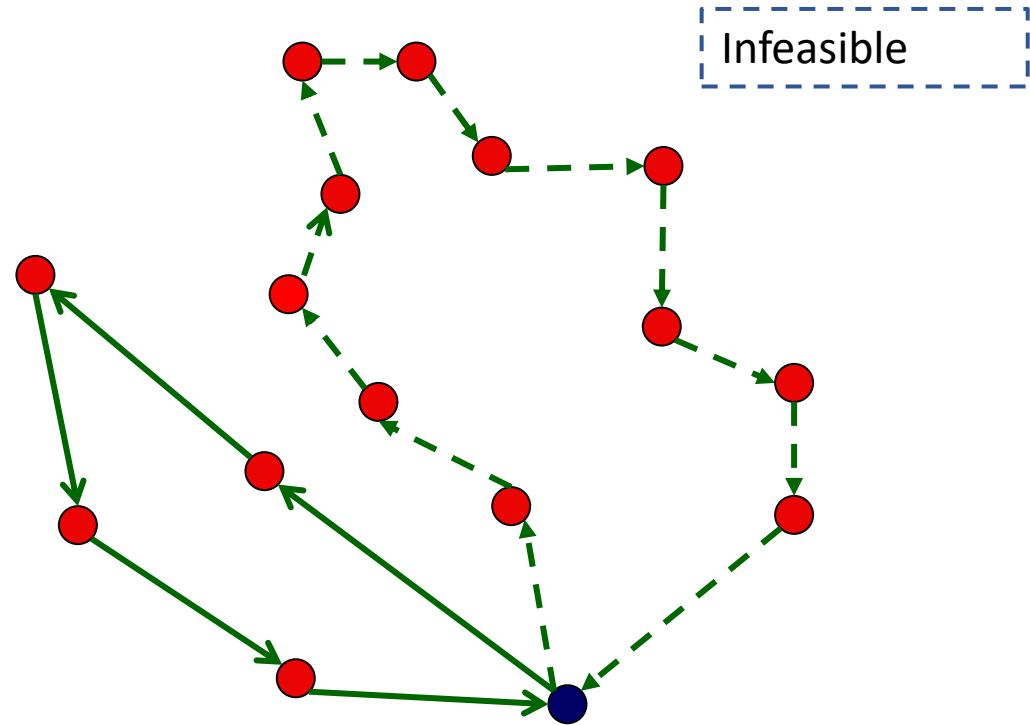
- 1-move



Soft Constraints + Tabu

E.g. VRP

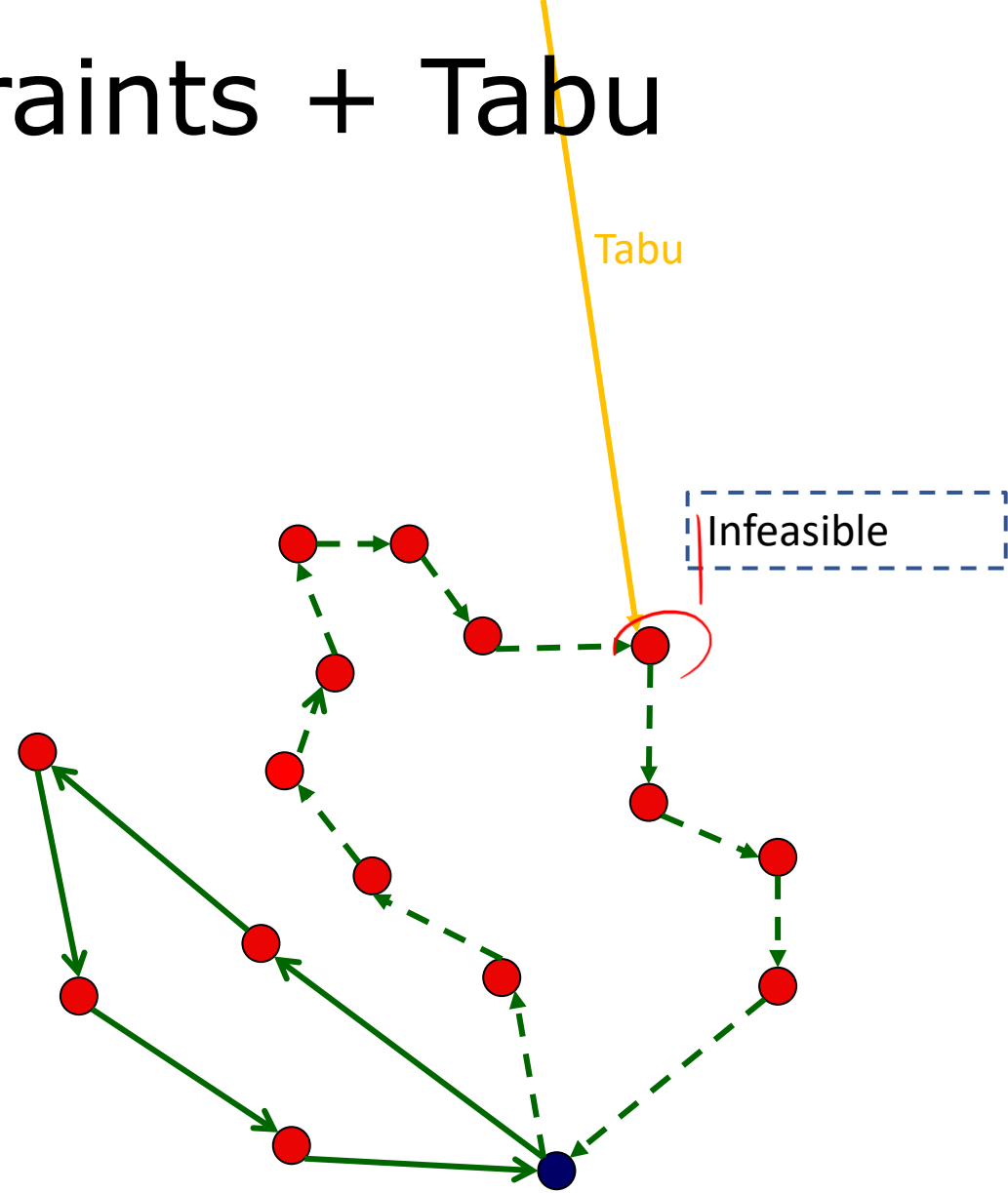
- 1-move



Soft Constraints + Tabu

E.g. VRP

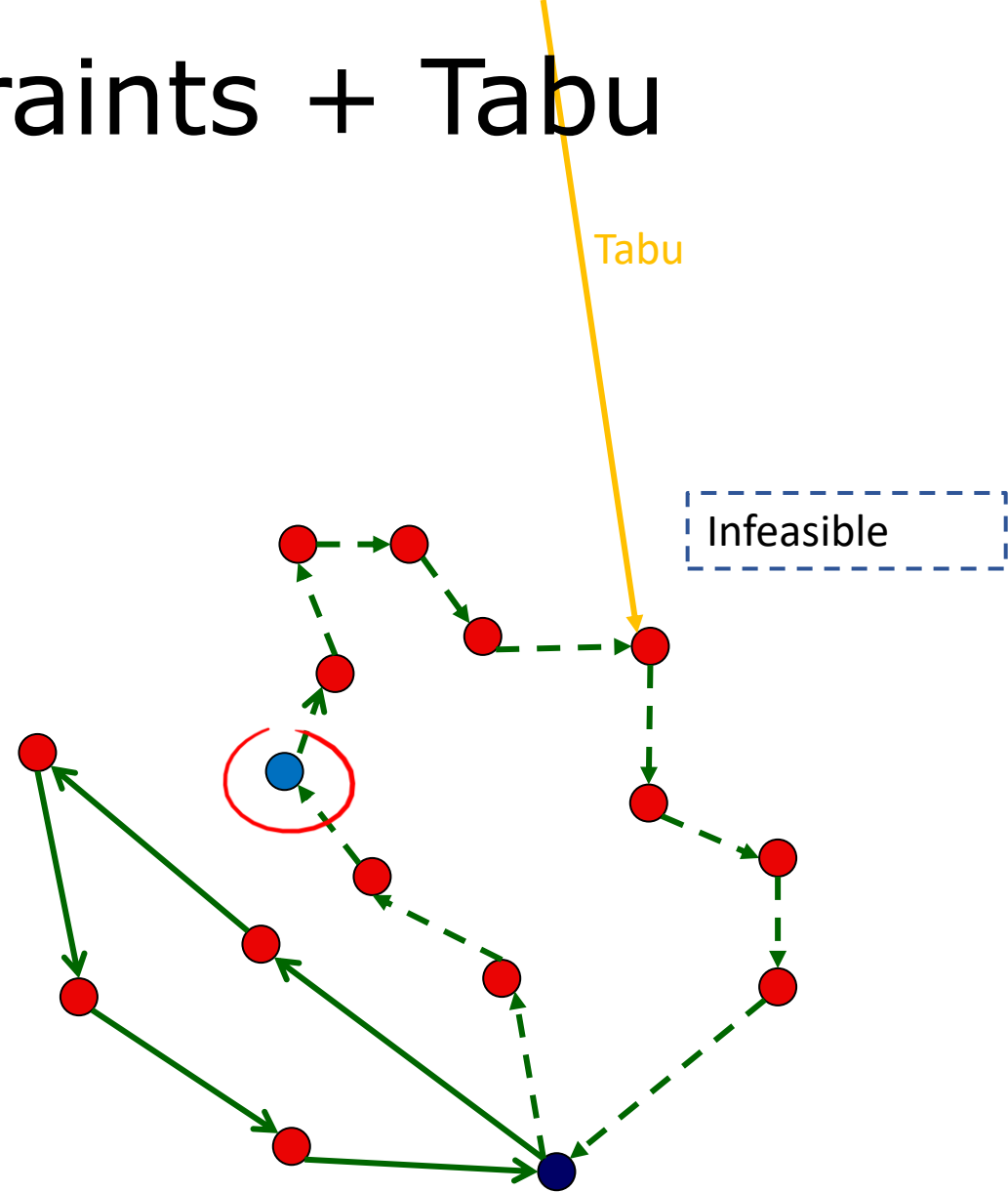
- 1-move



Soft Constraints + Tabu

E.g. VRP

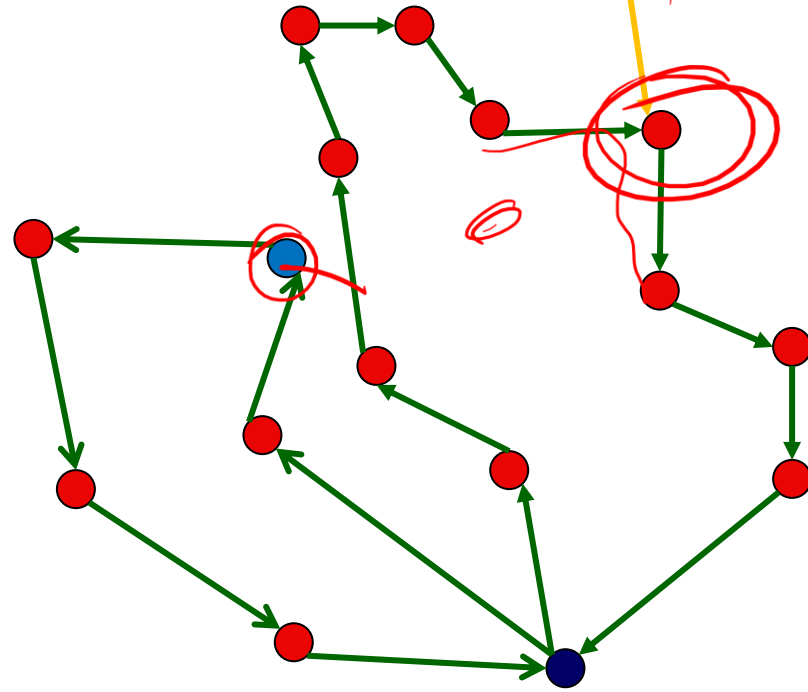
- 1-move



Soft Constraints + Tabu

E.g. VRP

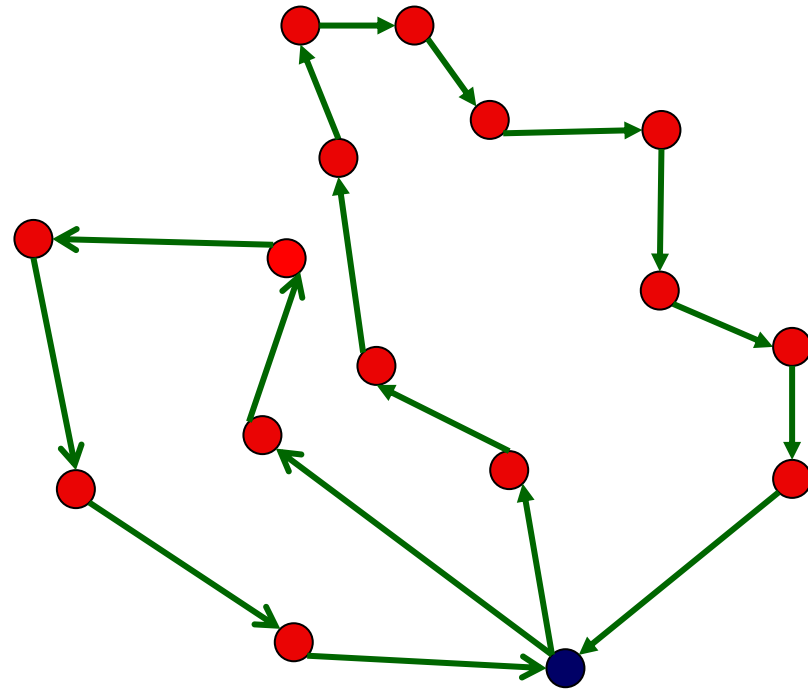
- 1-move



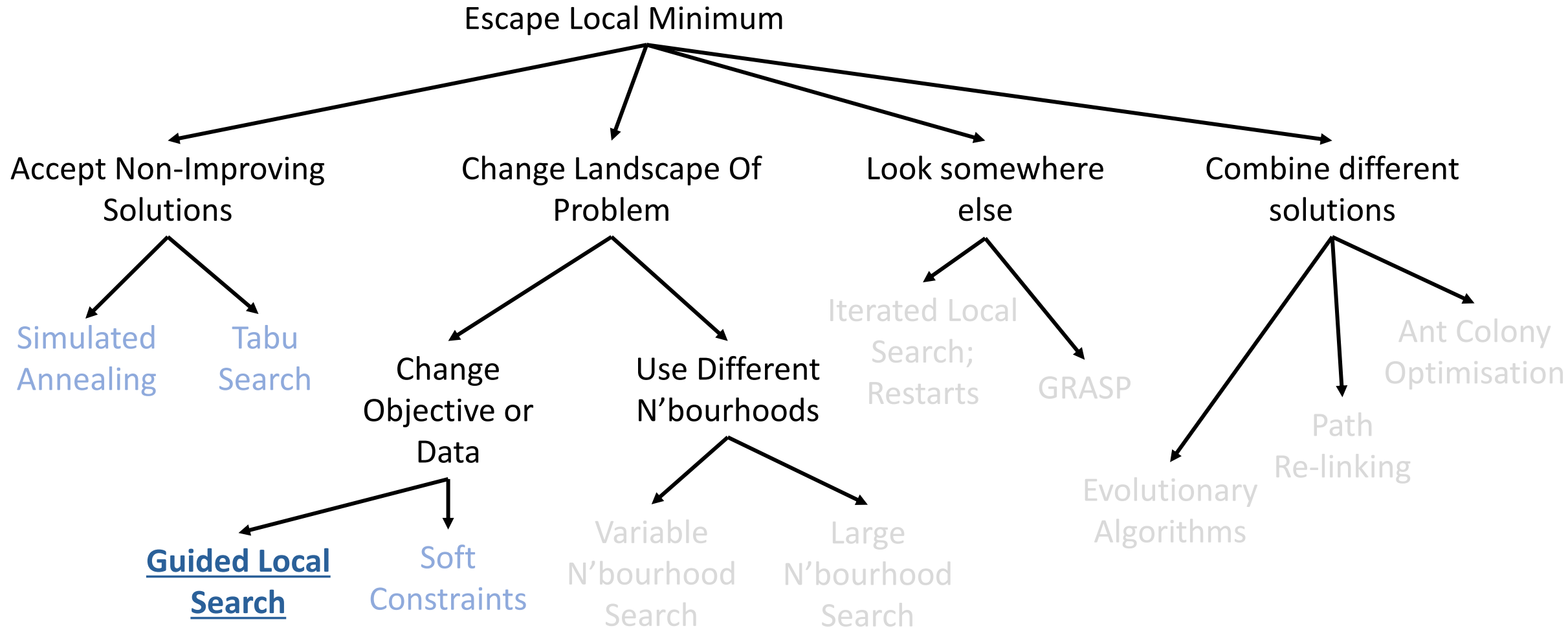
Soft Constraints + Tabu

E.g. VRP

- 1-move



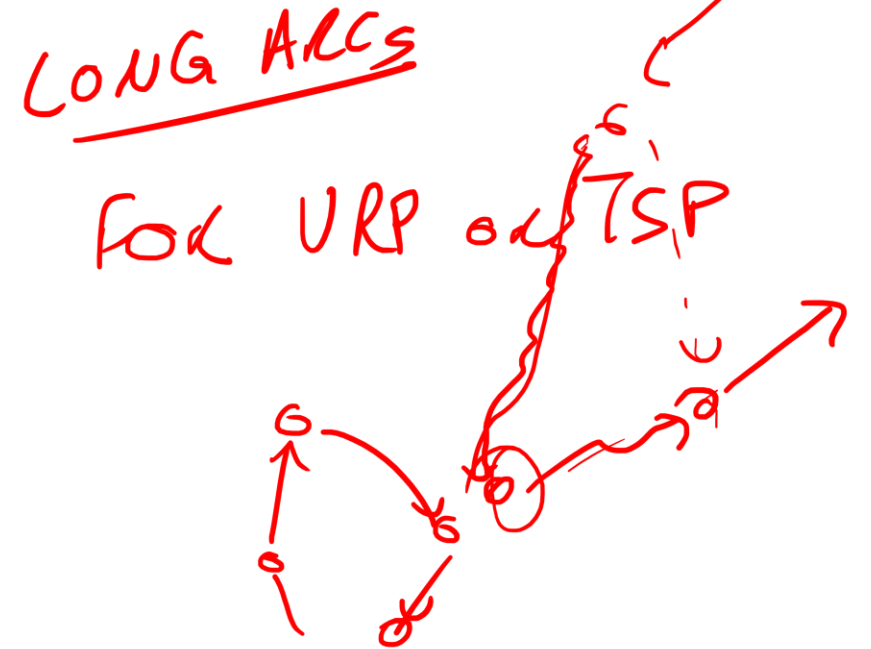
Meta-heuristics: An Incomplete Survey



Guided Local Search

Basic idea:

- Select a feature that indicates a poor solution
- Penalise a solution that exhibits that feature
- Start with zero penalty
- Repeat
 - Perform Local Search to minimise original objective + penalties
 - Select elements to penalise
 - Increase penalty on selected elements



Guided Local Search

Local Search

- Do local search with an *updated objective* $\underbrace{h(s)}_{\text{\$ millions}} = \underbrace{g(s)}_{10 \sim 100} + \underbrace{\lambda}_{\text{\$ millions}} \cdot \sum_{i=1}^M \underbrace{p_i \cdot I_i(s)}_{10 \sim 100}$
- Updated objective
 - $h(s)$: Augmented objective
 - $g(s)$: Original objective
 - λ : “normalisation” parameter
 - p_i : Count of times feature i has been penalised
 - $I_i(s)$: Indicator function: 1 if feature i in solution s ; 0 otherwise

Guided Local Search

GLS

Select elements to penalise:

- Update penalty of features that maximise Utility
- c_i : Original cost of feature
- $I_i(s)$: Does solution s exhibit feature i
- At each iteration
 - Local Search using augmented objective
 - Select maximum utility features
 - Set $p_i = p_i + 1$ for all selected features
- Penalty increases each iteration
 - Local Search tries harder to eliminate feature
- Utility decreases the more often you penalise a feature
 - Eventually select other features

$$util(s_*, f_i) = I_i(s_*) \cdot \frac{c_i}{1 + p_i}$$

Handwritten annotations for the utility formula:
- $I_i(s_*)$ is labeled "CUR SOL" with an arrow pointing to it.
- c_i is circled and labeled "MUST BE IN CUR SOL" and "ALC LENGTH".
- $1 + p_i$ is underlined.

$$h(s) = g(s) + \lambda \cdot \sum_{i=1}^M p_i \cdot I_i(s)$$

Handwritten annotation: A red arrow points to the $h(s)$ term in the equation.

Guided Local Search – TSP

- **Feature:** an arc (i,j)
- $I_{ij}(s) = 1$ if arc (i,j) is present; 0 otherwise
- **At each iteration**
 - Penalise the longest arc. 4-
 - Try harder to get rid of it 4-
- **As the search progresses**
 - Utility of first arc decreases
 - Other arcs start being penalised

$$h(s) = g(s) + \lambda \cdot \sum_{i=1}^M p_i \cdot I_i(s)$$

$$util(s_*, f_i) = I_i(s_*) \cdot \frac{c_i}{1 + p_i}$$

Meta-heuristics: An Incomplete Survey

Escape Local Minimum

Accept Non-Improving
Solutions ✓

Simulated
Annealing

Tabu
Search

Change Landscape Of
Problem

Change
Objective or
Data ✓

Data

Guided Local
Search

Soft
Constraints

NOT POPULAR
SO ANY MORE

DA

✓

USUALLY
POPULAR

Use Different
N'bourhoods

Variable
N'bourhood
Search

Large
N'bourhood
Search

FRi

Look somewhere
else

Iterated Local
Search;
Restarts

GRASP

FRi

Combine different
solutions

Evolutionary
Algorithms

→

Ant Colony
Optimisation

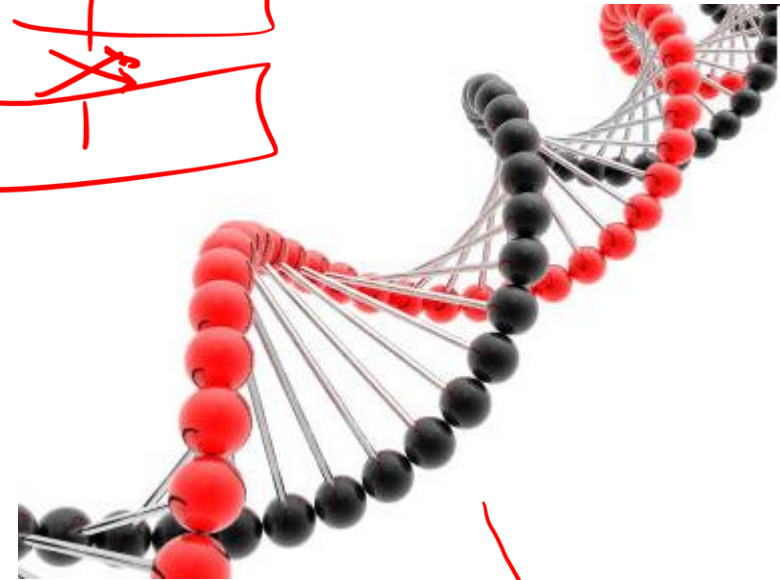
Path
Re-linking

↓

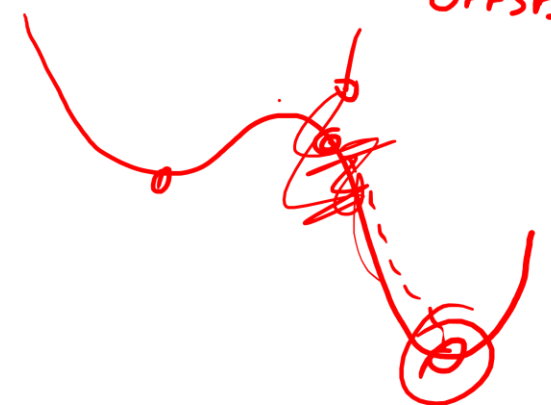
Genetic Algorithms

- Generate a population of solutions (construct methods)
- Evaluate fitness (objective)
- Create next generation:
 - Choose two solutions from population
 - Combine the two (two ways)
 - [Mutate]
 - Produce offspring (calculate fitness)
 - [Improve] LOCAL SEARCH ON OFFSP.
 - Repeat until population doubles
- Apply selection:
 - Bottom half "dies"
- Repeat

Turns it into a
Memetic Algorithm



NEW OFFSP.



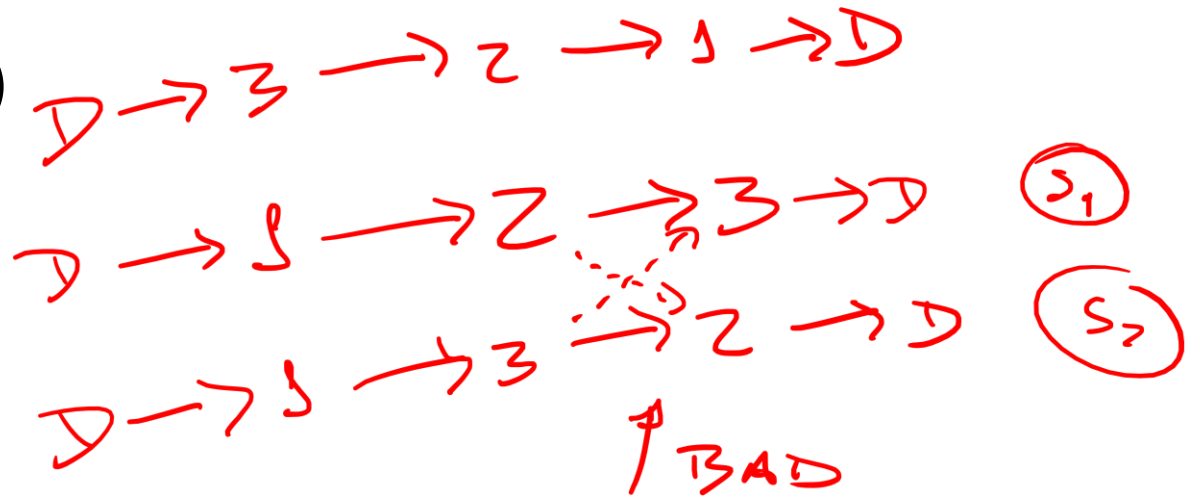
Genetic Algorithms

Solution Representation is key

- Needs to fulfil multiple goals
 - Easy to calculate fitness (objective)
 - Easy to perform crossover (merge)
 - Easy to manipulate (mutation)
 - Easy for local search

- E.g. VRP

- First attempts used array for each route, or successor info
- Very difficult for crossover
- Better rep turns out to be a single array



[3 | 2 | 1]

Genetic Algorithms

E.g. VRP

- “Split” method
- Introduced by Prins (2004)
- Solution represented as a “Grand Tour” (ordering of all customers)
- Split algorithm divides the tour into feasible routes
 - Uses Dynamic Programming

3 TRUCKS

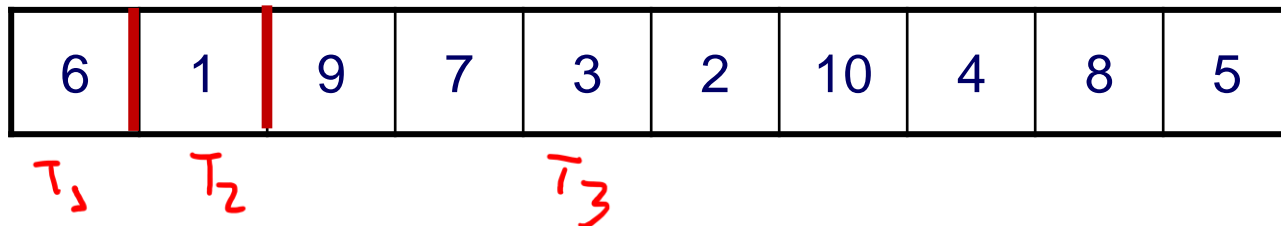
6	1	9	7	3	2	10	4	8	5
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4- GRAND TOUR

Genetic Algorithms

E.g. VRP

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Genetic Algorithms

E.g. VRP

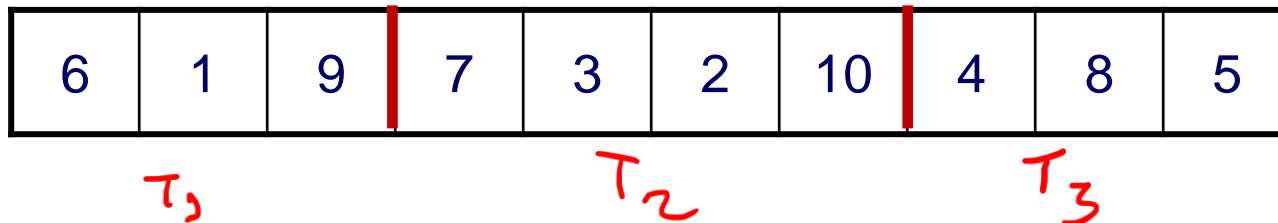
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Genetic Algorithms

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- Split algorithm divides the tour into feasible routes
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6133 F.
125

Genetic Algorithms

T_1			T_2							
1	4	6		2	3	8	9	5	10	7
1	10	8	2		5	4	9	3	6	7
6	1	9	7	3		2	10	4	8	5
1	9	7	10		8	6	4	3	2	5

2 Trucks

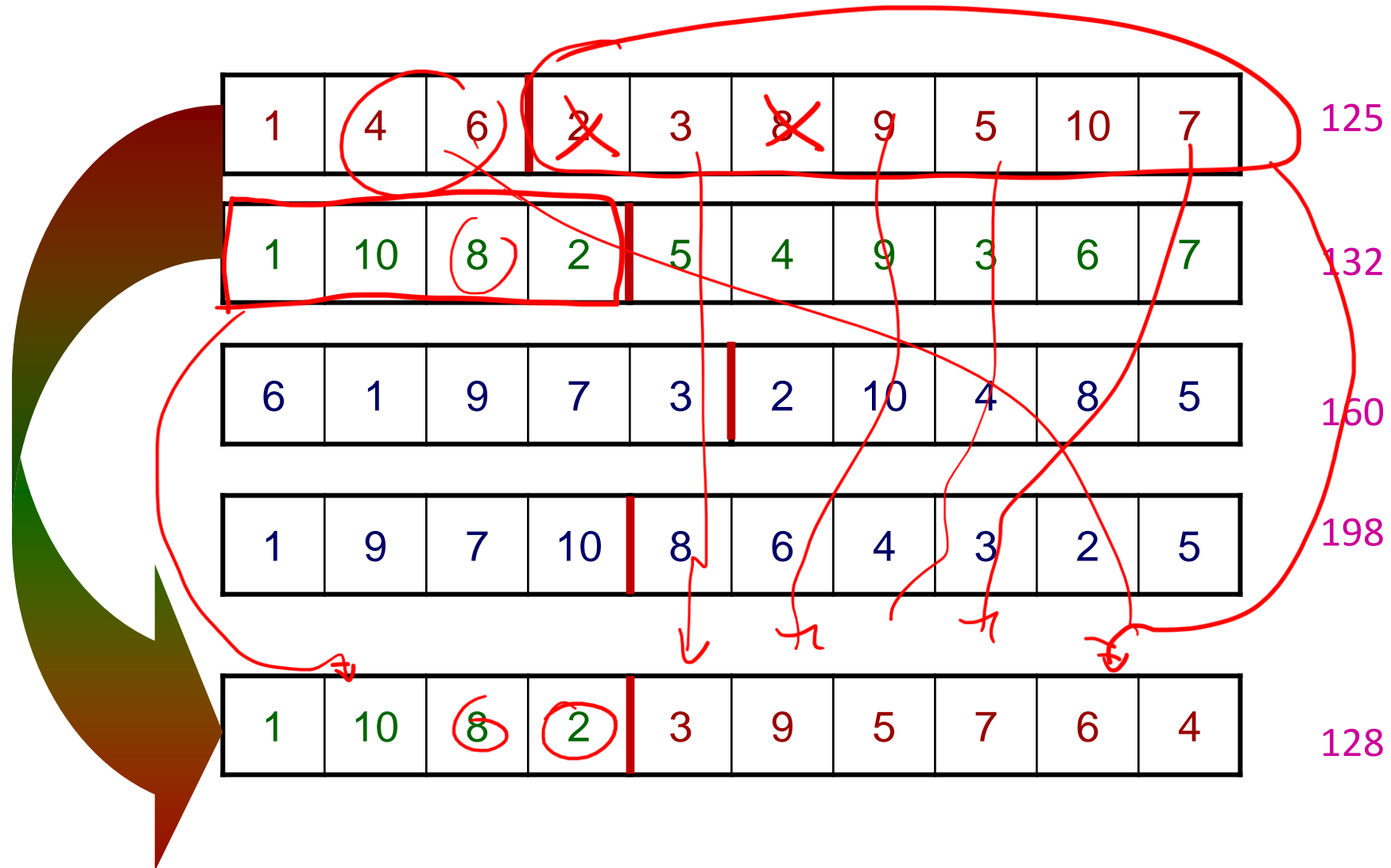
125

132

160

198

Genetic Algorithms



Genetic Algorithms

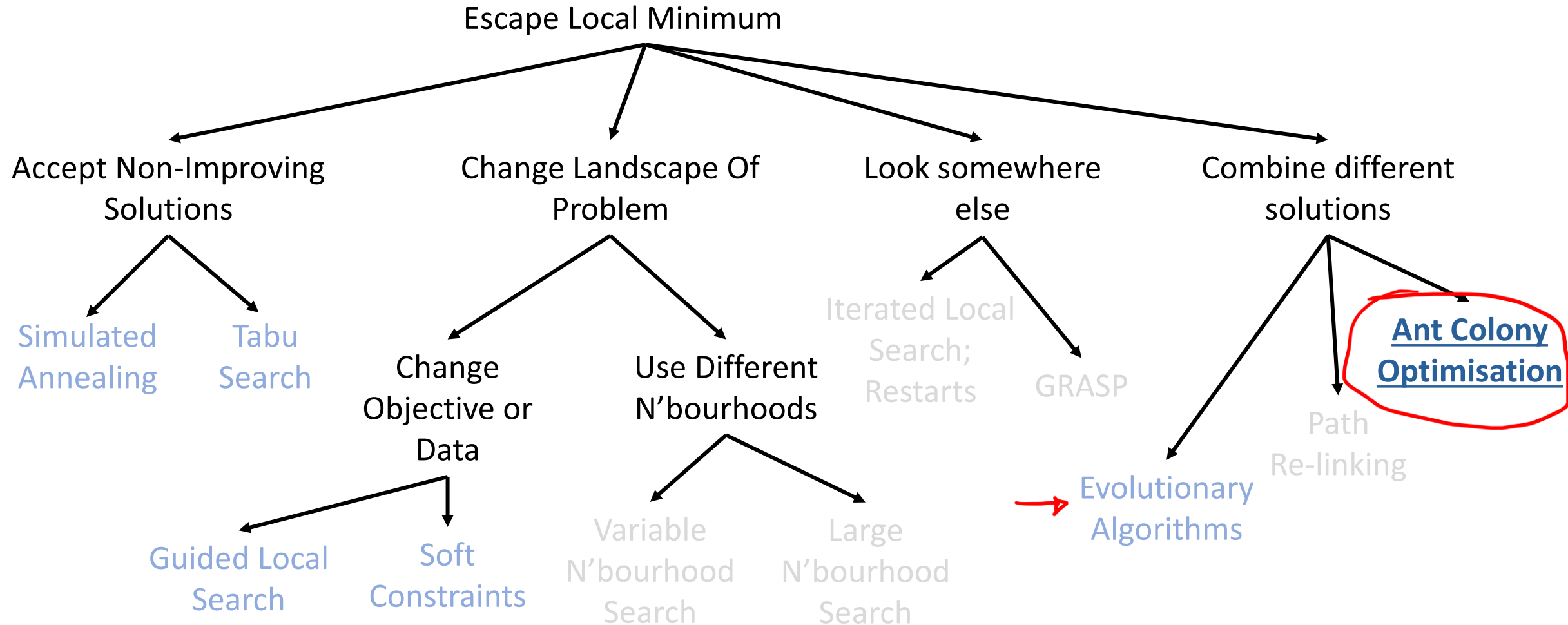


Genetic Algorithms

Diversification:

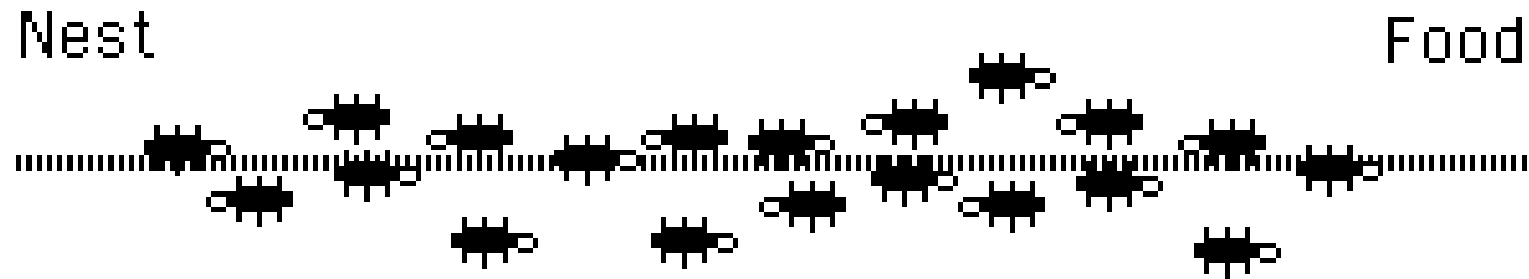
- Big problem is getting a homogenous population
- Too much intensification, not enough diversification
EXPLORATION
- Some algorithms explicitly measure diversity
 - keep lower-quality solutions that maintain diversity
- Meta-meta: Soft constraints
 - Maintain a separate population of infeasible solutions

Meta-heuristics: An Incomplete Survey



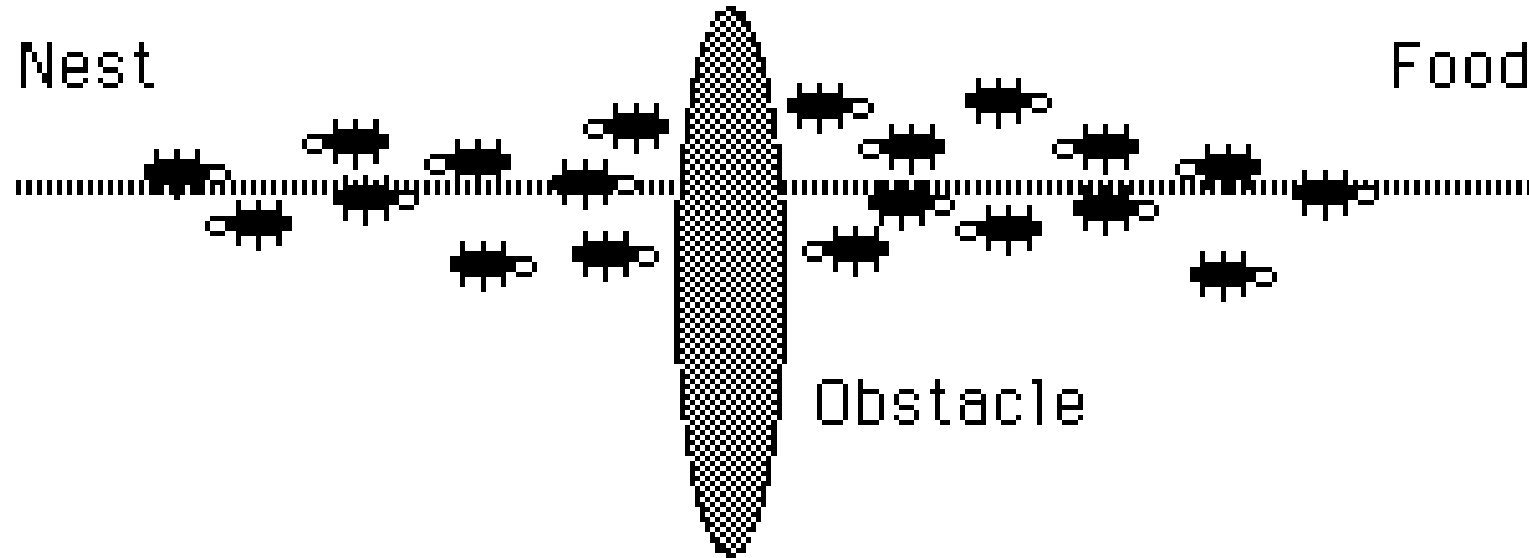
Ant Colony Optimisation (ACO)

- By analogy to foraging behaviour of Ants



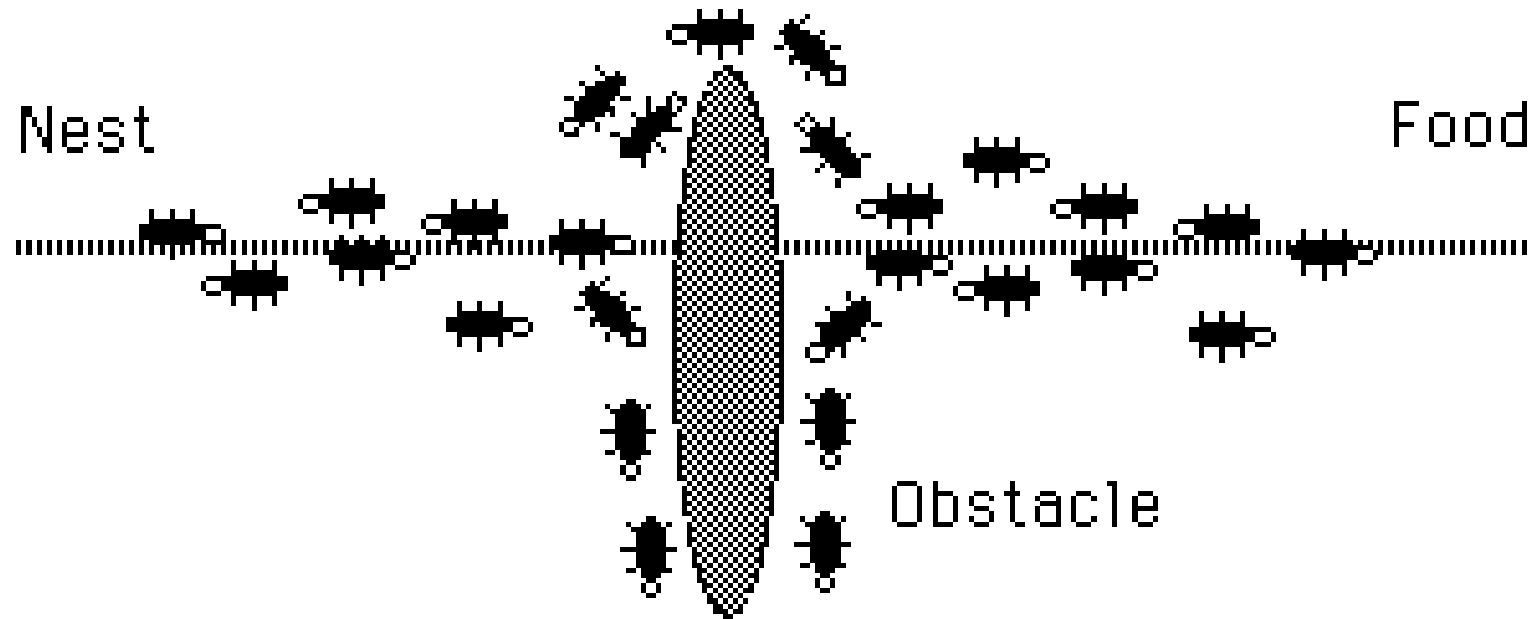
Ant Colony Optimisation (ACO)

- An obstacle appears!



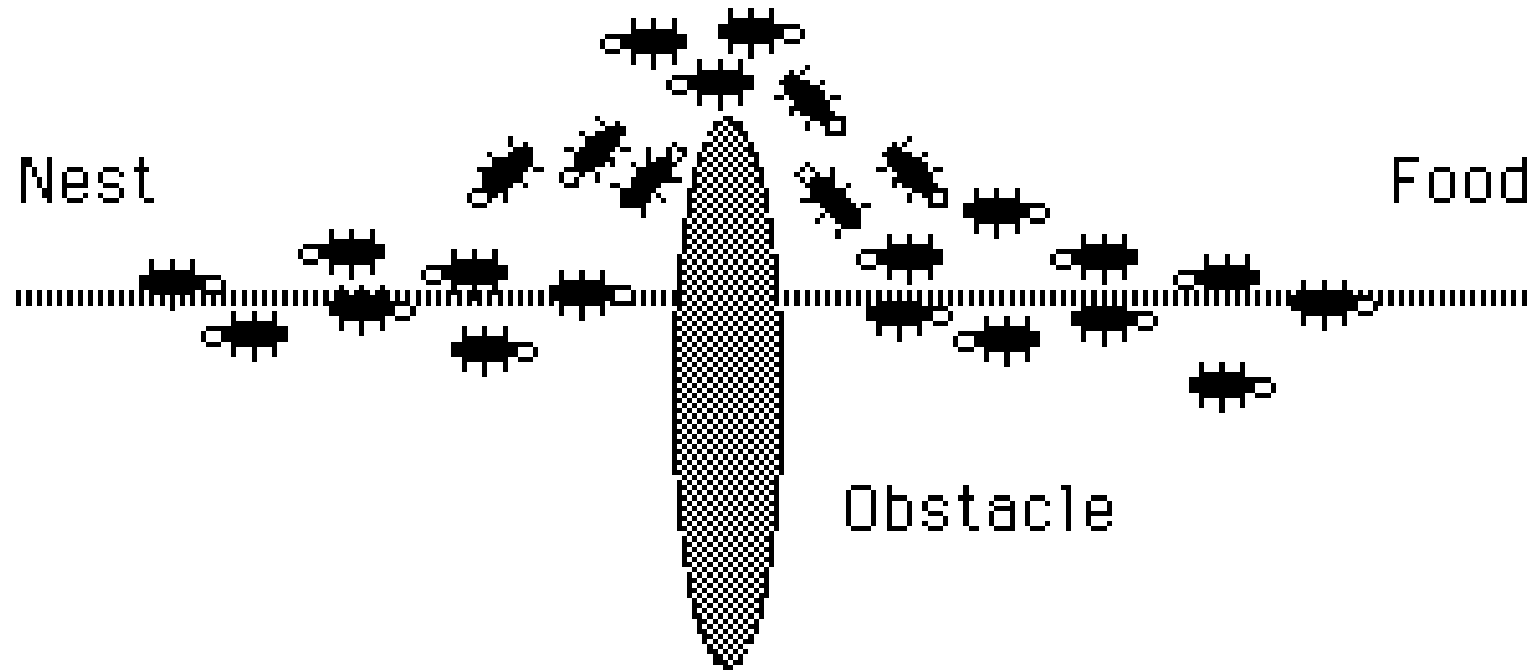
Ant Colony Optimisation (ACO)

- Everybody flip a coin



Ant Colony Optimisation (ACO)

- Shortest path is reinforced



Ant Colony Optimisation (ACO)


TCP PACKETS IN NET
CELL COM.

E.g.: Want to find shortest paths in a communications network

- Send out ^{PACKETS} ants that choose a path
 - Partly at random (our naïve heuristic)
 - Partly influenced by previous ants: Pheromone trail – our meta-heuristic
- The first ant to get to a destination increases the Pheromone on its path
- Pheromone levels decrease over time
 - More ants select the best path
 - The best path gets reinforced ↵

Ant Colony Optimisation (ACO)

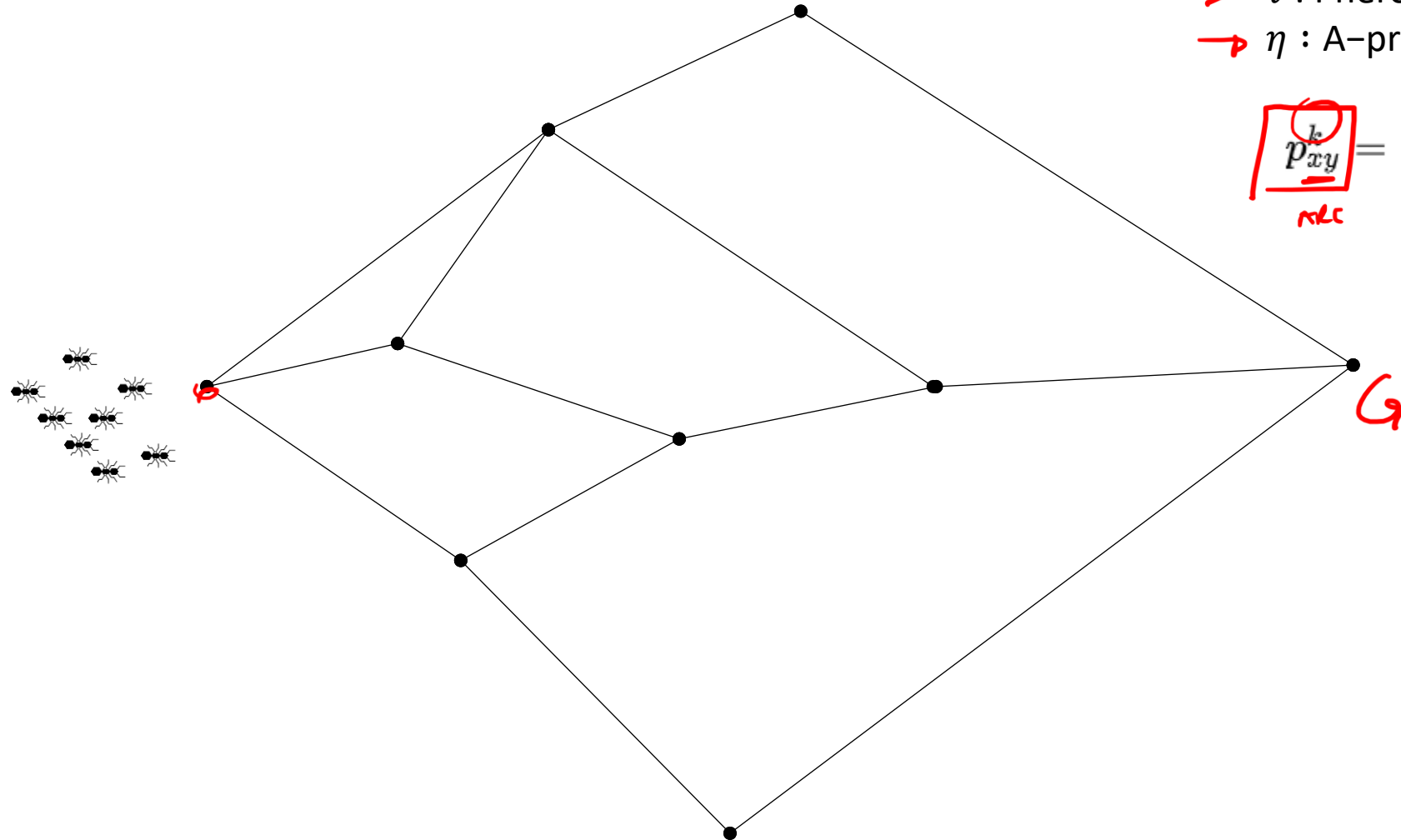
Advantages:

- (Relatively) Simple
- Distributed 
- Easy to parallelise
- Robust:
 - If the network changes, new pheromones will be deposited and a new path found

Disadvantages:

- Sensitive to parameter settings
 - Lay down too much pheromone → Lock in poor solution early (poor diversity)
 - Lay down too little → Slow to converge (poor intensification)
 - Decay pheromone too slowly → Bad paths persist
 - Decay too quickly → Best path is forgotten

Ant Colony Optimisation (ACO) – TSP



Probability that ant chooses arc xy

→ τ : Pheromone strength

→ η : A-priori "attractiveness"

$$\underbrace{p_{xy}^k}_{\text{rule}} = \frac{(\tau_{xy}^\alpha)(\eta_{xy}^\beta)}{\sum_{z \in \text{allowed}_x} (\tau_{xz}^\alpha)(\eta_{xz}^\beta)}$$

Ant Colony Optimisation (ACO) – TSP

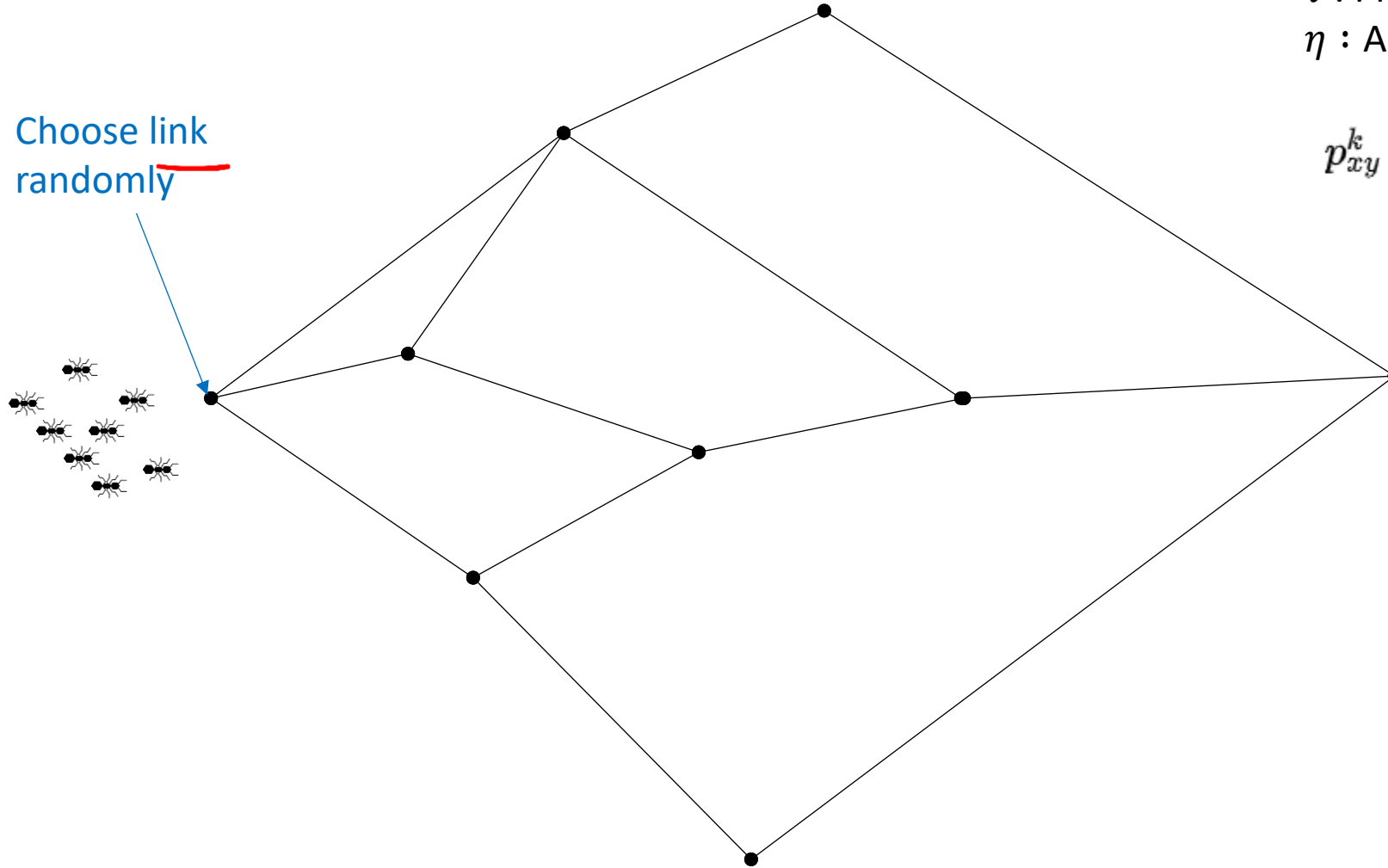
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Choose link
randomly



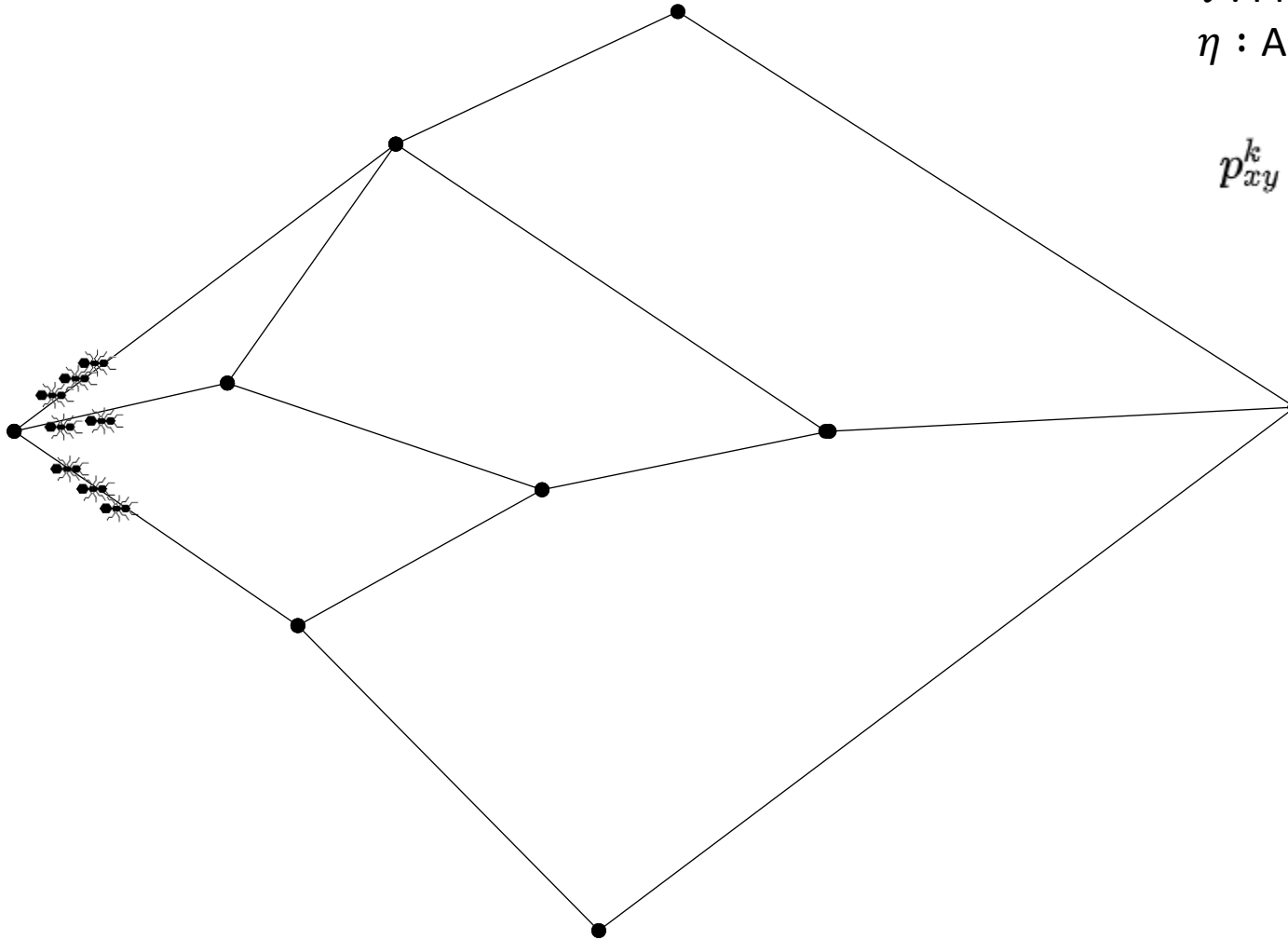
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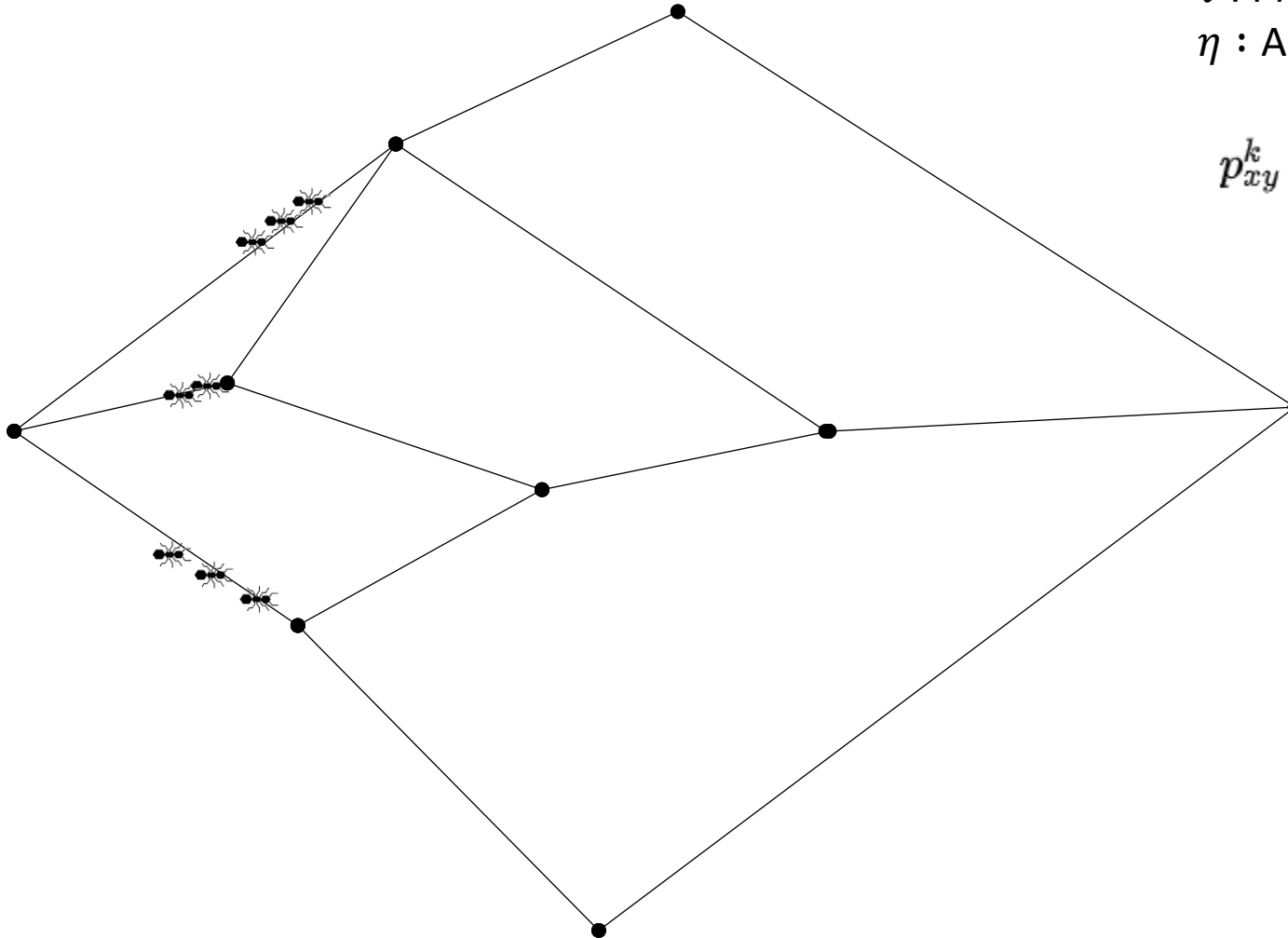
Ant Colony Optimisation (ACO) – TSP

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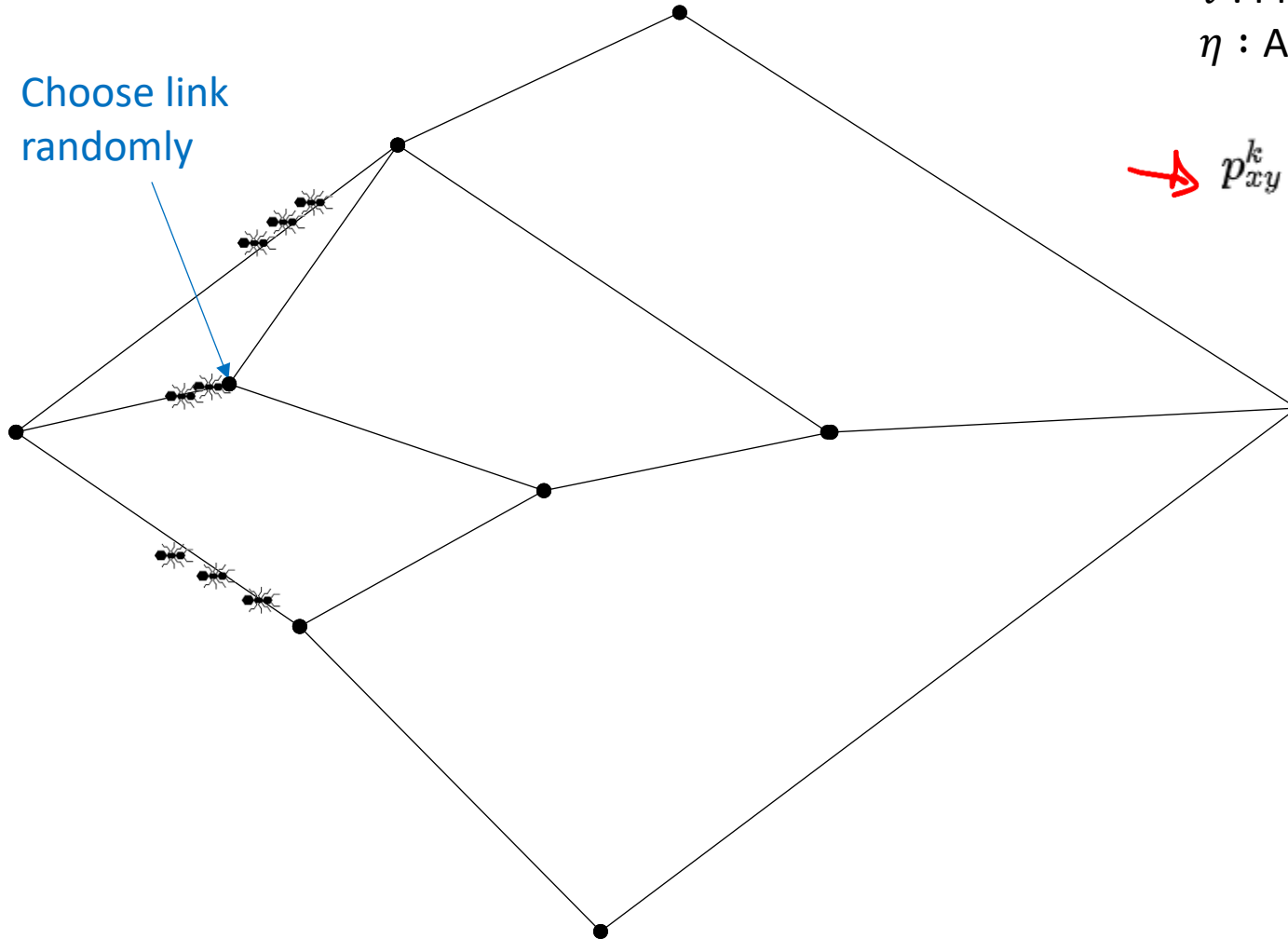
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Ant Colony Optimisation (ACO) – TSP



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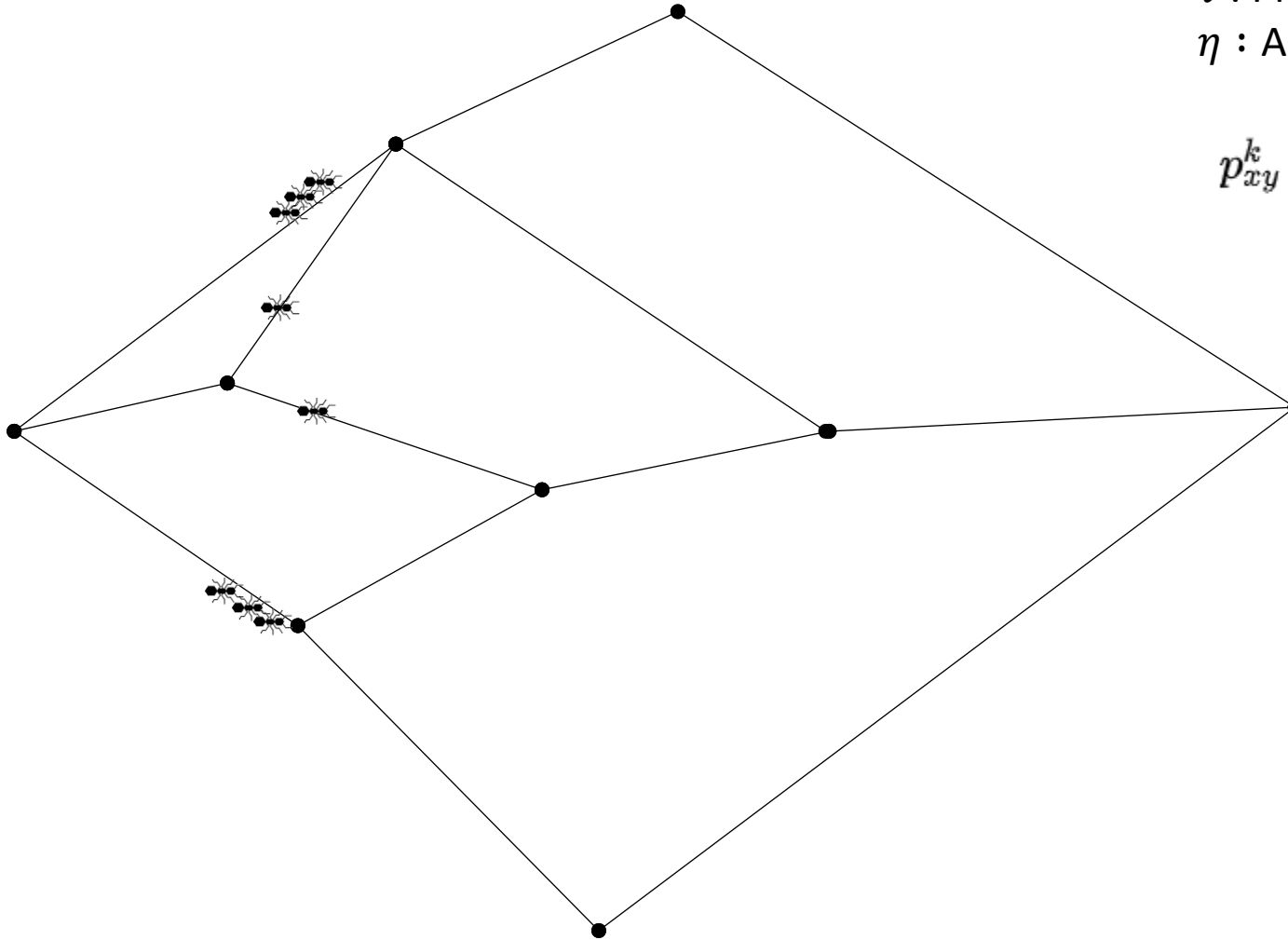
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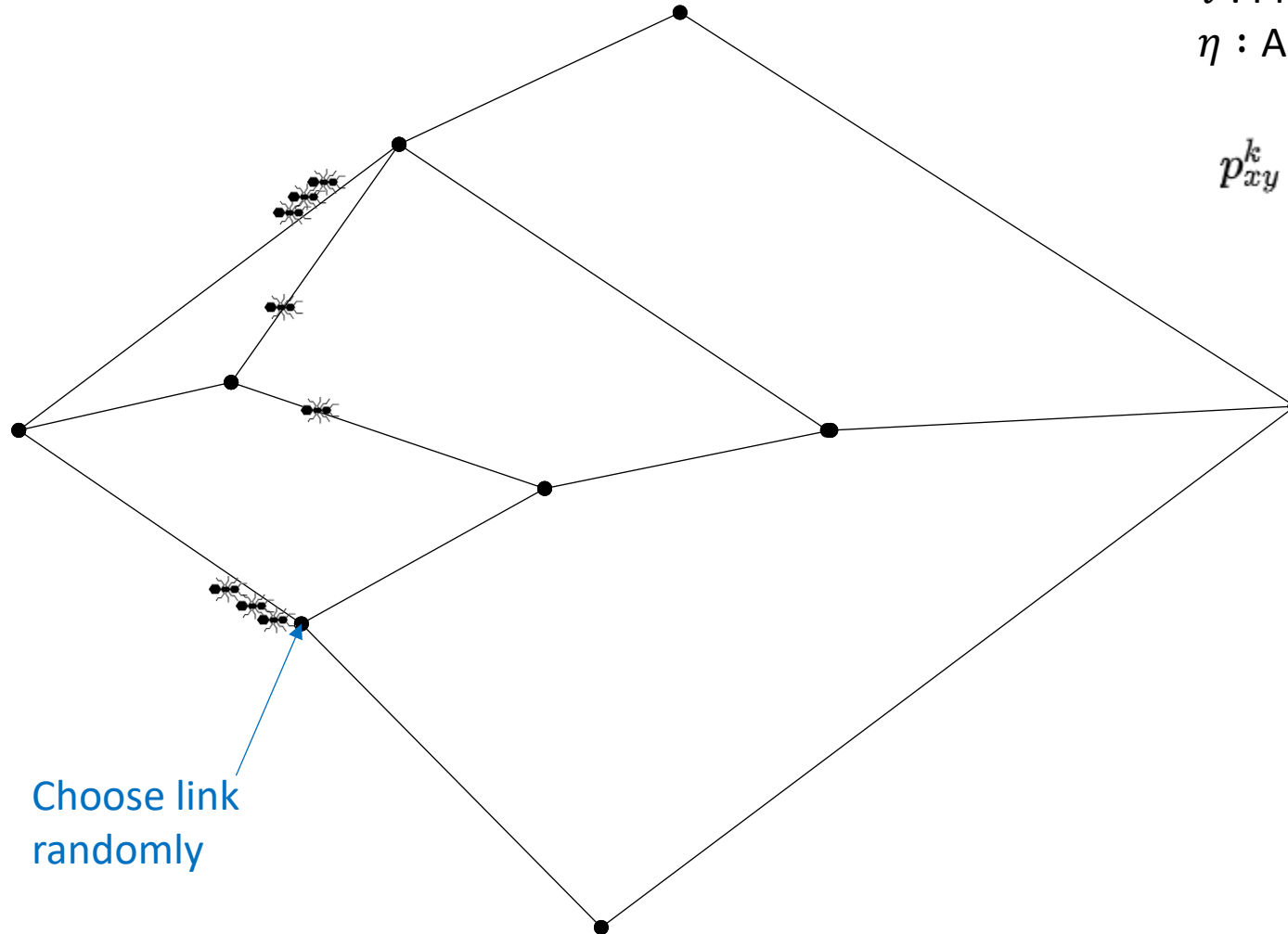
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Choose link
randomly

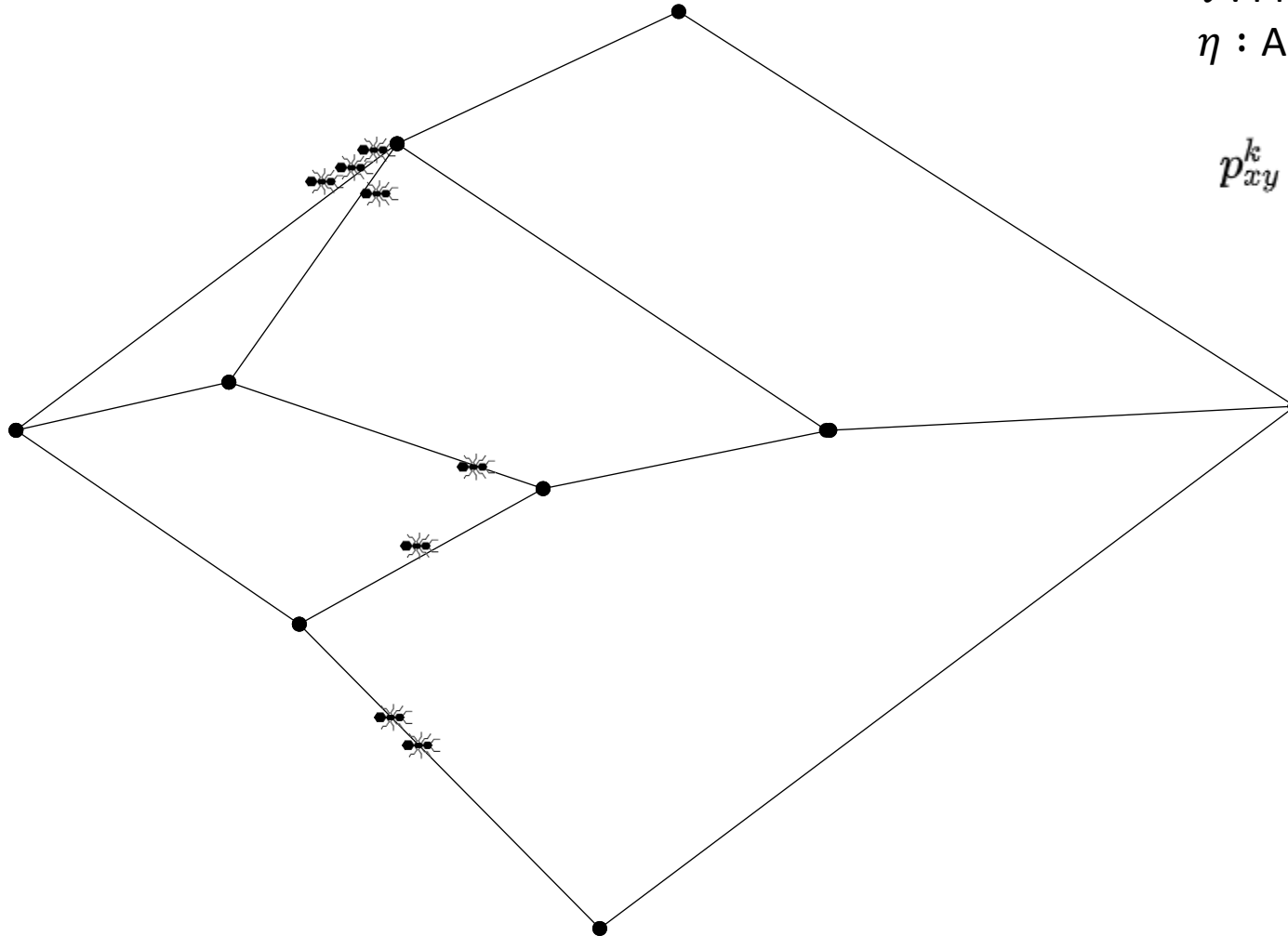
Ant Colony Optimisation (ACO) – TSP

Probability that ant chooses arc xy

τ : Pheromone strength

η : A-priori "attractiveness"

$$p_{xy}^k = \frac{(\tau_{xy}^\alpha)(\eta_{xy}^\beta)}{\sum_{z \in \text{allowed}_x} (\tau_{xz}^\alpha)(\eta_{xz}^\beta)}$$



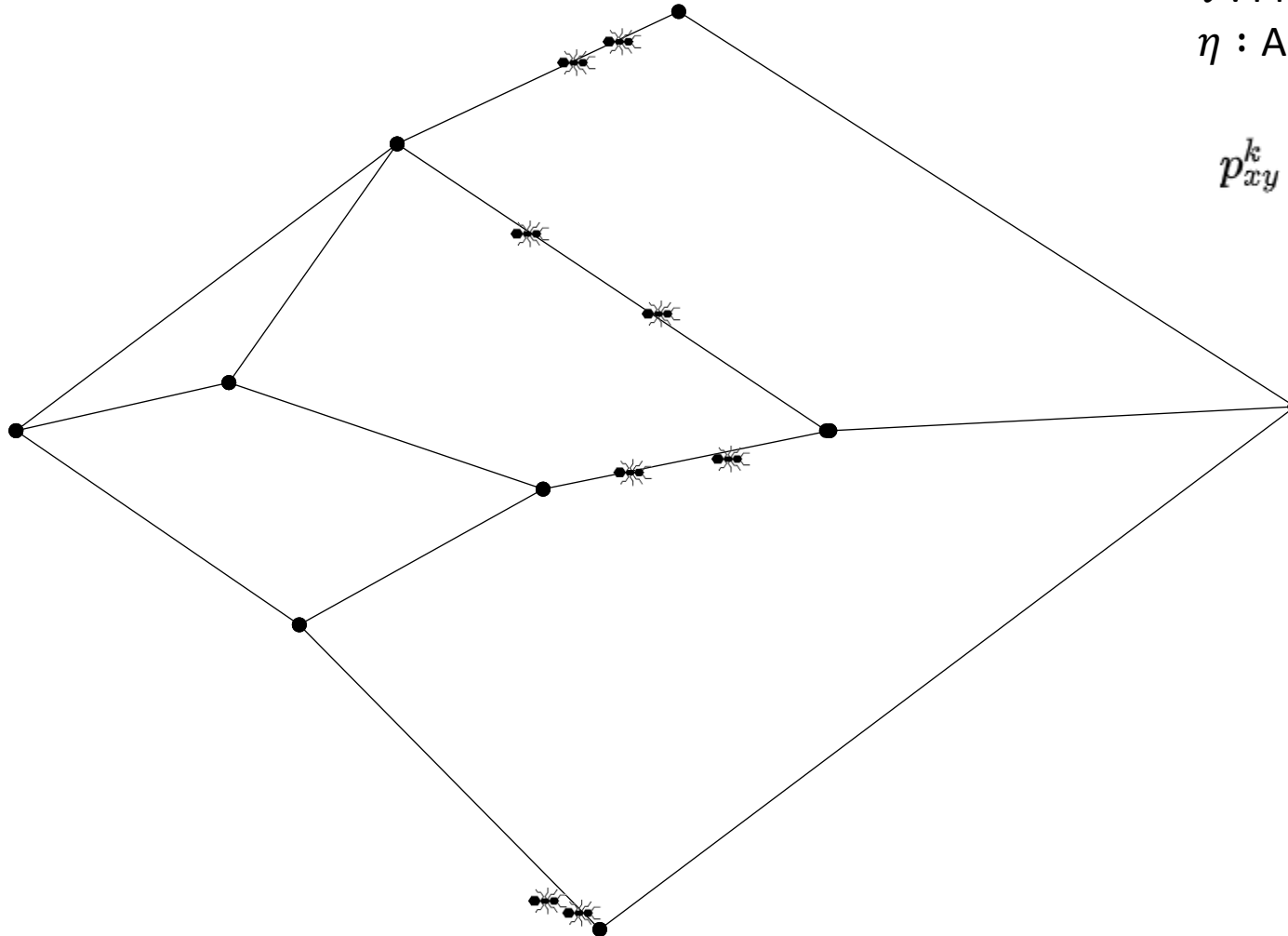
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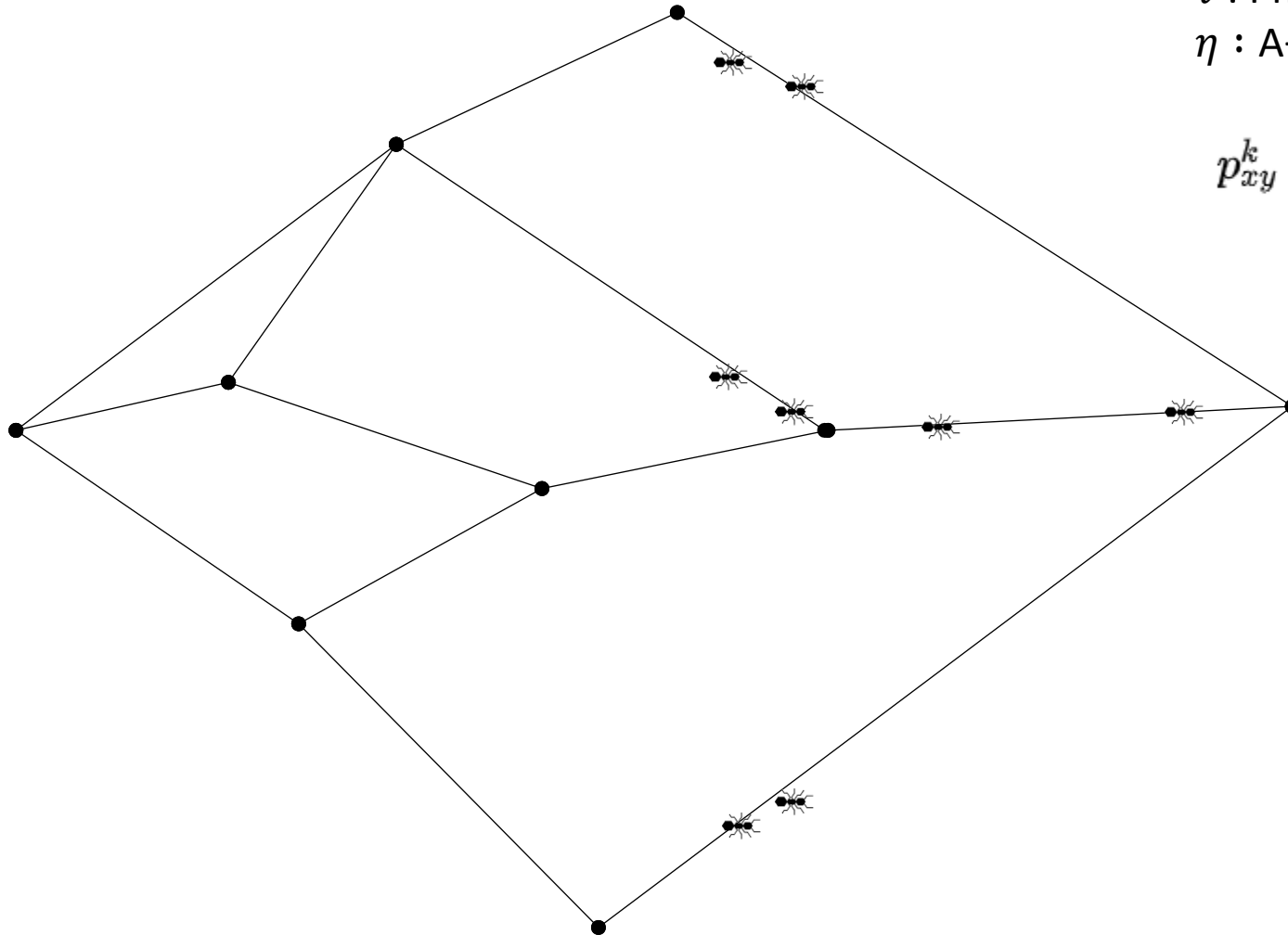
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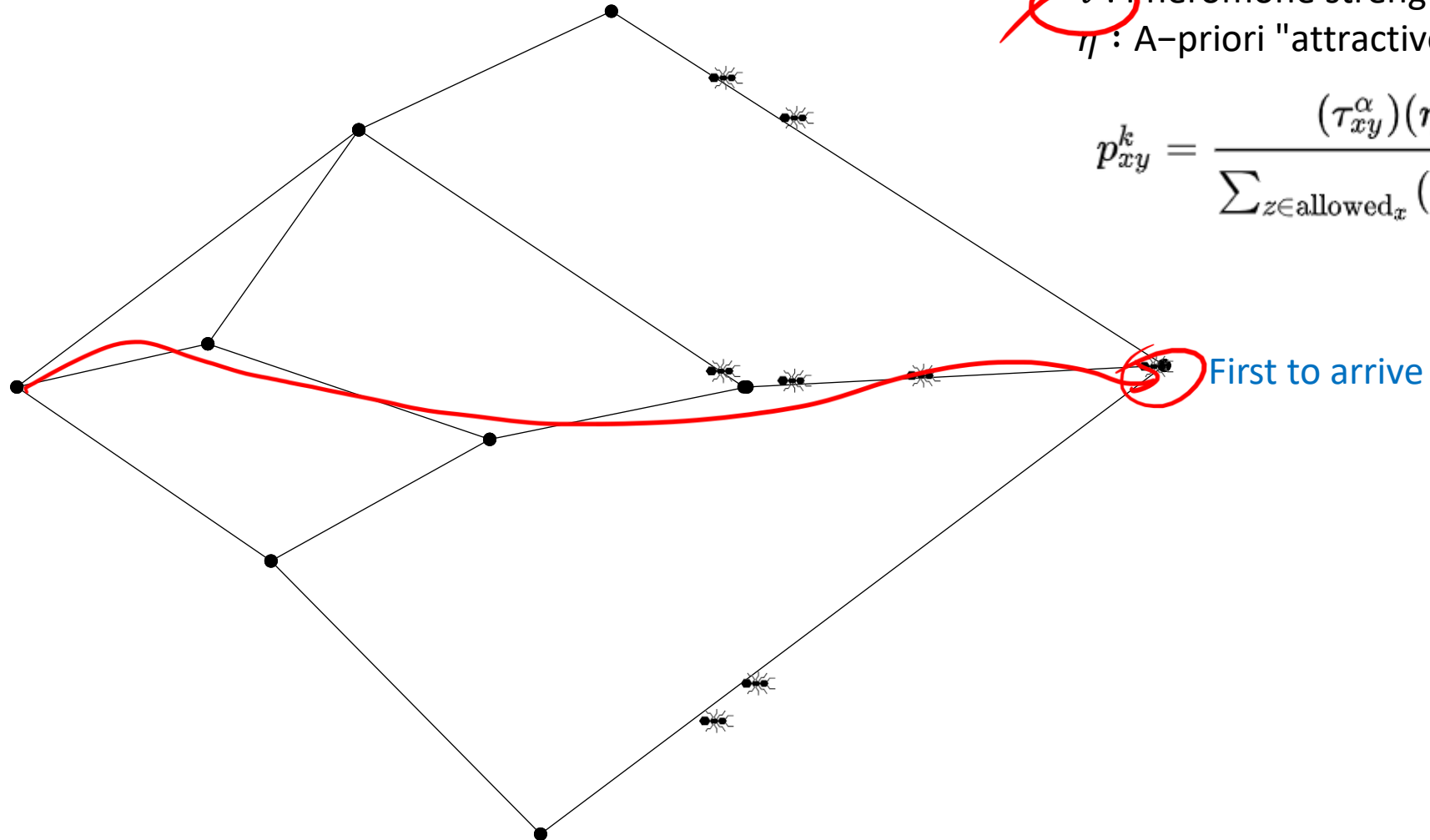
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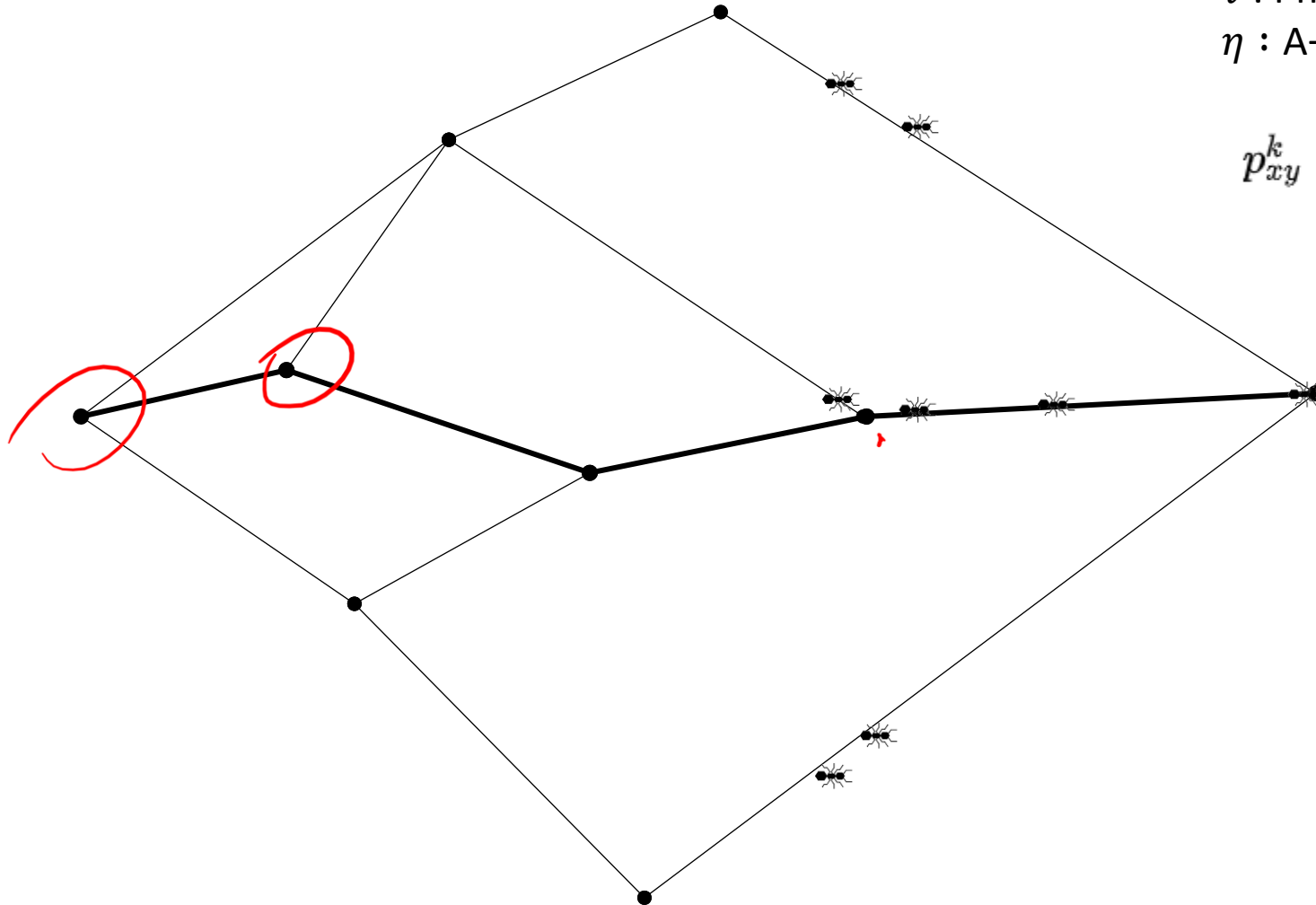
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Update
pheromones

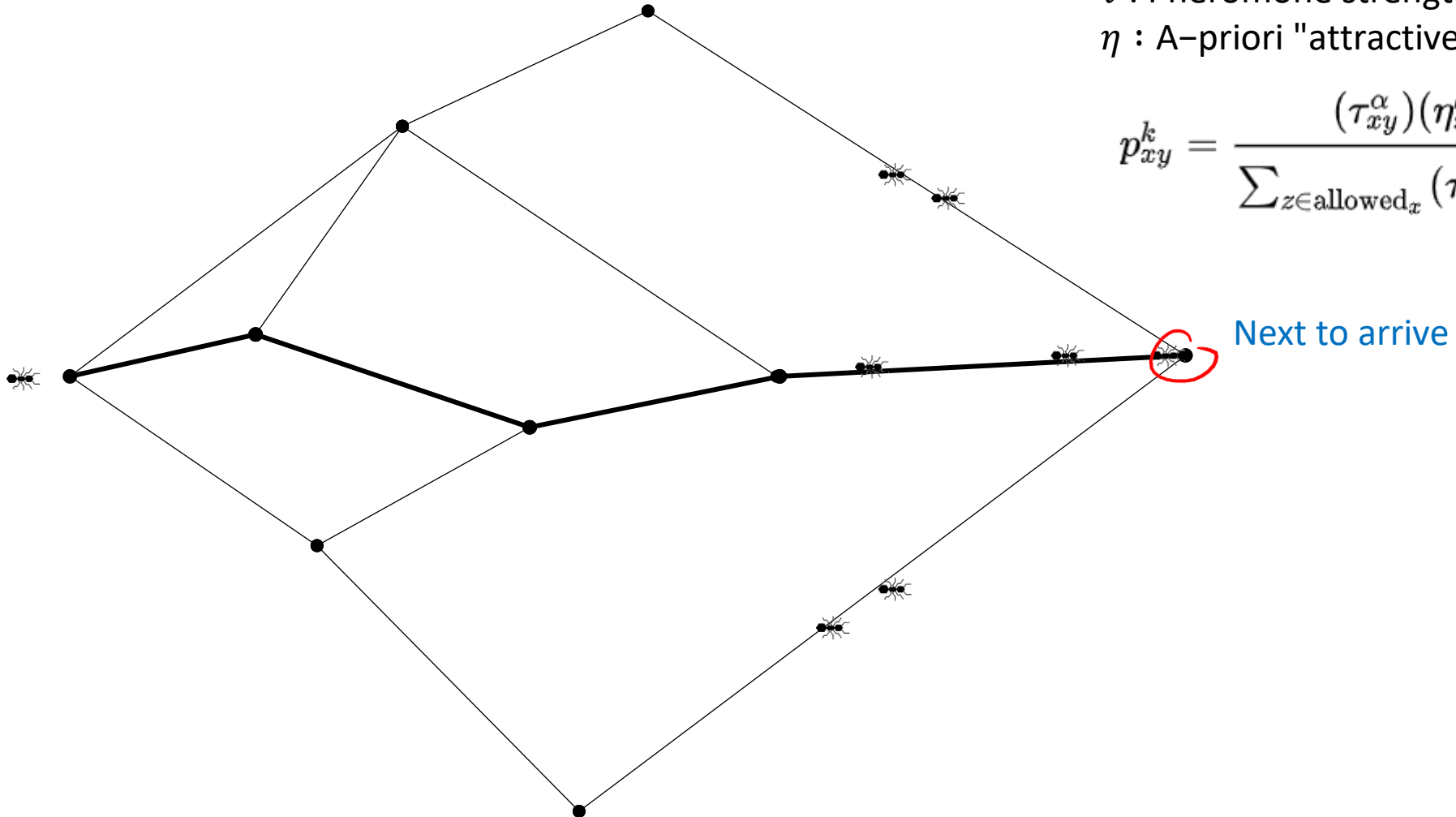
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Probability that ant chooses arc xy

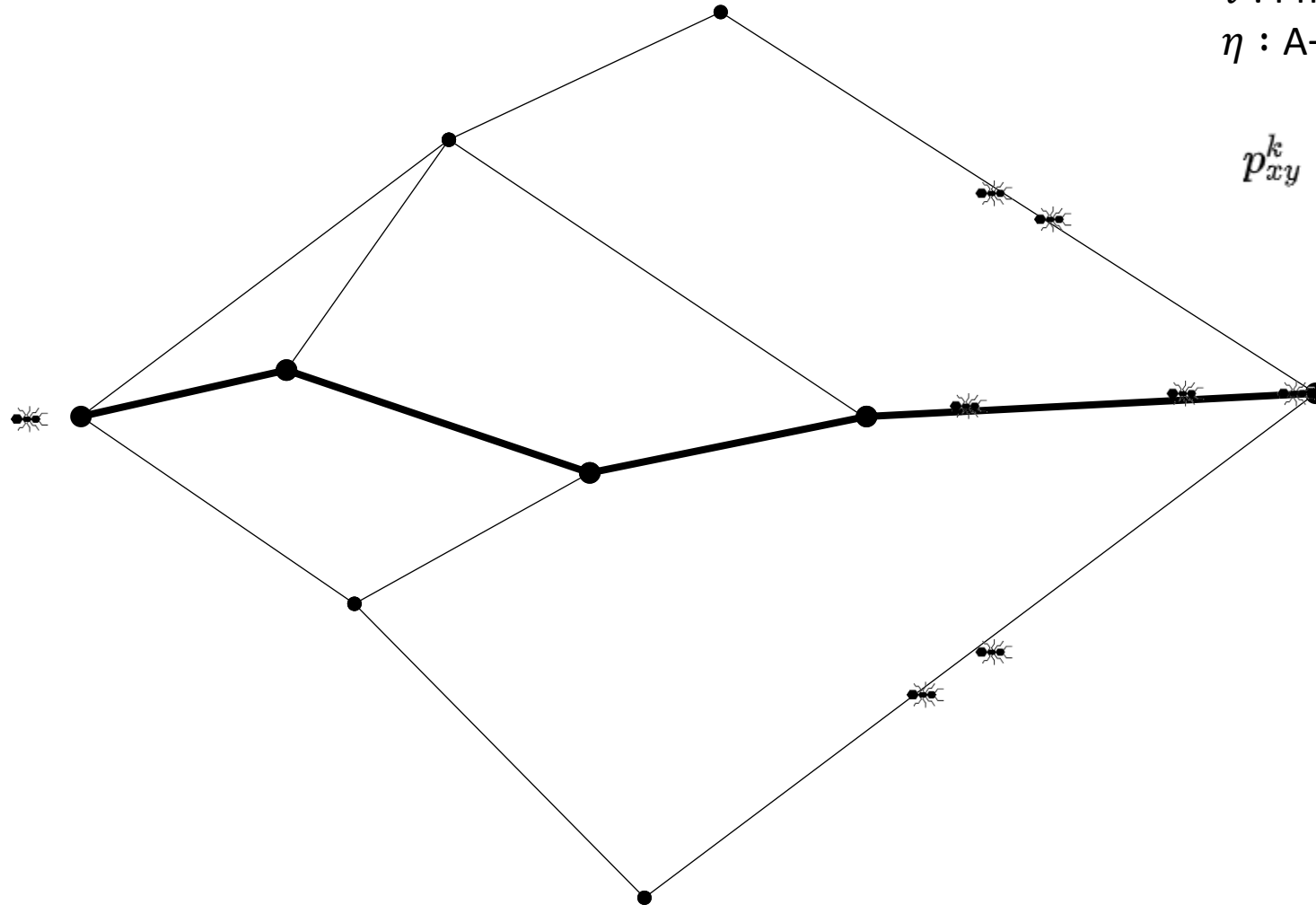
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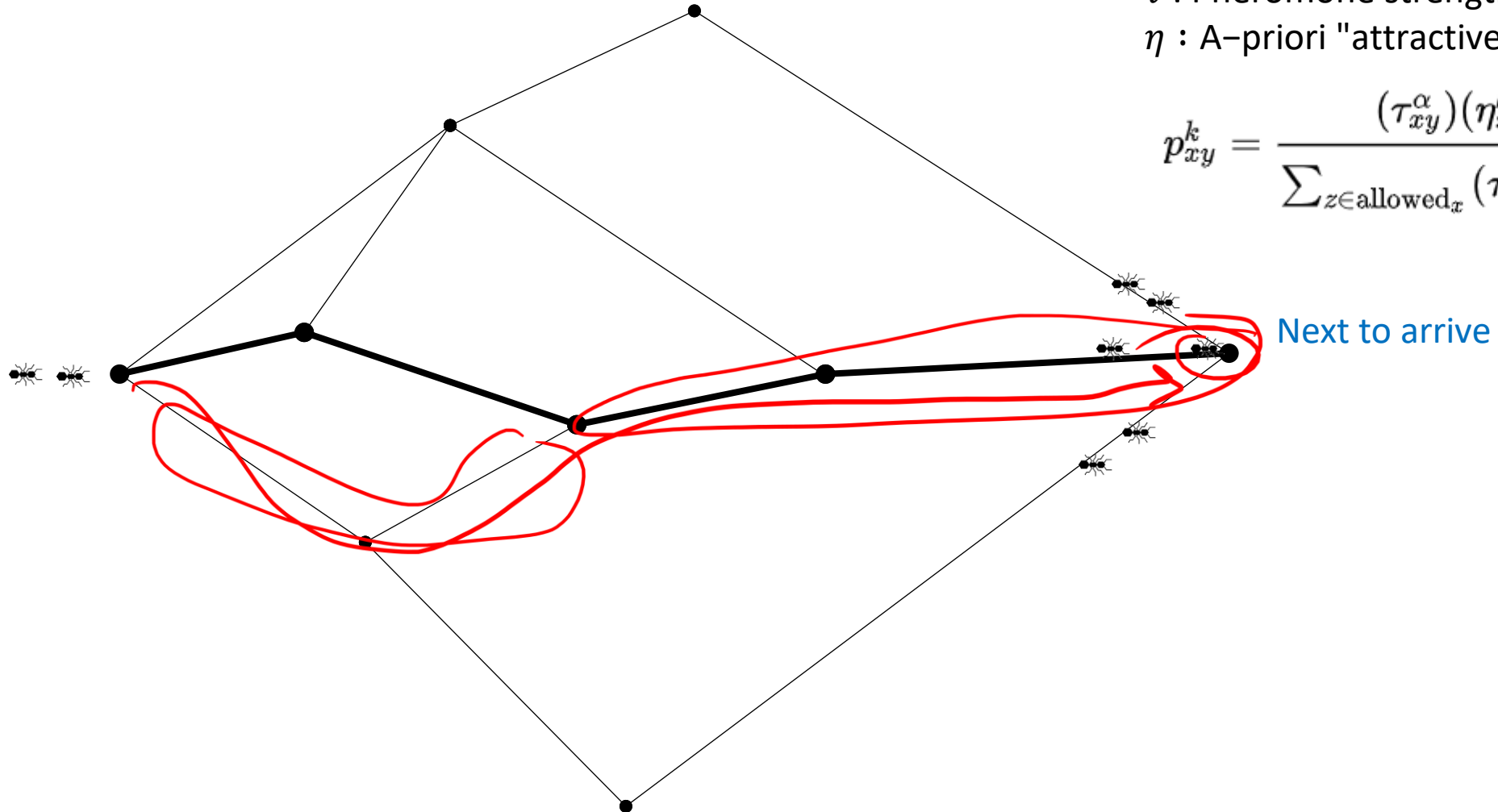
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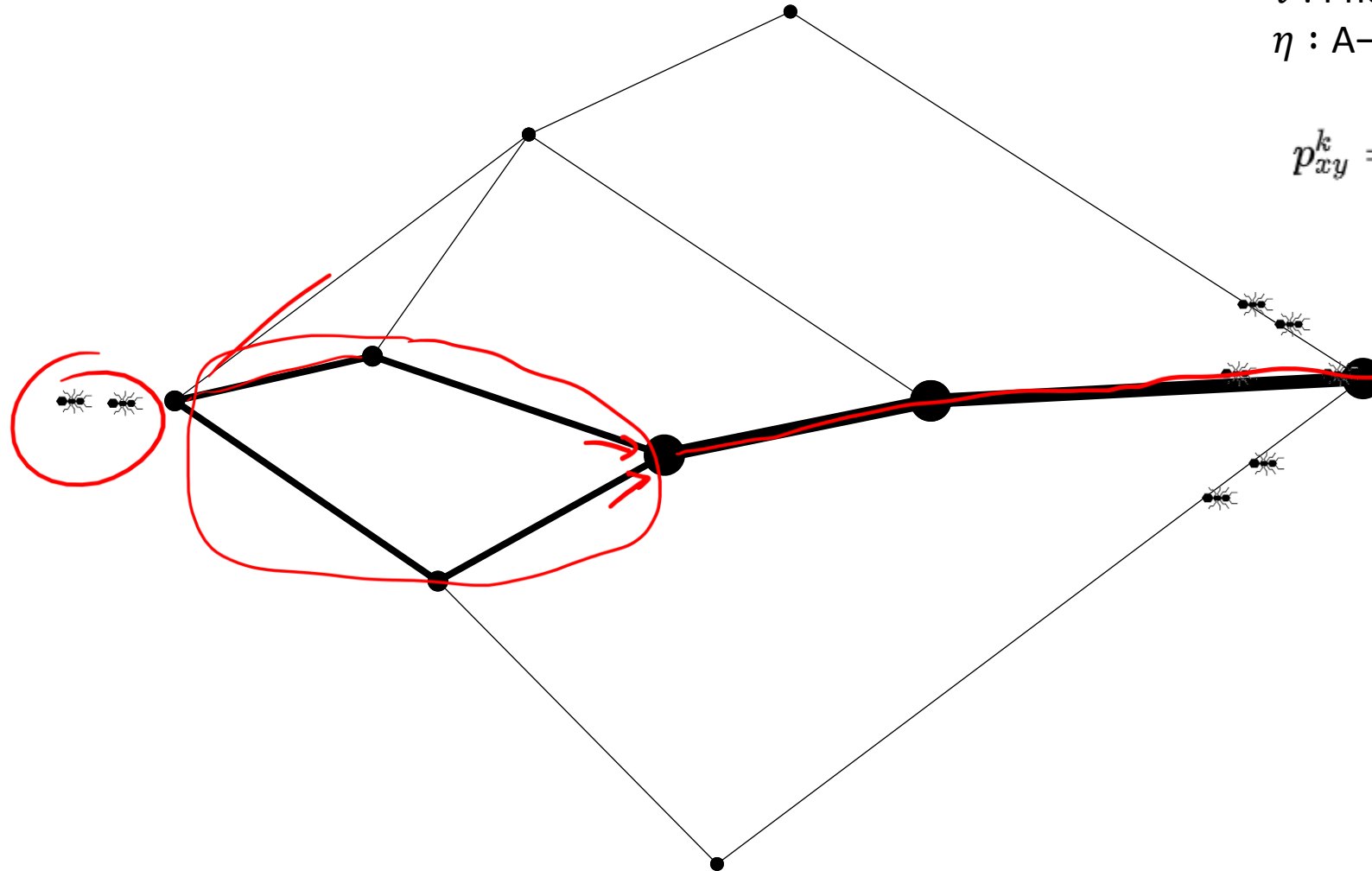
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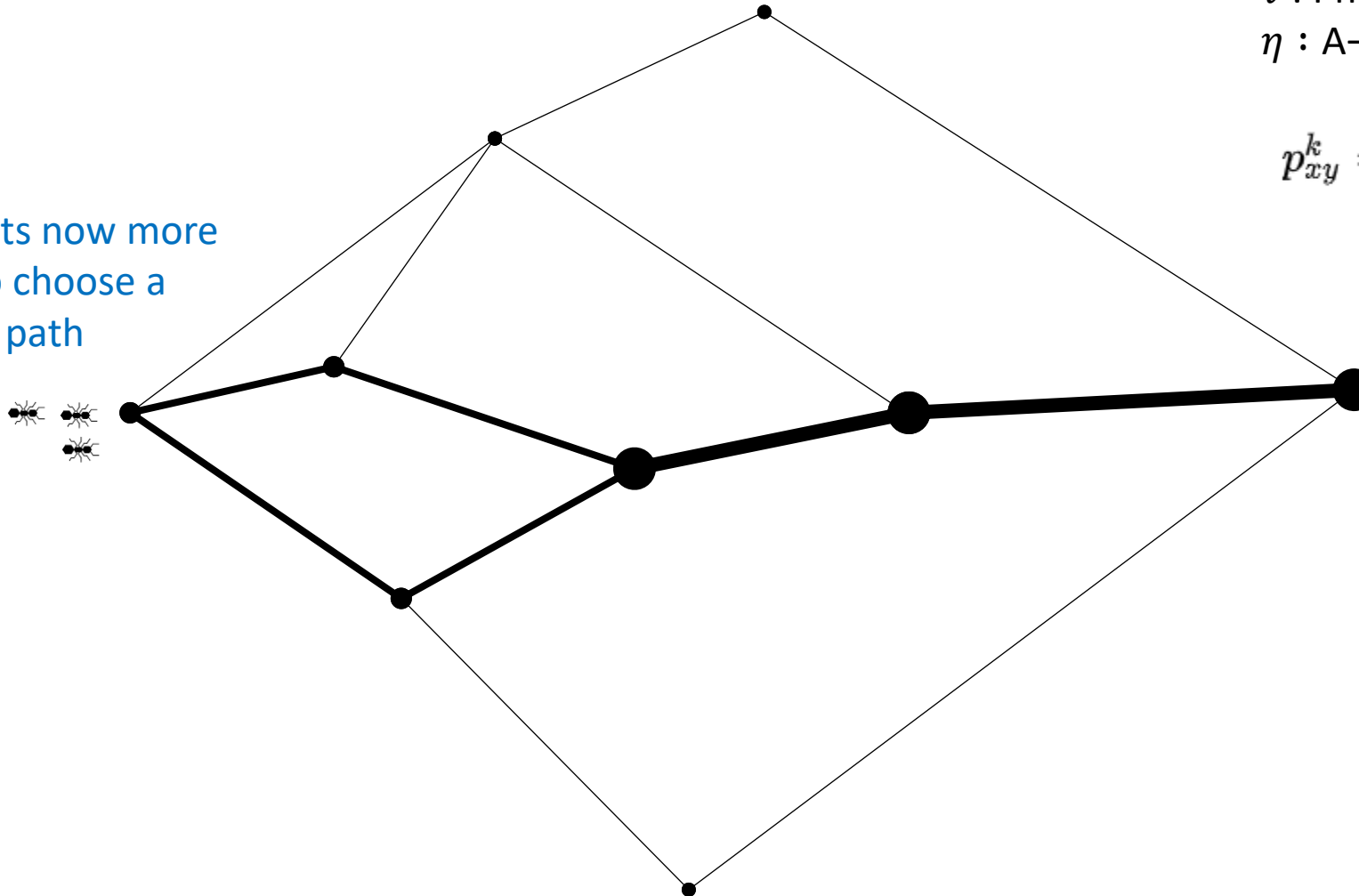
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New ants now more
likely to choose a
shorter path



Ant Colony Optimisation (ACO) – TSP

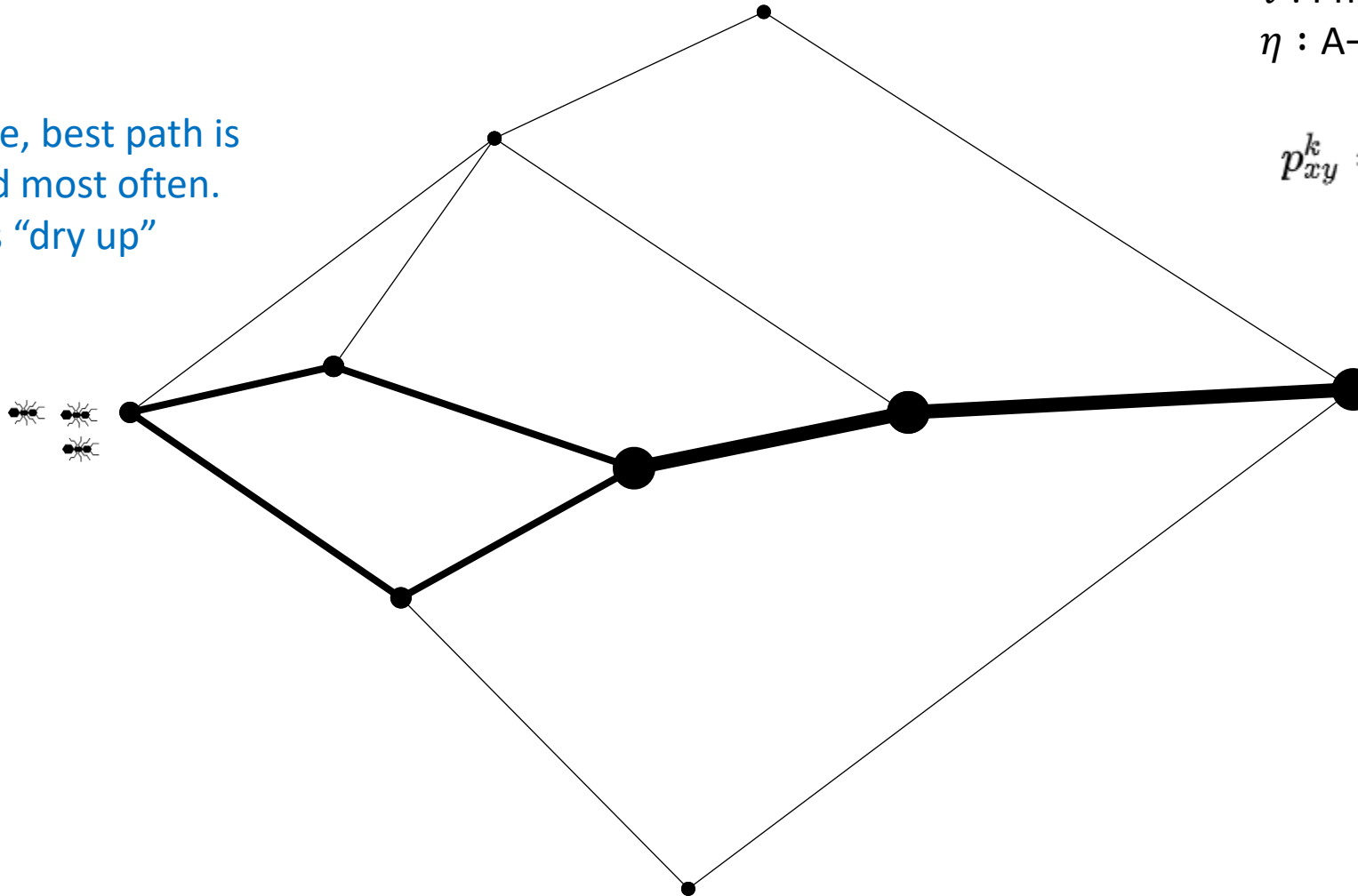
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Over time, best path is
traversed most often.
Old trails "dry up"



Ant Colony Optimisation (ACO) – TSP

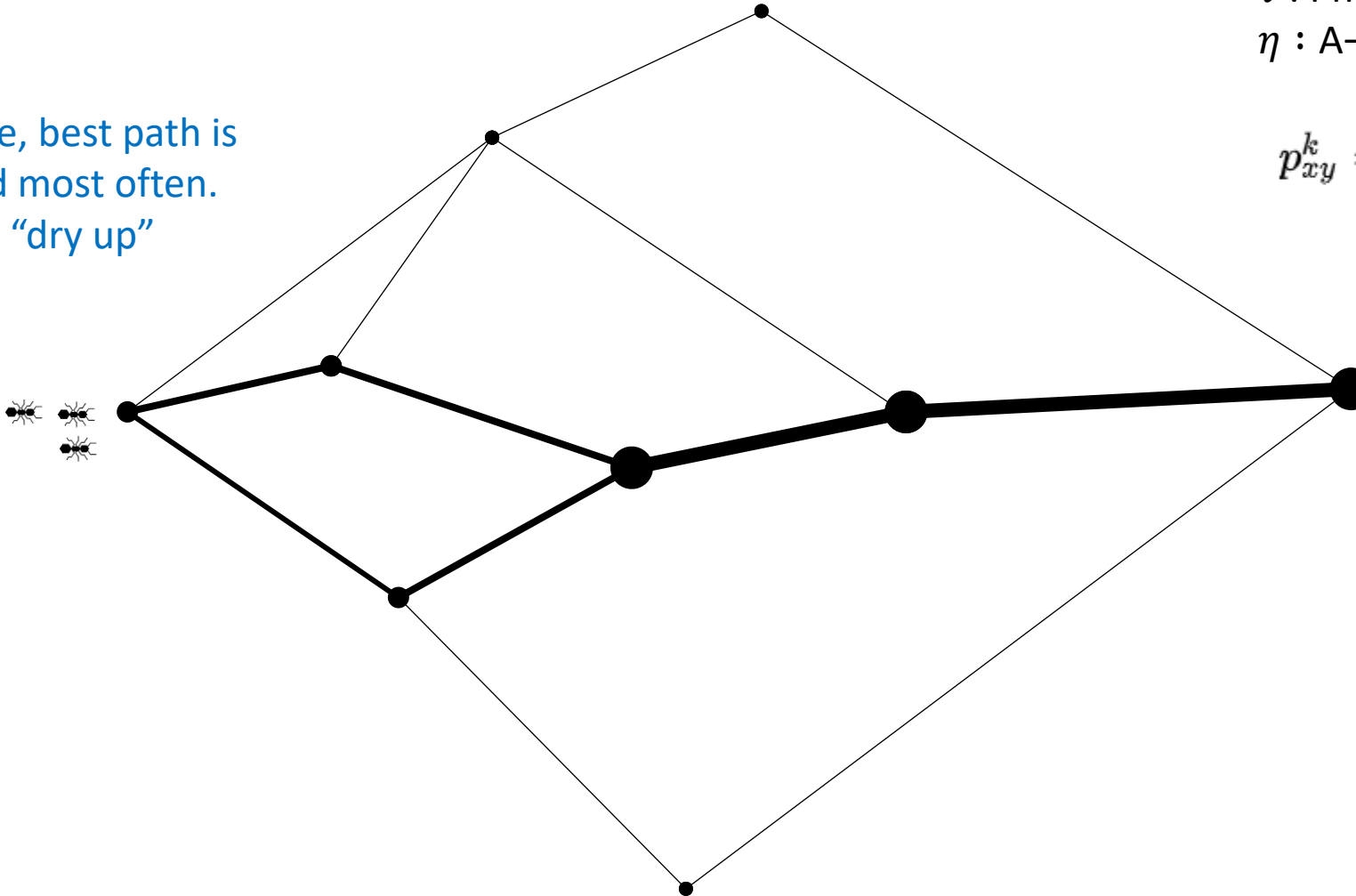
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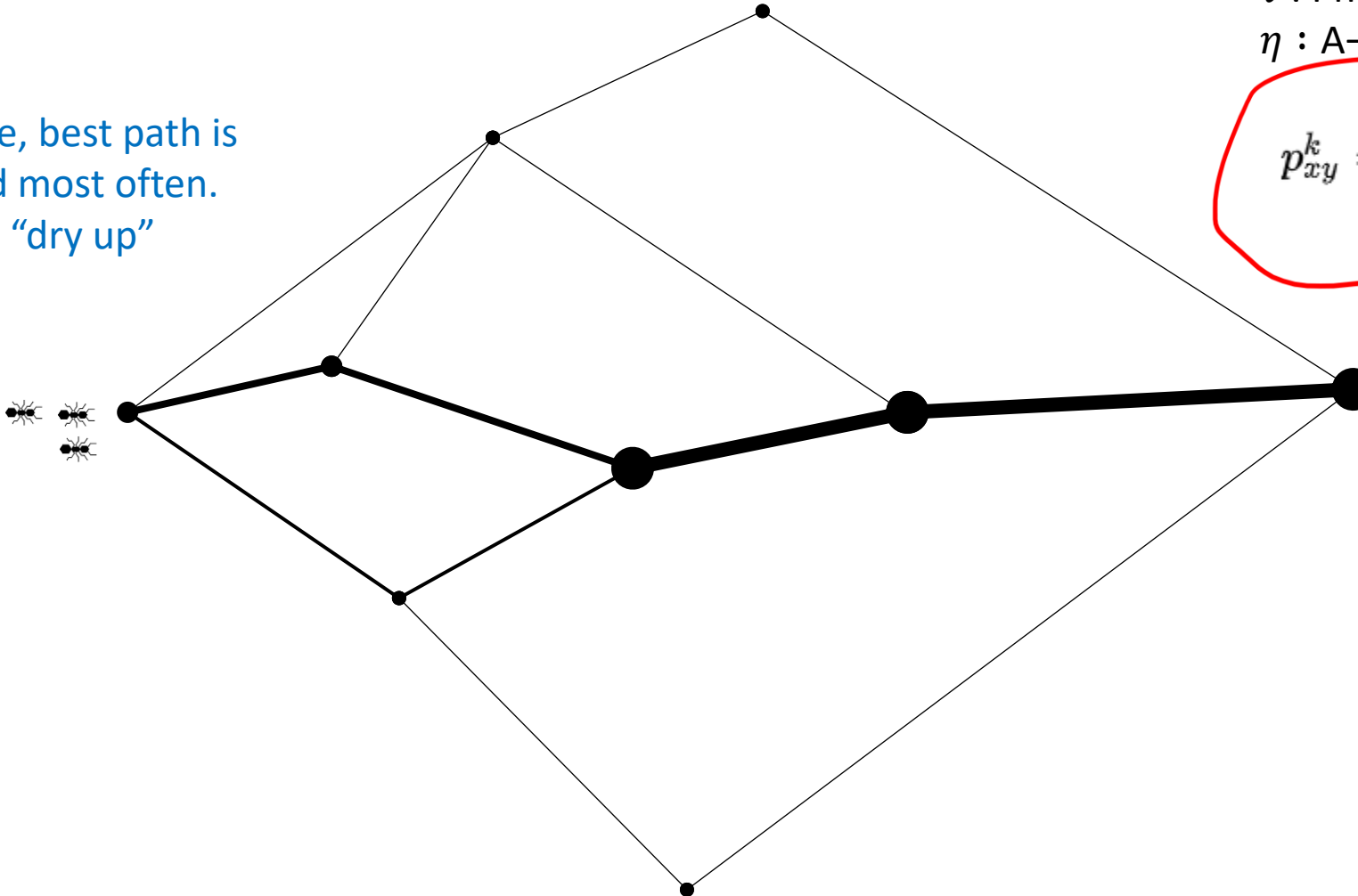
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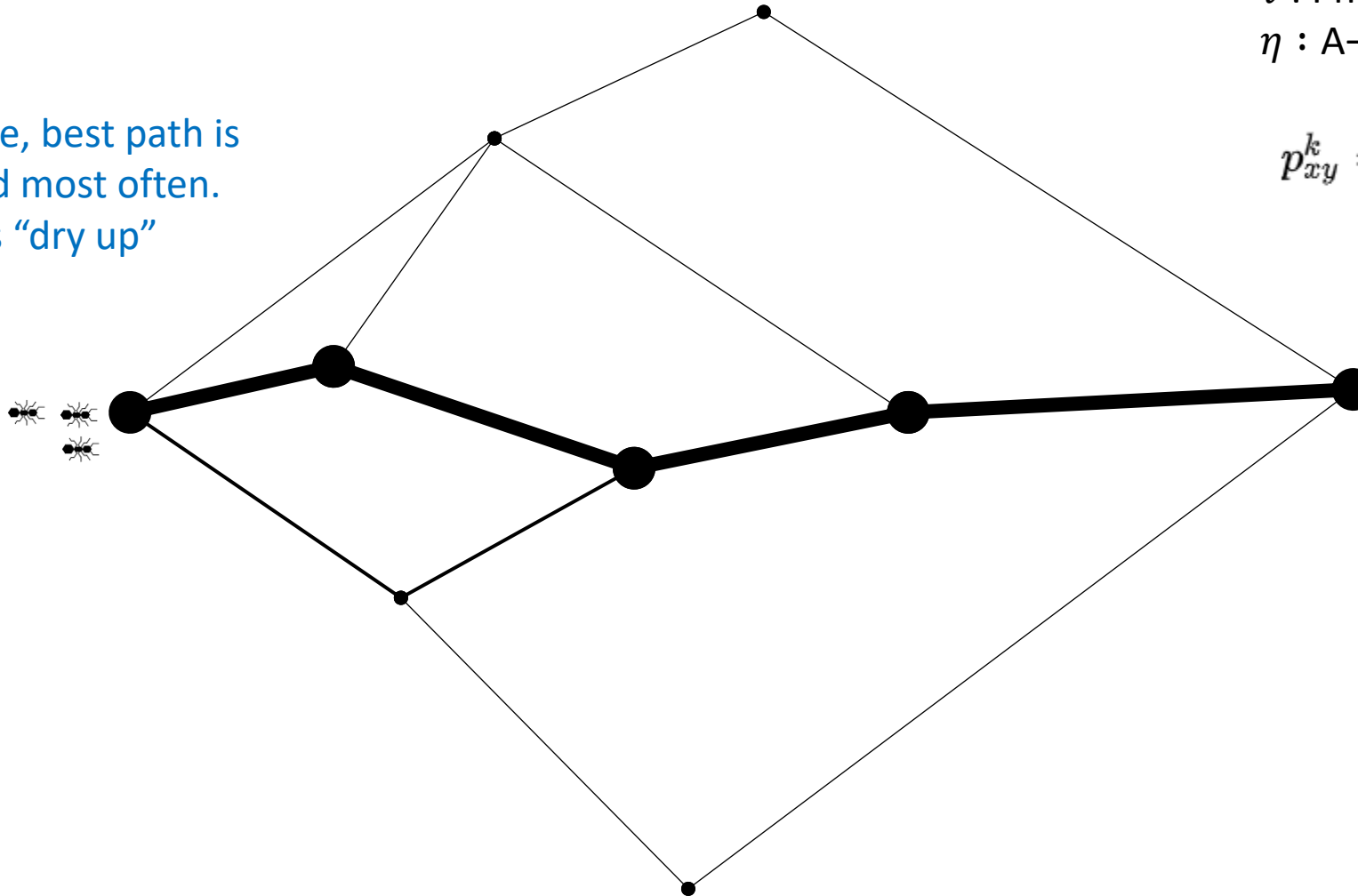
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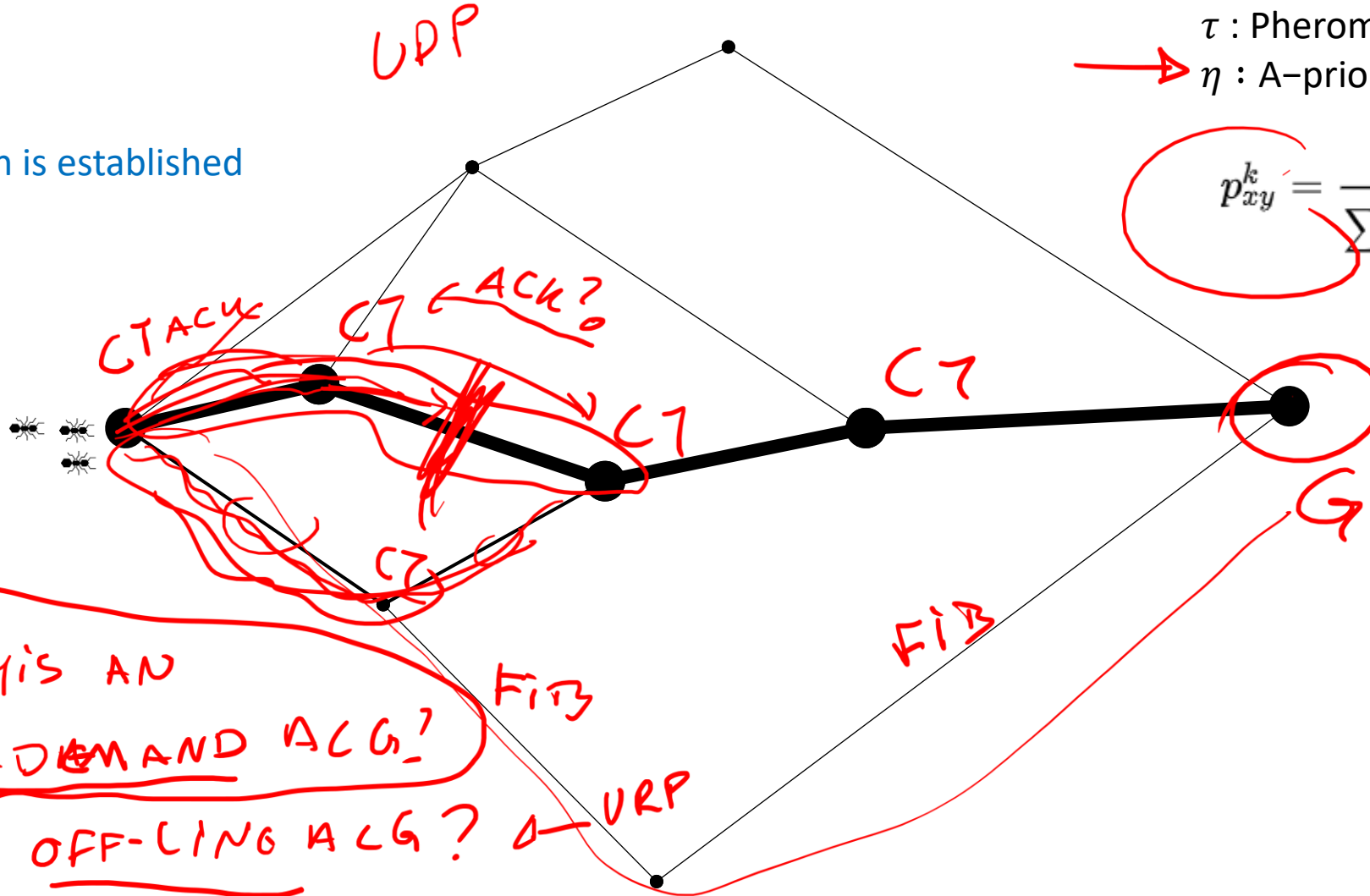
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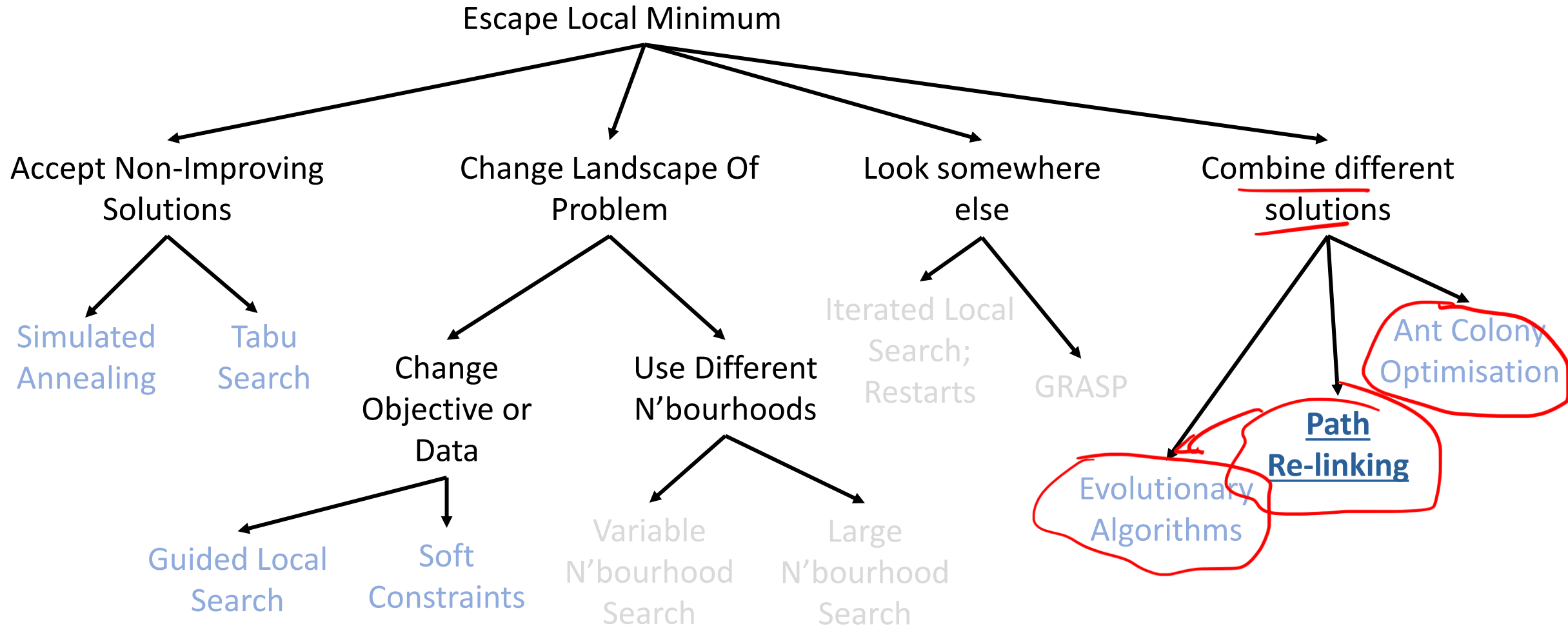
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Best path is established



Meta-heuristics: An Incomplete Survey



Path Relinking

Basic idea:

- Take two solutions
- “Walk” between them

For TSP:

GA POP-BASED ALG
BIG # OF OFFS

4 DIFF
SOL.

S₁ →

1	4	6	2	3	8	9	5	10	7
---	---	---	---	---	---	---	---	----	---

1	10	6	2	3	8	9	5	4	7
---	----	---	---	---	---	---	---	---	---

1	10	8	2	3	6	9	5	4	7
---	----	---	---	---	---	---	---	---	---

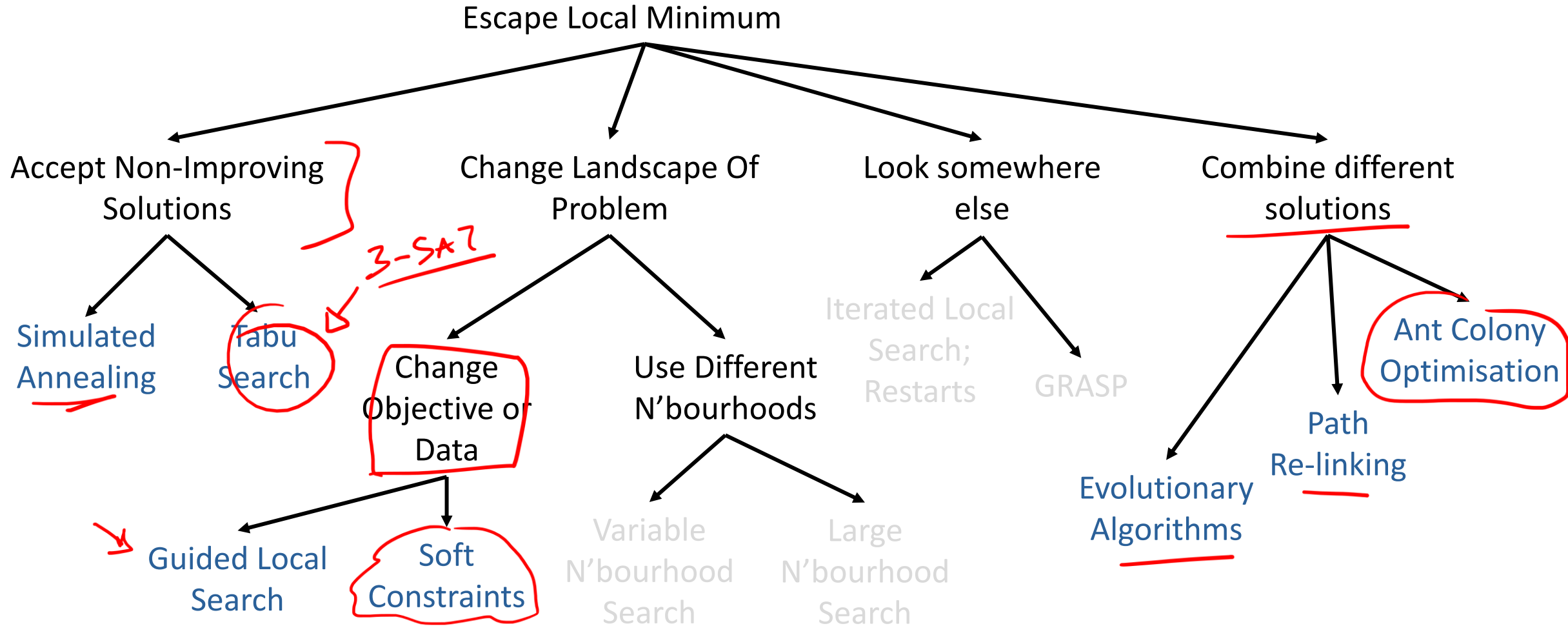
1	10	8	2	5	6	9	3	4	7
---	----	---	---	---	---	---	---	---	---

1	10	8	2	5	4	9	3	6	7
---	----	---	---	---	---	---	---	---	---

S₂ →

1	10	8	2	5	4	9	3	6	7
---	----	---	---	---	---	---	---	---	---

Meta-heuristics



Conclusions

- We've looked at the characteristics of Meta-heuristics
 - Problem independent on top of Problem-dependent heuristics
 - Often Randomised – "Stochastic Local Search" (also a book by Hoos & Stützle)
 - Diversification / Intensification (Exploration / Exploitation)
- We've looked at a few Meta-heuristics
 - Accepting non-improving solutions
 - Combining solutions
- Next time
 - More Meta-heuristics

NAME OF
BOOK



IN AZ

V.N.S
L.N.S