

# ANNEALING QUANTUM COMPUTING AND OPTIMIZATION

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Chief Development Officer  
June 17<sup>th</sup>, 2024



# PRIMARY APPROACHES TO QUANTUM COMPUTING



**ANNEALING**  
AN EASIER ON-RAMP  
TO QUANTUM COMPUTING  
Natively optimization  
Commercial today

**ANNEALING  
OR  
GATE**

**GATE-MODEL**  
HIGHER INVESTMENT  
COST & LEARNING CURVE  
Suited to differential equations  
7+ years to commercialization

## COMBINATORIAL OPTIMIZATION

Employee Scheduling  
Autonomous Vehicle Routing  
Peptide Design  
Fraud Detection  
Patient Trial Optimization

## LINEAR ALGEBRA & FACTORIZATION

Machine Learning  
Cryptography  
Drug Toxicity  
Global Weather Modeling

## DIFFERENTIAL EQUATIONS

Designer Drugs  
New Materials  
Longer-Life Batteries

QC industry, except D-Wave, almost exclusively focused on gate-model QC

# LONG TERM ADVANTAGE IN OPTIMIZATION

OPTIMIZATION IS A KEY APPLICATION AREA FOR ANNEALING QC



- More resilient to errors
- Does not require significant preprocessing or tuning
- Does not require high bandwidth qubit control
- Technology is scaling to thousands of qubits
- Near-term large-scale quantum computing technology



# LONG TERM ADVANTAGE IN OPTIMIZATION

OPTIMIZATION IS A KEY APPLICATION AREA FOR ANNEALING QC

Research points to QA outperforming in scale, quality, and speed

## Optimization Applications as Quantum Performance Benchmarks

Thomas Lubinski,<sup>1,2</sup> Carleton Coffrin,<sup>3</sup> Catherine McGeoch,<sup>4</sup>  
Pratik Sathe,<sup>5,6,7</sup> Joshua Apanavicius,<sup>8,9</sup> and David E. Bernal Neira<sup>6,10,11</sup>  
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<sup>6</sup>*Research Institute of Advanced Computer Science, Universities Space Research Association, Mountain View, CA, USA*

<sup>7</sup>*Theoretical Division (T4), Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA*

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<sup>9</sup>*Indiana University Quantum Science and Engineering Center, Bloomington, Indiana 47405, USA*

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(Dated: February 5, 2024)

# LONG TERM ADVANTAGE IN OPTIMIZATION

OPTIMIZATION IS A KEY APPLICATION AREA FOR ANNEALING QC

NISQ-era systems are not competitive in optimization

Article | [Open access](#) | Published: 12 March 2024

## Short-depth QAOA circuits and quantum annealing on higher-order ising models

[Elijah Pelofske](#) , [Andreas Bärtzsch](#)  & [Stephan Eidenbenz](#)

[npj Quantum Information](#) **10**, Article number: 30 (2024) | [Cite this article](#)

**2127** Accesses | **3** Altmetric | [Metrics](#)

# LONG TERM ADVANTAGE IN OPTIMIZATION

OPTIMIZATION IS A KEY APPLICATION AREA FOR ANNEALING QC



Fault tolerant gate-model systems have high overhead

## Focus beyond Quadratic Speedups for Error-Corrected Quantum Advantage

Ryan Babbush, Jarrod R. McClean, Michael Newman, Craig Gidney, Sergio Boixo, and Hartmut Neven  
PRX Quantum **2**, 010103 – Published 29 March 2021



# APPLICATION-ORIENTED BENCHMARKING



- End users assessing QC technology care about performance on specific applications
- End users assessing QC technology also care about cost of computation
  - Total execution time
  - Energy required
- Application focus makes it possible to compare different quantum computing technologies and modalities
- Application focus makes it possible to understand emerging advantages to using quantum computing technologies over classical approaches
- As new hardware becomes available, and as new application classes are identified, there is a strong framework for assessment

# APPLICATION-ORIENTED BENCHMARKING



Quantum Computing

IEEE Transactions on  
Quantum Engineering

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## Application-Oriented Performance Benchmarks for Quantum Computing

**THOMAS LUBINSKI<sup>1,2</sup>**, **SONIKA JOHRI<sup>3</sup>**, **PAUL VAROSY<sup>4</sup>**,  
**JEREMIAH COLEMAN<sup>5</sup>**, **LUNING ZHAO<sup>3</sup>**, **JASON NECAISE<sup>6</sup>**,  
**CHARLES H. BALDWIN<sup>7</sup>**, **KARL MAYER<sup>7</sup>**, AND **TIMOTHY PROCTOR<sup>8</sup>**

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Corresponding author: Thomas Lubinski (e-mail: tlubinski@quantumcircuits.com).

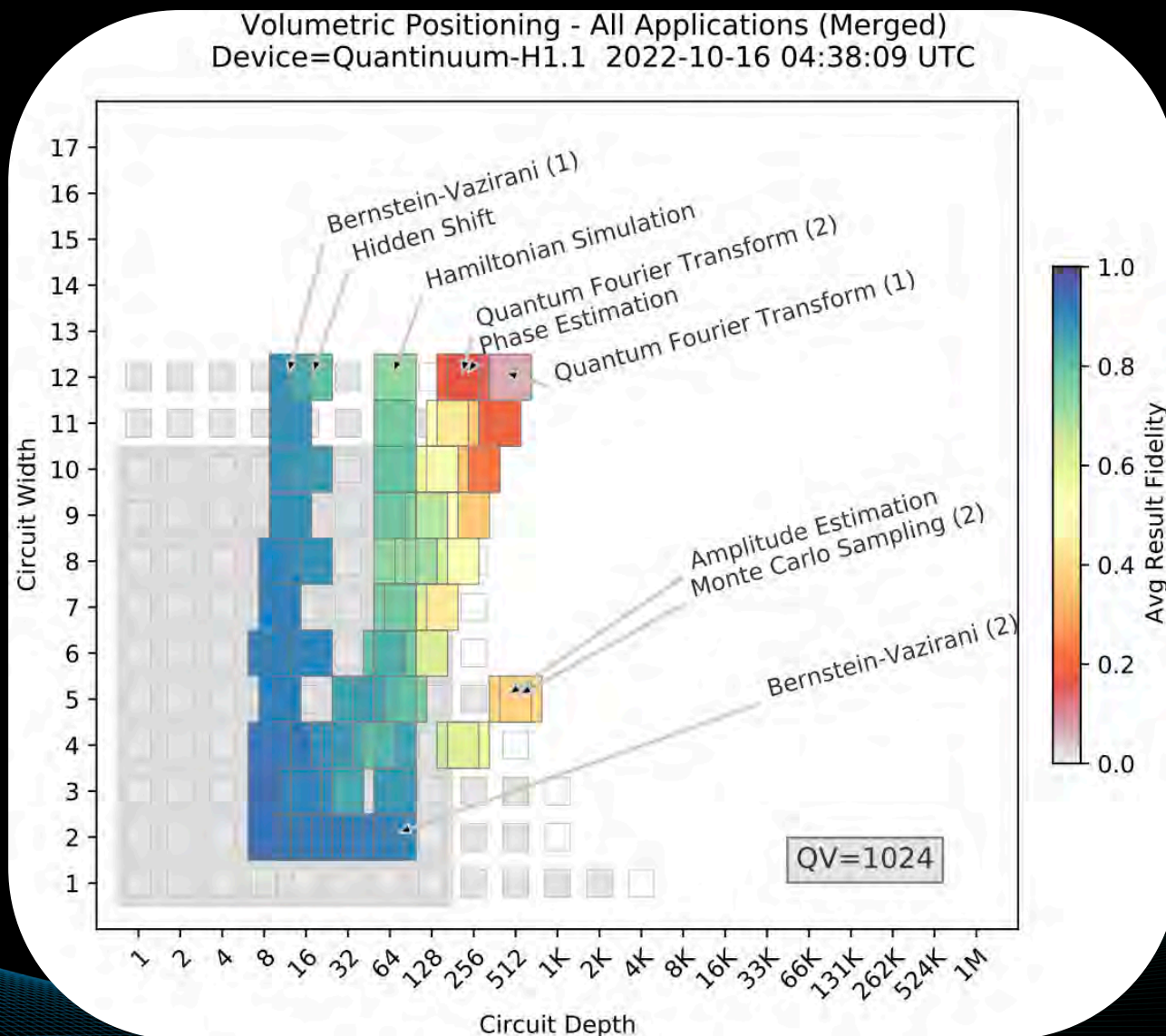
This work was supported by the Quantum Economic Development Consortium. The work of Timothy Proctor was supported by the U.S. Department of Energy, Office of Science, Office of Advanced Scientific Computing Research, through the Quantum Testbed Program.

- This is the framework IonQ has adopted



# APPLICATION-ORIENTED BENCHMARKING

- Adapting 'volumetric' metrics to actual applications
- Gate-model focused
- Mix of algorithmic complexity
  - Tutorial
  - Subroutine
  - Functional/Complete
- Advantages: stepping toward application performance
- Disadvantage:
  - Execution time ignored
  - Transpilation/compilation resources ignored
  - Hard to interpret problem scaling



Lubinski et al 2021

# ADDING A KEY APPLICATION AREA: OPTIMIZATION

## ASSESS MULTIPLE QUANTUM COMPUTING PLATFORMS FOR OPTIMIZATION

### Optimization Applications as Quantum Performance Benchmarks

Thomas Lubinski,<sup>1,2</sup> Carleton Coffrin,<sup>3</sup> Catherine McGeoch,<sup>4</sup>  
Pratik Sathe,<sup>5,6,7</sup> Joshua Apanavicius,<sup>8,9</sup> and David E. Bernal Neira<sup>6,10,11</sup>  
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<sup>7</sup>*Theoretical Division (T4), Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA*

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<sup>9</sup>*Indiana University Quantum Science and Engineering Center, Bloomington, Indiana 47405, USA*

<sup>10</sup>*Quantum Artificial Intelligence Laboratory, NASA Ames Research Center, Mountain View, CA, USA*

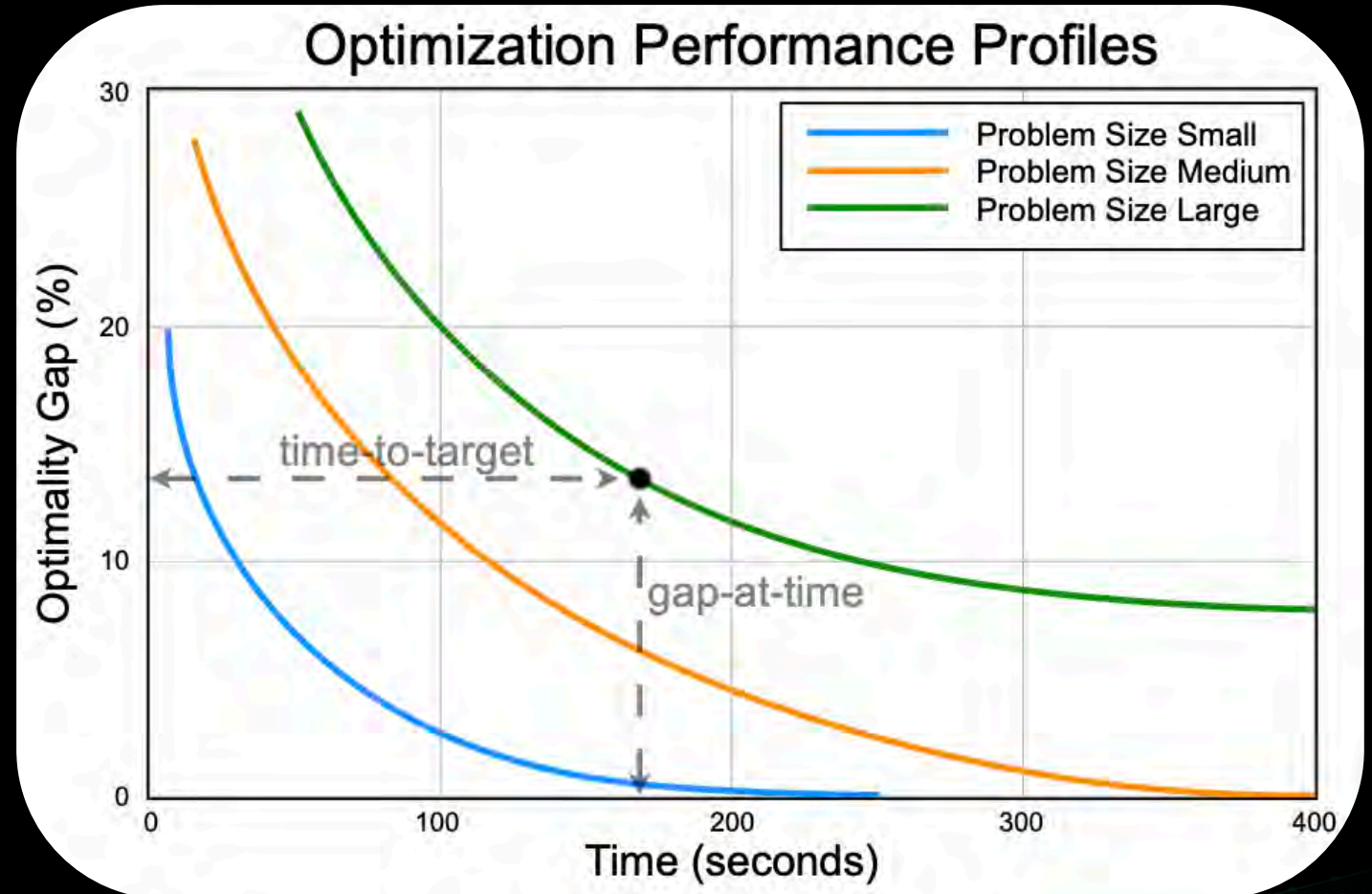
<sup>11</sup>*Davidson School of Chemical Engineering, Purdue University, West Lafayette, IN, USA*

(Dated: February 5, 2024)



# ADDING A KEY APPLICATION AREA: OPTIMIZATION

- Several performance criteria involved with assessing optimization performance
- Problem scale
- Time to a quality target
- Time to optimal
- Quality after a particular time
- 'Quantum execution time' and 'cumulative execution time' are important: variational approaches need tuning
- Operations Research field primarily focused on 'gap-at-time'



Lubinski et al 2024

# ADDING A KEY APPLICATION AREA: OPTIMIZATION



- Use MAX-CUT problem class
- Challenging combinatorial optimization class
- Unconstrained discrete optimization problem
- Well suited to QA
- Well suited to QAOA
- Useful for comparing many quantum computing technology platforms



**FIG. 3: The MaxCut Problem.** For an undirected graph consisting of nodes, or vertices, ( $V$ ) and edges ( $E$ ), partition the vertices into complementary sets such that the number of edges between the sets is the greatest. This graph shows one solution to one instance of the MaxCut problem for a graph with eight nodes, using colored nodes and edges. Nodes with different colors belong to the two sets of the solution cut. The number of solid red edges that connect nodes from different sets is the MaxCut of that graph.

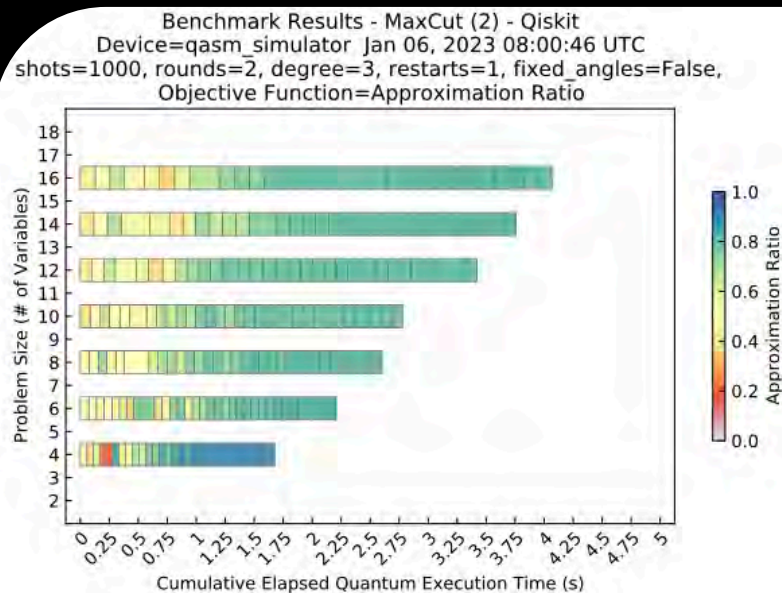
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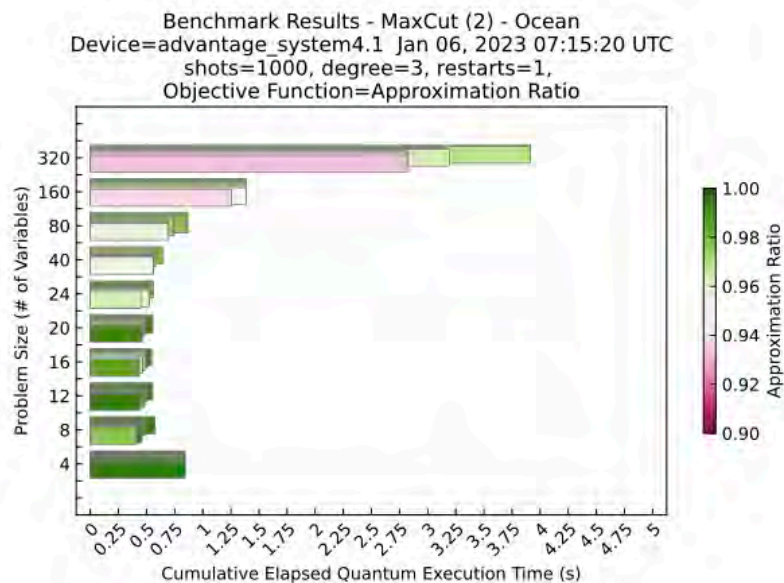
# APPLICATION-ORIENTED BENCHMARKING: OPTIMIZATION



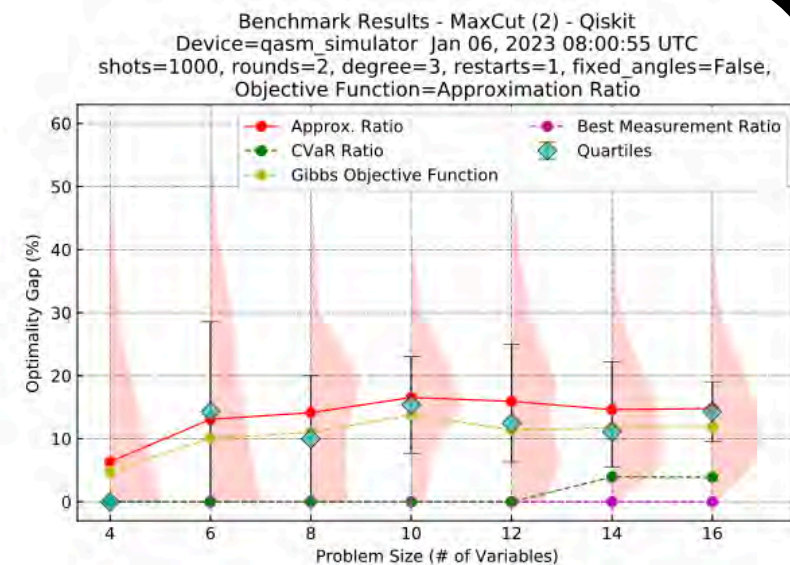
- Characterizes Performance of QAOA and Quantum Annealing
- Quantum execution time and application problem scale: central to benchmarking
- Ideal QAOA (gate) simulator struggling to return answers at a small scale



(a)



(b)



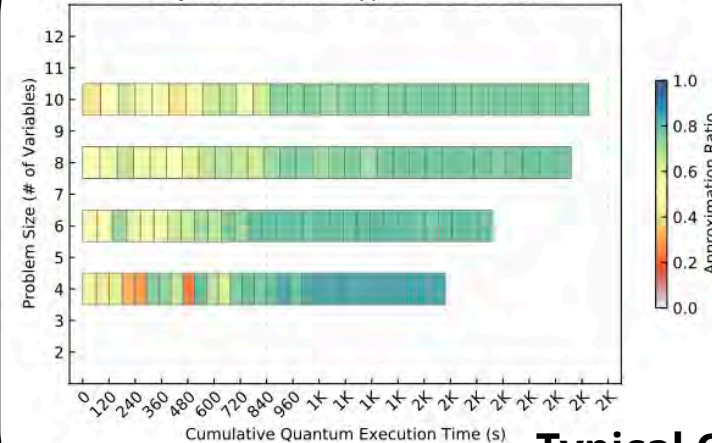
(c)

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# COMPARING APPROACHES: QUANTUM ANNEALING WINS

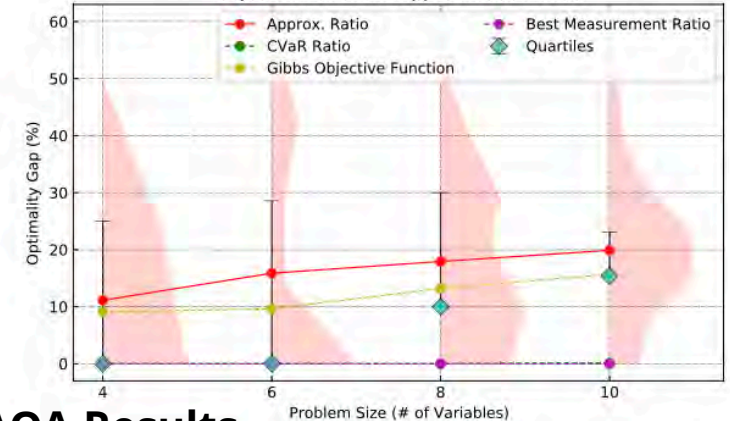
- QA: solves larger instances
- QA: provides higher quality solutions
- QA: significantly lower run times

Benchmark Results - MaxCut (2) - Qiskit  
Device=ionq\_qpu.aria-1-r2-s1000 Jan 07, 2023 01:09:18 UTC  
shots=1000, rounds=2, degree=3, restarts=1, fixed\_angles=False,  
Objective Function=Approximation Ratio



(a)

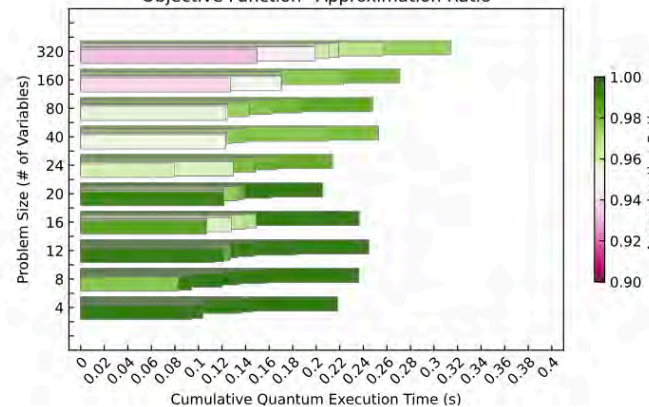
Benchmark Results - MaxCut (2) - Qiskit  
Device=ionq\_qpu.aria-1-r2-s1000 Jan 21, 2023 18:27:40 UTC  
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Objective Function=Approximation Ratio



(b)

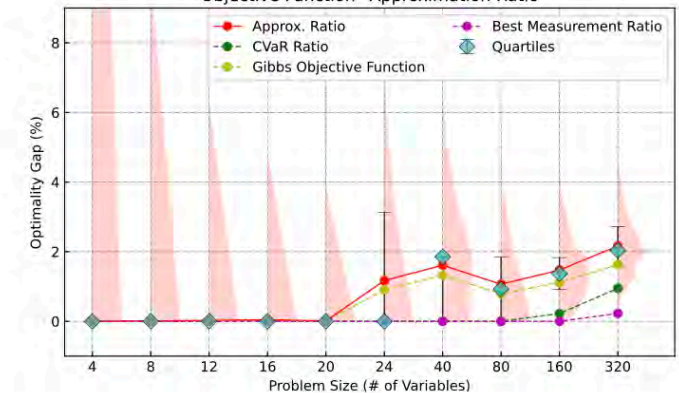
**Typical QAOA Results  
(Trapped Ion Qubits)**

Benchmark Results - MaxCut (2) - Ocean  
Device=advantage\_system4.1 Jan 06, 2023 07:15:23 UTC  
shots=1000, degree=3, restarts=1,  
Objective Function=Approximation Ratio



(a)

Benchmark Results - MaxCut (2) - Ocean  
Device=advantage\_system4.1 Jan 06, 2023 07:24:52 UTC  
shots=1000, degree=3, restarts=1,  
Objective Function=Approximation Ratio



(b)

**Typical Quantum Annealing Result**

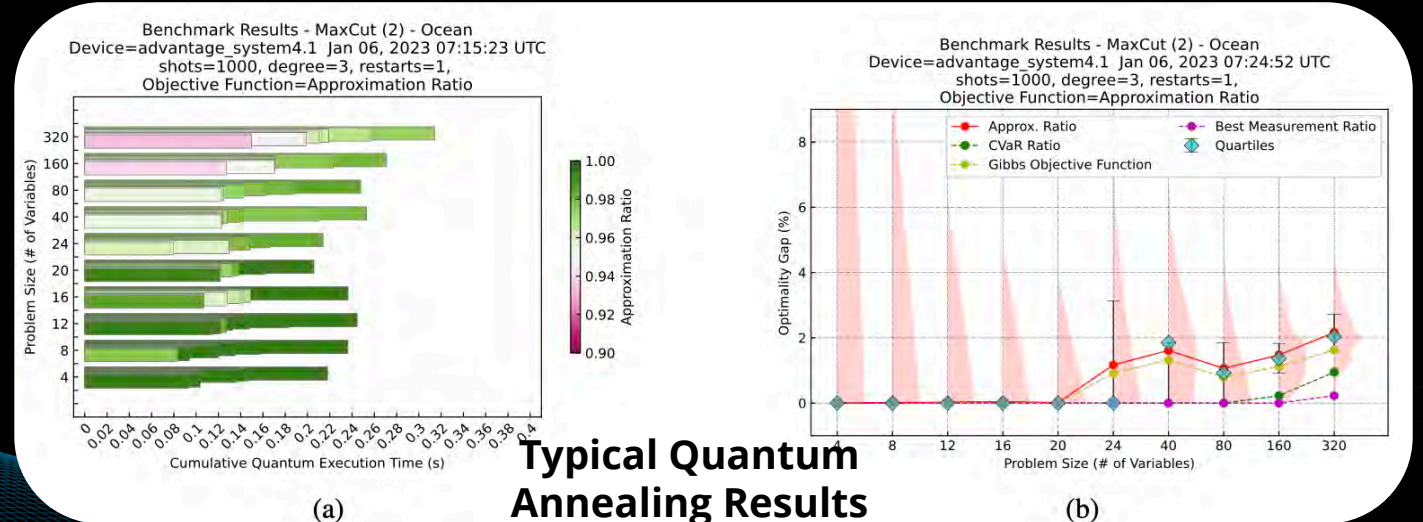
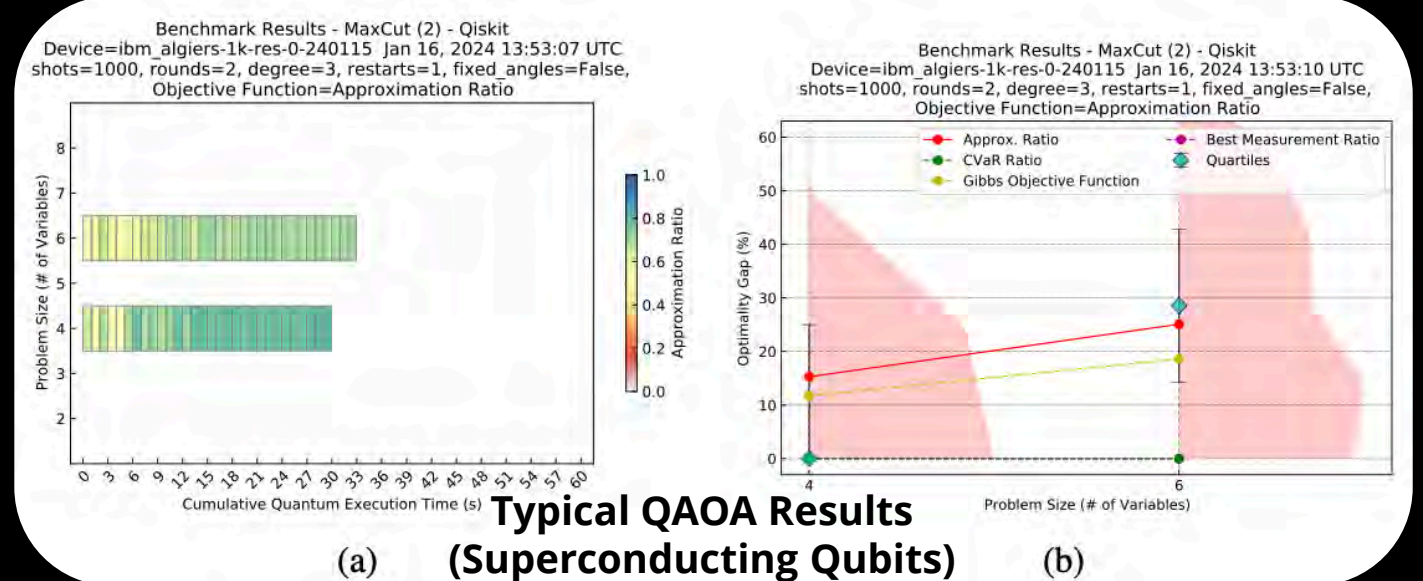
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**D-WAVE**



# COMPARING APPROACHES: QUANTUM ANNEALING WINS

- QA: solves larger instances
- QA: provides higher quality solutions
- QA: significantly lower run times



Lubinski et al 2024

# ADDING A KEY APPLICATION AREA: ISING SPIN GLASSES



Article

nature

## Quantum critical dynamics in a 5,000-qubit programmable spin glass

<https://doi.org/10.1038/s41586-023-05867-2>

Received: 27 July 2022

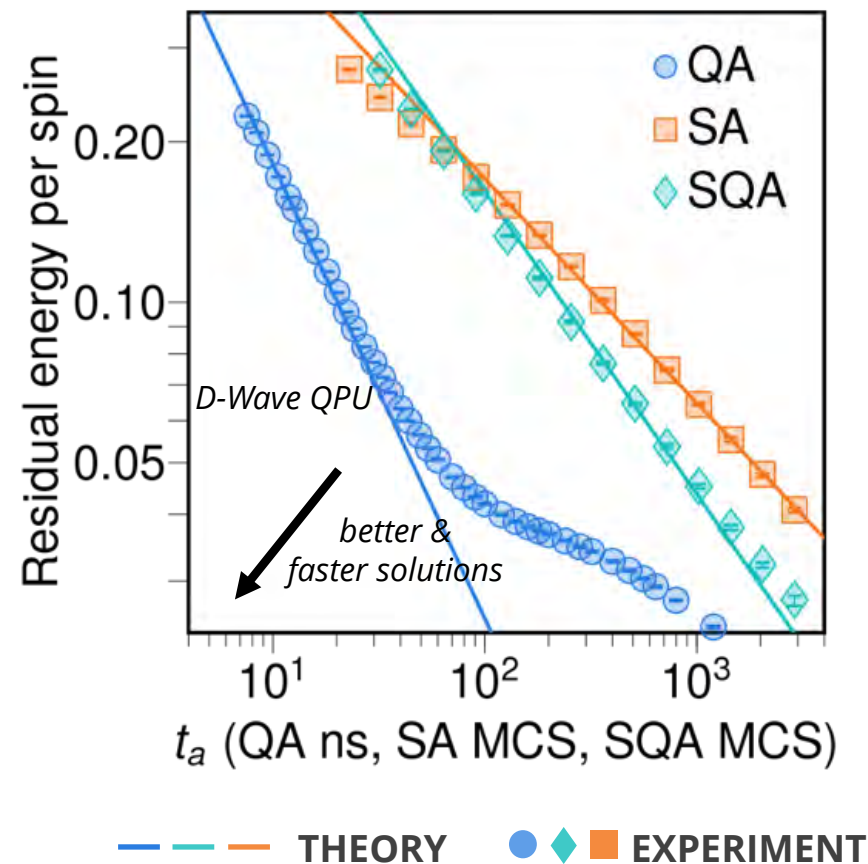
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Check for updates

Andrew D. King<sup>1</sup>, Jack Raymond<sup>1</sup>, Trevor Lanting<sup>1</sup>, Richard Harris<sup>1</sup>, Alex Zucca<sup>1</sup>, Fabio Altomare<sup>1</sup>, Andrew J. Berkley<sup>1</sup>, Kelly Boothby<sup>1</sup>, Sara Ejtemaee<sup>1</sup>, Colin Enderud<sup>1</sup>, Emile Hoskinson<sup>1</sup>, Shuiyuan Huang<sup>1</sup>, Eric Ladizinsky<sup>1</sup>, Allison J. R. MacDonald<sup>1</sup>, Gaelen Marsden<sup>1</sup>, Reza Molavi<sup>1</sup>, Travis Oh<sup>1</sup>, Gabriel Poulin-Lamarre<sup>1</sup>, Mauricio Reis<sup>1</sup>, Chris Rich<sup>1</sup>, Yuki Sato<sup>1</sup>, Nicholas Tsai<sup>1</sup>, Mark Volkmann<sup>1</sup>, Jed D. Whittaker<sup>1</sup>, Jason Yao<sup>1</sup>, Anders W. Sandvik<sup>2</sup> & Mohammad H. Amin<sup>1\*</sup>

- Another well studied and challenging combinatorial optimization task
- Growing evidence that harnessing coherent quantum dynamics gives a scaling advantage
- Basis for computational supremacy investigation



QA: Quantum Annealing

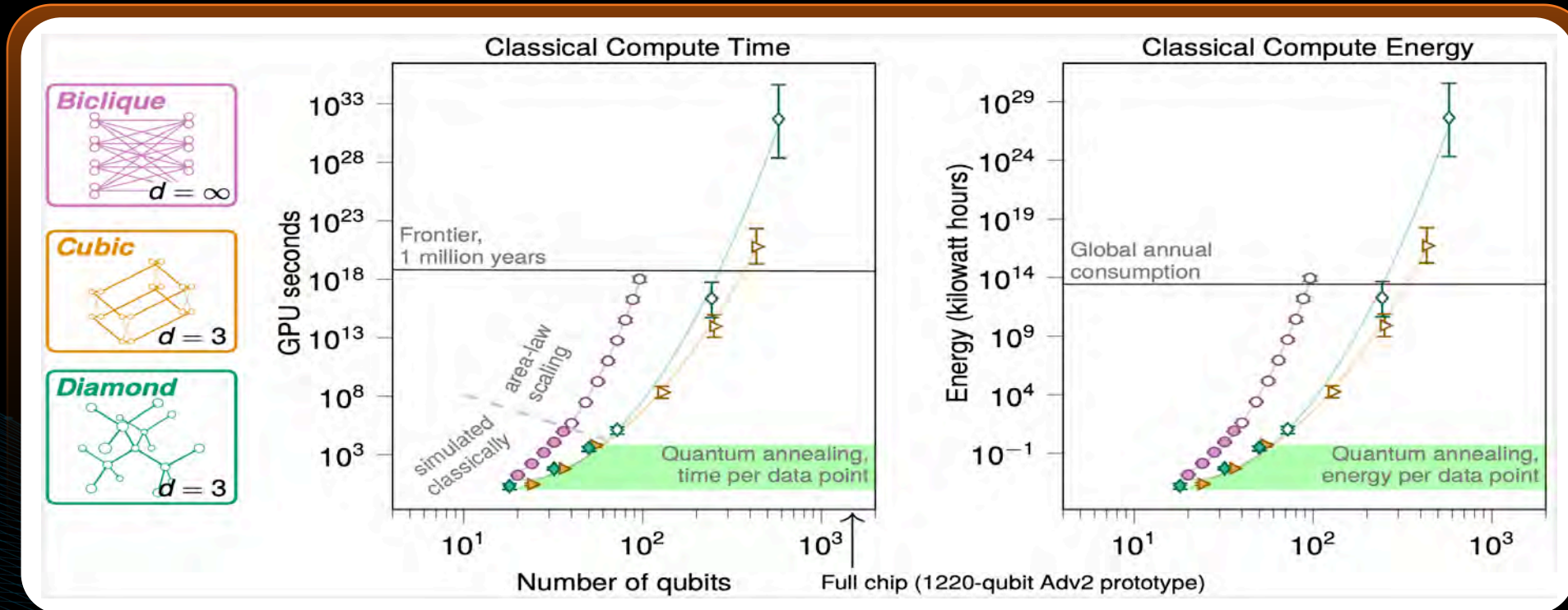
SA: Simulated Annealing

SQA: Simulated Quantum Annealing



# COMPUTATIONAL SUPREMACY IN QUANTUM SIMULATION USING ADVANTAGE2™ PROTOTYPE

We believe D-Wave is the first in the world to demonstrate quantum supremacy on real-world problems; These problems cannot be solved by classical computers. <https://arxiv.org/abs/2403.00910>



- Classical computations performed on **FRONTIER AND SUMMIT SUPERCOMPUTERS AT OAK RIDGE NATIONAL LAB**
- **EXPONENTIAL ADVANTAGE** over state-of-the-art classical techniques (tensor networks, neural networks, heuristics)
- **CLASSICAL COMPUTERS TOO SLOW** and power hungry for all but the smallest instances

# CAN GATE-MODEL QC SYSTEMS EMULATE ANNEALING QC SYSTEMS? NO.

- In principle, gate-model systems can simulate annealing systems
- In practice, the overhead is prohibitive -- even for very simple systems!
- This analysis does not even account for the overhead involved with error correction

## The Cost of Emulating a Small Quantum Annealing Problem in the Circuit-Model

Javier Gonzalez-Conde,<sup>1,2,\*</sup> Zachary Morrell,<sup>3</sup> Marc Vuffray,<sup>4</sup> Tameem Albash,<sup>5</sup> and Carleton Coffrin<sup>3,†</sup>

<sup>1</sup>*Department of Physical Chemistry, University of the Basque Country UPV/EHU, Apartado 644, 48080 Bilbao, Spain*

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(Dated: February 28, 2024)

Demonstrations of quantum advantage for certain sampling problems has generated considerable excitement for quantum computing and has further spurred the development of circuit-model quantum computers, which represent quantum programs as a sequence of quantum gates acting on a finite number of qubits. Amongst this excitement, analog quantum computation has become less prominent, with the expectation that circuit-model quantum computers will eventually be sufficient for emulating analog quantum computation and thus rendering analog quantum computation obsolete. In this work we explore the basic requirements for emulating a specific analog quantum computation in the circuit model: the preparation of a biased superposition of degenerate ground states of an Ising Hamiltonian using an adiabatic evolution. We show that the overhead of emulation is substantial even for this simple problem. This supports using analog quantum computation for solving time-dependent Hamiltonian dynamics in the short and mid-term, assuming analog errors can be made low enough and coherence times long enough to solve problems of practical interest.