

# **VISVESVARAYA TECHNOLOGICAL UNIVERSITY**

“JnanaSangama”, Belgaum -590014, Karnataka.



## **LAB REPORT on**

## **Artificial Intelligence (23CS5PCAIN)**

*Submitted by*

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*in partial fulfillment for the award of the degree of*  
**BACHELOR OF ENGINEERING**  
*in*  
**COMPUTER SCIENCE AND ENGINEERING**



**B.M.S. COLLEGE OF ENGINEERING**

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**Bull Temple Road, Bangalore 560019**  
(Affiliated To Visvesvaraya Technological University, Belgaum)  
**Department of Computer Science and Engineering**



**CERTIFICATE**

This is to certify that the Lab work entitled “Artificial Intelligence (23CS5PCAIN)” carried out by **Sakshi B R (1BM22CS233)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements in respect of an Artificial Intelligence (23CS5PCAIN) work prescribed for the said degree.

Dr. Seema patil Assistant Professor Department of CSE, BMSCE	Dr. Joythi S Nayak Professor & HOD Department of CSE, BMSCE
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Github Link:

<https://github.com/Sakshiibr/AI>

### Program 1

Implement Tic - Tac - Toe Game

Implement vacuum cleaner agent

### Algorithm:

The image shows a handwritten algorithm for a Tic Tac Toe game in a notebook. The notebook has a header with 'GoodLuck', 'Page No.', and 'Date 24/3/24'. The title 'Lab - 1' is written in the center. The main title 'Tic Tac Toe' is written on the left. The algorithm is a list of steps starting with arrows. The steps are: 1. Initialize the 2D array of 3 row and 3 column with empty space. 2. Create the function 'board' for display. 3. Take the input from the user as 'x' or 'o'. 4. Handle the I/P of the user by checking the row, column, diagonal wise by the condition. 5. Create the function victory to check. Iterate and check if all the row/col are occupied by same icon. If occupies -> True. If not -> False. 6. Create a function for draw. Iterate over the board and check whether all the cells are filled or not. If filled -> break. 7. Create a function for draw. Iterate over the board and check/whether all the cells are. 8. Create the main game function draw Board. loop the game.

GoodLuck Page No.  
Date 24/3/24

Lab - 1

Tic Tac Toe

- Initialize the 2D array of 3 row and 3 column with empty space
- Create the function "board" for display
- Take the input from the user as 'x' or 'o'
- Handle the I/P of the user by checking the row, column, diagonal wise by the condition.
- Create the function victory to check  
Iterate and check if all the row/col are occupied by same icon  
if occupies → True  
If not → False
- Create a function for draw  
Iterate over the board and check whether all the cells are filled or not  
if filled → break
- Create a function for draw  
Iterate over the board and check/whether all the cells are
- Create the main game function draw Board.  
loop the game

- Ask current player to make move
- Update the move
- Check for the victory and print message
- Check for draw & print draw message
- Ask for draw & print draw message
- Ask for next player move
- Update the move and it goes on.

11.1.15



## Lab - 1

Implement vacuum world cleaner

function Reflex - vacuum - Agent (Location, status)  
return an action

if Status = Dirty then  
return suck

else if location = A then  
return Right

else if location = B then  
return left

Input: Location A

Status 0

Dust in another = 1

Algorithm:-

- Take input:  
Take input from user for the initial location of the vacuum  
Take input from user for the status of the room (0 for clean, 1 for dirty).
- Check if the current room is dirty  
If dirty:  
clean the room  
Increase the total cost by 1  
If already clean, print a message that the room is already clean
- Move to the next room



- Clean the rooms
- Check goal state
- Print total cleaning cost

### Output

Current state: ['A': 0, 'B': 0]

Vacuum is in Room A

Total cost so far: 0

Enter initial location of the vacuum (A or B): A

Enter the status for Room A : 1

Enter the status for Room B : 0

Suck at A

Move Right to B

Move Left to A

Total cost : 1

Goal Reached

11/10/20

## Code:

### 1.1 Implement Tic –Tac –Toe Game

```
# Initialize the board
board = [' ' for _ in range(9)]

# Function to draw the board
def draw_board():
    row1 = '| {} | {} | {} |'.format(board[0], board[1], board[2])
    row2 = '| {} | {} | {} |'.format(board[3], board[4], board[5])
    row3 = '| {} | {} | {} |'.format(board[6], board[7], board[8])
    print()
    print(row1)
    print(row2)
    print(row3)
    print()

# Function for player's move
def player_move(icon):
    if icon == 'X':
        number = 1
    elif icon == 'O':
        number = 2
    print("Your turn, player {}".format(number))
    choice = int(input("Enter your move (1-9): ").strip())
    if board[choice - 1] == ' ':
        board[choice - 1] = icon
    else:
        print()
        print("That space is taken!")

# Function to check for victory
def is_victory(icon):
    if (board[0] == icon and board[1] == icon and board[2] == icon)
or \
    (board[3] == icon and board[4] == icon and board[5] == icon)
or \
    (board[6] == icon and board[7] == icon and board[8] == icon)
or \
    (board[0] == icon and board[3] == icon and board[6] == icon)
or \
    (board[1] == icon and board[4] == icon and board[7] == icon)
or \
    (board[2] == icon and board[5] == icon and board[8] == icon)
or \
    (board[0] == icon and board[4] == icon and board[8] == icon)
or \
```



```

        (board[2] == icon and board[4] == icon and board[6] ==
icon):
    return True
    else:
        return False

# Function to check for a draw
def is_draw():
    if ' ' not in board:
        return True
    else:
        return False

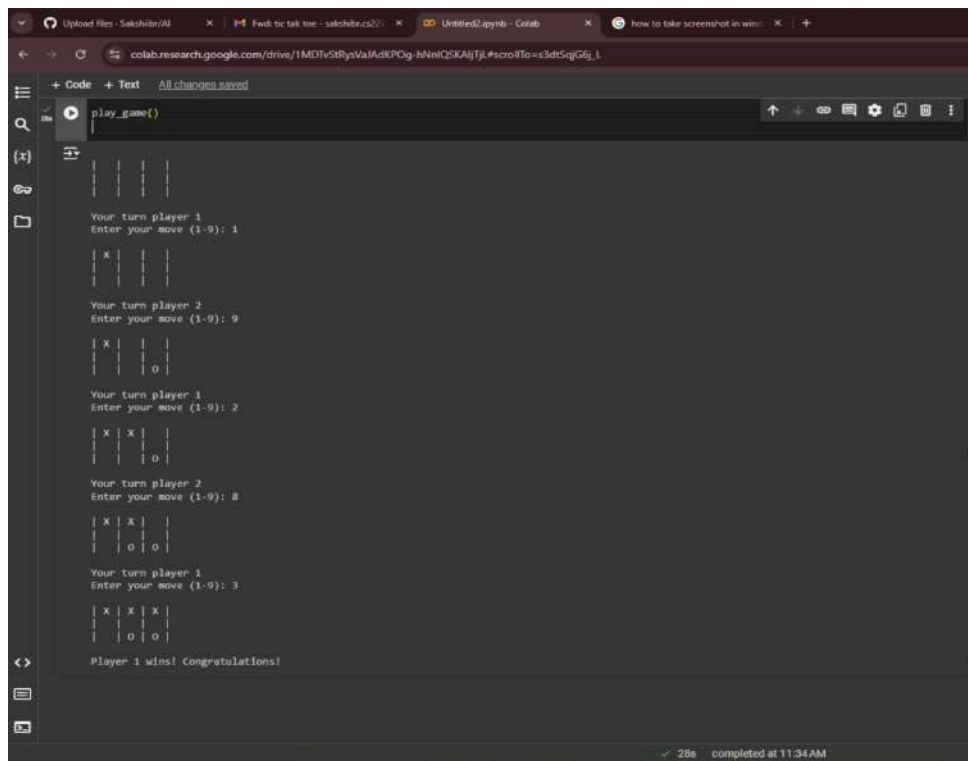
# Function to play the game
def play_game():
    draw_board()
    while True:
        player_move('X')
        draw_board()
        if is_victory('X'):
            print("Player 1 wins! Congratulations!")
            break
        elif is_draw():
            print("It's a draw!")
            break

        player_move('O')
        draw_board()
        if is_victory('O'):
            print("Player 2 wins! Congratulations!")
            break
        elif is_draw():
            print("It's a draw!")
            break

# Start the game
play_game()

```

Output:



```
colab.research.google.com/drive/1MDTv58RysVaIAxKPOg-hNniQSKAjTj#scrollTo=s3dt5qG6j_L

+ Code + Text All changes saved

play_game()

| | | |
| | | |
| | | |

Your turn player 1
Enter your move (1-9): 1

| X | | |
| | | |
| | | |

Your turn player 2
Enter your move (1-9): 9

| X | | |
| | | |
| | O | |

Your turn player 1
Enter your move (1-9): 2

| X | X | |
| | | |
| | O | |

Your turn player 2
Enter your move (1-9): 8

| X | X | |
| | | |
| | O | O |

Your turn player 1
Enter your move (1-9): 3

| X | X | X |
| | | |
| | O | O |

Player 1 wins! Congratulations!

✓ 28s completed at 11:34 AM
```

```
| | | |
| | | |
| | | |

Your turn player 1
Enter your move (1-9): 1

| X | | |
| | | |
| | | |

Your turn player 2
Enter your move (1-9): 9

| X | | |
| | | |
| | O | |

Your turn player 1
Enter your move (1-9): 3

| X | | X |
| | | |
| | O | |

Your turn player 2
Enter your move (1-9): 2

| X | O | X |
| | | |
| | O | |

Your turn player 1
Enter your move (1-9): 7

| X | O | X |
| | | |
| X | | O |

Your turn player 2
Enter your move (1-9): 4

| X | O | X |
| O | | |
| X | | O |

Your turn player 1
Enter your move (1-9): 6

| X | O | X |
| O | | X |
| X | | O |

Your turn player 2
Enter your move (1-9): 5

| X | O | X |
| O | O | X |
| X | | O |

Your turn player 1
Enter your move (1-9): 8

| X | O | X |
| O | O | X |
| X | X | O |

It's a draw!
```

## 1.2 Implement vacuum cleaner agent

```
# Reflex function for vacuum cleaner
def reflex(loc, status, cost):
    s = status # Track the current status of the location
    if status == 1: # If the location is dirty
        cost += 1
        print(f'SUCK at {loc}')
        s = 0 # The location is now clean
    if loc == "A":
        print("Move RIGHT to B")
        loc = "B" # Move to B
    elif loc == "B":
        print("Move LEFT to A")
        loc = "A" # Move to A
    return cost, loc, s # Return updated cost, location, and status

# Function to check goal state
def goal(a_status, b_status):
    if a_status == 0 and b_status == 0:
        print("Goal reached")
    else:
        print("Goal not reached")

# Input for the starting location and statuses
loc = input("Enter the starting location of the vacuum (A or B): ").strip()
cost = 0
a_status = int(input("Enter the status of location A (0 for clean, 1 for dirty): "))
b_status = int(input("Enter the status of location B (0 for clean, 1 for dirty): "))

# Simulate cleaning process
if loc == "A":
    cost, loc, a_status = reflex("A", a_status, cost)
    cost, loc, b_status = reflex("B", b_status, cost)
elif loc == "B":
    cost, loc, b_status = reflex("B", b_status, cost)
    cost, loc, a_status = reflex("A", a_status, cost)

# Output the total cost and goal status
print(f'Total cost: {cost}')
goal(a_status, b_status)
```

### Output:

---

```
Enter the starting location of the vacuum (A or B): A
Enter the status of location A (0 for clean, 1 for dirty): 0
Enter the status of location B (0 for clean, 1 for dirty): 0
Move RIGHT to B
Move LEFT to A
Total cost: 0
Goal reached
```

---

```
Enter the starting location of the vacuum (A or B): B
Enter the status of location A (0 for clean, 1 for dirty): 1
Enter the status of location B (0 for clean, 1 for dirty): 1
SUCK at A
Move RIGHT to B
SUCK at B
Move LEFT to A
Total cost: 2
Goal reached
```

```
Enter the starting location of the vacuum (A or B): A
Enter the status of location A (0 for clean, 1 for dirty): 1
Enter the status of location B (0 for clean, 1 for dirty): 0
SUCK at A
Move RIGHT to B
Move LEFT to A
Total cost: 1
Goal reached
```

```
Enter the starting location of the vacuum (A or B): A
Enter the status of location A (0 for clean, 1 for dirty): 0
Enter the status of location B (0 for clean, 1 for dirty): 1
Move RIGHT to B
SUCK at B
Move LEFT to A
Total cost: 1
Goal reached
```

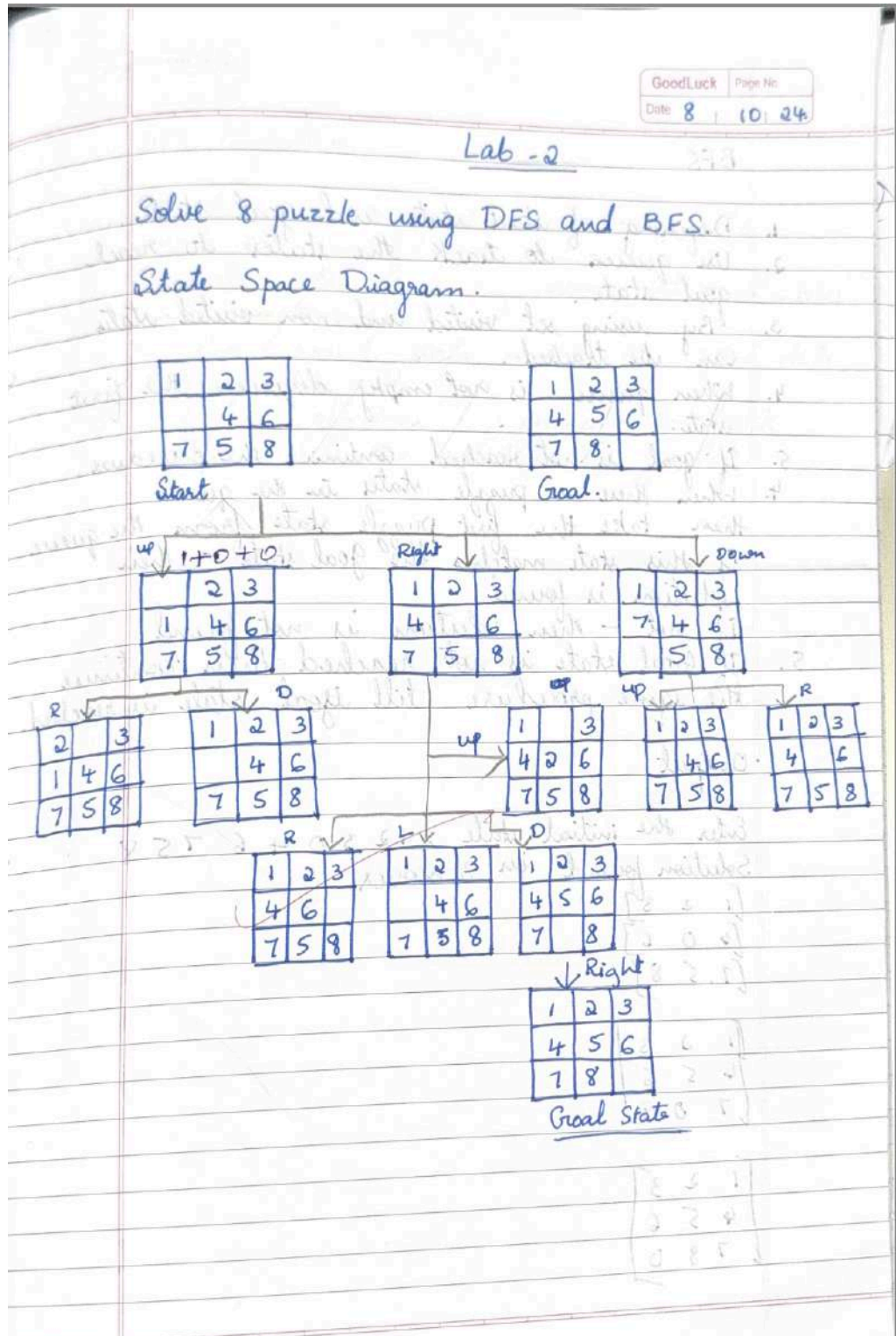


## Program 2

Implement 8 puzzle problems using Depth First Search (DFS)

Implement Iterative deepening search algorithm

### Algorithm:



## BFS

1. Defining of start state and goal state.
2. Use queue to track the states to reach goal state.
3. By using set visited and non visited states can be tracked.
4. When queue is not empty dequeue the first state.
5. If goal is not reached continue the procedure.
4. When there are puzzle states in the queue then take the first puzzle state from the queue. If this state matches the goal state - then solution is found. If not - then solution is not found.
5. If goal state is not reached then continue the same procedure till goal state is reached.

## Output

Enter the initial state : 1 2 3 0 4 6 7 5 8

Solution found in 3 moves

[1 2 3]

[4 0 6]

[7 5 8]

[1 3 3]

[4 5 6]

[7 0 8]

[1 2 3]  
[4 5 6]  
[7 8 0]

## DFS Algorithm.

1. Set the goal configuration of the puzzle
2. Locate the empty space
3. Generate valid state by moving adjacent tiles into empty space
4. If the current state matches the goal state return the path
5. If no solution is found - backtrack. Continue till the solution is found.

Initial State

2	3	1
4		3
2	2	5

Goal State

3	2	5
4	2	1
2		5

Goal State



Assignment 1

Lab Program: 5

Implement Iterative Deepening search algorithm.

function ITERATIVE-DEEPENING-SEARCH(problem)

returns a solution, or failure

for depth = 0 to  $\infty$  do

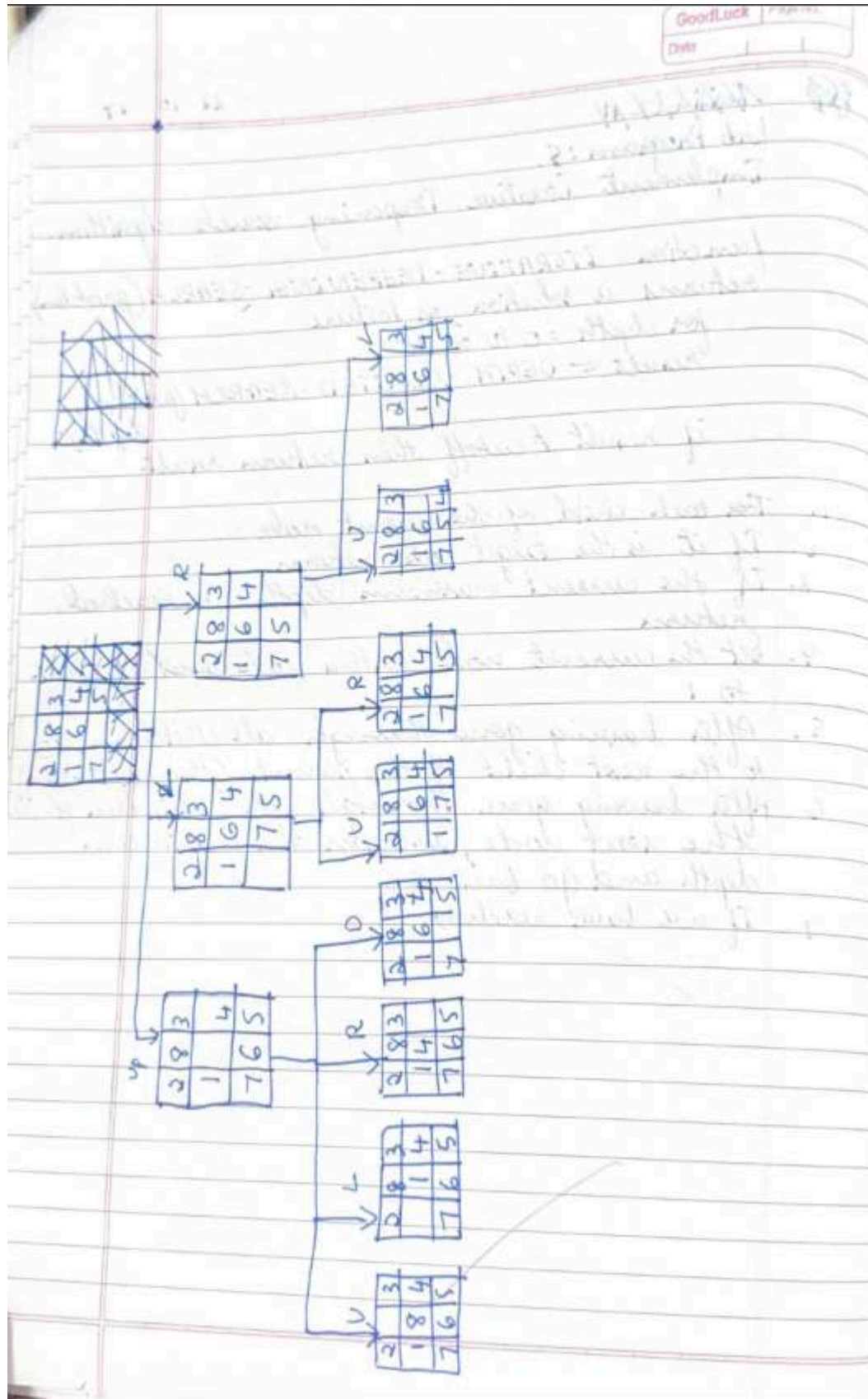
result  $\leftarrow$  DEPTH-LIMITED-SEARCH(problem, depth)

if result  $\neq$  cutoff then return result.

1. For each child of the current node
2. If it is the target node, return
3. If the current maximum depth is reached, return
4. Set the current node to this node and go back to 1
5. After having gone through all children, go to the next child of the parent (the next sibling)
6. After having gone through all children of the start node, increase the maximum depth and go back to 1
7. If we have reached







## Code:

### 2.1 Implement 8 puzzle problems using Depth First Search (DFS):

```
from collections import deque

# Goal state for the 8-puzzle
goal_state = [[1, 2, 3],
              [4, 5, 6],
              [7, 8, 0]]

# Possible moves
moves = {'up': (-1, 0), 'down': (1, 0), 'left': (0, -1), 'right': (0, 1)}

# Function to find the position of the blank (0)
def find_blank(state):
    for i in range(len(state)):
        for j in range(len(state[i])):
            if state[i][j] == 0:
                return i, j

# Function to check if a state is the goal state
def is_goal(state):
    return state == goal_state

# Function to generate neighbors by moving the blank tile
def get_neighbors(state):
    neighbors = []
    blank_row, blank_col = find_blank(state)
    for move, (dr, dc) in moves.items():
        new_row, new_col = blank_row + dr, blank_col + dc
        if 0 <= new_row < 3 and 0 <= new_col < 3:
            # Create a new state by swapping tiles
            new_state = [row[:] for row in state]
            new_state[blank_row][blank_col], new_state[new_row][new_col] =
new_state[new_row][new_col], new_state[blank_row][blank_col]
            neighbors.append((new_state, move))
    return neighbors

# Function to print the puzzle state
def print_puzzle(state):
    for row in state:
        print(row)
    print()

# BFS algorithm to solve the puzzle
def bfs(start_state):
```

```

queue = deque([(start_state, [])]) # Queue stores (current state, path to reach it)
visited = set() # To avoid revisiting states
visited.add(tuple(tuple(row) for row in start_state)) # Convert state to a tuple for
hashing

```

```

while queue:
    current_state, path = queue.popleft()

    # Check if the goal is reached
    if is_goal(current_state):
        return current_state, path

    # Explore neighbors
    for neighbor, move in get_neighbors(current_state):
        state_tuple = tuple(tuple(row) for row in neighbor)
        if state_tuple not in visited:
            visited.add(state_tuple)
            queue.append((neighbor, path + [move]))

```

```

return None, None

```

```

# Function to get user input for the initial state

```

```

def get_user_input():
    print("Enter the initial state of the 8-puzzle (row by row):")
    state = []
    for i in range(3):
        while True:
            try:
                row = list(map(int, input(f"Enter row {i+1} (3 integers, space-separated):").split()))
                if len(row) != 3 or any(x not in range(9) for x in row):
                    raise ValueError
                state.append(row)
                break
            except ValueError:
                print("Invalid input. Please enter 3 integers between 0 and 8.")
    return state

```

```

# Function to demonstrate the solution step by step

```

```

def demonstrate_solution(start_state, solution_path):
    current_state = start_state
    print("Initial state:")
    print_puzzle(current_state)
    for move in solution_path:
        print(f'Move: {move}')
        for neighbor, move_name in get_neighbors(current_state):
            if move_name == move:

```

```

        current_state = neighbor
        print_puzzle(current_state)
        break

# Main function
if __name__ == "__main__":
    start_state = get_user_input()
    final_state, solution_path = bfs(start_state)
    if solution_path:
        print("Solution found. Steps are demonstrated below:")
        demonstrate_solution(start_state, solution_path)
    else:
        print("No solution found.")

```

## Output:

```

Enter the initial state of the 8-puzzle (row by row):
Enter row 1 (3 integers, space-separated): 1 2 3
Enter row 2 (3 integers, space-separated): 0 4 6
Enter row 3 (3 integers, space-separated): 7 5 8
Solution found. Steps are demonstrated below:
Initial state:
[1, 2, 3]
[0, 4, 6]
[7, 5, 8]

Move: right
[1, 2, 3]
[4, 0, 6]
[7, 5, 8]

Move: down
[1, 2, 3]
[4, 5, 6]
[7, 0, 8]

Move: right
[1, 2, 3]
[4, 5, 6]
[7, 8, 0]

```

---

```

Enter the initial state of the 8-puzzle (row by row):
Enter row 1 (3 integers, space-separated): 1 3 2
Enter row 2 (3 integers, space-separated): 4 6 0
Enter row 3 (3 integers, space-separated): 7 5 8
No solution found.

```

---



## 2.2 Implement Iterative deepening search algorithm:

```
from copy import deepcopy

# Directions for moving the blank space (0): up, down, left, right
DIRECTIONS = [(-1, 0), (1, 0), (0, -1), (0, 1)]

class PuzzleState:
    def __init__(self, board, parent=None, move=""):
        self.board = board
        self.parent = parent
        self.move = move

    # Find the position of the blank (0)
    def get_blank_position(self):
        for i in range(3):
            for j in range(3):
                if self.board[i][j] == 0:
                    return i, j

    # Generate successor states by moving the blank space
    def generate_successors(self):
        successors = []
        x, y = self.get_blank_position()
        for dx, dy in DIRECTIONS:
            new_x, new_y = x + dx, y + dy
            if 0 <= new_x < 3 and 0 <= new_y < 3:
                new_board = deepcopy(self.board)
                new_board[x][y], new_board[new_x][new_y] = new_board[new_x][new_y],
new_board[x][y]
                successors.append(PuzzleState(new_board, parent=self))
        return successors

    # Check if the current state matches the goal state
    def is_goal(self, goal_state):
        return self.board == goal_state

    # String representation of the puzzle state
    def __str__(self):
        return "\n".join([" ".join(map(str, row)) for row in self.board])

# Depth-limited search (DLS)
def depth_limited_search(current_state, goal_state, depth):
    if depth == 0 and current_state.is_goal(goal_state):
        return current_state
    if depth > 0:
```

```

        for successor in current_state.generate_successors():
            found = depth_limited_search(successor, goal_state, depth - 1)
            if found:
                return found
    return None

# Iterative deepening search (IDS)
def iterative_deepening_search(start_state, goal_state):
    depth = 0
    while True:
        print(f"\nSearching at depth level: {depth}")
        result = depth_limited_search(start_state, goal_state, depth)
        if result:
            return result
        depth += 1

# Get user input for start and goal states
def get_user_input():
    print("Enter the start state (use 0 for the blank):")
    start_state = []
    for _ in range(3):
        row = list(map(int, input().split()))
        start_state.append(row)
    print("Enter the goal state (use 0 for the blank):")
    goal_state = []
    for _ in range(3):
        row = list(map(int, input().split()))
        goal_state.append(row)
    return start_state, goal_state

# Main function
def main():
    start_board, goal_board = get_user_input()
    start_state = PuzzleState(start_board)
    goal_state = goal_board
    result = iterative_deepening_search(start_state, goal_state)
    if result:
        print("\nGoal reached!")
        path = []
        while result:
            path.append(result)
            result = result.parent
        path.reverse()
        for state in path:
            print(state, "\n")
    else:
        print("Goal state not found.")

```

```
if __name__ == "__main__":  
    main()
```

### Output:

```
Enter the start state (use 0 for the blank):  
2 8 3  
1 6 4  
7 0 5  
Enter the goal state (use 0 for the blank):  
1 2 3  
8 0 4  
7 6 5  
  
Searching at depth level: 0  
  
Searching at depth level: 1  
  
Searching at depth level: 2  
  
Searching at depth level: 3  
  
Searching at depth level: 4  
  
Searching at depth level: 5  
  
Goal reached!  
2 8 3  
1 6 4  
7 0 5  
  
2 8 3  
1 0 4  
7 6 5  
  
2 0 3  
1 8 4  
7 6 5  
  
0 2 3  
1 8 4  
7 6 5  
  
1 2 3  
0 8 4  
7 6 5  
  
1 2 3  
8 0 4  
7 6 5
```

### Program 3

Implement A\* search algorithm

**Algorithm:**

Good Luck  
Date 15/10/24

lab - 3

For 8 puzzle problem using A\* implementation to calculate  $f(n)$  using

a)  $g(n)$  = depth of a node  
 $h(n)$  = heuristic value  $\Rightarrow$  no of misplaced tiles.  
 $f(n) = g(n) + h(n)$

b)  $g(n)$  = depth  
 $h(n)$  = heuristic value  $\Rightarrow$  manhattan distance  
 $f(n) = g(n) + h(n)$ .

Draw the state space diagram for

2	8	3
1	6	4
7		5

1	2	3
8		4
7	6	5

Initial state                      Goal state.



a)

2	8	3
1	6	4
7		5

$g=0$   
 $h=4$

1	2	3
8		4
7	6	5

Goal state

2	8	3
1	6	4
7	5	

$g(n)=1$   
 $h(n)=5$   
 $f(n)=6$

2	8	3
	1	4
7	6	5

$g(n)=1$   
 $h(n)=3$   
 $f(n)=4$

2	8	3
	1	6
7		5

$g(n)=1$   
 $h(n)=5$   
 $f(n)=6$

2	8	3
1	4	
7	6	5

$g=2$   
 $h=4$   
 $f=6$

2	8	3
	1	4
7	6	5

$g=2$   
 $h=3$   
 $f=5$

2	8	3
1	8	4
7	6	5

$g=2$   
 $h=3$   
 $f=5$

2	8	3
1	6	4
7		5

$g=2$   
 $h=4$   
 $f=6$

8	3	
2	1	4
7	6	5

$g=3$   
 $h=3$   
 $f=6$

2	8	3
	7	1
	4	6

$g=3$   
 $h=4$   
 $f=7$

2	8	3
	1	4
7	6	5

$g=3$   
 $h=3$   
 $f=6$

2	3	
1	8	4
7	6	5

$g=3$   
 $h=2$   
 $f=5$

2	3	
1	8	4
7	6	5

$g=3$   
 $h=4$   
 $f=7$

2	8	3
1	4	
7	6	5

$g=3$   
 $h=4$   
 $f=7$

1	2	3
	8	4
7	6	5

$g=4$   
 $h=1$

2		3
1	8	4
7	6	5

$g=4$   
 $h=3$

1	2	3
8		4
7	6	5

$g=5$   
 $h=0$   
 $f=5$

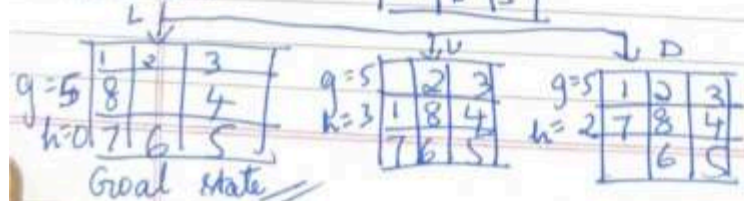
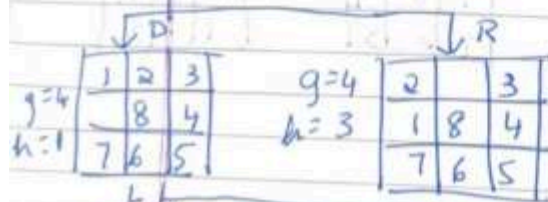
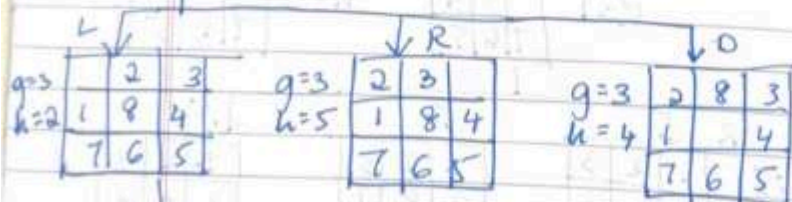
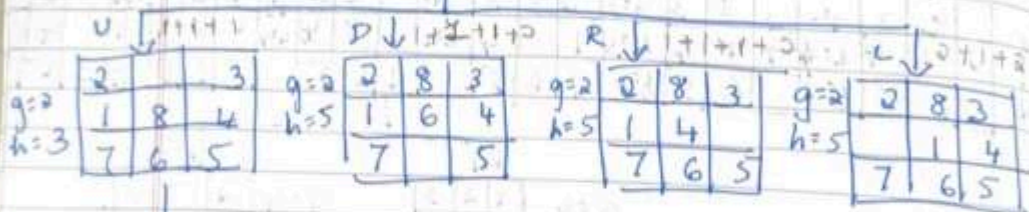
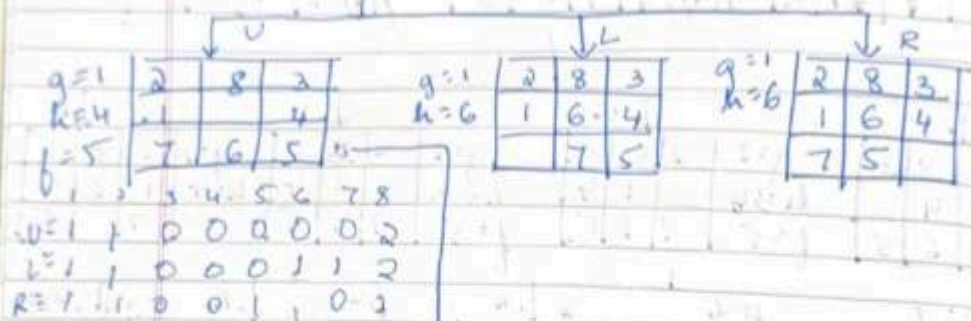
1	2	3
7	8	4
7	6	5

Goal state

2	3	
1	8	4
7	6	5

1	2	3
8		4
7	6	5

Grand state



Algorithm for heuristic:

1. Initialize open list and closed list.  
open list - States to be explored.  
closed list - States that are already explored.
2. Define function that is  $g(n)$ ,  $h(n)$ ,  $f$  and  $f(n)$  where  $h(n)$  is no misplaced tiles.
3. Initialize open list with start state.  
Start  $g(n) = 0$ .
4. Select  $f(n)$  which is least and continue with the procedure.  $\rightarrow$  Where  $f(n) = g(n) + h(n)$
5. If goal is reached then stop the procedure.

Algorithm for Manhattan

1. Initialize open list and closed list  
where open list is states that are to be explored and closed list is states that are already explored.
2. Define functions where  
 $g(n)$  is depth of node  
 $h(n)$  is number of moves and  $f(n)$
3. Initialize open list with start state  
Start  $g(n) = 0$ .
4. Select  $f(n)$  which has lowest value and continue with the procedure  
where  $f(n) = g(n) + h(n)$
5. If the goal is reached then stop the procedure

$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$   
 $\begin{bmatrix} 2 & 3 & 4 \\ 1 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$



(\*)/10 0/0

Initial state

$$\begin{bmatrix} 2 & 8 & 3 \\ 1 & 6 & 4 \\ 7 & 0 & 5 \end{bmatrix}$$

Goal state

$$\begin{bmatrix} 1 & 2 & 3 \\ 8 & 0 & 4 \\ 7 & 6 & 5 \end{bmatrix}$$

Sol found with cost: 5

Steps

$$\begin{bmatrix} 2 & 8 & 3 \\ 1 & 6 & 4 \\ 7 & 0 & 5 \end{bmatrix}$$

$$\begin{bmatrix} 2 & 8 & 3 \\ 1 & 0 & 4 \\ 7 & 6 & 5 \end{bmatrix}$$

$$\begin{bmatrix} 2 & 0 & 3 \\ 1 & 8 & 4 \\ 7 & 6 & 5 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 0 & 8 & 4 \\ 7 & 6 & 5 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 8 & 0 & 4 \\ 7 & 6 & 5 \end{bmatrix}$$

  
 P. K.

## Code:

### Heuristic

```
import heapq

# Define the goal state as a tuple of tuples
GOAL_STATE = ((1, 2, 3),
              (8, 0, 4),
              (7, 6, 5))

# Heuristic: Count the number of misplaced tiles
def misplaced_tile(state):
    misplaced = 0
    for i in range(3):
        for j in range(3):
            if state[i][j] != 0 and state[i][j] != GOAL_STATE[i][j]:
                misplaced += 1
    return misplaced

# Find the position of the blank tile (0)
def find_blank(state):
    for i in range(3):
        for j in range(3):
            if state[i][j] == 0:
                return i, j

# Generate neighbors by moving the blank tile
def generate_neighbors(state):
    neighbors = []
    x, y = find_blank(state)
    directions = [(0, 1), (0, -1), (1, 0), (-1, 0)] # Right, Left, Down, Up
    for dx, dy in directions:
        nx, ny = x + dx, y + dy
        if 0 <= nx < 3 and 0 <= ny < 3:
            # Create a new state by swapping tiles
            new_state = [list(row) for row in state]
            new_state[x][y], new_state[nx][ny] = new_state[nx][ny], new_state[x][y]
            neighbors.append(tuple(tuple(row) for row in new_state))
    return neighbors

# Reconstruct the path from the start state to the goal state
def reconstruct_path(came_from, current):
    path = [current]
    while current in came_from:
        current = came_from[current]
    path.append(current)
```

```

    path.reverse()
    return path

# A* search algorithm
def a_star(start):
    open_list = []
    heapq.heappush(open_list, (0 + misplaced_tile(start), 0, start)) # (f(n), g(n), state)
    g_score = {start: 0} # Cost from start to the current state
    came_from = {}
    visited = set()

    while open_list:
        _, g, current = heapq.heappop(open_list)

        # Check if we have reached the goal
        if current == GOAL_STATE:
            path = reconstruct_path(came_from, current)
            return path, g

        visited.add(current)

        # Explore neighbors
        for neighbor in generate_neighbors(current):
            if neighbor in visited:
                continue

            tentative_g = g_score[current] + 1 # Each move has a cost of 1

            # If this path is better, update scores and add to the queue
            if tentative_g < g_score.get(neighbor, float('inf')):
                came_from[neighbor] = current
                g_score[neighbor] = tentative_g
                f_score = tentative_g + misplaced_tile(neighbor) # f(n) = g(n) + h(n)
                heapq.heappush(open_list, (f_score, tentative_g, neighbor))

    return None, None # No solution found

# Print a given puzzle state
def print_state(state):
    for row in state:
        print(row)
    print()

# Main function
if __name__ == "__main__":
    start_state = ((2, 8, 3),
                   (1, 6, 4),

```

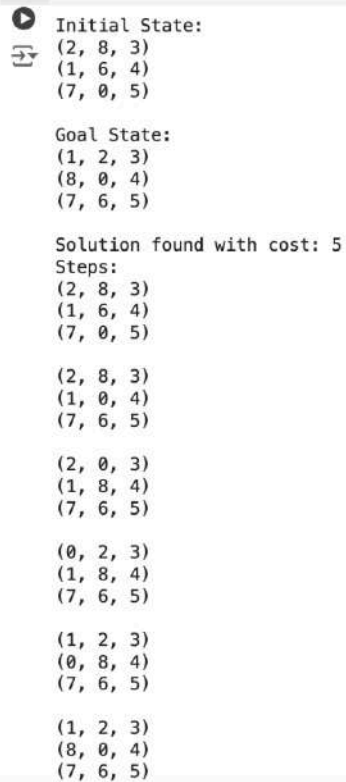


(7, 0, 5))

```
print("Initial State:")
print_state(start_state)
print("Goal State:")
print_state(GOAL_STATE)

solution, cost = a_star(start_state)
if solution:
    print(f"Solution found with cost: {cost}")
    print("Steps:")
    for step in solution:
        print_state(step)
else:
    print("No solution found.")
```

### Output:



```
Initial State:
(2, 8, 3)
(1, 6, 4)
(7, 0, 5)

Goal State:
(1, 2, 3)
(8, 0, 4)
(7, 6, 5)

Solution found with cost: 5
Steps:
(2, 8, 3)
(1, 6, 4)
(7, 0, 5)

(2, 8, 3)
(1, 0, 4)
(7, 6, 5)

(2, 0, 3)
(1, 8, 4)
(7, 6, 5)

(0, 2, 3)
(1, 8, 4)
(7, 6, 5)

(1, 2, 3)
(0, 8, 4)
(7, 6, 5)

(1, 2, 3)
(8, 0, 4)
(7, 6, 5)
```

## Manhattan:

```
import heapq

# Define the goal state as a tuple of tuples
GOAL_STATE = ((1, 2, 3),
              (8, 0, 4),
              (7, 6, 5))

# Heuristic: Calculate the Manhattan distance for each tile
def manhattan_distance(state):
    distance = 0
    for i in range(3):
        for j in range(3):
            value = state[i][j]
            if value != 0:
                goal_x, goal_y = divmod(value - 1, 3) # Find the goal position of the current tile
                distance += abs(goal_x - i) + abs(goal_y - j)
    return distance

# Find the position of the blank tile (0)
def find_blank(state):
    for i in range(3):
        for j in range(3):
            if state[i][j] == 0:
                return i, j

# Generate neighbors by moving the blank tile
def generate_neighbors(state):
    neighbors = []
    x, y = find_blank(state)
    directions = [(0, 1), (0, -1), (1, 0), (-1, 0)] # Right, Left, Down, Up
    for dx, dy in directions:
        nx, ny = x + dx, y + dy
        if 0 <= nx < 3 and 0 <= ny < 3:
            # Create a new state by swapping tiles
            new_state = [list(row) for row in state]
            new_state[x][y], new_state[nx][ny] = new_state[nx][ny], new_state[x][y]
            neighbors.append(tuple(tuple(row) for row in new_state))
    return neighbors

# Reconstruct the path from the start state to the goal state
def reconstruct_path(came_from, current):
    path = [current]
    while current in came_from:
        current = came_from[current]
    path.append(current)
```

```

    path.reverse()
    return path

# A* search algorithm
def a_star(start):
    open_list = []
    heapq.heappush(open_list, (manhattan_distance(start), 0, start)) # (f(n), g(n), state)
    g_score = {start: 0} # Cost from start to the current state
    came_from = {}
    visited = set()

    while open_list:
        f, g, current = heapq.heappop(open_list)

        # Check if we have reached the goal
        if current == GOAL_STATE:
            path = reconstruct_path(came_from, current)
            return path, g

        visited.add(current)

        # Explore neighbors
        for neighbor in generate_neighbors(current):
            if neighbor in visited:
                continue

            tentative_g = g_score[current] + 1 # Each move has a cost of 1

            # If this path is better, update scores and add to the queue
            if tentative_g < g_score.get(neighbor, float('inf')):
                came_from[neighbor] = current
                g_score[neighbor] = tentative_g
                f_score = tentative_g + manhattan_distance(neighbor) # f(n) = g(n) + h(n)
                heapq.heappush(open_list, (f_score, tentative_g, neighbor))

    return None, None # No solution found

# Print a given puzzle state
def print_state(state):
    for row in state:
        print(row)
    print()

# Main function
if __name__ == "__main__":
    start_state = ((2, 8, 3),
                   (1, 6, 4),

```

(7, 0, 5))

```
print("Initial State:")
print_state(start_state)
print("Goal State:")
print_state(GOAL_STATE)

solution, cost = a_star(start_state)
if solution:
    print(f'Solution found with cost: {cost}')
    print("Steps:")
    for step in solution:
        print_state(step)
else:
    print("No solution found.")
```

### Output:

```
Initial State:
(2, 8, 3)
(1, 6, 4)
(7, 0, 5)

Goal State:
(1, 2, 3)
(8, 0, 4)
(7, 6, 5)

Solution found with cost: 5
Steps:
(2, 8, 3)
(1, 6, 4)
(7, 0, 5)

(2, 8, 3)
(1, 0, 4)
(7, 6, 5)

(2, 0, 3)
(1, 8, 4)
(7, 6, 5)

(0, 2, 3)
(1, 8, 4)
(7, 6, 5)

(1, 2, 3)
(0, 8, 4)
(7, 6, 5)

(1, 2, 3)
(8, 0, 4)
(7, 6, 5)
```

## Program 4

Implement Hill Climbing search algorithm to solve N-Queens problem

### Algorithm:

Lab - 5

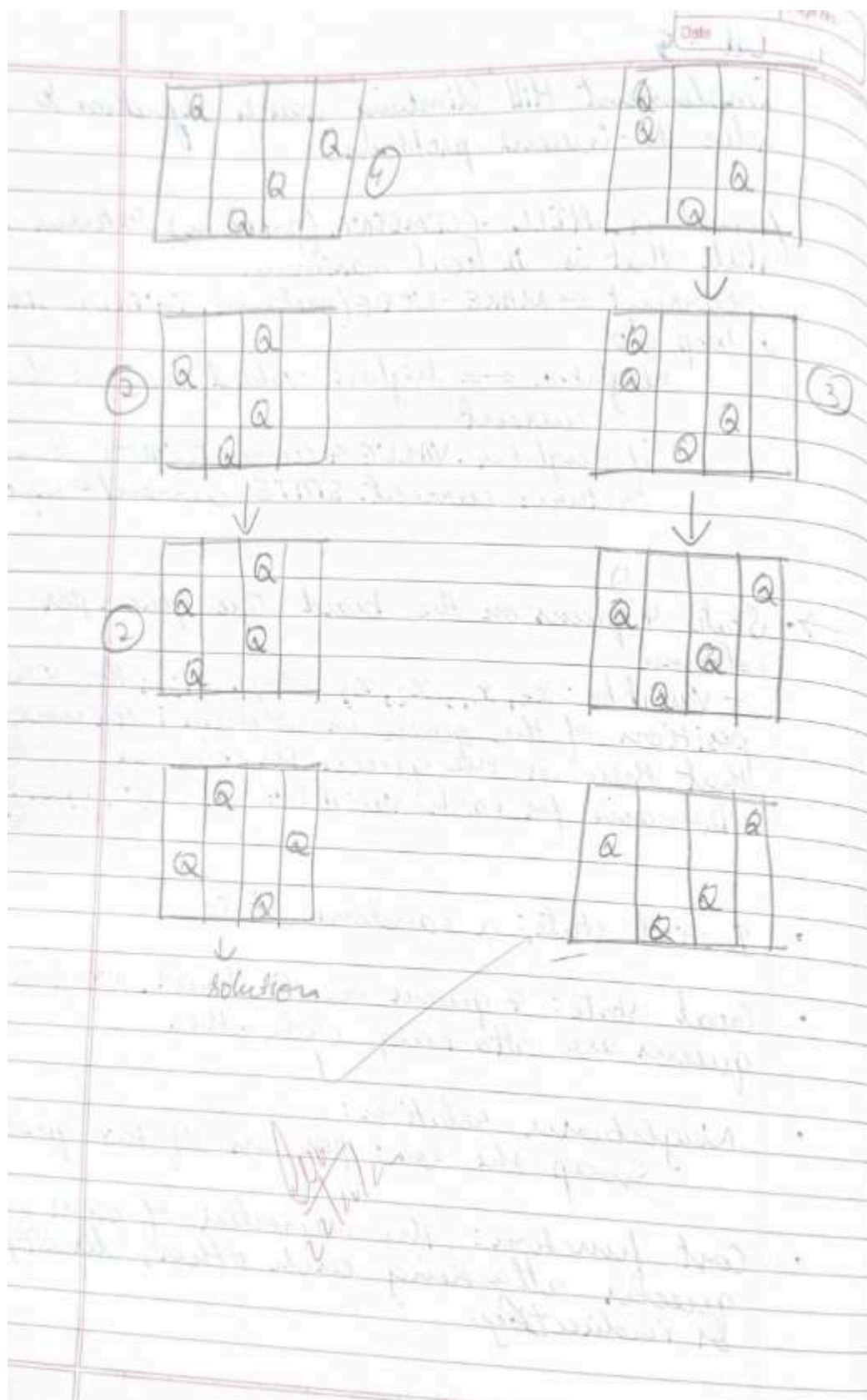
Implement Hill Climbing search algorithm to solve N-Queens problem

function HILL-CLIMBING(problem) returns a state that is a local maximum  
    current  $\leftarrow$  MAKE-NODE(problem, INITIAL-STATE)  
    loop do  
        neighbor  $\leftarrow$  a highest-valued successor of current  
        if neighbor.VALUE  $\leq$  current.VALUE then  
            returns current.STATE  
        current  $\leftarrow$  neighbor

→ State: 4 queens on the board. One queen per column

- Variables:  $x_0, x_1, x_2, x_3$  where  $x_i$  is the row position of the queen in column  $i$ . Assume that there is one queen per column
- Domain for each variable:  $x_i \in \{0, 1, 2, 3\}, \forall i$ .

- Initial state: a random state
- Goal state: 4 queens on the board. No pair of queens are attacking each other
- Neighbors relation:  
    Swap the row positions of two queens
- Cost function: The number of pairs of queens attacking each other, directly or indirectly.





**Code:**

```
import random

def get_attacking_pairs(state):
    """Calculates the number of attacking pairs of queens."""
    attacks = 0
    n = len(state)
    for i in range(n):
        for j in range(i + 1, n):
            # Check if queens are in the same column or diagonals
            if state[i] == state[j] or abs(state[i] - state[j]) == abs(i - j):
                attacks += 1
    return attacks

def generate_successors(state):
    """Generates all possible successors by moving each queen to every other column in
    its row."""
    n = len(state)
    successors = []
    for row in range(n):
        for col in range(n):
            if col != state[row]: # Only generate new states with different columns
                new_state = state[:]
                new_state[row] = col
                successors.append(new_state)
    return successors

def hill_climbing(n):
    """Hill climbing algorithm for N-Queens problem."""
    # Start with a random state
    current = [random.randint(0, n - 1) for _ in range(n)]
    steps = 0

    while True:
        current_attacks = get_attacking_pairs(current)
        successors = generate_successors(current)

        # Find the neighbor with the minimum attacks
        neighbor = min(successors, key=get_attacking_pairs)
        neighbor_attacks = get_attacking_pairs(neighbor)
        steps += 1

        print(f'Step {steps}: Current State: {current}, Attacks: {current_attacks}')

        # If no better neighbor is found, return the current state
        if neighbor_attacks >= current_attacks:
```

```

        return current, current_attacks

    # Move to the better neighbor
    current = neighbor

def print_board(state):
    """Prints the board with queens placed."""
    n = len(state)
    board = [["." for _ in range(n)] for _ in range(n)]
    for row in range(n):
        board[row][state[row]] = "Q"
    for row in board:
        print(" ".join(row))
    print("\n")

# Set the size of the board
n = 8 # Change this value to test with different board sizes

solution, attacks = hill_climbing(n)
print("Final State (Solution):", solution)
print("Number of Attacking Pairs:", attacks)
print_board(solution)

```

### Output:

```

Step 1: Current State: [0, 0, 0, 2], Attacks: 4, Cost: 4
Step 2: Current State: [0, 3, 0, 2], Attacks: 1, Cost: 1
Step 3: Current State: [1, 3, 0, 2], Attacks: 0, Cost: 0
Final State (Solution): [1, 3, 0, 2]
Number of Attacking Pairs: 0
. Q . .
. . . Q
Q . . .
. . Q .

```

## Program 5

Simulated Annealing to Solve 8-Queens problem

### Algorithm:

Good Luck Page No. \_\_\_\_\_  
Date 29/10/24

Lab - 5

Write a program to implement Simulated Annealing Algorithm.

function SIMULATED-ANNEALING(problem, schedule) returns a solution state  
inputs: problem, a problem  
schedule, a mapping from time to "temperature"

```
current ← MAKE-NODE(problem, INITIAL-STATE)
for t = 1 to ∞ do
    T ← schedule(t)
    if T = 0 then return current
    next ← a randomly selected successor of current
    ΔE ← next.VALUE - current.VALUE
    if ΔE > 0 then current ← next
    else current ← next only with probability  $e^{-\Delta E/T}$ 
```

The Simulated Annealing Algorithm  
The alg can be decomposed in 4 simple steps

1. Start at a random point  $x$
2. Choose a new point  $x_j$  on a neighbourhood  $N(x)$
3. Decide whether or not to move to the new point  $x_j$ . The decision will be made based on the probability function  $P(x, x_j, T)$   
$$P(x, x_j, T) = \begin{cases} e^{-\frac{F(x_j) - F(x)}{T}} & \text{if } F(x_j) \geq F(x) \\ 1 & \text{if } F(x_j) < F(x) \end{cases}$$
4. Reduce  $T$

Output

8 queens

The best position found is [0 8 5 2 6 3 7 4]  
The no of queens that are not attacking each other is 0

MST

Edges in Minimum Spanning Tree

0--2 (weight=1)

2--3 (weight=3)

2--1 (weight=2)

Total weight

Sudoku using simulated annealing

1	5	3	4	6	7	8	1	9	2
6	7	2	1	9	5	8	3	4	
1	9	8	5	4	2	5	6	7	
8	5	9	7	6	1	4	8	3	

3

Due  
29/10/21

**Code:**

```
import numpy as np
from scipy.optimize import dual_annealing

def queens_max(position):
    # This function calculates the number of pairs of queens that are not attacking each other
    position = np.round(position).astype(int)
    n = len(position)
    queen_not_attacking = 0

    for i in range(n - 1):
        for j in range(i + 1, n):
            # Check if queens i and j are not attacking each other
            if position[i] != position[j] and abs(position[i] - position[j]) != (j - i):
                queen_not_attacking += 1

    return -queen_not_attacking # Return negative for maximization

# Bounds for each queen's position (0 to 7 for an 8x8 chessboard)
bounds = [(0, 7) for _ in range(8)]

# Use dual_annealing for simulated annealing optimization
result = dual_annealing(queens_max, bounds)

# Display the results
best_position = np.round(result.x).astype(int)
best_objective = -result.fun

print('The best position found is:', best_position)
print('The number of queens that are not attacking each other is:', best_objective)
```

**Output:**

```
➡ The best position found is: [3 5 7 2 0 6 4 1]
  The number of queens that are not attacking each other is: 28
```

**5.2 SUDOKU PROBLEM**

```
import numpy as np
import random
import math

def is_valid(puzzle, row, col, num):
    """Check if a number can be placed at a specific position."""
```

```

    if num in puzzle[row] or num in puzzle[:, col]:
        return False
    box_x, box_y = row // 3 * 3, col // 3 * 3
    if num in puzzle[box_x:box_x + 3, box_y:box_y + 3]:
        return False
    return True

def initial_fill(puzzle):
    """Fill the empty cells in the puzzle with valid random values."""
    filled = puzzle.copy()
    for row in range(9):
        for col in range(9):
            if filled[row][col] == 0:
                possible_values = [num for num in range(1, 10) if is_valid(filled, row, col, num)]
                if possible_values:
                    filled[row][col] = random.choice(possible_values)
    return filled

def objective(puzzle):
    """Calculate the number of conflicts in the Sudoku puzzle."""
    conflicts = 0
    # Row conflicts
    for row in range(9):
        conflicts += 9 - len(set(puzzle[row]))
    # Column conflicts
    for col in range(9):
        conflicts += 9 - len(set(puzzle[:, col]))
    # Box conflicts
    for box_x in range(0, 9, 3):
        for box_y in range(0, 9, 3):
            box = puzzle[box_x:box_x+3, box_y:box_y+3].flatten()
            conflicts += 9 - len(set(box))
    return conflicts

def simulated_annealing(puzzle, max_iter=100000, start_temp=1.0, end_temp=0.01, alpha=0.99):
    """Solve the Sudoku puzzle using simulated annealing."""
    current_state = initial_fill(puzzle)
    current_score = objective(current_state)
    temp = start_temp

    for iteration in range(max_iter):
        if current_score == 0: # Solution found
            break
        # Randomly pick an empty cell
        row, col = random.randint(0, 8), random.randint(0, 8)
        while puzzle[row][col] != 0:
            row, col = random.randint(0, 8), random.randint(0, 8)

```



```

# Create a new state with a random value in the chosen cell
new_state = current_state.copy()
new_value = random.randint(1, 9)
if is_valid(new_state, row, col, new_value):
    new_state[row][col] = new_value

new_score = objective(new_state)
delta_score = new_score - current_score

# Accept new state based on simulated annealing criteria
if delta_score < 0 or random.uniform(0, 1) < math.exp(-delta_score / temp):
    current_state, current_score = new_state, new_score

# Decrease temperature
temp *= alpha
if temp < end_temp:
    break

return current_state

# Example usage:
puzzle = np.array([
    [5, 3, 0, 0, 7, 0, 0, 0, 0],
    [6, 0, 0, 1, 9, 5, 0, 0, 0],
    [0, 9, 8, 0, 0, 0, 0, 6, 0],
    [8, 0, 0, 0, 6, 0, 0, 0, 3],
    [4, 0, 0, 8, 0, 3, 0, 0, 1],
    [7, 0, 0, 0, 2, 0, 0, 0, 6],
    [0, 6, 0, 0, 0, 0, 2, 8, 0],
    [0, 0, 0, 4, 1, 9, 0, 0, 5],
    [0, 0, 0, 0, 8, 0, 0, 7, 9]
])

solved_puzzle = simulated_annealing(puzzle)
print("Solved Sudoku:\n", solved_puzzle)

```

## Output:

```

Solved Sudoku:
[[5 3 4 2 7 6 9 1 0]
 [6 2 7 1 9 5 4 3 8]
 [1 9 8 3 4 0 5 6 2]
 [8 1 2 7 6 4 0 9 3]
 [4 0 9 8 5 3 7 2 1]
 [7 0 3 9 2 1 8 5 6]
 [3 6 5 0 0 7 2 8 4]
 [2 8 0 4 1 9 3 0 5]
 [0 4 1 5 8 2 6 7 9]]

```

---

### 5.3 MST (Minimum Spanning Tree)

```
import random
import math
from collections import defaultdict

class Graph:
    def __init__(self):
        self.edges = defaultdict(list)

    def add_edge(self, u, v, weight):
        """Add an edge to the graph."""
        self.edges[u].append((v, weight))
        self.edges[v].append((u, weight))

    def get_edges(self):
        """Get all edges of the graph."""
        return [(u, v, weight) for u in self.edges for v, weight in self.edges[u] if u < v]

def random_spanning_tree(graph):
    """Generate a random spanning tree using a randomized Prim's-like approach."""
    nodes = list(graph.edges.keys())
    random.shuffle(nodes)
    tree_edges = set()
    selected = {nodes[0]}
    while len(selected) < len(nodes):
        u = random.choice(list(selected))
        candidates = [(v, weight) for v, weight in graph.edges[u] if v not in selected]
        if candidates:
            v, weight = random.choice(candidates)
            tree_edges.add((u, v, weight))
            selected.add(v)
    return tree_edges

def energy(tree):
    """Calculate the total weight of the tree."""
    return sum(weight for u, v, weight in tree)

def generate_neighbor(tree, graph):
    """Generate a neighboring tree by removing and adding an edge."""
    tree_list = list(tree)
    if len(tree_list) < 2:
        return tree

    # Remove a random edge from the tree
    u, v, weight = random.choice(tree_list)
    new_tree = tree - {(u, v, weight)}
```

```

# Try to add a valid edge to keep the tree connected
nodes_in_tree = {x for edge in new_tree for x in edge[:2]}
candidates = [
    (u, v, w) for u in nodes_in_tree for v, w in graph.edges[u]
    if v not in nodes_in_tree and (u, v, w) not in tree and (v, u, w) not in tree
]

if candidates:
    u, v, weight = random.choice(candidates)
    new_tree.add((u, v, weight))

return new_tree

def simulated_annealing(graph):
    """Find a minimum spanning tree using simulated annealing."""
    T = 1.0
    final_temperature = 0.001
    cooling_factor = 0.95

    current_solution = random_spanning_tree(graph)
    best_solution = current_solution

    while T > final_temperature:
        for _ in range(100):
            neighbor = generate_neighbor(current_solution, graph)
            current_energy = energy(current_solution)
            neighbor_energy = energy(neighbor)

            # Accept neighbor if it's better or probabilistically
            if neighbor_energy < current_energy or random.random() < math.exp((current_energy -
neighbor_energy) / T):
                current_solution = neighbor

            # Update the best solution found
            if energy(current_solution) < energy(best_solution):
                best_solution = current_solution

        # Cool down
        T *= cooling_factor

    return best_solution

if __name__ == "__main__":
    random.seed(42)
    graph = Graph()
    edges = [(0, 1, 4), (0, 2, 1), (1, 2, 2), (1, 3, 5), (2, 3, 3)]

```

```
for u, v, weight in edges:
    graph.add_edge(u, v, weight)

mst = simulated_annealing(graph)
print("Edges in the Minimum Spanning Tree:")
for u, v, weight in mst:
    print(f"{u} -- {v} (weight: {weight})")
print("Total weight:", energy(mst))
```

### Output:

---

```
⇒ Edges in the Minimum Spanning Tree:
  2 -- 0 (weight: 1)
  2 -- 1 (weight: 2)
  Total weight: 3
```

---

## Program 6

Create a knowledge base using propositional logic and show that the given query entails the knowledge base or not.

### Algorithm:

Good Luck Page No.  
Date 12/11/24

Lab - 6

Program - 6

Implementation of Truth-Table enumeration algorithm for deciding propositional entailment i.e., create a knowledge base using propositional logic and show that the given query entails the knowledge base or not

Algorithm:

```
function T-T-Entails? (KB,  $\alpha$ ) returns True or false
    input: KB, the knowledge base, a sentence
           in propositional logic & the query, a
           sentence in propositional logic
    Symbols  $\leftarrow$  a list of propositional symbols
                  in KB and  $\alpha$ 
    return TT-CHECK-ALL (KB,  $\alpha$ , Symbols,  $\{ \}$ )

function TT-CHECK-ALL (KB,  $\alpha$ , Symbols, models)
    returns true or false
    if EMPTY? (Symbols) then
        if PL-TRUE? (KB, model) then return
            PL-TRUE? ( $\alpha$ , model)
        else return true // when KB is false,
            always return true
    else do
        P  $\leftarrow$  First (Symbols)
        rest  $\leftarrow$  REST (Symbols)
        return (TT-CHECK-ALL (KB,  $\alpha$ , rest, model)
             $\cup$  {P = true})
```

and  
 $\text{TT-CHECK-ALL}(KB, \alpha, \text{rest}, \text{mode } U, \text{fp} = \text{false})$

⇒ Propositional Inference Enumeration Method

$\alpha = A \vee B$        $KB = (A \vee C) \wedge (B \vee C)$

A	B	C	$A \vee C$	$B \vee C$	KB	$\alpha$
false	false	false	false	true	false	false
false	false	true	true	false	false	false
false	true	false	false	true	false	true
false	true	true	true	true	true	true
true	false	false	true	true	true	true
true	false	true	true	false	false	true
true	true	false	true	true	true	true
true	true	true	true	true	true	true

Combinations where both KB and  $\alpha(A \vee B)$  are true:

A	B	C
0	1	1
1	0	0
1	1	0
1	1	1



**Code:**

```
import itertools

def evaluate_formula(formula, valuation):
    """
    Evaluate the propositional formula under the given truth assignment (valuation).
    The formula is a string of logical operators like 'AND', 'OR', 'NOT', and can contain variables 'A',
    'B', 'C'.
    """
    # Create a local environment (dictionary) for variable assignments
    env = {var: valuation[i] for i, var in enumerate(['A', 'B', 'C'])}

    # Replace logical operators with Python equivalents
    formula = formula.replace('AND', 'and').replace('OR', 'or').replace('NOT', 'not')

    # Replace variables in the formula with their corresponding truth values
    for var in env:
        formula = formula.replace(var, str(env[var]))

    # Evaluate the formula and return the result (True or False)
    try:
        return eval(formula)
    except Exception as e:
        raise ValueError(f"Error in evaluating formula: {e}")

def truth_table(variables):
    """
    Generate all possible truth assignments for the given variables.
    """
    return list(itertools.product([False, True], repeat=len(variables)))

def entails(KB, alpha):
    """
    Decide if KB entails alpha using a truth-table enumeration algorithm.
    KB is a propositional formula (string), and alpha is another propositional formula (string).
    """
    # Generate all possible truth assignments for A, B, and C
    assignments = truth_table(['A', 'B', 'C'])
    print(f"{'A':<10} {'B':<10} {'C':<10} {'KB':<15} {'alpha':<15} {'KB entails alpha?'}") # Header for
the truth table
    print("-" * 70) # Separator for readability

    for assignment in assignments:
        # Evaluate KB and alpha under the current assignment
        KB_value = evaluate_formula(KB, assignment)
        alpha_value = evaluate_formula(alpha, assignment)
```

```

# Print the current truth assignment and the results for KB and alpha
print(f' {str(assignment[0]):<10} {str(assignment[1]):<10} {str(assignment[2]):<10}'
      f' {str(KB_value):<15} {str(alpha_value):<15} {'Yes' if KB_value and alpha_value else
'No'})

# If KB is true and alpha is false, then KB does not entail alpha
if KB_value and not alpha_value:
    return False

# If no counterexample was found, then KB entails alpha
return True

# Define the formulas for KB and alpha
alpha = 'A OR B'
KB = '(A OR C) AND (B OR NOT C)'

# Check if KB entails alpha
result = entails(KB, alpha)

# Print the final result of entailment
print(f'\nDoes KB entail alpha? {'Yes' if result else 'No'})

```

### Output:

A	B	C	KB	alpha	KB entails alpha?
False	False	False	False	False	No
False	False	True	False	False	No
False	True	False	False	True	No
False	True	True	True	True	Yes
True	False	False	True	True	Yes
True	False	True	False	True	No
True	True	False	True	True	Yes
True	True	True	True	True	Yes

Does KB entail alpha? True

## Program 7

Implement unification in first order logic

### Algorithm:

Good Luck Page No. \_\_\_\_\_  
Date 19/11/24

Lab - 7

Implement unification in first order logic

Algorithm: Unify ( $\psi_1, \psi_2$ )

Step 1: If  $\psi_1$  or  $\psi_2$  is a variable or constant, then:

- If  $\psi_1$  or  $\psi_2$  are identical, then return NIL
- Else if  $\psi_1$  is a variable,
  - Then if  $\psi_1$  occurs in  $\psi_2$ , then return FAILURE
  - Else return  $\{\psi_2/\psi_1\}$
- Else if  $\psi_2$  is a variable,
  - If  $\psi_2$  occurs in  $\psi_1$ , then return FAILURE,
  - Else return  $\{\psi_1/\psi_2\}$
- Else return FAILURE

Step 2: If the initial Predicate symbol in  $\psi_1$  and  $\psi_2$  are not same, then return FAILURE.

Step 3: If  $\psi_1$  and  $\psi_2$  have a different number of arguments, then return FAILURE

Step 4: Set Substitution set (SUBST) to NIL

Step 5: For  $i=1$  to the number of elements in  $\psi_1$ ,

- Call Unify function with the  $i^{\text{th}}$  element of  $\psi_1$  and  $i^{\text{th}}$  element of  $\psi_2$ , and put the result into S
- If S = failure then return Failure
- If S  $\neq$  NIL then do,
  - Apply S to the remainder of both  $L_1$  and  $L_2$
  - SUBST = APPEND(S, SUBST).

Step 6: Return SUBST

Eg:  $p(x, f(y)) \rightarrow \text{①}$   
 $p(a, f(g(h))) \rightarrow \text{②}$

① & ② are identical if x is replaced with a

$p(a, f(y)) \rightarrow p(a, f(g(h)))$   
 $p(a, f(g(h)))$

EX  $\rightarrow P(n, F(y)) \rightarrow \textcircled{1}$   
 $P(a, F(g(n))) \rightarrow \textcircled{2}$

$\textcircled{1}$  and  $\textcircled{2}$  are identical if  $x$  is replaced with  $a$  in  $\textcircled{1}$   $a/n$

$P(a, F(y)) \rightarrow \textcircled{1}$   
 if  $y$  is replaced with  $g(n)$   
 $P(a, F(g(n))) \rightarrow \textcircled{2}$

Now  $\textcircled{1}$  &  $\textcircled{2}$  are same, so they are unified

$\rightarrow$  Eg.  $Eats(x, Apple)$   
 $Eats(Riya, y)$

$x$  is replaced with Riya  
 $Riya/x$

$Eats(Riya, Apple)$

$y$  is replace with Apple

$Apple/y$   
 $Eat(Riya, Apple)$

$\rightarrow$  Eg.  $g(x, a), f(y)$   
 $Q(a, (n, a), f(y)) \rightarrow \textcircled{1}$   
 $Q(a, g(f(b), a), x) \rightarrow \textcircled{2}$

replace  $n$  with  $f(n) \rightarrow \textcircled{1}$

$Q(a, g(f(n), a), f(y))$

replace  $x$  with  $f(y) \rightarrow \textcircled{2}$   
 $x/f(y)$

$Q(a, g(f(n), a), f(y))$

Now both are same, they are unified

Lab-8

## Forward Reasoning Algorithm

$$Q \quad \psi_1 = P(f(a), g(y)) \\ \psi_0 = P(x, x)$$

1st one is fail

$$Q \quad \psi_1 = P(b, x, f(g(z))) \\ \psi_0 = P(z, f(y), f(y))$$

2nd one is pass

Iteration 1:

Attempting to unify :  $P(f(a), g(y))$   
&  $P(x, x)$   
current substitution : empty

Iteration 2:

Attempting to unify :  $f(a)$  &  $x$   
current substitution : empty  
Added substitution :  $x \rightarrow f(a)$

Attempting to unify :  $g(y)$  &  $x$   
current substitution :  $x \rightarrow f(a)$   
unification failed : Diff  
Predicates and argument length.



Output  
 Unifying  $P(b, x, f(g(z)))$  with  $P(z, f(y), f(y))$   
 Unifying  $b$  with  $z$   
 Substitution:  $b \rightarrow z$   
 Unifying  $f(g(z))$  with  $f(y)$   
 Substitution:  $f(g(z)) \rightarrow f(y)$

Final Result:  
 Unification successful  
 Substitution:  $b \rightarrow z, x \rightarrow f(y), f(g(z)) \rightarrow f(y)$

14.11.21



**Code:**

```
class UnificationError(Exception):
    """Custom exception for unification errors."""
    pass

def occurs_check(var, term, subst):
    """Check if `var` occurs in `term` (to prevent circular substitutions)."""
    if var == term:
        return True
    elif isinstance(term, (list, tuple)):
        return any(occurs_check(var, t, subst) for t in term)
    elif isinstance(term, str) and term in subst:
        return occurs_check(var, subst[term], subst)
    return False

def is_variable(term):
    """Check if `term` is a variable (starting with `?`)."""
    return isinstance(term, str) and term.startswith('?')

def unify(psi1, psi2, subst=None):
    """Attempt to unify two terms, `psi1` and `psi2`, under the given substitution."""
    if subst is None:
        subst = {}

    if psi1 == psi2:
        return subst
    elif is_variable(psi1):
        if psi1 in subst:
            return unify(subst[psi1], psi2, subst)
        elif occurs_check(psi1, psi2, subst):
            raise UnificationError(f"Occurs check failed: {psi1} in {psi2}")
        else:
            subst[psi1] = psi2
            return subst
    elif is_variable(psi2):
        if psi2 in subst:
            return unify(psi1, subst[psi2], subst)
        elif occurs_check(psi2, psi1, subst):
            raise UnificationError(f"Occurs check failed: {psi2} in {psi1}")
        else:
            subst[psi2] = psi1
            return subst
    elif isinstance(psi1, list) and isinstance(psi2, list):
        if psi1[0] != psi2[0]:
            raise UnificationError(f"Predicate symbols don't match: {psi1[0]} != {psi2[0]}")
        if len(psi1) != len(psi2):
```

```

        raise UnificationError(f"Argument lengths don't match: {len(psi1)} != {len(psi2)}")
    for arg1, arg2 in zip(psi1[1:], psi2[1:]): # Skip the predicate symbol (first element)
        subst = unify(arg1, arg2, subst)
    return subst
else:
    raise UnificationError(f"Cannot unify {psi1} with {psi2}")

def get_input():
    """Get input from the user and perform unification."""
    try:
        term1 = eval(input("Enter the first term (e.g., ['P', 'b', 'x', ['f', ['g', 'z']]]): "))
        term2 = eval(input("Enter the second term (e.g., ['P', 'z', ['f', 'y'], ['f', 'y']]): "))
        substitution = unify(term1, term2)
        print("Unification successful!")
        print("Substitution:", substitution)
    except UnificationError as e:
        print("Unification failed:", e)
    except Exception as e:
        print("Invalid input or error:", e)

# Run the unification input prompt
get_input()

```

## Output:

```

Enter the first term (e.g., ['P', 'b', 'x', ['f', ['g', 'z']]]): ['P', ['f', ['a']], ['g', ['?y']]]
Enter the second term (e.g., ['P', 'z', ['f', 'y'], ['f', 'y']]): ['P', '?x', '?x']
Unification failed: Predicate symbols don't match: g != f

```

[+ Code](#) [+ Text](#)

```

Enter the first term (e.g., ['P', 'b', 'x', ['f', ['g', 'z']]]): ['P', 'b', '?x', ['f', ['g', '?z']]]
Enter the second term (e.g., ['P', 'z', ['f', 'y'], ['f', 'y']]): ['P', '?z', ['f', '?y'], ['f', '?y']]
Unification successful!
Substitution: {'?z': 'b', '?x': ['f', '?y'], '?y': ['g', '?z']}

```

## Program 8

Create a knowledge base consisting of first order logic statements and prove the given query using forward reasoning.

Algorithm:

Good Luck Page No.  
Date 26 11 24

Lab - 8

→ First Order Logic

function FOL-FC-ASK (KB,  $\alpha$ ) returns a substitution or false

inputs: KB, the knowledge base, a set of first-order definite clauses  
 $\alpha$ , the query, an atomic sentence.

local variables: new, the new sentences inferred at each iteration

repeat until new is empty

new  $\leftarrow \{\}$

for each rule in KB do

$(p_1 \wedge \dots \wedge p_n \Rightarrow q) \in \text{STANDARDIZE-VARIABLES}$

for each  $\theta$  such that  $\text{SUBST}(\theta, p_1 \wedge \dots \wedge p_n) = \text{SUBST}(\theta, \text{rule})$

for some  $p_1 \dots p_n$  in KB

$q' \leftarrow \text{SUBST}(\theta, q)$

if  $q'$  does not unify with some sentence already in KB or new then

add  $q'$  to new

$\theta \leftarrow \text{UNIFY}(q', \alpha)$

if  $\theta$  is not fail then return  $\theta$

add new to KB

return false

26/11/24

Ques  
As per the law, it is a crime for an American to sell weapons to hostile nations. Country A, an enemy of America, has some missiles were sold to it by Robert, who is an American citizen.

Prove that "Robert is criminal"

Representation in FOL

It is a crime for American to sell weapons to hostile nations

Let's say  
 $American(p) \wedge Weapon(q) \wedge Seller(p, q) \wedge Hostile(r) \Rightarrow Criminal(p)$

Country A has some missiles

$\exists x Owns(A, x) \wedge Missiles(x)$

Existential instantiation, introducing a new constant T1:

$Owns(A, T1)$

missile (T1)

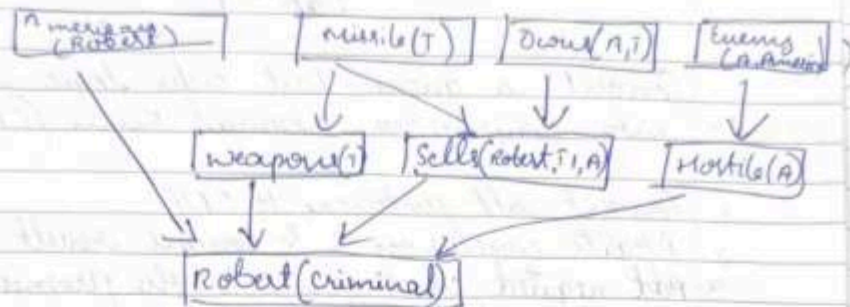
All of the missiles were sold to country A by Robert

$\forall x Missiles(x) \wedge Owns(A, x) \Rightarrow Seller(Robert, x, A)$

Missiles are weapons  
 $Missile(x) \Rightarrow Weapon(x)$

Enemy of America is known as hostile

$\forall x Enemy(x, America) \Rightarrow Hostile(x)$



Output:

Enter your FOL statements

> American(p)  $\wedge$  weapon(q)  $\wedge$  Sells(p, q, r)  $\wedge$  Hostile(r)  $\Rightarrow$  criminal(p)

>  $\forall x$  owns(A, x)  $\wedge$  missile(x)

> owns(A, T)

> missile(T)

>  $\forall x$  missile(x)  $\wedge$  owns(A, x)  $\Rightarrow$  Sells(Robert, x, A)

> missile(x)  $\Rightarrow$  weapon(x)

>  $\forall x$  Enemy(x, America)  $\Rightarrow$  Hostile(x)

> American(Robert)

> Enemy(A, America)

> done

Enter the query to prove criminal(Robert)

Proves: criminal(Robert)

16-11-2

**Code:**

```
class UnificationError(Exception):
    """Custom exception for unification errors."""
    pass

def occurs_check(var, term, subst):
    """Check if `var` occurs in `term` (to prevent circular substitutions)."""
    if var == term:
        return True
    elif isinstance(term, (list, tuple)):
        return any(occurs_check(var, t, subst) for t in term)
    elif isinstance(term, str) and term in subst:
        return occurs_check(var, subst[term], subst)
    return False

def is_variable(term):
    """Check if `term` is a variable (starting with `?`)."""
    return isinstance(term, str) and term.startswith('?')

def unify(psi1, psi2, subst=None):
    """Attempt to unify two terms, `psi1` and `psi2`, under the given substitution."""
    if subst is None:
        subst = {}

    if psi1 == psi2:
        return subst
    elif is_variable(psi1):
        if psi1 in subst:
            return unify(subst[psi1], psi2, subst)
        elif occurs_check(psi1, psi2, subst):
            raise UnificationError(f"Occurs check failed: {psi1} in {psi2}")
        else:
            subst[psi1] = psi2
            return subst
    elif is_variable(psi2):
        if psi2 in subst:
            return unify(psi1, subst[psi2], subst)
        elif occurs_check(psi2, psi1, subst):
            raise UnificationError(f"Occurs check failed: {psi2} in {psi1}")
        else:
            subst[psi2] = psi1
            return subst
    elif isinstance(psi1, list) and isinstance(psi2, list):
        if psi1[0] != psi2[0]:
            raise UnificationError(f"Predicate symbols don't match: {psi1[0]} != {psi2[0]}")
        if len(psi1) != len(psi2):
```



```

        raise UnificationError(f"Argument lengths don't match: {len(psi1)} != {len(psi2)}")
    for arg1, arg2 in zip(psi1[1:], psi2[1:]): # Skip the predicate symbol (first element)
        subst = unify(arg1, arg2, subst)
    return subst
else:
    raise UnificationError(f"Cannot unify {psi1} with {psi2}")

def get_input():
    """Get input from the user and perform unification."""
    try:
        term1 = eval(input("Enter the first term (e.g., ['P', 'b', 'x', ['f', ['g', 'z']]]): "))
        term2 = eval(input("Enter the second term (e.g., ['P', 'z', ['f', 'y'], ['f', 'y']]): "))
        substitution = unify(term1, term2)
        print("Unification successful!")
        print("Substitution:", substitution)
    except UnificationError as e:
        print("Unification failed:", e)
    except Exception as e:
        print("Invalid input or error:", e)

# Run the unification input prompt
get_input()

```

## Output:

```

Enter the rules:
Enter rule (or 'done' to finish): American(p) AND Weapon(q) AND Sells(p, q, r) AND Hostile(r) => Criminal(p)
Enter rule (or 'done' to finish):  $\exists x$  (Owns(A, x) AND Missile(x)) => Missile(x) AND Weapon(x)
Enter rule (or 'done' to finish):  $\forall x$  (Missile(x) AND Owns(A, x)) => Sells(Robert, x, A)
Enter rule (or 'done' to finish): Missile(x) => Weapon(x)
Enter rule (or 'done' to finish):  $\forall x$  (Enemy(x, America)) => Hostile(x)
Enter rule (or 'done' to finish): done

Enter the facts:
Enter fact (or 'done' to finish): American(Robert)
Enter fact (or 'done' to finish): Enemy(A, America)
Enter fact (or 'done' to finish): Owns(A, T1)
Enter fact (or 'done' to finish): Missile(T1)
Enter fact (or 'done' to finish): done

Enter the query:
Enter the query: Criminal(Robert)

Final facts:
{'Enemy(A, America)', 'Owns(A, T1)', 'American(Robert)', 'Missile(T1)'}

Query 'Criminal(Robert)' inferred: True

```

## Program 9

Create a knowledge base consisting of first order logic statements and prove the given query using Resolution

### Algorithm:

Good Luck Page No. \_\_\_\_\_  
Date 06.11.2020

Lab - 9

Convert a given first order logic statements into Conjunctive Normal Form (CNF)

1. Convert all sentences to CNF
2. Negate conclusion S & convert result to CNF
3. Add negated conclusion S to the premise clauses
4. Repeat until contradiction or no progress is made:
  - a. Select 2 clauses (call them parent clauses)
  - b. Resolve them together, performing all required unifications
  - c. If resolved resolvent is the empty clause, a contradiction has been found (i.e., S follows from the premises)
  - d. If not, add resolvent to the premises

If we succeed in Step 4, we have proved the conclusion.

Give KB or Premises:

- a. John likes all kind of food
- b. Apple and vegetables are food
- c. Anything anyone eats and not killed is food
- d. Ail eats peanuts and still alive
- e. Harry eats everything that Ail eats
- f. Anyone who is alive implies not killed
- g. Anyone who is not killed implies alive
- h. Representation in FOL

- a.  $\forall x: \text{food}(x) \rightarrow \text{likes}(\text{John}, x)$
- b.  $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$
- c.  $\forall x \forall y: \text{eats}(x, y) \wedge \neg \text{killed}(x) \rightarrow \text{food}(y)$
- d.  $\text{eats}(\text{Ail}, \text{peanuts}) \wedge \text{alive}(\text{Ail})$
- e.  $\forall x: \text{eats}(\text{Ail}, x) \rightarrow \text{eats}(\text{Harry}, x)$
- f.  $\forall x: \text{killed}(x) \rightarrow \neg \text{alive}(x)$
- g.  $\forall x: \text{alive}(x) \rightarrow \neg \text{killed}(x)$
- h.  $\text{likes}(\text{John}, \text{peanuts})$

Eliminate implication  $\alpha \Rightarrow \beta$  with  $\neg \alpha \vee \beta$

- $\forall x \neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
- $\text{food}(\text{Apple}) \wedge \neg \text{food}(\text{vegetables})$
- $\forall x \forall y \neg [\text{eats}(x, y) \wedge \neg \text{killed}(x)] \vee \text{food}(y)$
- $\text{eats}(\text{Anil}, \text{peanuts}) \wedge \neg \text{alive}(\text{Anil})$
- $\forall x \neg \text{eats}(\text{Anil}, x) \vee \text{eats}(\text{Harry}, x)$
- $\forall x \neg [\neg \text{killed}(x)] \vee \text{alive}(x)$
- $\forall x \neg \text{alive}(x) \vee \neg \text{killed}(x)$
- $\text{likes}(\text{John}, \text{Peanuts})$

Move negation ( $\neg$ ) inwards and rewrite

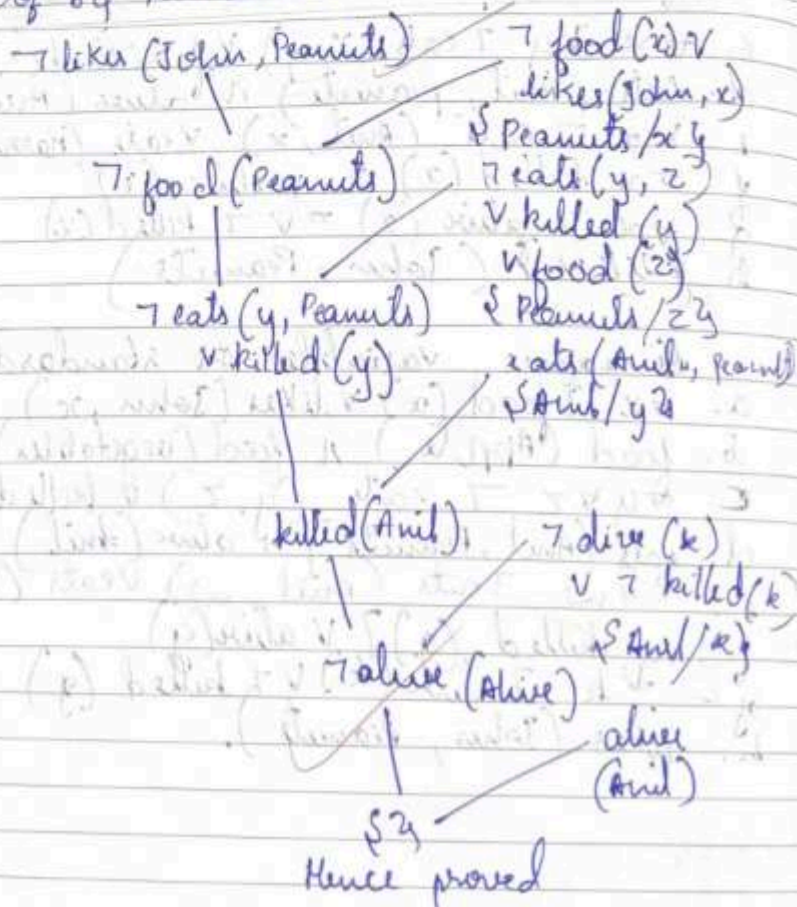
- $\forall x \neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
- $\text{food}(\text{Apple}) \wedge \neg \text{food}(\text{vegetables})$
- $\forall x \forall y \neg \text{eats}(x, y) \vee \neg \text{killed}(x) \vee \text{food}(y)$
- $\text{eats}(\text{Anil}, \text{peanuts}) \wedge \neg \text{alive}(\text{Anil})$
- $\forall x \neg \text{eats}(\text{Anil}, x) \vee \text{eats}(\text{Harry}, x)$
- $\forall x \text{killed}(x) \vee \text{alive}(x)$
- $\forall x \neg \text{alive}(x) \Rightarrow \forall \neg \text{killed}(x)$
- $\text{likes}(\text{John}, \text{Peanuts})$

Rename variables or standardize variables

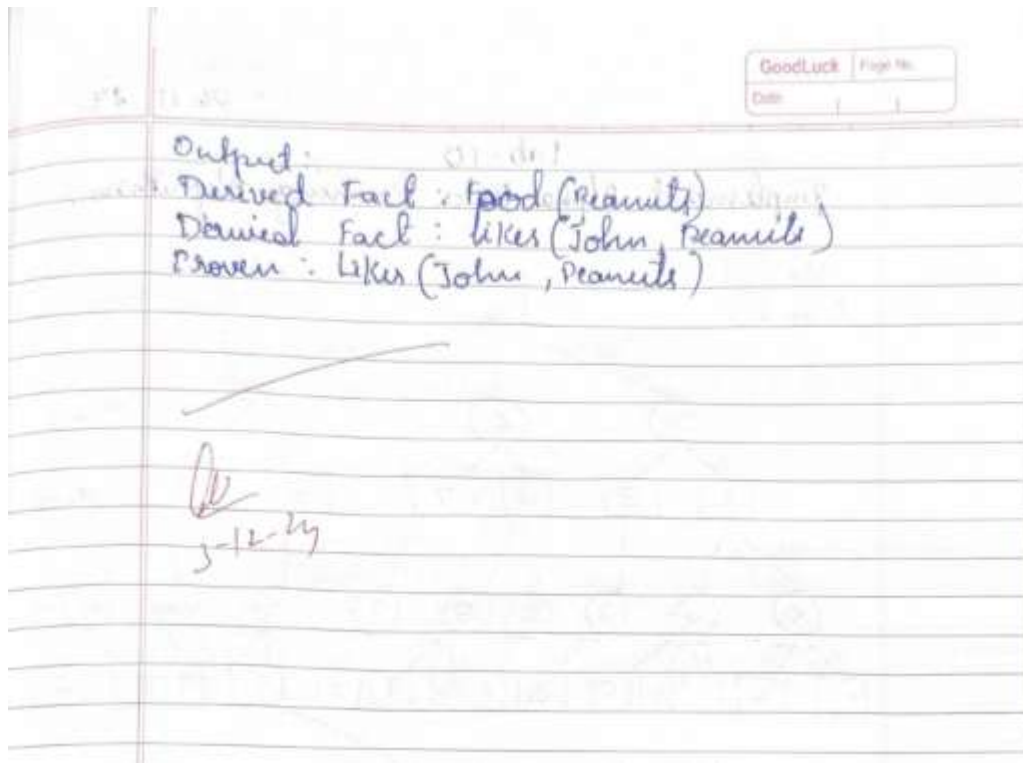
- $\forall x \neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
- $\text{food}(\text{Apple}) \wedge \neg \text{food}(\text{vegetables})$
- $\forall y \forall z \neg \text{eats}(y, z) \vee \neg \text{killed}(y) \vee \text{food}(z)$
- $\text{eats}(\text{Anil}, \text{Peanuts}) \wedge \neg \text{alive}(\text{Anil})$
- $\forall u \neg \text{eats}(\text{Anil}, u) \vee \text{eats}(\text{Harry}, u)$
- $\forall g \text{killed}(g) \vee \text{alive}(g)$
- $\forall k \neg \text{alive}(k) \vee \neg \text{killed}(g)$
- $\text{likes}(\text{John}, \text{Peanuts})$

- Drop Universal Quantifier
- $\neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
  - $\text{food}(\text{apple})$
  - $\text{food}(\text{vegetables})$
  - $\neg \text{eats}(y, z) \vee \text{killed}(y) \vee \text{food}(z)$
  - $\text{eats}(\text{Anil}, \text{Peanuts})$
  - $\text{alive}(\text{Anil})$
  - $\neg \text{eats}(\text{Anil}, w) \vee \text{eats}(\text{Harry}, w)$
  - $\text{killed}(g) \vee \text{alive}(g)$
  - $\neg \text{alive}(k) \vee \neg \text{killed}(k)$
  - $\text{likes}(\text{John}, \text{Peanuts})$

Proof by Resolution







### Code:

import re

class ForwardReasoning:

def \_\_init\_\_(self, rules, facts):

self.rules = rules # List of rules (condition -> result)

self.facts = set(facts) # Known facts

def match\_condition(self, condition):

"""Check if all conditions match the current facts."""

variable\_map = {}

for cond in condition:

fact\_match = False

for fact in self.facts:

if self.match\_fact(cond, fact, variable\_map):

fact\_match = True

break

if not fact\_match:

return False, variable\_map

return True, variable\_map

def match\_fact(self, cond, fact, variable\_map):

"""Match a condition to a fact, handling variables."""

var\_pattern = re.compile(r'\b?[a-zA-Z]+\b') # Match variables starting with '?'

```

condition_parts = cond.split()
fact_parts = fact.split()

if len(condition_parts) != len(fact_parts):
    return False

for cond_part, fact_part in zip(condition_parts, fact_parts):
    if var_pattern.match(cond_part): # If it's a variable
        if cond_part not in variable_map:
            variable_map[cond_part] = fact_part
        elif variable_map[cond_part] != fact_part:
            return False
    elif cond_part != fact_part: # If it's a constant, they must match
        return False
return True

def infer(self, query):
    """Forward chaining algorithm to infer if the query can be derived."""
    applied_rules = True
    while applied_rules:
        applied_rules = False
        for condition, result in self.rules:
            matched, variable_map = self.match_condition(condition)
            if matched and result not in self.facts:
                self.facts.add(result) # Add the result to known facts
                applied_rules = True
                print(f'Applied rule: {condition} -> {result}')
                # If the query is inferred, return True immediately
                if self.match_fact(query, result, variable_map):
                    return True
        # Return True if the query is in facts after the reasoning process, else False
        return query in self.facts

def get_input_rules():
    """Get input for rules from the user."""
    rules = []
    while True:
        rule = input("Enter rule (or 'done' to finish): ").strip()
        if rule.lower() == "done":
            break
        if "=>" in rule:
            condition_str, result = rule.split("=>")
            conditions = set(condition_str.strip().split(" AND "))
            result = result.strip()
            rules.append((conditions, result))
    return rules

```



```

def get_input_facts():
    """Get input for facts from the user."""
    facts = set()
    while True:
        fact = input("Enter fact (or 'done' to finish): ").strip()
        if fact.lower() == "done":
            break
        facts.add(fact)
    return facts

def get_input_query():
    """Get input for the query from the user."""
    return input("Enter the query: ").strip()

# Main program to run the forward reasoning
def main():
    print("Enter the rules:")
    rules = get_input_rules()
    print("\nEnter the facts:")
    facts = get_input_facts()
    print("\nEnter the query:")
    query = get_input_query()

    # Initialize and run forward reasoning
    reasoner = ForwardReasoning(rules, facts)
    result = reasoner.infer(query)

    # Output results
    print("\nFinal facts:")
    print(reasoner.facts)
    print(f"\nQuery '{query}' inferred: {result}")

# Call the main function to start
main()

```

### Output:

---

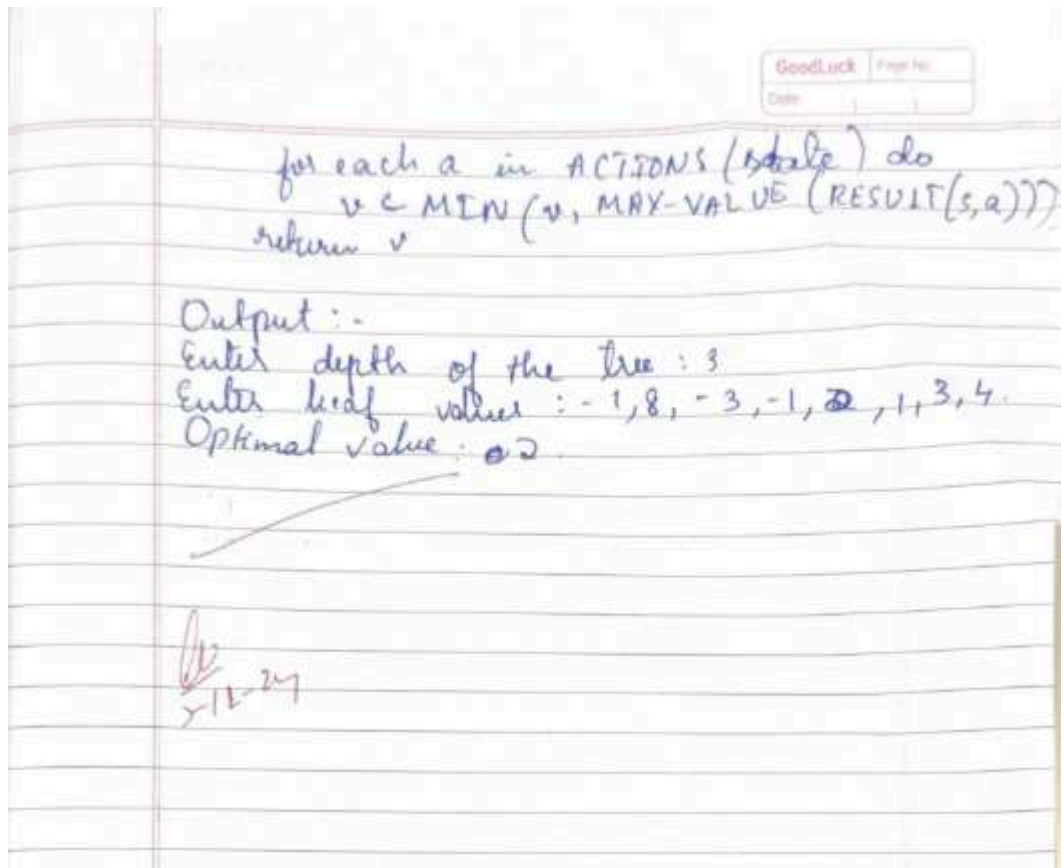
➞ Does John like peanuts? Yes

---

### Implement Alpha-Beta Pruning.

**Algorithm:**





### Code:

```
import math
```

```
def minimax(node, depth, is_maximizing):  
    """
```

Implement the Minimax algorithm to solve the decision tree.

Parameters:

node (dict): The current node in the decision tree, with the following structure:

```
{  
    'value': int,  
    'left': dict or None,  
    'right': dict or None  
}
```

depth (int): The current depth in the decision tree.

is\_maximizing (bool): Flag to indicate whether the current player is the maximizing player.

Returns:

int: The utility value of the current node.

```
    """
```

```
# Base case: Leaf node
```

```
if node['left'] is None and node['right'] is None:
```

```

    return node['value']

# Recursive case
if is_maximizing:
    best_value = -math.inf
    if node['left']:
        best_value = max(best_value, minimax(node['left'], depth + 1, False))
    if node['right']:
        best_value = max(best_value, minimax(node['right'], depth + 1, False))
    return best_value
else:
    best_value = math.inf
    if node['left']:
        best_value = min(best_value, minimax(node['left'], depth + 1, True))
    if node['right']:
        best_value = min(best_value, minimax(node['right'], depth + 1, True))
    return best_value

# Example usage
decision_tree = {
    'value': 5,
    'left': {
        'value': 6,
        'left': {
            'value': 7,
            'left': {
                'value': 4,
                'left': None,
                'right': None
            },
            'right': {
                'value': 5,
                'left': None,
                'right': None
            }
        },
        'right': {
            'value': 3,
            'left': {
                'value': 6,
                'left': None,
                'right': None
            },
            'right': {
                'value': 9,
                'left': None,
                'right': None
            }
        }
    },
    'right': {
        'value': 3,
        'left': {
            'value': 6,
            'left': None,
            'right': None
        },
        'right': {
            'value': 9,
            'left': None,
            'right': None
        }
    }
}

```

```

    }
  },
  'right': {
    'value': 8,
    'left': {
      'value': 7,
      'left': {
        'value': 6,
        'left': None,
        'right': None
      },
      'right': {
        'value': 9,
        'left': None,
        'right': None
      }
    },
    'right': {
      'value': 8,
      'left': {
        'value': 6,
        'left': None,
        'right': None
      },
      'right': None
    }
  }
}

```

```

# Find the best move for the maximizing player
best_value = minimax(decision_tree, 0, True)
print(f"The best value for the maximizing player is: {best_value}")

```

### Output:

```

➞ The best value for the maximizing player is: 6

```