

The image is a cover for a business report. It features a dark background with a blurred image of a person in a suit. Overlaid on the image are various digital and data-related graphics. In the upper right, there's a hexagonal grid with some cells highlighted in yellow. Below it, a hand is shown interacting with a digital interface, with a line graph and a bar chart visible. To the right of the hand, there's a digital display showing '180 pts'. In the lower left, a hand is holding a small globe. The entire image is bisected by a diagonal white line. The text 'BUSINESS REPORT' is written in a blue, outlined font across the middle.

BUSINESS REPORT

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Objective:

Problem 1:

To investigate the correlation between foot injuries and player positions within a male football team, aiming to provide insights into injury patterns that may inform targeted preventive measures and optimize player performance and well-being.

Problem 2:

To analyse the breaking strength distribution of gunny bags used for packaging cement, characterized by a normal distribution with a mean of 5 kg per sq. cm and a standard deviation of 1.5 kg per sq. cm. The aim is to address inquiries related to the quality and durability of the packaging material, thereby enhancing insights into potential wastage or pilferage within the supply chain.

Problem 3:

To assess the Brinell's hardness index of a batch of stones received by Zingaro Stone Printing, aiming to determine their suitability for achieving the desired printing quality. The objective is to ensure that the stone surfaces meet the minimum requirement of a Brinell's hardness index of at least 150, thereby enabling optimal image printing quality and maintaining client satisfaction standards.

Problem 4:

To analyse dental implant data, investigating the influence of various factors—including implant method, treatment temperature, alloy composition, and dentist preference—on the hardness of metal implants within dental cavities. The aim is to discern patterns and dependencies that contribute to variations in implant hardness, thereby facilitating informed decision-making for optimizing dental implant procedures and outcomes.

Problem 1:

1.1 probability that a randomly chosen player would suffer an injury:

The probability that a randomly chosen player would suffer an injury is 0.6170212765957447

Probability of a Randomly Chosen Player Suffering an Injury

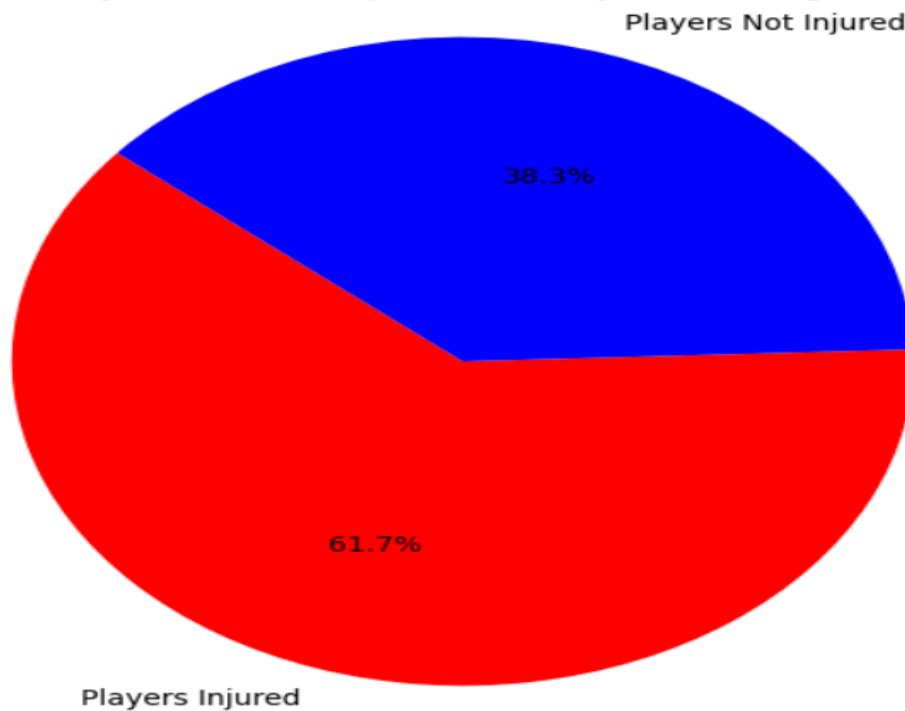


Fig 1.1

1.2 probability that a player is a forward or a winger:

The probability that a player is a forward or a winger 0.5234042553191489.

Probability Visualization

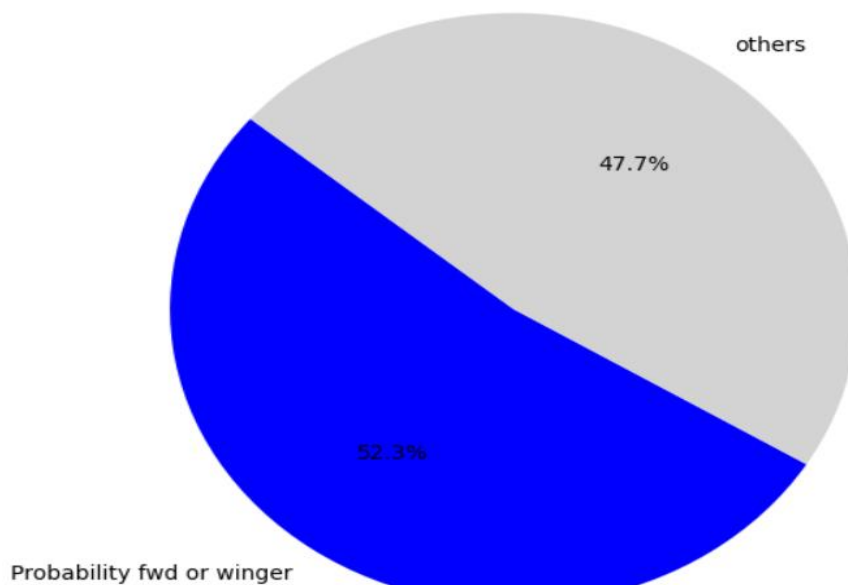


Fig 1.2

1.3 probability that a randomly chosen player plays in a striker position and has a foot injury:

Probability of a randomly chosen player being a striker and having a foot injury: 0.19148936170212766.

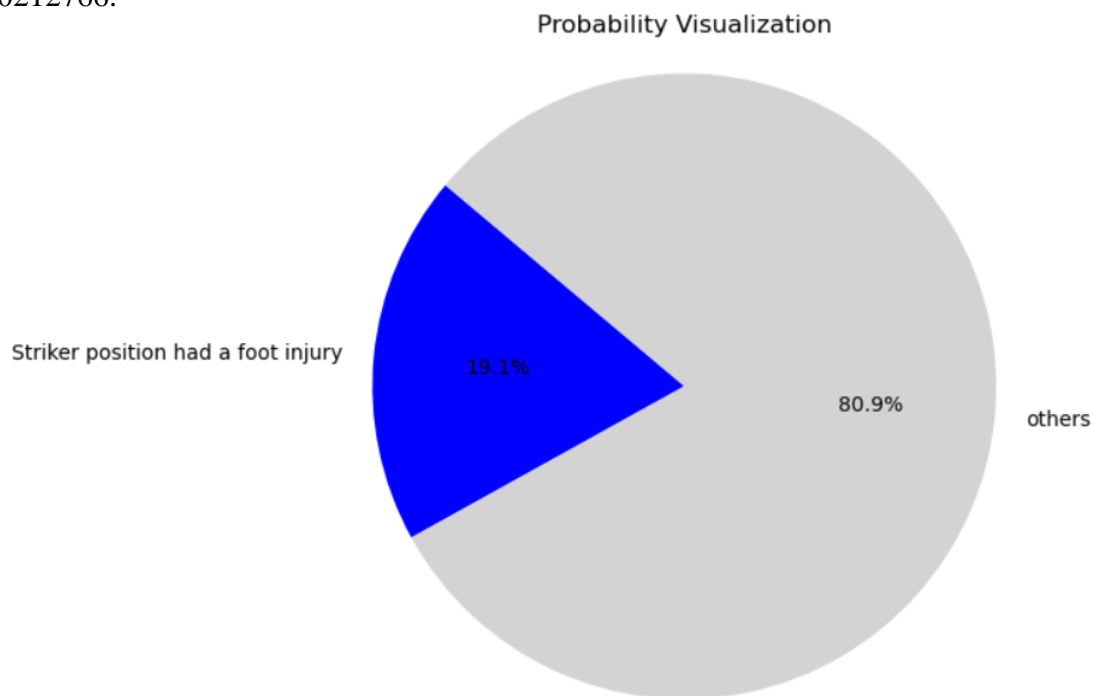


Fig 1.3

1.4 probability that a randomly chosen injured player is a striker:

The probability that a randomly chosen injured player is a striker 0.3103448275862069

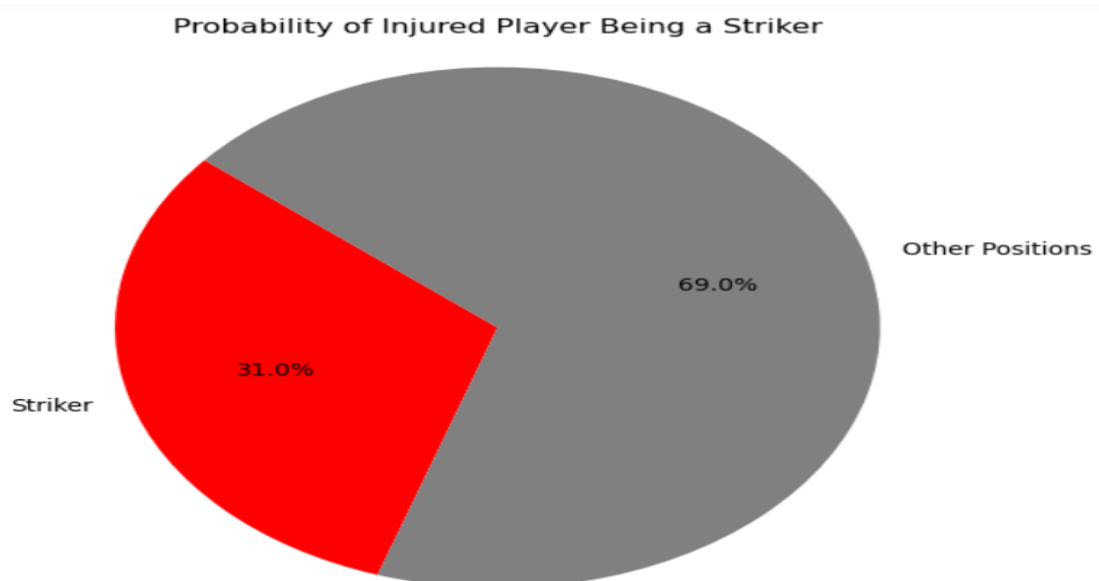
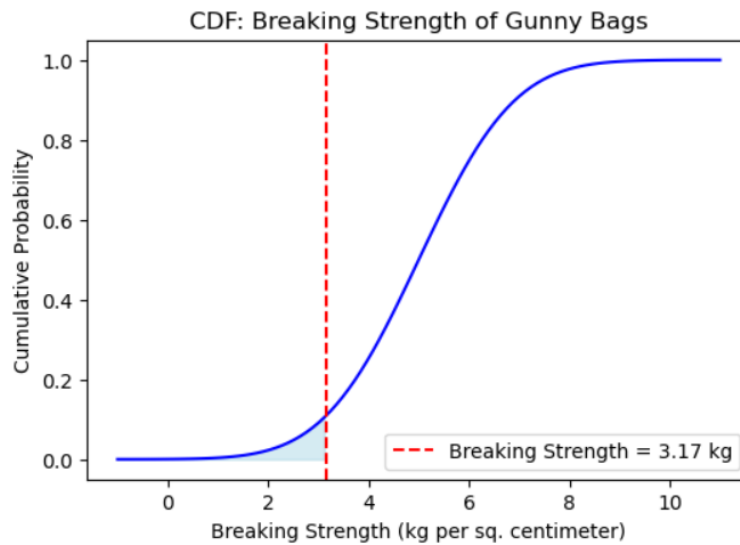


Fig 1.4

Problem 2:

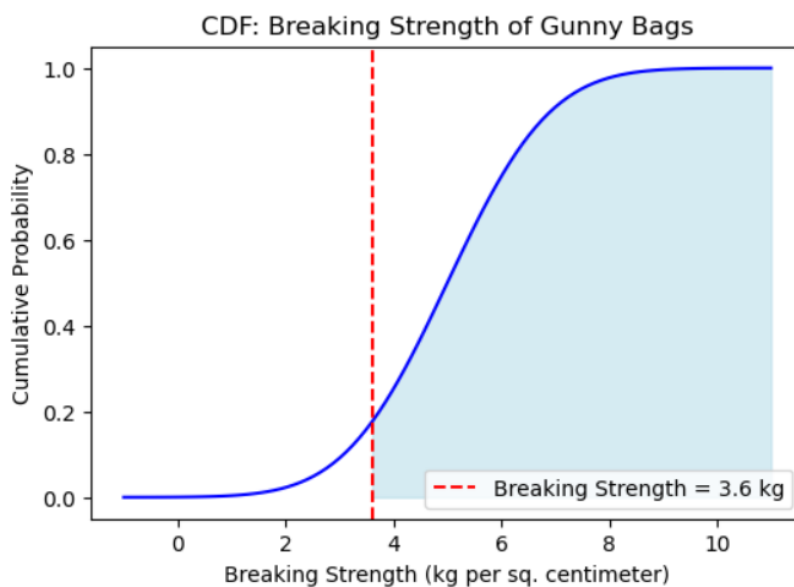
2.1 Proportion of the gunny bags have a breaking strength of less than 3.17 kg per square cm:



Proportion of gunny bags with a breaking strength of less than 3.17 kg per sq cm: 0.11123243744783456

Fig 2.1

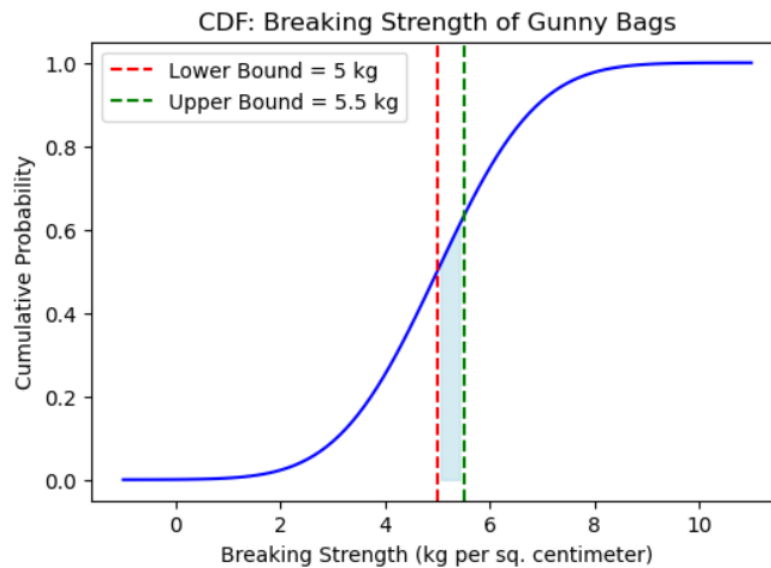
2.2 Proportion of the gunny bags have a breaking strength of at least 3.6 kg per square cm:



Proportion of gunny bags with a breaking strength of at least 3.6 kg per sq cm: 0.8246760551477705

Fig 2.2

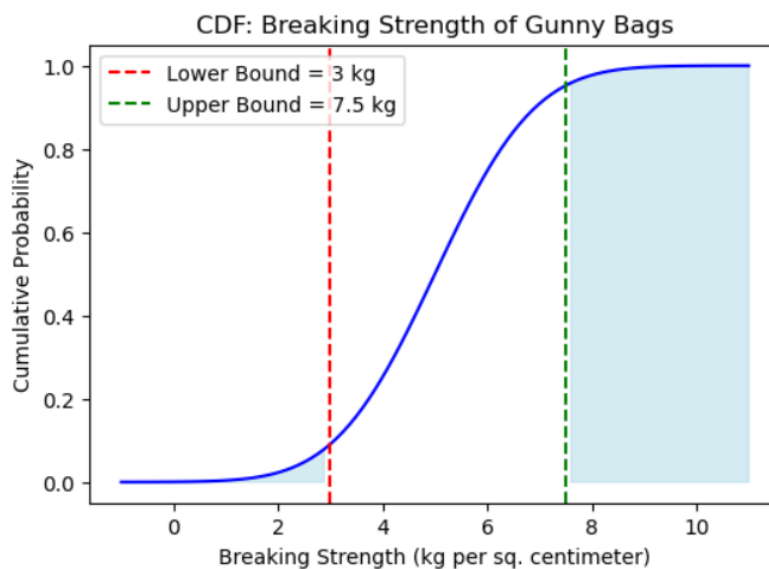
2.3 Proportion of the gunny bags have a breaking strength between 5 and 5.5 kg per square cm:



Proportion of gunny bags with breaking strength between 5 and 5.5 kg per sq cm: 0.13055865981823633

Fig 2.3

2.4 Proportion of the gunny bags have a breaking strength NOT between 3 and 7.5 kg per square cm.



Proportion of gunny bags with breaking strength NOT between 3 and 7.5 kg per sq cm: 0.13900157199868257

Fig 2.4

Problem 3:

3.1 Zingaro has reason to believe that the unpolished stones may not be suitable for printing:

Null Hypothesis :

- The mean Brinell's hardness index of unpolished stones is equal to or greater than 150 (suitable for printing).

Alternative Hypothesis:

- The mean Brinell's hardness index of unpolished stones is less than 150 (not suitable for printing).

Fig 3.1.1

Loaded the required file. The dataset consists of 75 rows and 2 columns.

	Unpolished	Treated and Polished
0	164.481713	133.209393
1	154.307045	138.482771
2	129.861048	159.665201
3	159.096184	145.663528
4	135.256748	136.789227
...
70	123.067611	142.293544
71	171.822218	140.124092
72	88.135994	141.393091
73	145.150397	131.370530
74	170.854823	144.502647

75 rows × 2 columns

Table 3.1.1

RangeIndex: 75 entries, 0 to 74

Data columns (total 2 columns):

#	Column	Non-Null Count	Dtype
0	Unpolished	75 non-null	float64
1	Treated and Polished	75 non-null	float64

dtypes: float64(2)
memory usage: 1.3 KB

Fig 3.1.2

Test Statistic: -4.164629601426757

P-value: 8.342573994839304e-05

Reject the null hypothesis. There is sufficient evidence to conclude that the mean Brinell's hardness index of unpolished stones is less than 150.

Rejected the Null Hypothesis

Fig 3.1.3

3.2 Is the mean hardness of the polished and unpolished stones the same:

Null Hypothesis :

- The mean hardness of polished stones is equal to the mean hardness of unpolished stones.

Alternative Hypothesis :

- The mean hardness of polished stones is not equal to the mean hardness of unpolished stones.

Fig 3.2.1

Test Statistic: 3.2422320501414053

P-value: 0.0014655150194628353

Reject the null hypothesis. There is sufficient evidence to conclude that the mean hardness of polished and unpolished stones is not the same.

Fig 3.2.2

Problem 4:

4.1 Hardness of implants vary depending on dentists:

Loaded the required file, loaded the data. The dataset consists of 107 rows and 14 columns.

	Dentist	Method	Alloy	Temp	Response	Unnamed: 5	Unnamed: 6	Unnamed: 7	Unnamed: 8	Unnamed: 9	Unnamed: 10	Unnamed: 11	Unnamed: 12	Unnamed: 13
0	1.0	1.0	1.0	1500.0	813.0	NaN	NaN	Anova: Two-Factor Without Replication	NaN	NaN	NaN	NaN	NaN	NaN
1	1.0	1.0	1.0	1600.0	792.0	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN
2	1.0	1.0	1.0	1700.0	792.0	NaN	NaN	SUMMARY	Count	Sum	Average	Variance	NaN	NaN
3	1.0	1.0	2.0	1500.0	907.0	NaN	NaN	1	4	2315	578.75	523721.583333	NaN	NaN
4	1.0	1.0	2.0	1600.0	792.0	NaN	NaN	1	4	2394	598.5	584819	NaN	NaN
...
102	NaN	NaN	NaN	NaN	NaN	NaN	NaN	Rows	513114.013889	89	5765.325999	0.778206	0.917216	NaN
103	NaN	NaN	NaN	NaN	NaN	NaN	NaN	Columns	156164270.208333	3	52054756.736111	7026.375161	0.0	NaN
104	NaN	NaN	NaN	NaN	NaN	NaN	NaN	Error	1978064.041667	267	7408.479557	NaN	NaN	NaN
105	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN
106	NaN	NaN	NaN	NaN	NaN	NaN	NaN	Total	158655448.263889	359	NaN	NaN	NaN	NaN

107 rows x 14 columns

Table 4.1.1

```
RangeIndex: 107 entries, 0 to 106
Data columns (total 14 columns):
#   Column                Non-Null Count  Dtype
---  -
0   Dentist                90 non-null    float64
1   Method                 90 non-null    float64
2   Alloy                  90 non-null    float64
3   Temp                   90 non-null    float64
4   Response               90 non-null    float64
5   Unnamed: 5             0 non-null     float64
6   Unnamed: 6             0 non-null     float64
7   Unnamed: 7             102 non-null   object
8   Unnamed: 8             100 non-null   object
9   Unnamed: 9             100 non-null   object
10  Unnamed: 10            99 non-null    object
11  Unnamed: 11            98 non-null    object
12  Unnamed: 12            3 non-null     object
13  Unnamed: 13            3 non-null     object
dtypes: float64(7), object(7)
memory usage: 11.8+ KB
```

Fig 4.1.1

State the null and alternate hypotheses

Null and Alternative Hypotheses:

Null Hypothesis :

- There is no difference in the mean hardness of implants among different dentists.

Alternative Hypothesis:

- There is a difference in the mean hardness of implants among different dentists.

Fig 4.1.2

Check the assumptions of the hypothesis test.

Shapiro-Wilk Normality Test Results:

Dentist 1.0: p-value = 0.1856756955385208

Dentist 2.0: p-value = 0.7310513854026794

Dentist 3.0: p-value = 0.5520960092544556

Dentist 4.0: p-value = 0.002037237398326397

Dentist 5.0: p-value = 0.5022943019866943

Levene's Test for Homogeneity of Variances:

Test Statistic: 3.7082282441933954

P-value: 0.007858817382355401

Fig 4.1.3

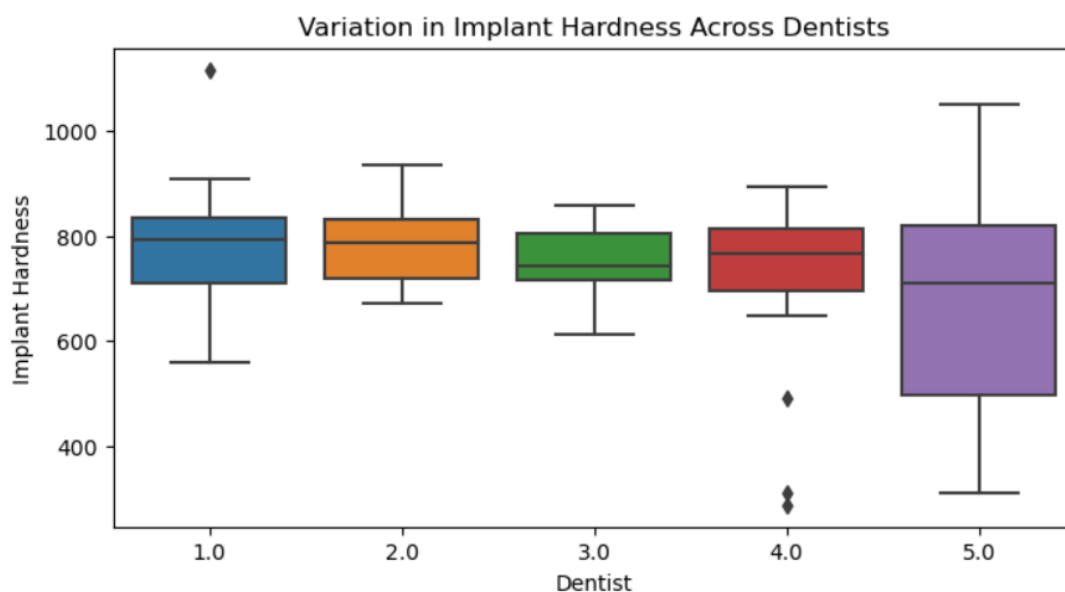


Fig 4.1.4

Conduct the hypothesis test and compute the p-value and write down conclusions from the test results.

One-way ANOVA Test Results:

F-statistic: 1.9345366474464367

P-value: 0.11206595023098852

The p-value is greater than or equal to the significance level, indicating no significant differences exist among dentists in terms of implant hardness.

Hypothesis Test:

One-way ANOVA Test: The p-value obtained is approximately 0.112, which is greater than the significance level of 0.05. Therefore, we fail to reject the null hypothesis. This indicates that there are no significant differences in implant hardness among the different dentists.

Conclusion:

Based on the results of the hypothesis test, we conclude that there are no significant differences in implant hardness among the different dentists.

Fig 4.1.5

There is no sufficient data for Alloy type 1&2.

4.2 Hardness of implants vary depending on methods:

State the null and alternate hypotheses.

Null Hypothesis :

- The mean hardness of implants is the same across all methods.

Alternative Hypothesis :

- The mean hardness of implants varies depending on the method used.

Fig 4.2.1

Check the assumptions of the hypothesis test.

Shapiro-Wilk Normality Test Results:

Method 1.0: Shapiro-Wilk Statistic = 0.9652422666549683, P-value = 0.41838711500167847

Method 2.0: Shapiro-Wilk Statistic = 0.9371030926704407, P-value = 0.07601878046989441

Method 3.0: Shapiro-Wilk Statistic = 0.9091948866844177, P-value = 0.014201466925442219

Levene's Test for Homogeneity of Variances:

Test Statistic: 5.848571977210466

P-value: 0.004138452940152019

Fig 4.2.2

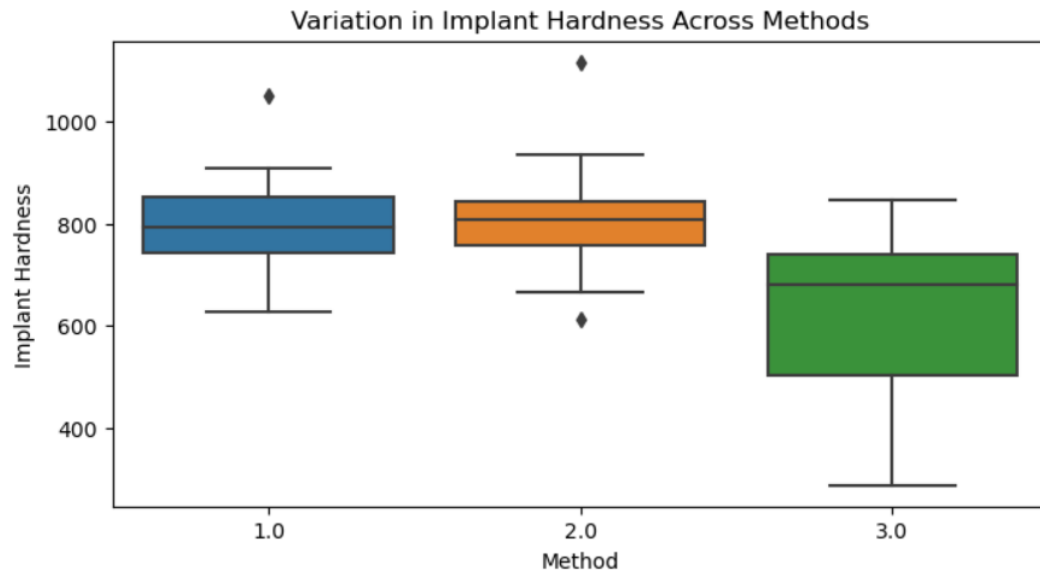


Fig 4.2.3

Conduct the hypothesis test and compute the p-value - Write down conclusions from the test results.

Welch's ANOVA Test Results:
F-statistic: 19.89268013119534
P-value: 7.683891892977992e-08

Conclusion:

P value : 7.683891892977992e-08

- ANOVA Test shows that there are statistically significant differences in hardness among the different methods of dental implantation. At least one pair of methods had significantly different hardness.
- Since the p-value is negligible we can reject the Null hypothesis.

Fig 4.2.4

separate analysis for the two types of alloys.

Games-Howell Post-Hoc Test Results for Alloy Type 1: Multiple Comparison of Means - Tukey HSD, FWER=0.05						
group1	group2	meandiff	p-adj	lower	upper	reject
1.0	2.0	-6.1333	0.987	-102.714	90.4473	False
1.0	3.0	-124.8	0.0085	-221.3807	-28.2193	True
2.0	3.0	-118.6667	0.0128	-215.2473	-22.086	True

Games-Howell Post-Hoc Test Results for Alloy Type 2: Multiple Comparison of Means - Tukey HSD, FWER=0.05						
group1	group2	meandiff	p-adj	lower	upper	reject
1.0	2.0	27.0	0.8212	-82.4546	136.4546	False
1.0	3.0	-208.8	0.0001	-318.2546	-99.3454	True
2.0	3.0	-235.8	0.0	-345.2546	-126.3454	True

Fig 4.2.5

The Games-Howell post-hoc test results for each group of alloys are as follows:

Alloy Type 1:

- There is a statistically significant difference in implant hardness between Method 1 and Method 3 (reject null hypothesis).
- There is a statistically significant difference in implant hardness between Method 2 and Method 3 (reject null hypothesis).
- There is no statistically significant difference in implant hardness between Method 1 and Method 2 (fail to reject null hypothesis).

Alloy Type 2:

- There is a statistically significant difference in implant hardness between Method 1 and Method 3 (reject null hypothesis).
- There is a statistically significant difference in implant hardness between Method 2 and Method 3 (reject null hypothesis).
- There is no statistically significant difference in implant hardness between Method 1 and Method 2 (fail to reject null hypothesis).

Fig 4.2.6

4.3 Interaction effect between the dentist and method:

Create Interaction Plot - Inferences from the plot

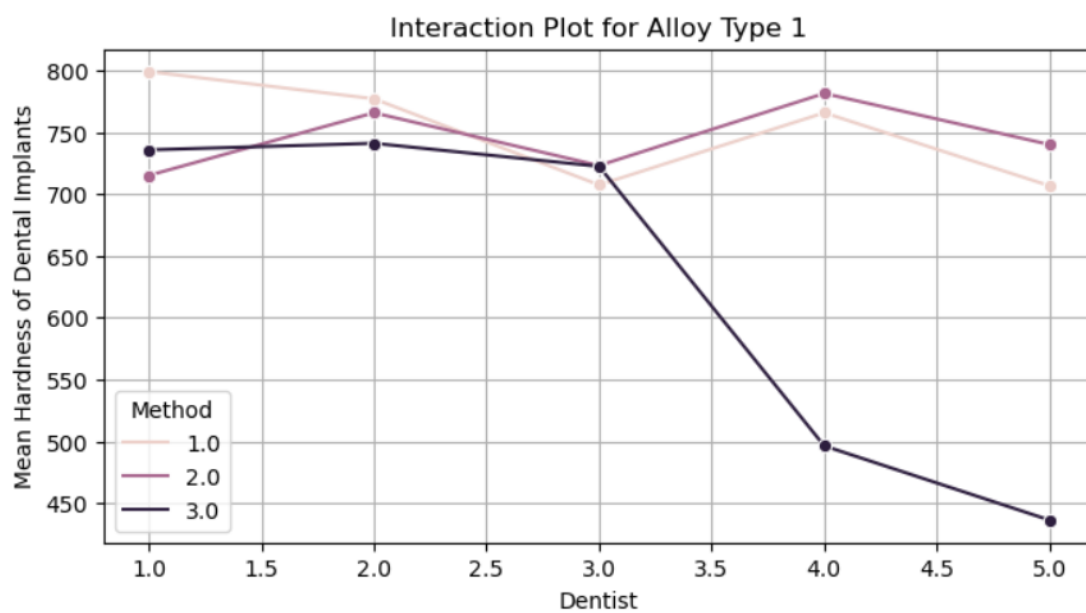
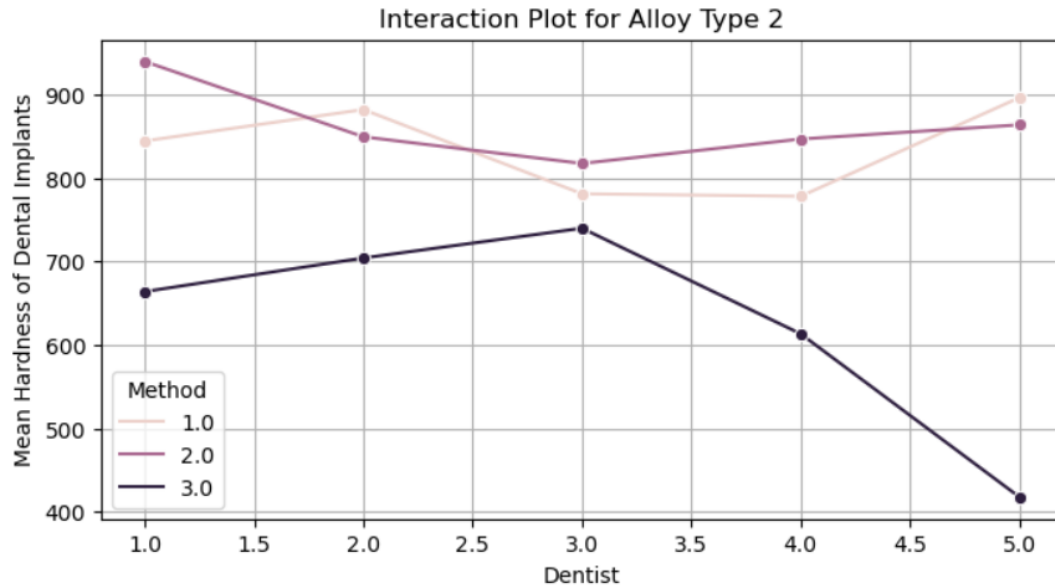


Fig 4.3.1



- Here we can see the mean hardness differs gradually among the dentists methods for both alloy types.

Fig 4.3.2

4.4 Hardness of implants vary depending on dentists and methods together:

State the null and alternate hypotheses.

Null Hypothesis :

- There is no interaction effect between dentists and methods on the hardness of implants.

Alternative Hypothesis :

- There is a significant interaction effect between dentists and methods on the hardness of implants.

Fig 4.4.1

Check the assumptions of the hypothesis test.

```
Dentist 1.0: Shapiro-Wilk p-value = 0.1856756955385208
Dentist 2.0: Shapiro-Wilk p-value = 0.7310513854026794
Dentist 3.0: Shapiro-Wilk p-value = 0.5520960092544556
Dentist 4.0: Shapiro-Wilk p-value = 0.002037237398326397
Dentist 5.0: Shapiro-Wilk p-value = 0.5022943019866943
Method 1.0: Shapiro-Wilk p-value = 0.41838711500167847
Method 2.0: Shapiro-Wilk p-value = 0.07601878046989441
Method 3.0: Shapiro-Wilk p-value = 0.014201466925442219
```

```
Levene's Test for Homogeneity of Variances:
Test Statistic: 3.9381047054545255
P-value: 0.0005175374842450017
```

Fig 4.4.2

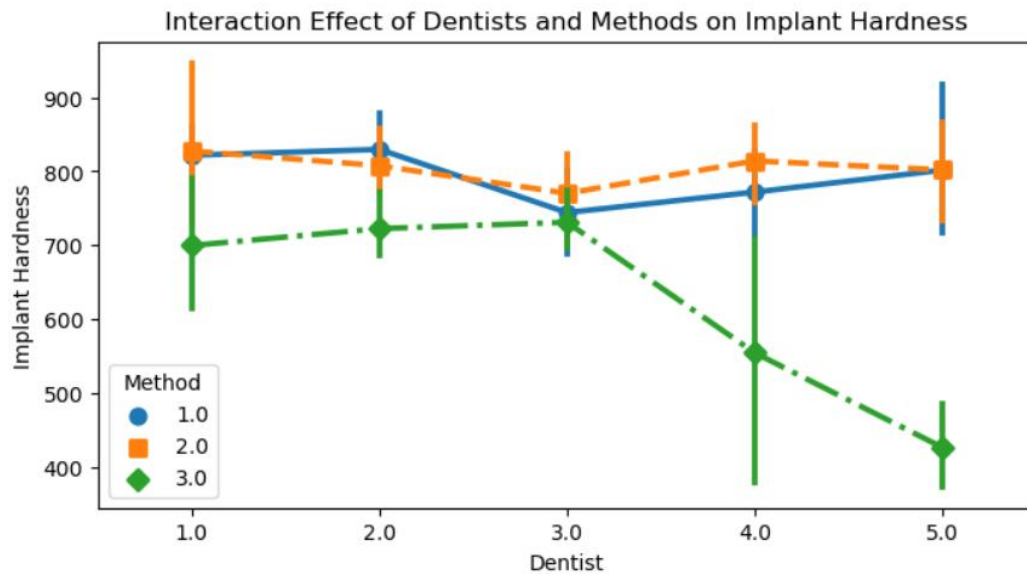


Fig 4.4.3

Based on the Shapiro-Wilk tests for normality and Levene's test for homogeneity of variances:

Normality of Residuals:

- Dentist 1.0: Shapiro-Wilk p-value = 0.186 (normal)
- Dentist 2.0: Shapiro-Wilk p-value = 0.731 (normal)
- Dentist 3.0: Shapiro-Wilk p-value = 0.552 (normal)
- Dentist 4.0: Shapiro-Wilk p-value = 0.002 (not normal)
- Dentist 5.0: Shapiro-Wilk p-value = 0.502 (normal)
- Method 1.0: Shapiro-Wilk p-value = 0.418 (normal)
- Method 2.0: Shapiro-Wilk p-value = 0.076 (normal)
- Method 3.0: Shapiro-Wilk p-value = 0.014 (not normal)

Homogeneity of Variances:

- Test Statistic: 3.938
- P-value: 0.001 Since the p-value is less than the chosen significance level, we reject the null hypothesis. This indicates that the variances of the residuals are not equal across all groups.

Fig 4.4.4

Conduct the hypothesis test and compute the p-value - Write down conclusions from the test results.

Two-way ANOVA Test Results:

P-value: 0.0019695151879771935

- The p-value obtained from the two-way ANOVA test is 0.00197. This p-value indicates that there is a statistically significant interaction effect between Dentist and Method on the hardness of dental implants.
- The significance of this result suggests that the effect of one factor (Dentist) on implant hardness depends on the level of the other factor (Method), and vice versa.

Fig 4.4.5

Identifying which dentists and methods combinations are different, and which interaction levels are different.

Post-hoc Tests for Alloy Type 1:

Dentist:

Multiple Comparison of Means - Tukey HSD, FWER=0.05

group1	group2	meandiff	p-adj	lower	upper	reject
1.0	2.0	11.3333	0.9996	-145.0423	167.709	False
1.0	3.0	-32.3333	0.9757	-188.709	124.0423	False
1.0	4.0	-68.7778	0.7189	-225.1535	87.5979	False
1.0	5.0	-122.2222	0.1889	-278.5979	34.1535	False
2.0	3.0	-43.6667	0.9298	-200.0423	112.709	False
2.0	4.0	-80.1111	0.5916	-236.4868	76.2646	False
2.0	5.0	-133.5556	0.1258	-289.9312	22.8201	False
3.0	4.0	-36.4444	0.9626	-192.8201	119.9312	False
3.0	5.0	-89.8889	0.4805	-246.2646	66.4868	False
4.0	5.0	-53.4444	0.8643	-209.8201	102.9312	False

Method:

Multiple Comparison of Means - Tukey HSD, FWER=0.05

group1	group2	meandiff	p-adj	lower	upper	reject
1.0	2.0	-6.1333	0.987	-102.714	90.4473	False
1.0	3.0	-124.8	0.0085	-221.3807	-28.2193	True
2.0	3.0	-118.6667	0.0128	-215.2473	-22.086	True

Fig 4.4.6

Post-hoc Tests for Alloy Type 2:

Dentist:

Multiple Comparison of Means - Tukey HSD, FWER=0.05

group1	group2	meandiff	p-adj	lower	upper	reject
1.0	2.0	-4.1111	1.0	-225.5687	217.3465	False
1.0	3.0	-36.5556	0.9895	-258.0131	184.902	False
1.0	4.0	-70.0	0.8941	-291.4576	151.4576	False
1.0	5.0	-90.1111	0.7724	-311.5687	131.3465	False
2.0	3.0	-32.4444	0.9933	-253.902	189.0131	False
2.0	4.0	-65.8889	0.9132	-287.3465	155.5687	False
2.0	5.0	-86.0	0.8008	-307.4576	135.4576	False
3.0	4.0	-33.4444	0.9925	-254.902	188.0131	False
3.0	5.0	-53.5556	0.9574	-275.0131	167.902	False
4.0	5.0	-20.1111	0.999	-241.5687	201.3465	False

Method:

Multiple Comparison of Means - Tukey HSD, FWER=0.05

group1	group2	meandiff	p-adj	lower	upper	reject
1.0	2.0	27.0	0.8212	-82.4546	136.4546	False
1.0	3.0	-208.8	0.0001	-318.2546	-99.3454	True
2.0	3.0	-235.8	0.0	-345.2546	-126.3454	True

Fig 4.4.7

Based on the post-hoc tests results:

AlloyType 1:

- Dentist: There are no significant differences observed among all pairs of dentists.
- Method: Significant differences are observed between Method 1 and Method 3, as well as between Method 2 and Method 3.

Alloy Type 2:

- Dentist: There are no significant differences observed among all pairs of dentists.
- Method: Significant differences are observed between Method 1 and Method 3, as well as between Method 2 and Method 3.
- These results suggest that for both types of alloys, the method used significantly affects the hardness of implants, with Method 3 showing differences compared to Method 1 and Method 2. However, there are no significant differences observed among dentists for either type of alloy.

Fig 4.4.8

