

# Rooted Binary Trees

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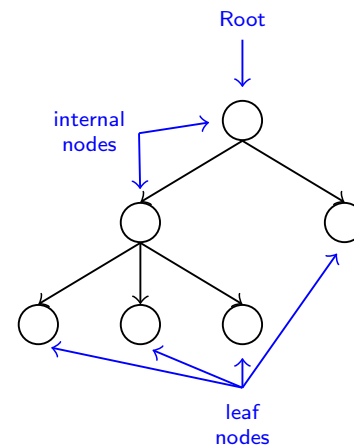
IIIT, Delhi  
Winter Semester,  
31<sup>st</sup> March, 2023

## Rooted Binary Trees

# A General Tree

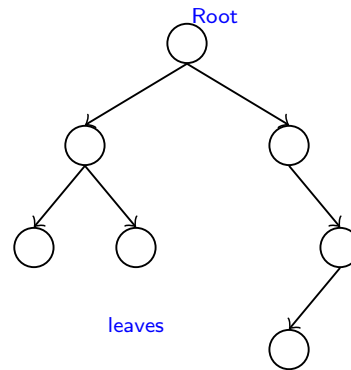
A (rooted) tree is an abstract data type

- one entry point, the *root*.
- Each node is either a *leaf* or an *internal node*.
- An internal node has 1 or more *children*.
- The internal node is *parent* of its child nodes.
- The *leaf nodes* have no children.



# Properties of Trees

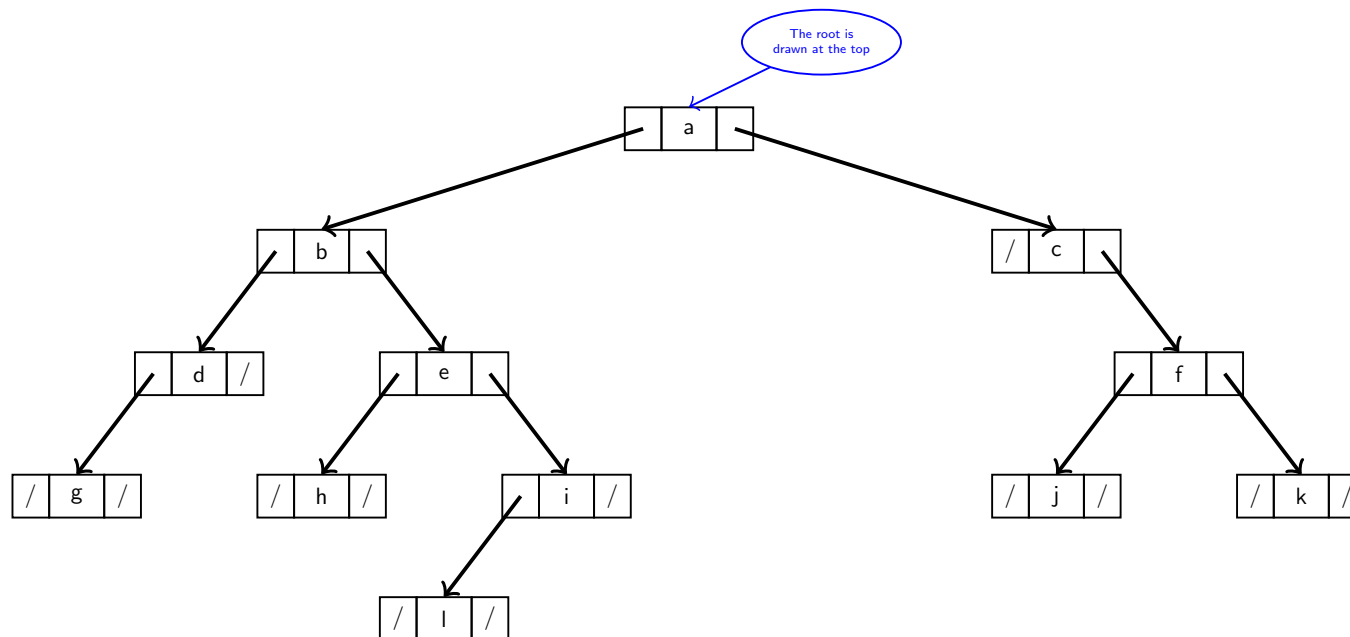
- Only access point is the root.
- All nodes, except the root, have one parent.



# Binary Trees

- Array, linked lists, stack, or queue are all **linear structures**.
- A **(rooted) tree** has a hierarchical structure (non-linear).
- The **(rooted) binary tree** is a special case of the general tree, having maximum of two child nodes.
- It is either empty or consists of
  - an element called the **root**,
  - and two distinct binary trees, called the **left subtree** and **right subtree**.

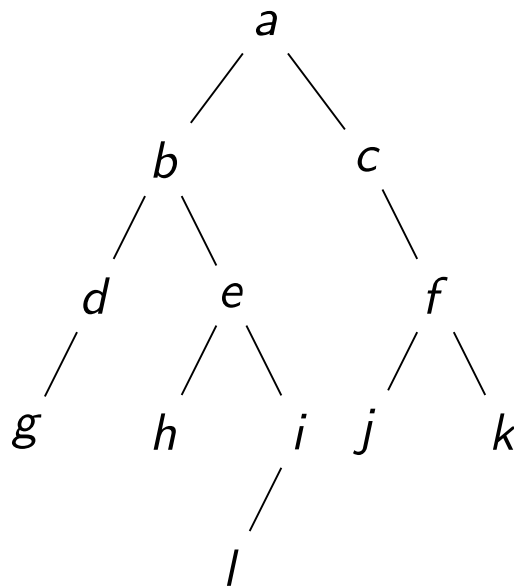
# Picture of a Binary Tree



# Binary Tree

- Each node consists of
  - Data value.
  - Left link: Points to the left child
  - Right link: Points to the right child
- Any node can have null value in its right link or in its left link.
- Leaf nodes have null values in left and right link.
- Children of a node are termed siblings

## Size and depth

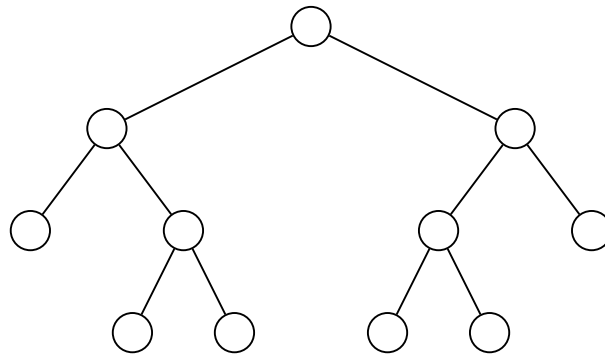


- The **size** of a binary tree is the number of nodes in it.
  - This tree has size 12.
- The **depth** of a node is its distance from the root.
  - **a** is at depth zero.
  - **e** is at depth 2.
- The **depth** of a binary tree is the depth of its deepest node.
  - This tree has depth 4.

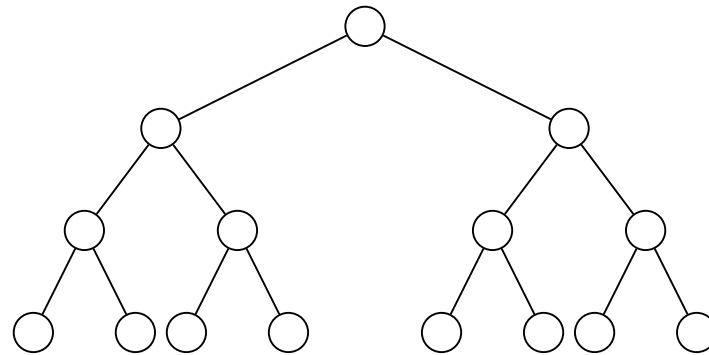


# Full Binary Tree

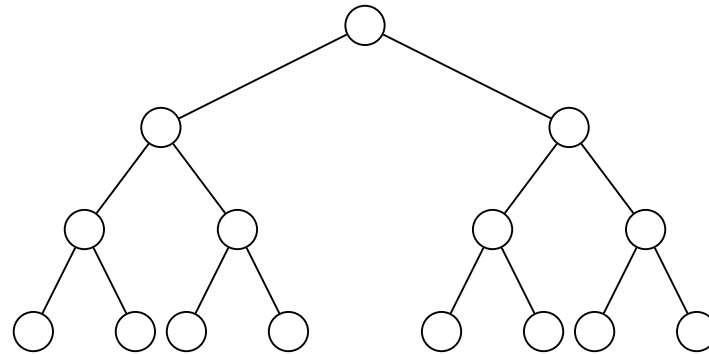
- Every node has zero or two children.



Height is  $\mathcal{O}(\log n)$



Height is  $\mathcal{O}(\log n)$



$$N = 1 + 2 + 4 + 8 + 16 + \dots$$

$$N = 2^0 + 2^1 + 2^2 + 2^3 + \dots + 2^{h-1}$$

$$N = \frac{2^h - 1}{2 - 1}$$

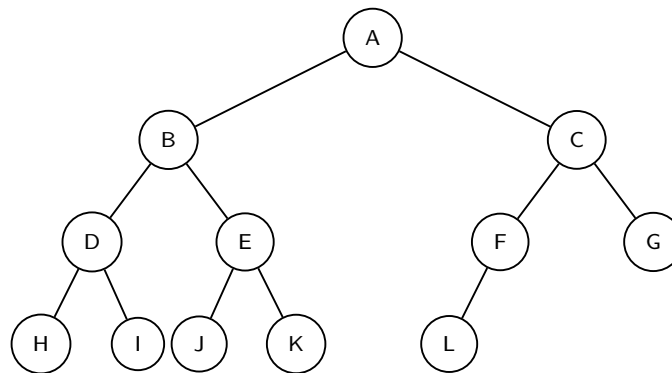
$$N + 1 = 2^h$$

Taking log of both sides

$$h = \log_2(N + 1)$$

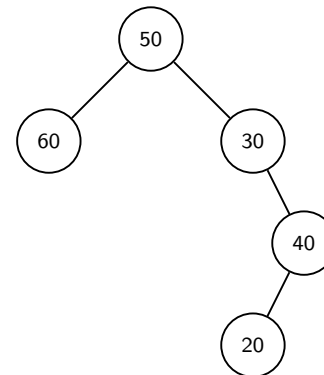
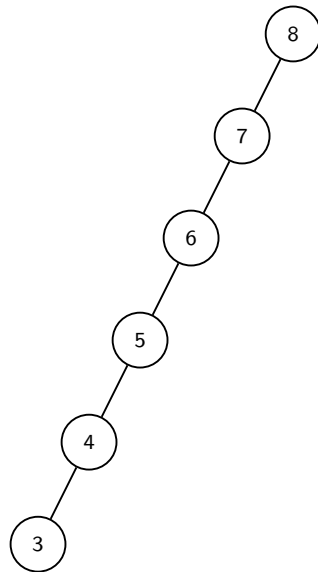
# Complete Tree

- Has all levels filled, except possibly the last level, where all nodes are as far left as possible.



# Skewed Tree

- A skewed tree is one which is predominantly leaning to one side.



## Binary Tree: Definition

- A **rooted binary tree** is defined recursively: it consists of
  - a **root**,
  - a **left subtree**, and
  - a **right subtree**
- A tree node can be constructed with or without any data.
- Array implementation of a tree is very messy if the tree is large and many of its internal nodes are missing

# Binary Tree Node in C

```
typedef struct BTreeNode {  
    int nData;  
    struct Node *pParent;  
    struct Node *pLeft;  
    struct Node *pRight;  
} BTreeNode;
```

## Traversing a Binary Tree

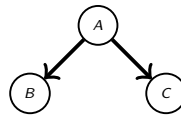


# Tree Traversals

- **Traverse (or walk):** To visit each node in the binary tree **exactly once**.
- They are naturally recursive.
- Popular ways to traverse a binary tree:
  - **Pre-order traversal:** **root**, left, right.
  - **In-order traversal:** left, **root**, right.
  - **Post-order traversal:** left, right, **root**.

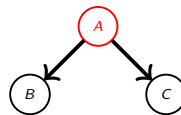
# Pre-order Traversal

- root, left, right.



# Pre-order Traversal

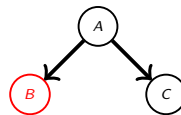
- root, left, right.



**Output:** A

# Pre-order Traversal

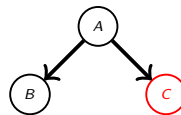
- root, left, right.



**Output:** *A, B*

# Pre-order Traversal

- root, left, right.

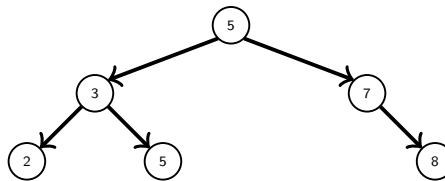


**Output:** *A, B, C*

# Pre-order Traversal

- root, left, right.
- The nodes are visited in root, left, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        printf ("%d, ", pRoot->nData);  
        display (pRoot->pLeft);  
        display (root->pRight);  
    }  
}
```

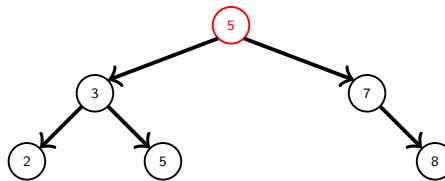


**Output:**

# Pre-order Traversal

- root, left, right.
- The nodes are visited in root, left, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        printf ("%d, ", pRoot->nData);  
        display (pRoot->pLeft);  
        display (root->pRight);  
    }  
}
```

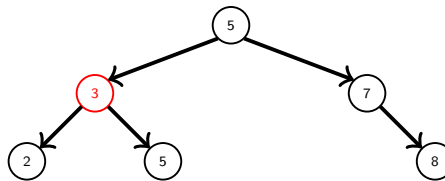


**Output: 5**

# Pre-order Traversal

- root, left, right.
- The nodes are visited in root, left, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        printf ("%d, ", pRoot->nData);  
        display (pRoot->pLeft);  
        display (root->pRight);  
    }  
}
```



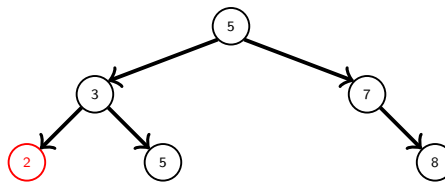
**Output:** 5, 3



# Pre-order Traversal

- root, left, right.
- The nodes are visited in root, left, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        printf ("%d, ", pRoot->nData);  
        display (pRoot->pLeft);  
        display (root->pRight);  
    }  
}
```

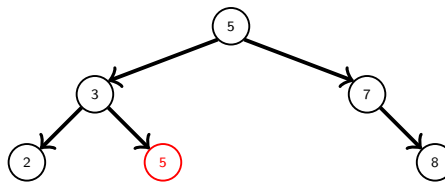


**Output:** 5, 3, 2

# Pre-order Traversal

- root, left, right.
- The nodes are visited in root, left, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        printf ("%d, ", pRoot->nData);  
        display (pRoot->pLeft);  
        display (root->pRight);  
    }  
}
```

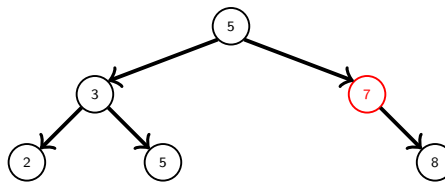


**Output:** 5, 3, 2, 5

# Pre-order Traversal

- root, left, right.
- The nodes are visited in root, left, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        printf ("%d, ", pRoot->nData);  
        display (pRoot->pLeft);  
        display (root->pRight);  
    }  
}
```

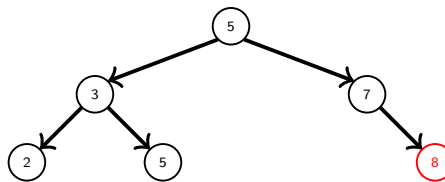


**Output:** 5, 3, 2, 5, 7

# Pre-order Traversal

- root, left, right.
- The nodes are visited in root, left, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        printf ("%d, ", pRoot->nData);  
        display (pRoot->pLeft);  
        display (root->pRight);  
    }  
}
```

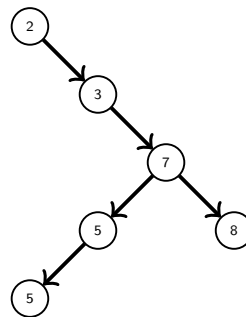


**Output:** 5, 3, 2, 5, 7, 8

# Pre-order Traversal

- root, left, right.
- The nodes are visited in root, left, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        printf ("%d, ", pRoot->nData);  
        display (pRoot->pLeft);  
        display (root->pRight);  
    }  
}
```

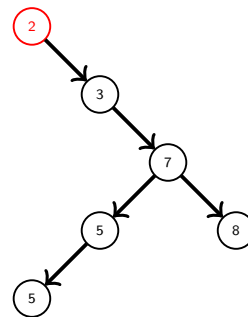


**Output:**

# Pre-order Traversal

- root, left, right.
- The nodes are visited in root, left, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        printf ("%d, ", pRoot->nData);  
        display (pRoot->pLeft);  
        display (root->pRight);  
    }  
}
```

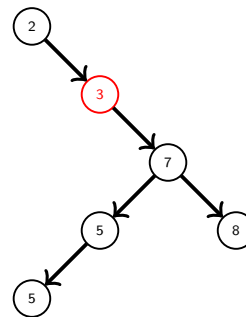


**Output: 2**

# Pre-order Traversal

- root, left, right.
- The nodes are visited in root, left, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        printf ("%d, ", pRoot->nData);  
        display (pRoot->pLeft);  
        display (root->pRight);  
    }  
}
```

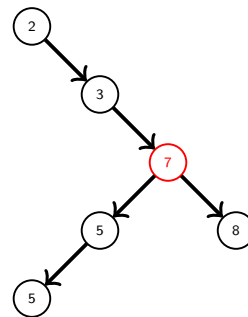


**Output:** 2, 3

# Pre-order Traversal

- root, left, right.
- The nodes are visited in root, left, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        printf ("%d, ", pRoot->nData);  
        display (pRoot->pLeft);  
        display (root->pRight);  
    }  
}
```



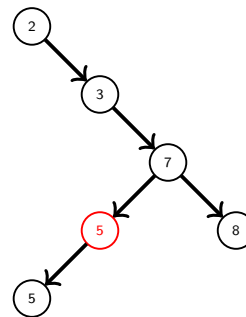
**Output:** 2, 3, 7



# Pre-order Traversal

- root, left, right.
- The nodes are visited in root, left, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        printf ("%d, ", pRoot->nData);  
        display (pRoot->pLeft);  
        display (root->pRight);  
    }  
}
```

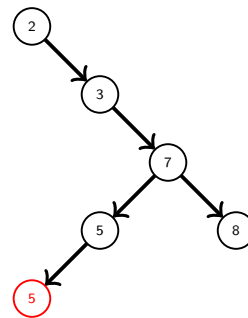


**Output:** 2, 3, 7, 5

# Pre-order Traversal

- root, left, right.
- The nodes are visited in root, left, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        printf ("%d, ", pRoot->nData);  
        display (pRoot->pLeft);  
        display (root->pRight);  
    }  
}
```

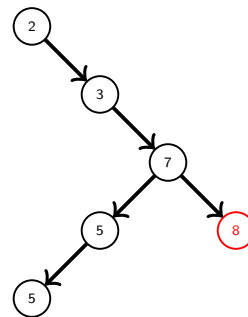


**Output:** 2, 3, 7, 5, 5

# Pre-order Traversal

- root, left, right.
- The nodes are visited in root, left, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        printf ("%d, ", pRoot->nData);  
        display (pRoot->pLeft);  
        display (root->pRight);  
    }  
}
```



**Output:** 2, 3, 7, 5, 5, 8

## PRE-ORDER-TREE-WALK( $root[T]$ )

**I/P:** The root of a binary tree  $T$ .

Begin

  if  $x \neq \mathbf{nil}$  then

    print  $Key[x]$ ;

    PRE-ORDER-TREE-WALK( $left[x]$ );

    PRE-ORDER-TREE-WALK( $right[T]$ );

  else

    return FLAG;

End

**Complexity:**

## PRE-ORDER-TREE-WALK( $root[T]$ )

**I/P:** The root of a binary tree  $T$ .

Begin

if  $x \neq \mathbf{nil}$  then

print  $Key[x]$ ;

PRE-ORDER-TREE-WALK( $left[x]$ );

PRE-ORDER-TREE-WALK( $right[T]$ );

else

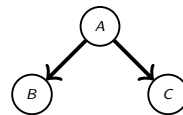
return FLAG;

End

**Complexity:**  $\Theta(n)$ , where  $n = \#$  nodes.

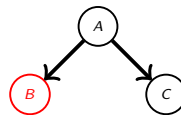
# In-order Traversal

- left, root, right.



# In-order Traversal

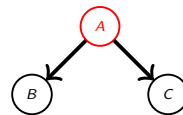
- left, **root**, right.



**Output:** *B*

# In-order Traversal

- left, root, right.

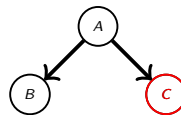


**Output:** *B, A*



# In-order Traversal

- left, root, right.

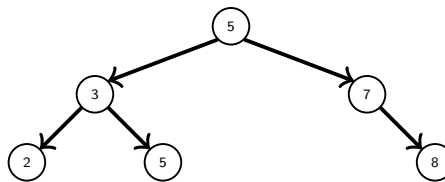


**Output:** *B, A, C*

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

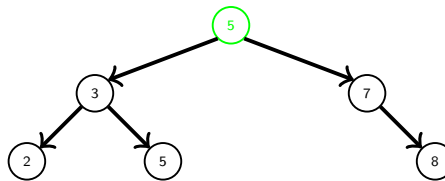


**Output:**

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
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        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
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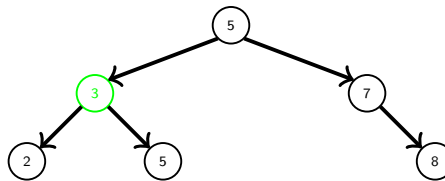


**Output:**

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
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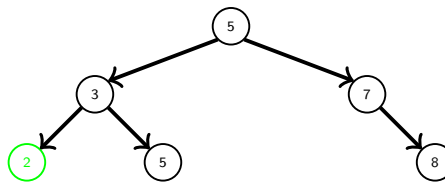


**Output:**

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

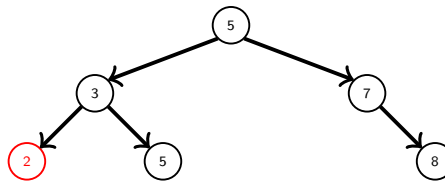


**Output:**

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

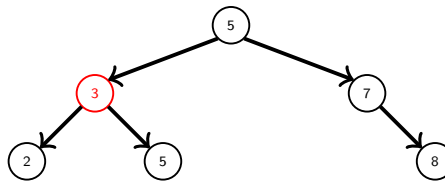


**Output: 2**

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

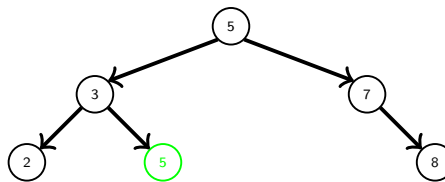


**Output:** 2, 3

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```



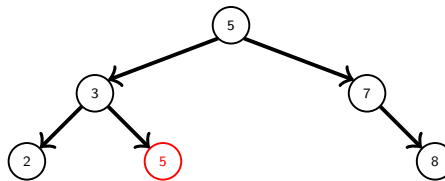
**Output:** 2, 3



# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

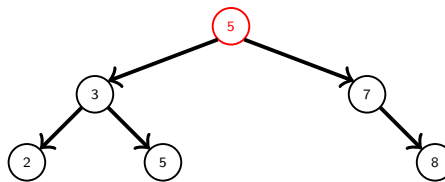


**Output:** 2, 3, 5

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

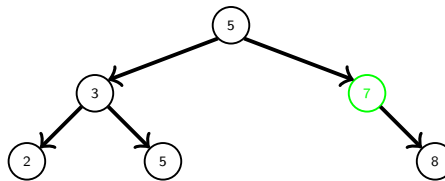


**Output:** 2, 3, 5, 5

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

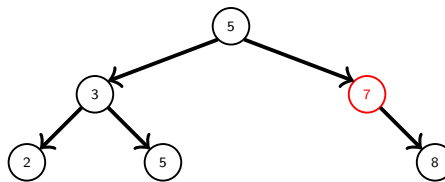


**Output:** 2, 3, 5, 5

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

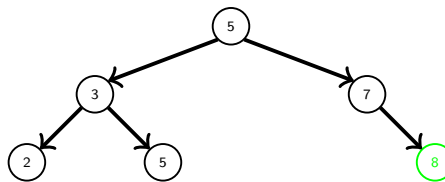


**Output:** 2, 3, 5, 5, 7

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

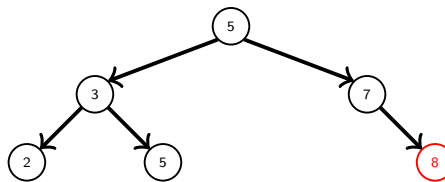


**Output:** 2, 3, 5, 5, 7

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

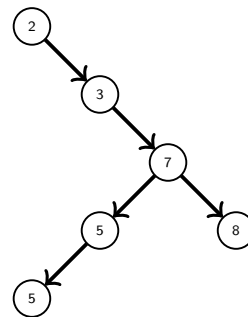


**Output:** 2, 3, 5, 5, 7, 8

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

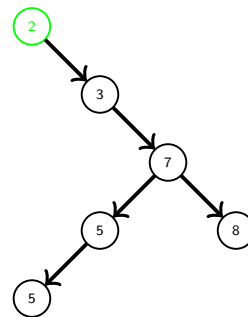


**Output:**

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```



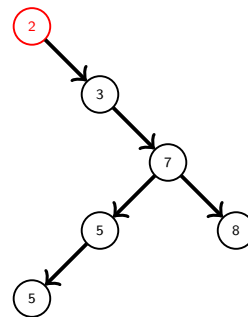
**Output:**



# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

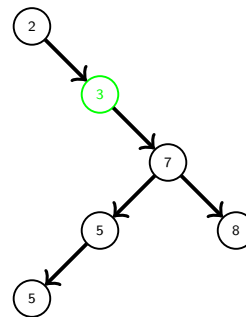


**Output: 2**

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

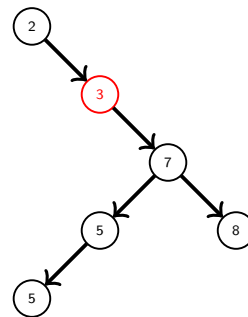


**Output: 2**

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

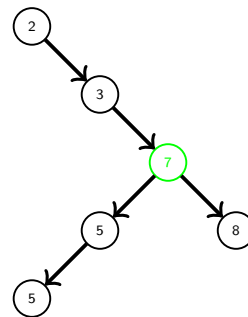


**Output:** 2, 3

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

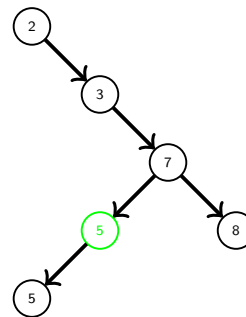


**Output:** 2, 3

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

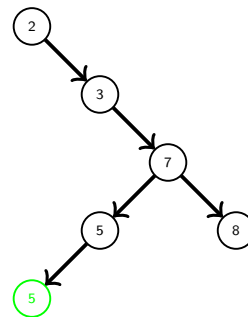


**Output:** 2, 3

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

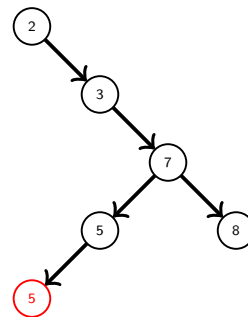


**Output:** 2, 3

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

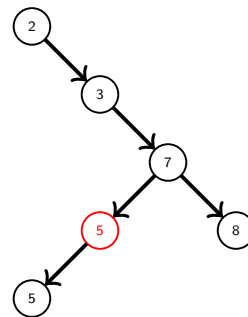


**Output:** 2, 3, 5

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```



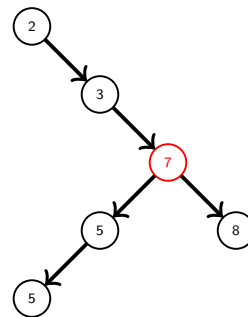
**Output:** 2, 3, 5, 5



# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

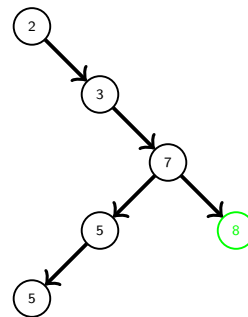


**Output:** 2, 3, 5, 5, 7

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```

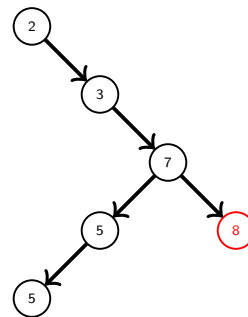


**Output:** 2, 3, 5, 5, 7

# In-order Traversal

- left, **root**, right.
- The nodes are visited in left, root, right fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        printf ("%d, ", pRoot->nData);  
        display (root->pRight);  
    }  
}
```



**Output:** 2, 3, 5, 5, 7, 8

## IN-ORDER-TREE-WALK( $root[T]$ )

**I/P:** The root of a binary tree  $T$ .

Begin

if  $x \neq \mathbf{nil}$  then

    IN-ORDER-TREE-WALK( $left[x]$ );

    print  $Key[x]$ ;

    IN-ORDER-TREE-WALK( $right[T]$ );

else

    return FLAG;

End

**Complexity:**

## IN-ORDER-TREE-WALK( $root[T]$ )

**I/P:** The root of a binary tree  $T$ .

Begin

if  $x \neq \mathbf{nil}$  then

    IN-ORDER-TREE-WALK( $left[x]$ );

    print  $Key[x]$ ;

    IN-ORDER-TREE-WALK( $right[T]$ );

else

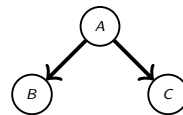
    return FLAG;

End

**Complexity:**  $\Theta(n)$ , where  $n = \#$  nodes.

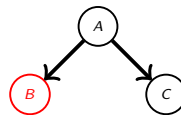
# Post-order Traversal

- left, right, root.



# Post-order Traversal

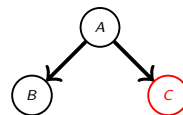
- left, right, **root**.



**Output:** *B*

# Post-order Traversal

- left, right, **root**.

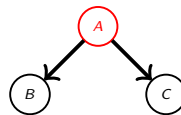


**Output:** *B, C*



# Post-order Traversal

- left, right, **root**.

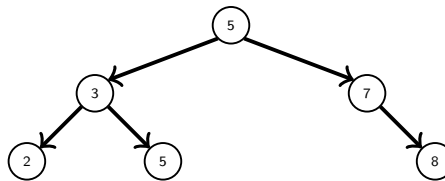


**Output:** *B, C, A*

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

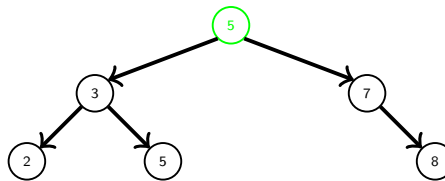


**Output:**

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

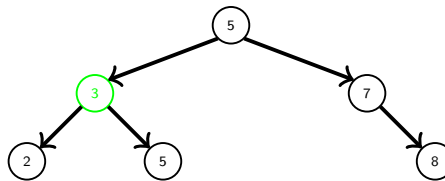


**Output:**

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

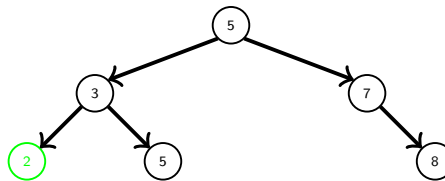


**Output:**

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

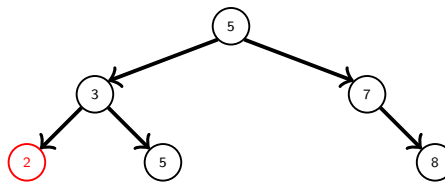


**Output:**

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

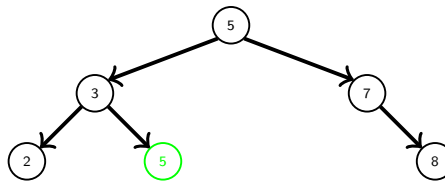


**Output: 2**

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

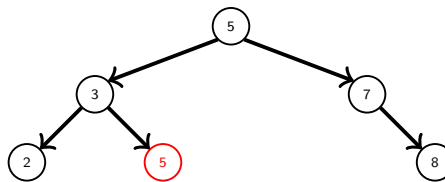


**Output: 2**

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```



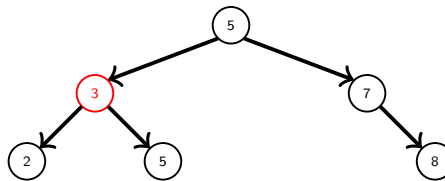
**Output:** 2, 5



# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

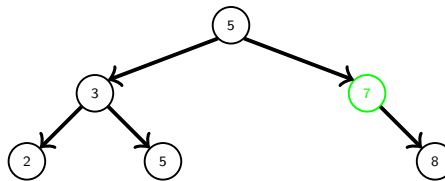


**Output:** 2, 5, 3

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

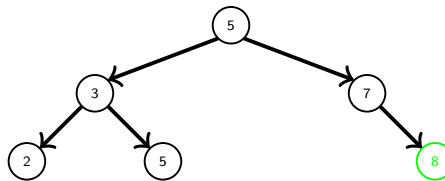


**Output:** 2, 5, 3

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

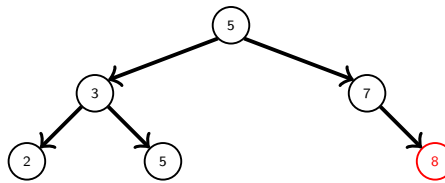


**Output:** 2, 5, 3

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

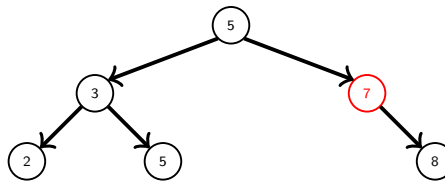


**Output:** 2, 5, 3, 8

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

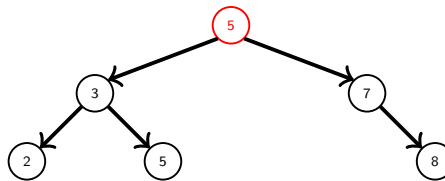


**Output:** 2, 5, 3, 8, 7

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

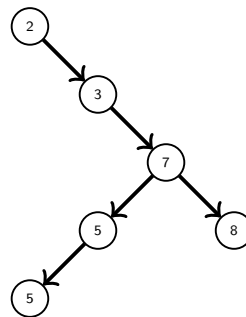


**Output:** 2, 5, 3, 8, 7, 5

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

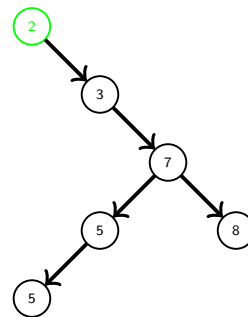


**Output:**

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```



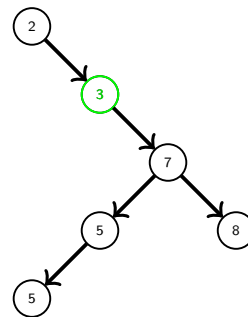
**Output:**



# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

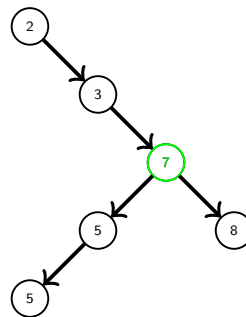


**Output:**

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

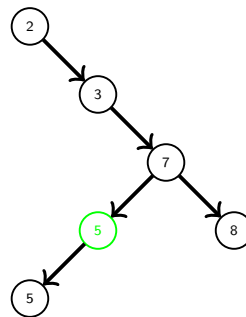


**Output:**

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

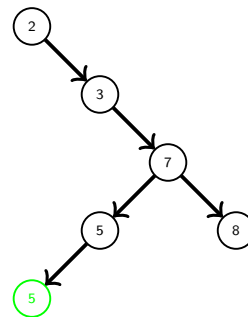


**Output:**

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

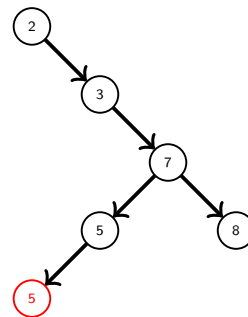


**Output:**

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

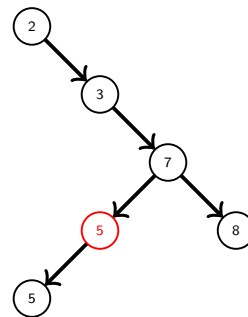


**Output: 5**

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

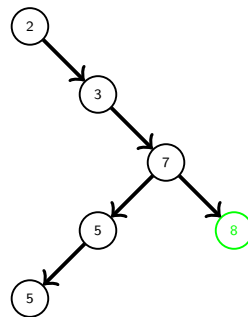


**Output:** 5, 5

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

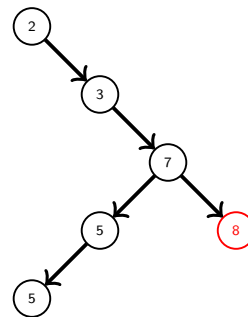


**Output:** 5, 5

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```



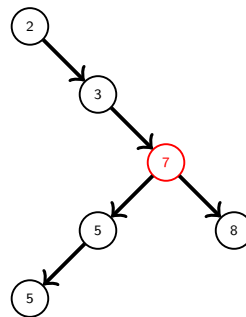
**Output:** 5, 5, 8



# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

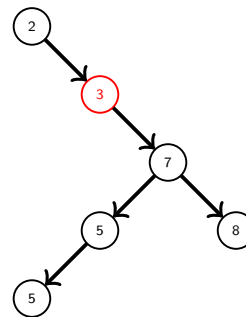


**Output:** 5, 5, 8, 7

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```

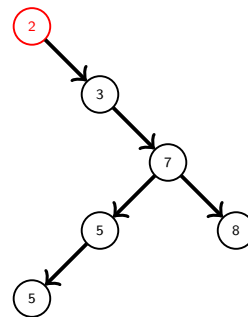


**Output:** 5, 5, 8, 7, 3

# Post-order Traversal

- left, right, **root**.
- The nodes are visited in left, right, root fashion.

```
/* preorder display */  
void display (Node *pRoot) {  
    if (pRoot!=null) {  
        display (pRoot->pLeft);  
        display (root->pRight);  
        printf ("%d, ", pRoot->nData);  
    }  
}
```



**Output:** 5, 5, 8, 7, 3, 2

## POST-ORDER-TREE-WALK( $root[T]$ )

**I/P:** The root of a binary tree  $T$ .

Begin

if  $x \neq \mathbf{nil}$  then

    IN-ORDER-TREE-WALK( $left[x]$ );

    IN-ORDER-TREE-WALK( $right[T]$ );

    print  $Key[x]$ ;

else

    return FLAG;

End

**Complexity:**

## POST-ORDER-TREE-WALK( $root[T]$ )

**I/P:** The root of a binary tree  $T$ .

Begin

if  $x \neq \mathbf{nil}$  then

    IN-ORDER-TREE-WALK( $left[x]$ );

    IN-ORDER-TREE-WALK( $right[T]$ );

    print  $Key[x]$ ;

else

    return FLAG;

End

**Complexity:**  $\Theta(n)$ , where  $n = \#$  nodes.

# Tree Traversals

- Different trees may have same **in-order traversal**.
- Similarly, there can be many trees whose **pre-order traversals** and **post-order traversals** are same.
- A tree **cannot** be reconstruct from just one traversal sequence.
- But, given two traversals one can reconstruct the tree uniquely.

Thank You for your kind attention!

## Books Consulted

- ① Chapter 4.3.3 of *Introduction to Algorithms: A Creative Approach* by [Udi Manber](#).
- ② Chapter 12 of *Introduction to Algorithms* by [Thomas H Cormen](#), [Charles E Leiserson](#), [Ronald L Rivest](#), [Clifford Stein](#).



Thank You for your kind attention!

Questions!!