

The Model

The model used is a Kinematic model neglecting the complex interactions between the tires and the road. The model equations are as follow:

```
x[t] = x[t-1] + v[t-1] * cos(psi[t-1]) * dt
y[t] = y[t-1] + v[t-1] * sin(psi[t-1]) * dt
psi[t] = psi[t-1] + v[t-1] / Lf * delta[t-1] * dt
v[t] = v[t-1] + a[t-1] * dt
cte[t] = f(x[t-1]) - y[t-1] + v[t-1] * sin(eps[t-1]) * dt
eps[t] = psi[t] - psides[t-1] + v[t-1] * delta[t-1] / Lf * dt
```

Where:

- x, y : Car's position.
- ψ : Car's heading direction.
- v : Car's velocity.
- cte : Cross-track error.
- ϵ : Orientation error.

Those values are considered the state of the model. In addition to that, L_f is the distance between the car of mass and the front wheels (this is provided by Udacity's seed project). The other two values are the model output:

- a : Car's acceleration (throttle).
- δ : Steering angle.

The objective is to find the acceleration (a) and the steering angle(δ) in the way it will minimize an objective function that is the combination of different factors:

- Square sum of cte and ϵ .
- Square sum of the difference actuators to penalize a lot of actuator's actions.
- Square sum of the difference between two consecutive actuator values to penalize sharp changes.

The weight for each of these factors were tuned manually to obtain a successful track ride without leaving the road.

Timestep Length and Elapsed Duration (N & dt)

The number of points(N) and the time interval(dt) define the prediction horizon. The number of points impacts the controller performance as well. I tried to keep the horizon around the same time the waypoints were on the simulator. With too many points the controller starts to run slower, and some times it went wild very easily. After trying with N from 10 to 25 and dt 100 to 1000 milliseconds, I decided to leave them fixed to 10 and 100 milliseconds to have a better result tuning the other parameters.

Polynomial Fitting and MPC Preprocessing

The waypoints provided by the simulator are transformed to the car coordinate system at [./src/main.cpp](#) from line 103 to line 111. Then a 3rd-degree polynomial is fitted to the transformed waypoints. These polynomial coefficients are used to calculate the cte and ϵ later on. They are used by the solver as well to create a reference trajectory.

Model Predictive Control with Latency

To handle actuator latency, the state values are calculated using the model and the delay interval. These values are used instead of the initial one. The code implementing that could be found at [./src/main.cpp](#) from line 131 to line 136.