

Lab - 3

Heuristic:

```
import heapq
GOAL_STATE = ((1, 2, 3),
              (8, 0, 4),
              (7, 6, 5))
def misplaced_tile(state):
    misplaced = 0
    for i in range(3):
        for j in range(3):
            if state[i][j] != 0 and state[i][j] !=
GOAL_STATE[i][j]:
                misplaced += 1
    return misplaced
def find_blank(state):
    for i in range(3):
        for j in range(3):
            if state[i][j] == 0:
                return i, j

def generate_neighbors(state):
    neighbors = []
    x, y = find_blank(state)
    directions = [(0, 1), (0, -1), (1, 0), (-1, 0)]

    for dx, dy in directions:
        nx, ny = x + dx, y + dy
        if 0 <= nx < 3 and 0 <= ny < 3:
            new_state = [list(row) for row in state]
            new_state[x][y], new_state[nx][ny] =
new_state[nx][ny], new_state[x][y]
            neighbors.append(tuple(tuple(row) for row in
new_state))

    return neighbors
def reconstruct_path(came_from, current):
    path = [current]
    while current in came_from:
        current = came_from[current]
        path.append(current)
    path.reverse()
```

```
    return path
```

```
def a_star(start):  
    open_list = []  
    heapq.heappush(open_list, (0 + misplaced_tile(start),  
0, start))
```

```
    g_score = {start: 0}  
    came_from = {}
```

```
    visited = set()
```

```
    while open_list:  
        _, g, current = heapq.heappop(open_list)
```

```
        if current == GOAL_STATE:  
            path = reconstruct_path(came_from, current)  
            return path, g
```

```
        visited.add(current)
```

```
        for neighbor in generate_neighbors(current):  
            if neighbor in visited:  
                continue  
            tentative_g = g_score[current] + 1
```

```
            if tentative_g < g_score.get(neighbor,  
float('inf')):  
                came_from[neighbor] = current  
                g_score[neighbor] = tentative_g  
                f_score = tentative_g +  
misplaced_tile(neighbor) #  $f(n) = g(n) + h(n)$ 
```

```
                heapq.heappush(open_list, (f_score,  
tentative_g, neighbor))
```

```
    return None, None
```

```
def print_state(state):  
    for row in state:  
        print(row)
```

```
print()
```

```
if __name__ == "__main__":  
    start_state = ((2, 8, 3),  
                  (1, 6, 4),  
                  (7, 0, 5))
```

```
print("Initial State:")  
print_state(start_state)
```

```
print("Goal State:")  
print_state(GOAL_STATE)
```

```
solution, cost = a_star(start_state)
```

```
if solution:  
    print(f"Solution found with cost: {cost}")  
    print("Steps:")  
    for step in solution:  
        print_state(step)  
else:  
    print("No solution found.")
```

Output:

```
Initial State:  
(2, 8, 3)  
(1, 6, 4)  
(7, 0, 5)  
  
Goal State:  
(1, 2, 3)  
(8, 0, 4)  
(7, 6, 5)  
  
Solution found with cost: 5  
Steps:  
(2, 8, 3)  
(1, 6, 4)  
(7, 0, 5)  
  
(2, 8, 3)  
(1, 0, 4)  
(7, 6, 5)  
  
(2, 0, 3)  
(1, 8, 4)  
(7, 6, 5)  
  
(0, 2, 3)  
(1, 8, 4)  
(7, 6, 5)  
  
(1, 2, 3)  
(0, 8, 4)  
(7, 6, 5)  
  
(1, 2, 3)  
(8, 0, 4)  
(7, 6, 5)
```