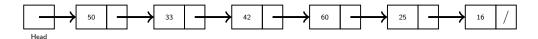
# Singly (Cont.), Doubly Linked Lists and Circular Linked Lists

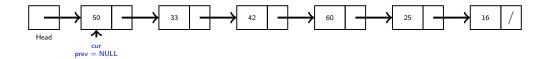
#### Subhabrata Samajder



IIIT, Delhi Winter Semester, 29<sup>th</sup> March, 2023 Reversing a Linked List

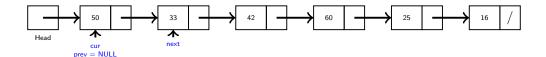


- Use 3 pointers: prev, cur, next
- Start with pointing cur to first node, and prev = NULL.



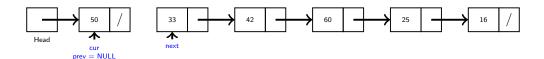
```
Node *prev = NULL, *cur = NULL, *next = NULL; cur = pFront;
```

- Use 3 pointers: prev, cur, next
- Start with pointing cur to first node, and prev = NULL.
- Traverse the list in a while loop till cur = NULL.
  - Set next = cur->pNext.



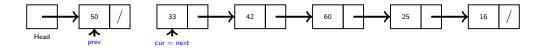
```
Node *prev = NULL, *cur = NULL, *next = NULL;
cur = pFront;
while (cur != NULL) {
   next = cur->pNext;
```

- Use 3 pointers: prev, cur, next
- Start with pointing cur to first node, and prev = NULL.
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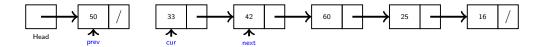
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Node *prev = NULL, *cur = NULL, *next = NULL;
cur = pFront;
while (cur != NULL) {
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```

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- Start with pointing cur to first node, and prev = NULL.
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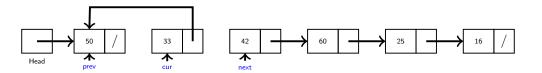
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Node *prev = NULL, *cur = NULL, *next = NULL;
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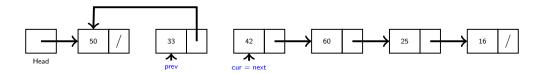
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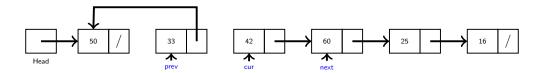
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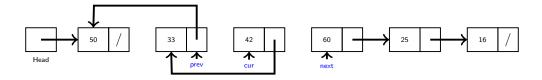
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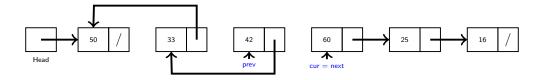
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cur = pFront;
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- Traverse the list in a while loop till cur = NULL.
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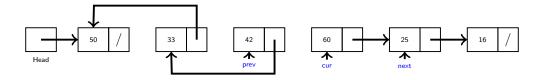
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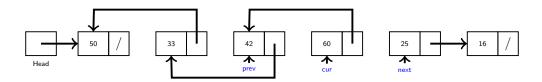
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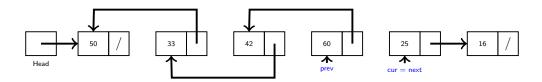
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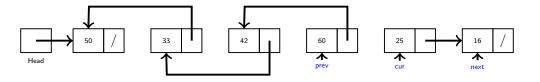
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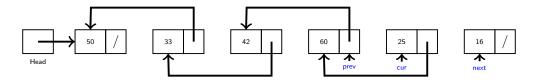
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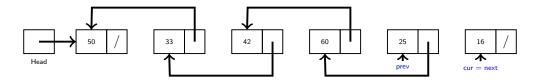
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while (cur != NULL) {
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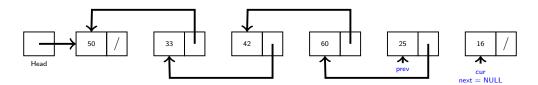
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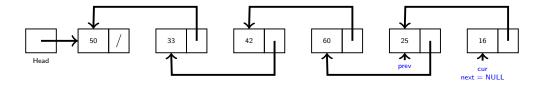
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cur = pFront;
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```

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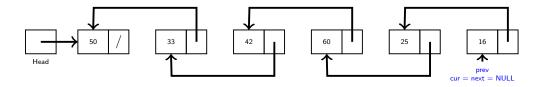
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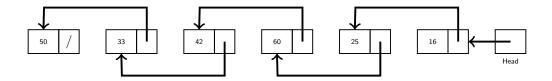
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cur = pFront;
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```
Node *prev = NULL, *cur = NULL, *next = NULL;
cur = pFront;
while (cur != NULL) {
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  cur->pNext = prev;
  prev = cur;
  cur = next; }
```

- Use 3 pointers: prev, cur, next
- Start with pointing cur to first node, and prev = NULL.
- Traverse the list in a while loop till cur = NULL.
- Set link for Front = prev.



```
Node *prev = NULL, *cur = NULL, *next = NULL;
cur = pFront;
while (cur != NULL) {
  next = cur->pNext;
  cur->pNext = prev;
  prev = cur;
  cur = next; }
pFront = prev;
```

#### Exercises

- Create a list with each node contain names of student and their CGPA.
- ② Given the above list, find the name of the student having the highest CGPA.
- Given a list, create two lists with alternate elements of first list.
- Append a list at end of another list.
- Oheck if two lists are identical.

Storing Polynomials in a Linked Lists

# Advantages of Linked lists

- Dynamic in nature. Memory allocated at run time.
- Insertion and Deletions are constant time operations (without the searching).
- No need to shift nodes as was necessary with arrays.
- Other data structures like queues, stacks are easily implemented using linked lists

# Polynomials

**Problem:** Add the polynomials

$$5 + 2x + 3x^{2}$$
,  
 $7x + 8$ ,  
 $13 + 9x + 3x^{2}$ .

# Polynomials

**Problem:** Add the polynomials

$$5 + 2x + 3x^{2}$$
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 $7x + 8$ ,  
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**Note:** We need to store only the coefficients and the exponents.

# Storing Polynomials Using Arrays

• **Polynomial:**  $5 + 2x + 3x^2$ 

**Array:** [5 2 3]

• Polynomial: 7x + 8

**Array:** [8 7 0]

# Storing Polynomials Using Arrays

• **Polynomial:**  $5 + 2x + 3x^2$ 

**Array:** [5 2 3]

• Polynomial: 7x + 8

**Array:** [8 7 0]

• That is, store only the coefficients in proper place.

# Issues in Storing Polynomials Using Arrays

• Polynomial:  $5 + 2x + 3x^2 + 6x^5$ Array:  $[5 \ 2 \ 3 \ 0 \ 0 \ 6]$ 

• Polynomial:  $5 + 2x + 3x^2 + 7x^{31}$ Array:  $\begin{bmatrix} 5 & 2 & 3 & 0 & 0 & 0 & \cdots & 0 & 7 \end{bmatrix}$ 

Need to store so many zeroes in a very large sized array

# Storing Polynomials Using Linked Lists

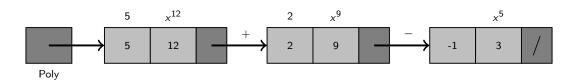
- Let us now see how two polynomials can be added.
- Let  $P_1$  and  $P_2$  be two polynomials
  - stored as linked lists
  - Each node contains exponent and coefficients values
  - in sorted (decreasing) order of exponents

• Addition Operation: Add terms of like-exponents.

# Representing a Polynomial Using a Linked List

Store the coefficient and exponent of each term in nodes

```
int item1[] = \{5, 12\};
int item2[] = \{2, 9\};
int item3[] = \{-1, 3\};
```

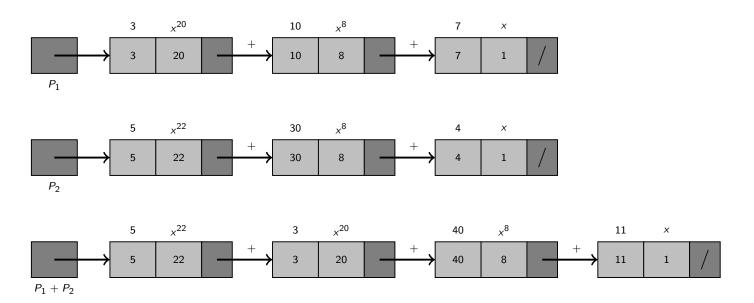


## Operations on Polynomials

- $P_1$  and  $P_2$  are stored as linked lists and are arranged in decreasing order of exponents.
- Scan these and add like terms.
- Store the resulting term only if it has non-zero coefficient.
- The number of terms in the result  $(P_1 + P_2)$  need not be known in advance.
- Uses as much space as there are terms in  $P_1 + P_2$ .

# Addition of Two Polynomials

One pass down each list: O(n+m).



# Multiplication of Two Polynomials

• Can be done as repeated addition.

• So, multiply  $P_1$  with each term of  $P_2$ .

Add the resulting polynomials.

**Doubly Linked Lists** 

## **Doubly Linked Lists**

Permits traversal of list in both directions.

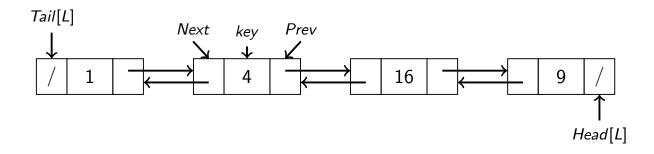
- Useful where navigation in both directions needed.
- Used by browsers to navigate forwards and backwards.
- Various applications use this for redo and undo functionalities.

## Doubly Linked List (Cont.)

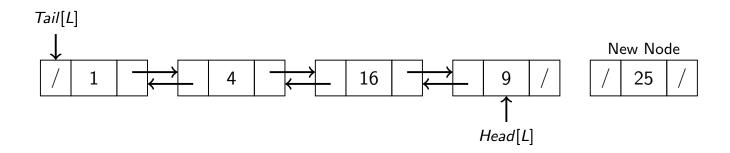
- Each element of a doubly linked list L is an object x with a key (or data) field and two other pointer fields:
  - next[x] points to it successor in the linked list and
  - prev[x] points to its predecessor.
- Head of L: If prev[x] = nil.
- Tail of L: If next[x] = nil.
- head[L]: Points to the first element of the list L.
- tail[L]: Points to the last element of the list L.
- **Empty List:** If head[L] = nil.

# C Implementation of a Doubly Linked List Node

```
typedef struct DLNode {
  int nKey;
  struct DLNode *pPrev, *pNext;
} DLNode;
```

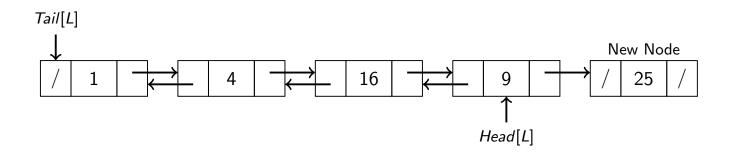


• Create a new node x.



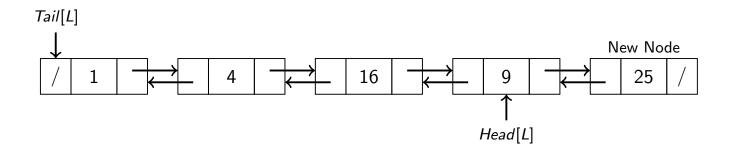
```
DLNode *pTemp;
pTemp = (DLNode *)malloc(sizeof(DLNode));
pTemp->nKey = 25;
pTemp->pPrev = NULL;
pTemp->pNext = NULL;
```

- Create a new node x.
- head[L].prev = x.



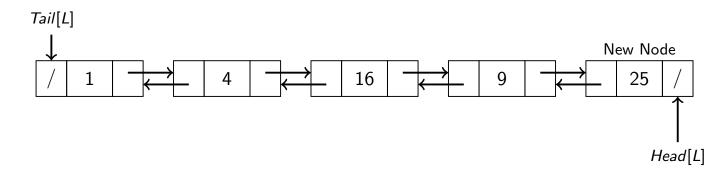
```
DLNode *pTemp;
pTemp = (DLNode *)malloc(sizeof(DLNode));
pTemp->nKey = 25;
pTemp->pPrev = NULL;
pTemp->pNext = NULL;
pHead->pPrev = pTemp;
```

- Create a new node x.
- head[L].prev = x.
- x.next = head[L].



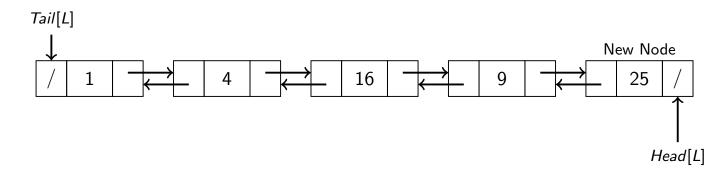
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pTemp->pPrev = NULL;
pTemp->pNext = NULL;
pHead->pPrev = pTemp;
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- Create a new node x.
- head[L].prev = x.
- x.next = head[L].
- head[L] = x.



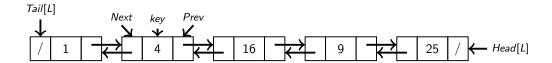
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pHead->pPrev = pTemp;
pTemp->pNext = pHead;
pHead = pTemp;
```

- Create a new node x.
- head[L].prev = x.
- x.next = head[L].
- head[L] = x.

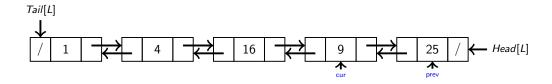


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pHead = pTemp;
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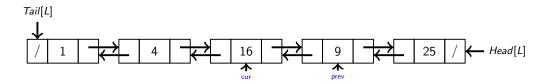
- Assume that the list is of length at least 2.
- Let d = 4.



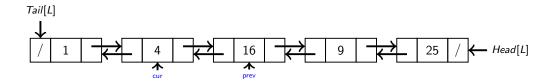
- Assume that the list is of length at least 2.
- Let d = 4.
- Set pointer prev to the first and cur to the second node.



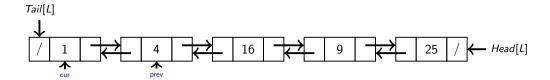
- Assume that the list is of length at least 2.
- Let d = 4.
- Set pointer prev to the first and cur to the second node.
- Traverse until prev->nKey = 4.



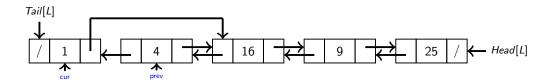
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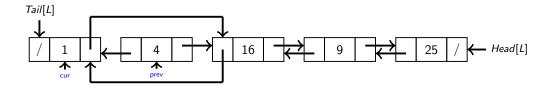
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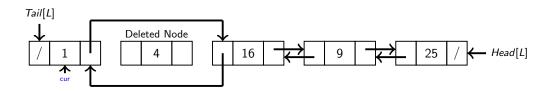
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- Let d = 4.
- Set pointer prev to the first and cur to the second node.
- Traverse until prev->nKey = 4.
- Set cur->pPrev = prev->pPrev.



- Assume that the list is of length at least 2.
- Let d = 4.
- Set pointer prev to the first and cur to the second node.
- Traverse until prev->nKey = 4.
- Set cur->pPrev = prev->pPrev.
- Set prev->pPrev->pNext = cur.



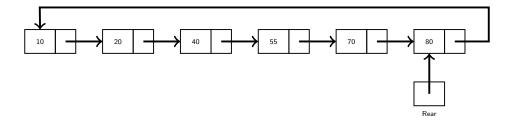
- Assume that the list is of length at least 2.
- Let d = 4.
- Set pointer prev to the first and cur to the second node.
- Traverse until prev->nKey = 4.
- Set cur->pPrev = prev->pPrev.
- Set prev->pPrev->pNext = cur.
- Set free(prev).



#### Circular Linked Lists

## Circular Linked Lists

- A Circular Linked List is a special type of Linked List
- It supports traversing from the end of the list to the beginning by making the last node point back to the head of the list.
- A Rear pointer is often used instead of a Head pointer.



## Motivation

• Usually sorted.

• Useful for playing video and sound files in "looping" mode.

• They are also a stepping stone for implementing graphs.

## Circular Linked List Operations

insertNode(Node \*Rear, int item)//adds a new node to ordered circular linked list

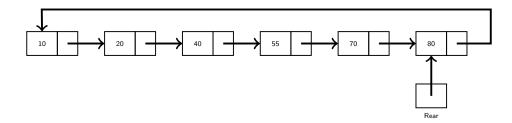
deleteNode(Node \*Rear, int item)//removes a node from circular linked list

print(Node \*Rear)//print the Circular Linked List once

## Traversing a Circular Linked List

```
void print(Node *Rear){
  Node *Cur;

if(Rear != NULL){
    Cur = Rear->pNext;
    do{
       printf("%d, ", Cur->nData);
       Cur = Cur->pNext;
    } while(Cur != Rear->pNext);
}
```



#### • Empty List:

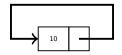
```
Note *New = NULL;

New = (Node *)malloc(sizeof(Node));

New->nData = 10;

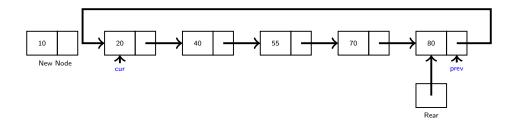
Rear = New;

Rear->pNext = Rear;
```



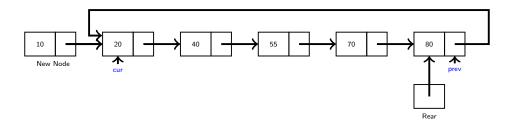
#### Inserting a Node at the Head:

```
Node *New = NULL;
New = (Node *)malloc(sizeof(Node));
New->nData = 10;
cur = Rear->pNext;
prev = Rear;
```



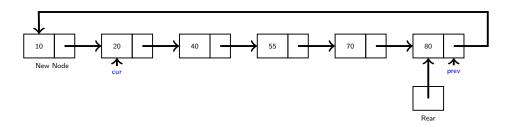
#### • Inserting a Node at the Head:

```
Node *New = NULL;
New = (Node *)malloc(sizeof(Node));
New->nData = 10;
cur = Rear->pNext;
prev = Rear;
New->pNext = Cur;
```



#### Inserting a Node at the Head:

```
Node *New = NULL;
New = (Node *)malloc(sizeof(Node));
New->nData = 10;
cur = Rear->pNext;
prev = Rear;
New->pNext = Cur;
Prev->pNext = New;
```



#### • Inserting a Node in the Middle:

```
Node *New = NULL;

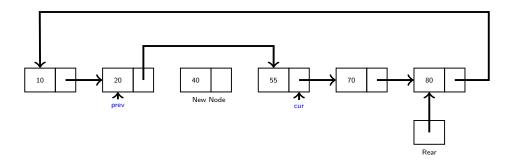
New = (Node *)malloc(sizeof(Node));

New->nData = 40;

cur = Rear.->pNext;

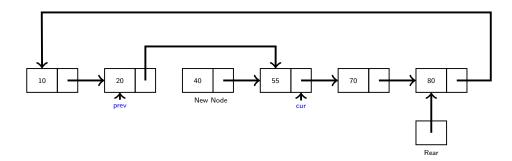
prev = Rear;

//Find the place to insert the node
```



#### Inserting a Node in the Middle:

```
Node *New = NULL;
New = (Node *)malloc(sizeof(Node));
New->nData = 40;
cur = Rear.->pNext;
prev = Rear;
//Find the place to insert the node
New->pNext = Cur;
```



#### Inserting a Node in the Middle:

```
Node *New = NULL;

New = (Node *)malloc(sizeof(Node));

New->nData = 40;

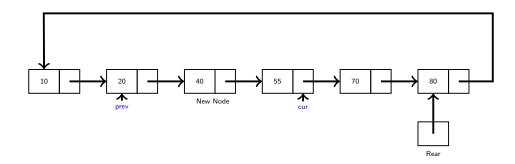
cur = Rear.->pNext;

prev = Rear;

//Find the place to insert the node

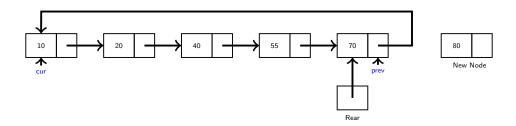
New->pNext = Cur;

Prev->pNext = New;
```



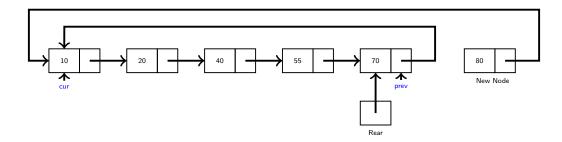
#### • Inserting a Node at the End:

```
Node *New = NULL;
New = (Node *)malloc(sizeof(Node));
New->nData = 80;
cur = Rear->pNext;
prev = Rear;
```



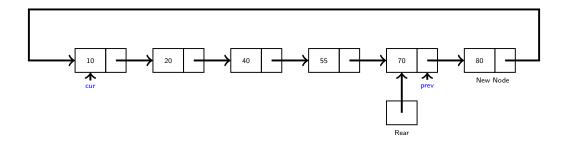
#### Inserting a Node at the End:

```
Node *New = NULL;
New = (Node *)malloc(sizeof(Node));
New->nData = 80;
cur = Rear->pNext;
prev = Rear;
New->pNext = Cur;
```



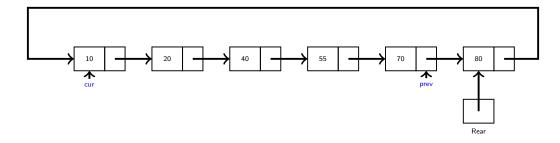
#### • Inserting a Node at the End:

```
Node *New = NULL;
New = (Node *)malloc(sizeof(Node));
New->nData = 80;
cur = Rear->pNext;
prev = Rear;
New->pNext = Cur;
Prev->pNext = New;
```



## • Inserting a Node at the End:

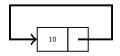
```
Node *New = NULL;
New = (Node *)malloc(sizeof(Node));
New->nData = 80;
cur = Rear->pNext;
prev = Rear;
New->pNext = Cur;
Prev->pNext = New;
Rear = New;
```



## Delete Node

#### • List of Size 1:

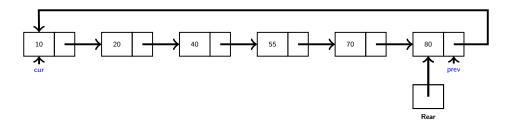
```
\begin{aligned} & \mathsf{free}(\mathsf{Rear}); \\ & \mathsf{Rear} = \mathsf{NULL}; \end{aligned}
```



## Delete Node

## • Deleting the Head Node:

```
\begin{aligned} &\mathsf{cur} = \mathsf{Rear}\text{-}\!\!>\!\! \mathsf{pNext};\\ &\mathsf{prev} = \mathsf{Rear}; \end{aligned}
```

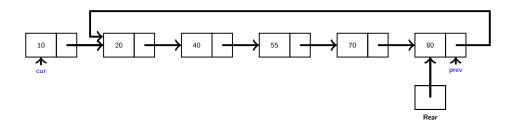


#### • Deleting the Head Node:

```
cur = Rear->pNext;

prev = Rear;

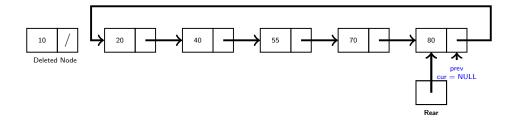
prev->pNext = cur->pNext;
```



#### Deleting the Head Node:

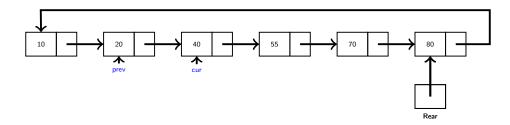
```
cur = Rear->pNext;
prev = Rear;

prev->pNext = cur->pNext;
free(cur);
cur = NULL;
```



#### • Deleting a Middle Node:

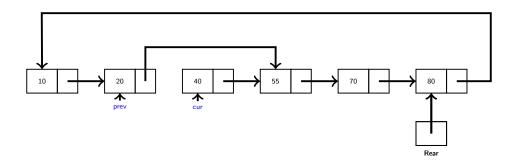
```
\label{eq:cur} \begin{split} & \mathsf{cur} = \mathsf{Rear}{-}\mathsf{>}\mathsf{pNext}; \\ & \mathsf{prev} = \mathsf{Rear}; \\ & //\mathsf{Find} \ \mathsf{the} \ \mathsf{node} \ \mathsf{to} \ \mathsf{delete} \end{split}
```



#### • Deleting a Middle Node:

```
cur = Rear->pNext;
prev = Rear;

//Find the node to delete
prev->pNext = Cur->pNext;
```

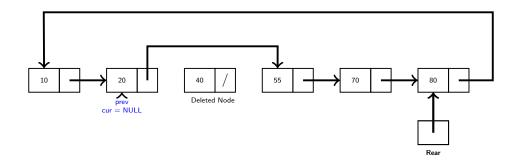


#### • Deleting a Middle Node:

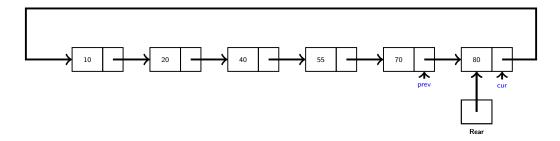
```
cur = Rear->pNext;
prev = Rear;

//Find the node to delete

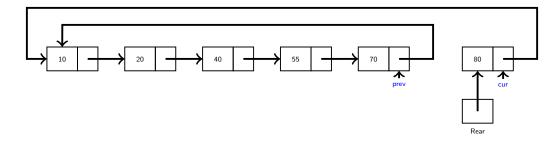
prev->pNext = Cur->pNext;
free(cur);
cur = NULL;
```



```
\begin{split} &\text{cur} = \text{Rear->pNext;} \\ &\text{prev} = \text{Rear;} \\ &\text{//Traverse till the end of the list, i.e., till cur} == \text{Rear} \end{split}
```

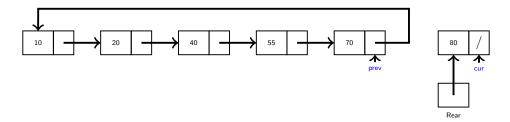


```
\label{eq:cur} \begin{split} &cur = Rear->pNext;\\ &prev = Rear;\\ &//Traverse \ till \ the \ end \ of \ the \ list, \ i.e., \ till \ cur == Rear\\ &prev->pNext = cur->pNext; \end{split}
```



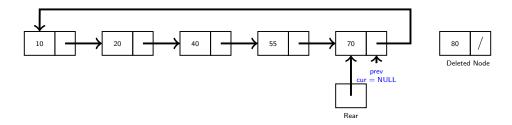
```
cur = Rear->pNext;
prev = Rear;

//Traverse till the end of the list, i.e., till cur == Rear
prev->pNext = cur->pNext;
free(cur);
```



```
cur = Rear->pNext;
prev = Rear;

//Traverse till the end of the list, i.e., till cur == Rear
prev->pNext = cur->pNext;
free(cur);
Rear = prev;
cur = NULL
```



#### Exercises

Assuming that there can exists at most one loop in a singly linked list, find an algorithm to determine whether a single linked list has a loop or not.

## **Books Consulted**

• Chapter 10.2 of *Introduction to Algorithms* by Thomas H Cormen, Charles E Leiserson, Ronald L Rivest, Clifford Stein.

Thank You for your kind attention!

# Questions!!