

OAA Tutorial 3

Ques 1) write a linear search pseudo code to search an element in a sorted array with minimum comparisons.

int linear_search (int A[], int n, int t)

{

 if (abs(A[0]-t) > abs(A[n-1]-t))
 for (i = n-1 to 0; i--)
 if (A[i] == t) { return i; }

 else

 for (i=0 to n-1; i++)
 if (A[i] == t)
 return i;

}

Ans 2) Iterative insertion sort .

void insertion (int A[], int n)

{

 for (i=1 to n)
 t = A[i];

 j=i;

 while (j>=0 & t < A[j]) {

 A[j+1] = A[j];

 j--;

}

 A[j+1] = last;

}

Insertion sort is also called online sorting algorithm because it will work if the elements to be sorted are provided one at a time with the understanding that the algorithm must keep the sequence sorted as more elements are added in.

Ans 3) Complexity of all the sorting algorithms are given below :

Sorting	Best case	worst case
Bubble sort	$O(n^2)$	$O(n^2)$
Selection sort	$O(n^2)$	$O(n^2)$
Insertion sort	$O(n^2)$	$O(n^2)$
Count sort	$O(n)$	$O(n+k)$
Quick sort	$O(n \log n)$	$O(n^2)$
Merge sort	$O(n \log n)$	$O(n \log n)$
Heap sort	$O(n \log n)$	$O(n \log n)$

Ans 4

Sorting	Inplace	Stable	online
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Bubble	✓	✓	✗
Selection	✓	✗	✗
insertion	✓	✓	✓
Count	✗	✓	✗
quick	✓	✗	✗
Merge	✗	✓	✗
Heap	✓	✗	✗

Iterative

Ans 5) Recursive / n pseudocode for binary search

Iterative

```
( int binarySearch( int arr[], int a )
```

```
{ int l = 0, r = arr.length - 1;
```

```
while (l <= r)
```

Σ

```
    int m = l + (r-l)/2;
```

```
    if (arr[m] == a)
```

```
        return m;
```

```
    if (arr[m] < a)
```

```
        l = m + 1;
```

```
    else
```

```
        r = m - 1;
```

Σ

```
return -1;
```

Σ

Recursive

```
int binarySearch( int arr[], int l, int r,  
                  int a )
```

Σ

```
if (r >= l)
```

Σ

```
    int mid = l + (r-l)/2;
```

```
    if (arr[mid] == a)
```

```
        return mid;
```

else if $\text{arr}[\text{mid}] > \text{x}$)

return $\text{binarysearch}(\text{arr}, 1, \text{mid}-1, \text{x})$;

else :

return $\text{binarysearch}(\text{arr}, \text{mid}+1, \text{n}, \text{x})$;

}

return (-1);

}

* linear search

Iterative : Time complexity = $O(n)$

space complexity = $O(1)$

Recursive : Time complexity = $O(n)$

space complexity = $O(n)$

* Binary search

Iterative : Time complexity = $O(\log n)$

space complexity = $O(1)$

Recursive : Time complexity = $O(\log n)$

space complexity = $O(\log n)$

Ans 6

$$\begin{array}{c} T(n) \\ \downarrow \\ T(n/2) \\ \downarrow \\ T(n/4) \\ \downarrow \\ | \\ | \\ T(n/2^R) \end{array}$$

$$\text{Recurrence Relation} = T(n/2) + O(1)$$

Ans 7

```

int n;
int A[n];
int key;
int l=0, j=n-1;
while (i < j)
{
    if ((A[i] + A[j]) == key)
        break;
    else if ((A[i] + A[j]) > key)
        j--;
    else
        i++;
}
cout << i << " " << j;

```

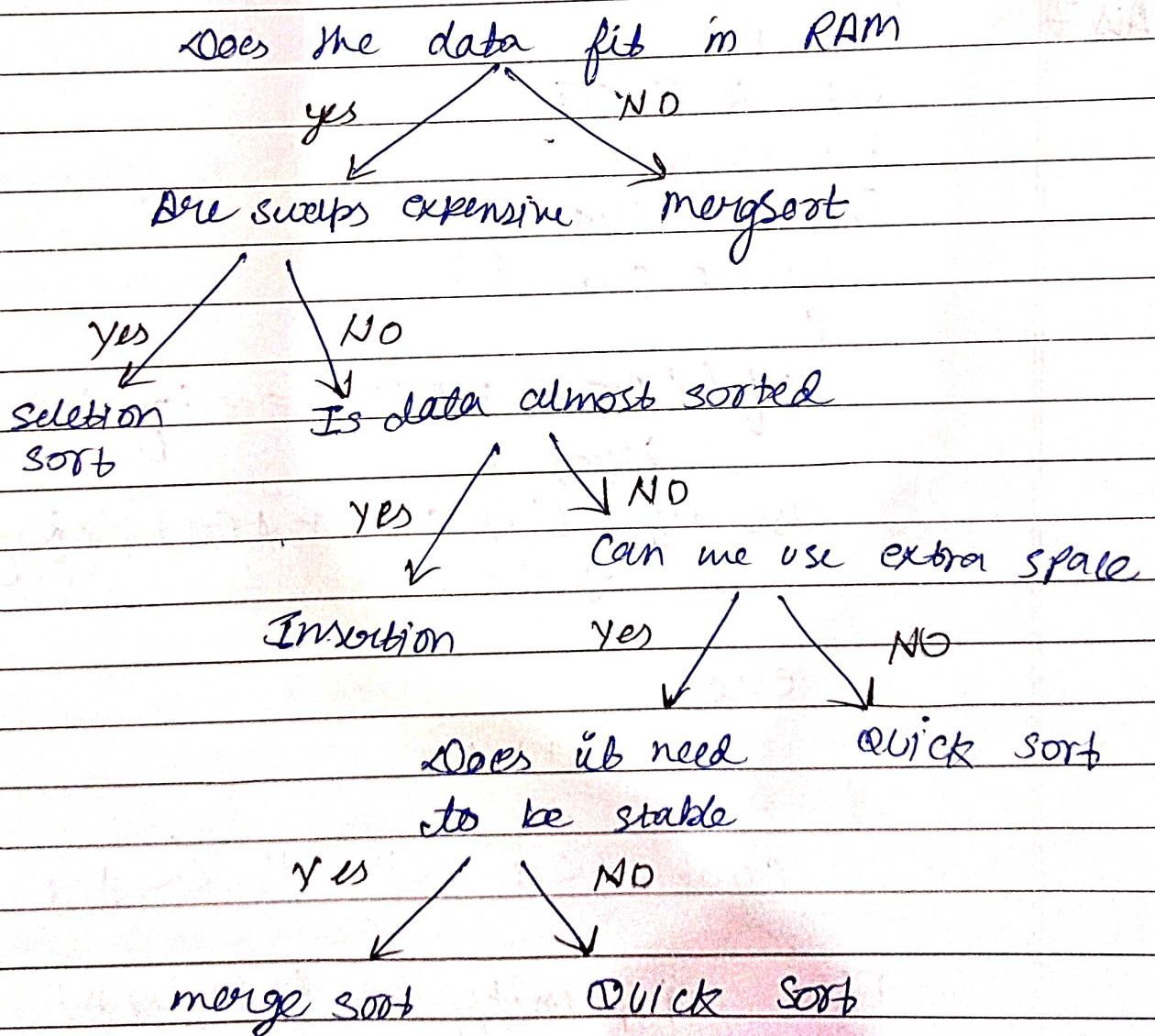
$$\text{Time complexity} = O(n \log n)$$

Ans 8

There is no best sorting algorithm. It depends on the situation or the type of array given.

Factor affecting sorting algorithm are:

- i) Runtime
- ii) Space
- iii) Stable
- iv) No. of swaps
- v) Will the data fit in RAM



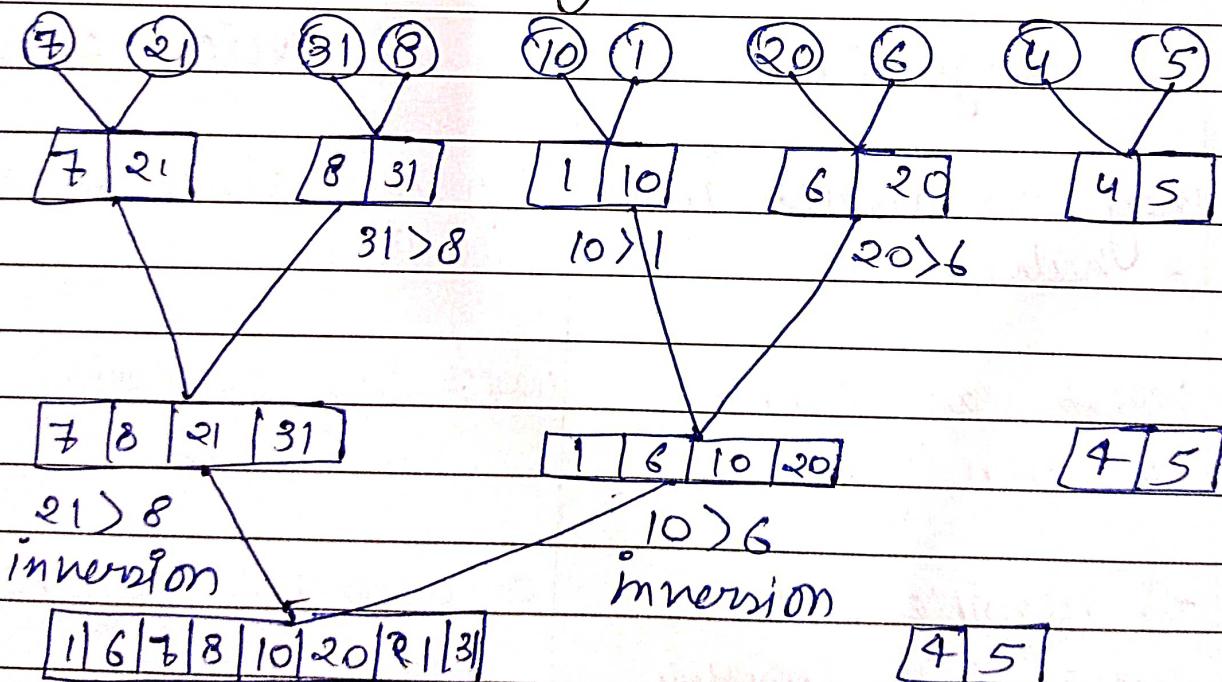
Ans q) Inversions in an array indicates how far the array is from being sorted. If the array is ~~from~~ already sorted, the inversion count is 0, ~~0~~ but if the array is sorted in reverse order, then the inversion is maximum.

conversion for inversion

$a[i] > a[j]$ and $i < j$

7 | 21 | 31 | 8 | 10 | 1 | 20 | 6 | 4 | 5

Dividing the array



7>4, 6>5, 7>4, 7>5, 8>4, 8>5, 10>4, 10>5, 20>4, 20>5
21>4, 21>5, 31>4, 31>5

Inversion count = 31 Ans

Ans 10 Best Case

$$\text{merge sort} = 2T(n/2) + n$$

$$\text{quick sort} = 2T(n/2) + n$$

Worst Case

~~merge~~

$$\text{merge sort} = 2T(n/2) + n$$

$$\text{quick sort} = T(n-1) + n$$

similarities : They both work on concepts of divide & conquerive algorithm

Difference

merge sort	quick sort
1) They are divided into 2 halves	They are divide in any ratio
2) worst case complexity is $O(n \log n)$	worst case complexity is $O(n^2)$
3) It require extra space NOT InPlace	It does not require extra space
4) It is external sorting	It is internal sorting
5) work consistently on any size of data set	work fast on small data set

Ans 10) Best Case

$$\text{Time Complexity} = O(n \log n)$$

Best Case occurs when the partition process always picks the middle element as pivot

* Worst Case

$$\text{Time complexity} = O(n^2)$$

when the array is sorted in ascending or descending order.

Ans 12) void selection (int A[], int n)

```

for (int i = 0; i < n - 1; i++)
    {
        int min = i;
        for (int j = i + 1; j < n; j++)
            {
                if (A[min] > A[j])
                    min = j;
                int key = A[min];
                while (min > i)
                    {
                        min--;
                    }
                A[i] = key;
            }
    }

```

Ans 13) void bubblesort (int A[], int n)

{

int i, j;

int f = 0;

for (i = 0 ; i < n ; i++)

{

for (j = 0 ; j < n - 1 ; j++)

{

if (A[j] > A[j + 1])

{

swap (A[j] , A[j + 1])

j = 1 ;

{

if {

(f == 0)

break ;

{

Ans 13*

your computer —————— sorting

Ans 13

when the data set is large enough to fit inside RAM, we use merge sort because it uses the divide and conquer approach in which it keeps dividing the array into smaller parts

until it can no longer be splitted.

It then merge the array divided in n parts. Therefore at a time only a part of array is taken on RAM

External sorting

It is used to sort massive amount of data. It is required when the data does not fit inside RAM and instead they must reside in the slower external memory.

During sorting, chunks of small data that can fit in main memory are read, sorted and written out to a temporary file.

During merging, the sorted subfiles are combined into a single large file.

Internal sorting

It is a type of sorting which is used when the entire collection of data is small enough to reside within RAM. Then there is no need of external memory for program execution.