

Smoothed Particle Hydrodynamics for Real-Time Fluid Simulation for Unity

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Abstract

Realistically animated fluids can add substantial realism to interactive applications such as virtual surgery simulators or computer games. In this paper we try to implement a Fluid Simulation using Smooth Particle Hydrodynamics (SPH) to simulate fluids with free surfaces in Unity Game Engine. The method is an extension of the SPH-based technique by Desbrun to animate highly deformable bodies adapting it for interactive real-time use in Unity.

My implementation leverages compute shaders to efficiently parallelize particle interactions on the GPU, enabling simulations with thousands of particles at interactive frame rates. Key physical effects such as pressure, velocity and external forces are incorporated, and rendering techniques are applied to visualize fluid dynamics.

Results demonstrate that the method produces visually plausible fluid motion with good performance across different particle counts. While not physically exact compared to high-resolution grid solvers, the approach balances realism and efficiency, making it suitable for applications where interactivity is critical. Future improvements may include surface tension modeling, multi-phase fluids, and integration with rigid-body dynamics.

1. Introduction

1.1 Motivation

Fluids (i.e liquids and gases) play an important role in every day life. Examples of fluid phenomena are wind, weather, ocean waves, waves induced by ships or simply pouring of a glass of water. As simple and ordinary these phenomena may seem, as complex and difficult it is to simulate them. Even though Computational Fluid Dynamics (CFD) is a well established research area with a long history, there are still many open research problems in the field. The reason for the complexity of fluid behaviour is the complex interplay of various phenomena such as convection, diffusion, turbulence and surface tension. Fluid phenomena are typically simulated off-time and then visualized in a second step e.g. in aerodynamics or optimization of turbines or pipes with the goal of being accurate as possible.

Less accurate methods that allow the simulation of fluid effects in real-time open up a variety of new applications. In the fields mentioned above real-time methods help to test whether a certain concept is promising during the design phase. Other applications for real-time simulation techniques for fluids are medical simulators, computer games or any type of virtual environment. We will take a look into the computer game side of the fluid simulation

1.2 Topic

The focus of this thesis is Smoothed Particle Hydrodynamics (SPH), a particle-based method for simulating the flow of fluids. While SPH can be also applied to gases, in this work the emphasis will be place on liquid fluids only.

2. Smooth Particle Hydrodynamics

Although Smoothed Particle Hydrodynamics (SPH) was developed for the simulation of astrophysical problems, the method is general enough to be used in any kind of fluid simulation.

SPH is an interpolation method for particle systems. With SPH, fluid quantities that are only defined at the discrete particle locations can be evaluated anywhere in space. For this purpose, SPH distributes quantities in a local neighborhood of each particle using radial symmetrical smoothing kernels.

According to SPH, a scalar quantity A is interpolated at location \mathbf{r} by a weighted sum of contributions from all particles:

$$A_s(\mathbf{r}) = \sum_j m_j \frac{A_j}{\rho_j} W(\mathbf{r} - \mathbf{r}_j, h) \quad (1)$$

where j iterates over all the particles, m_j is the mass of the particle j , \mathbf{r}_j its position, ρ_j is the density and A_j is the field quantity at \mathbf{r}_j .

The function $W(r, h)$ is called the smoothing kernel with core radius h . It defines the effective range of interaction in the simulation: We can use this to get the estimates on the density, pressure and viscosity of the given particle.

The particle mass and density appear in Eqn. (1) because each particle i represents a certain volume $V_i = \frac{m_i}{\rho_i}$. While the mass m_i is constant throughout the simulation and, in our case, the same for all the particles, the density ρ_i varies and needs to be evaluated at every time step. Through substitution into Eqn (1) we get for the density at location \mathbf{r}

$$\rho_s(\mathbf{r}) = \sum_j m_j \frac{\rho_j}{\rho_j} W(\mathbf{r} - \mathbf{r}_j, h) = \sum_j m_j W(\mathbf{r} - \mathbf{r}_j, h) \quad (2)$$

3. Modelling Fluids with Particles

In the Eulerian (grid based) formulation, isothermal fluids are described by a velocity field v , a density field ρ and a pressure field p . The evolution of these quantities over time is given by two equations. The first equation assures conservation of mass.

equation over here.

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0 \quad (3)$$

while the Navier-Stokes equation formulates conservation of momentum

equation over here.

$$\rho \left(\frac{\partial \mathbf{v}}{\partial t} + \mathbf{v} \cdot \nabla \mathbf{v} \right) = -\nabla p + \rho \mathbf{g} + \mu \nabla^2 \mathbf{v} \quad (4)$$

where g is the external force density field and μ the viscosity of the fluid. Many forms of the Navier-Stokes equation appear in the literature. Eqn. (4) represents a simplified version for incompressible fluids.

In the SPH formulation, the acceleration of a particle i is obtained from the Newton's second law:

$$\frac{d\mathbf{v}_i}{dt} = \frac{\mathbf{F}_i}{m_i} \quad (5)$$

where \mathbf{v}_i is the velocity of the particle and i and \mathbf{f}_i and ρ_i are the force density field and the density field evaluated at the location of particle i , respectively.

This formulation is equivalent to the continuum expression

$$\frac{d\mathbf{v}_i}{dt} = \frac{\mathbf{f}_i}{\rho_i} \quad (6)$$

where \mathbf{f}_i denotes the force per unity volume and ρ_i the density, as often written in SPH literature.

Now we will see the force density terms using SPH.

3.1 Pressure

Application of the SPH rule described in Eqn (1) to the pressure term $-\nabla p$ yields

$$\mathbf{f}_i^{pressure} = -\nabla p(\mathbf{r}_i) = -\sum_j m_j \frac{p_j}{\rho_j} \nabla W(\mathbf{r}_i - \mathbf{r}_j, h) \quad (7)$$

Unfortunately, this force is not symmetric as can be seen when only two particles interact. Since the gradient of the kernel is zero at its center, particle i only uses the pressure of particle j to compute its pressure force and vice versa. Because the pressures at the locations of the two particles are not equal in general, the pressure forces will not be symmetric. Different ways of symmetrization of Eqn. (7) have been proposed in the literature. But I have went with this

$$\mathbf{f}_i^{pressure} = -\nabla p(\mathbf{r}_i) = -\sum_j m_j \frac{p_i + p_j}{\rho_j} \nabla W(\mathbf{r}_i - \mathbf{r}_j, h) \quad (8)$$

The so computed pressure force is symmetric because it uses the arithmetic mean of the pressures of interacting particles.

Since particles only carry the three quantities mass, position and velocity, the pressure at particle locations has to be evaluated first. This is done in two steps. Eqn (2) yields the density at the location of the particle. Then, the pressure can be computed via the ideal gas state equation

$$p = k\rho \quad (9)$$

where k is the gas constant that depends on the temperature. In my simulation I have used a modified version of Eqn (9)

$$p = k(\rho - \rho_0) \quad (10)$$

where ρ_0 is the rest density. Which I have given as a constant

3.2 Viscosity

Application of the SPH rule to the viscosity term $\mu \nabla^2 \mathbf{v}$ again yields the asymmetric forces

$$\mathbf{f}_i^{viscosity} = \mu \nabla^2 \mathbf{v}(\mathbf{r}_a) = \mu \sum_j m_j \frac{v_j}{\rho_j} \nabla^2 W(\mathbf{r}_i - \mathbf{r}_j, h) \quad (11)$$

because the velocity field varies from particle to particle. Since viscosity forces are only dependent on the velocity differences and not on absolute velocities, there is a natural way to symmetrize the viscosity forces by using the velocity differences:

$$\mathbf{f}_i^{viscosity} = \mu \sum_j m_j \frac{v_j - v_i}{\rho_j} \nabla^2 W(\mathbf{r}_i - \mathbf{r}_j, h) \quad (12)$$

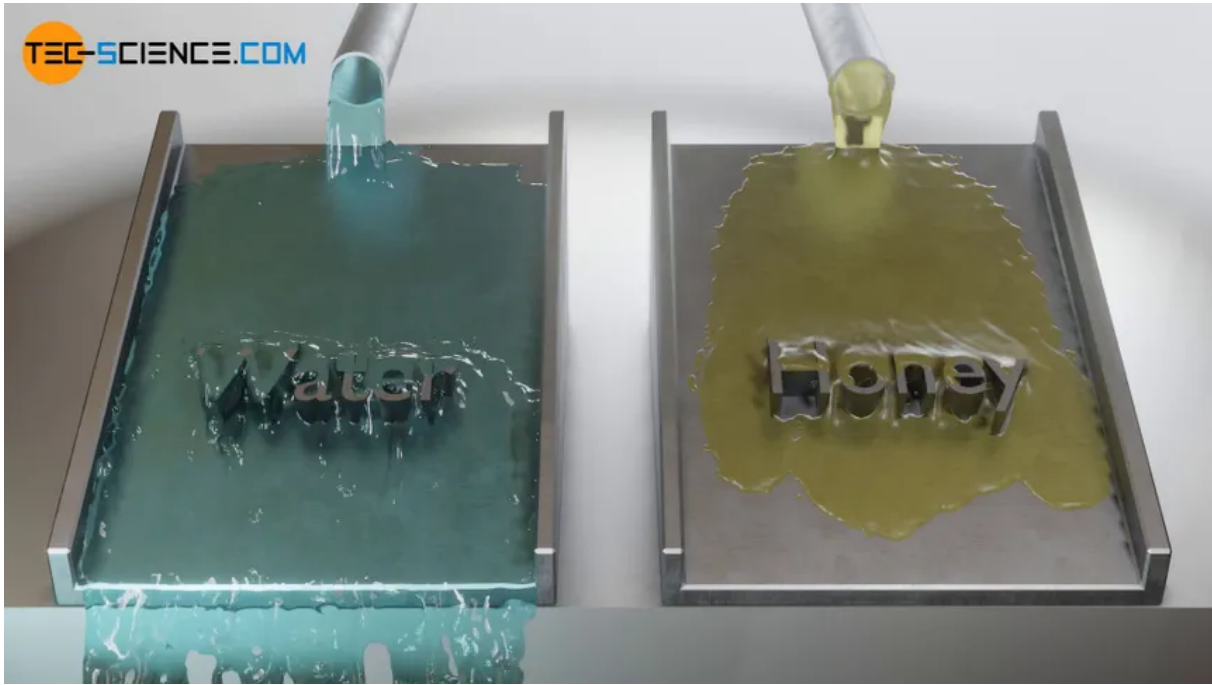


Figure 1: Difference viscosity makes to a fluid

3.3 External Forces

In the Unity Project which supports gravity, collision forces and forces caused by user interaction. These forces are applied directly to the particles without the use of SPH. When the particles collide with any solid object such as the blue box in my Unity Simulation, we simply push them out of the object and reflect the velocity component that is perpendicular to the object's surface.

4. Smoothing kernels

Smoothing kernels are fundamental in SPH as they determine how particle properties are interpolated over space. They provide stability, accuracy and computational efficiency to the simulation, such as density estimation, pressure forces, and viscosity. I have used two types of smoothing kernels

- Poly6 Kernel: This kernel is used for density estimation. It's smooth shape ensures that contributions from nearby particles are weighted appropriately, avoiding sharp discontinuities.

$$W_{\text{poly6}}(\mathbf{r}, h) = \frac{315}{64\pi h^9} \begin{cases} (h^2 - r^2)^3 & 0 \leq r \leq h \\ 0 & \text{otherwise} \end{cases} \quad (13)$$

- Spiky Kernel: Used for calculating pressure and viscosity forces. Its gradient is sharper near the particle center, which improves force calculations and help maintain stability.

$$W_{\text{spiky}}(\mathbf{r}, h) = \frac{15}{\pi h^6} \begin{cases} (h - r)^3 & 0 \leq r \leq h \\ 0 & \text{otherwise} \end{cases} \quad (14)$$

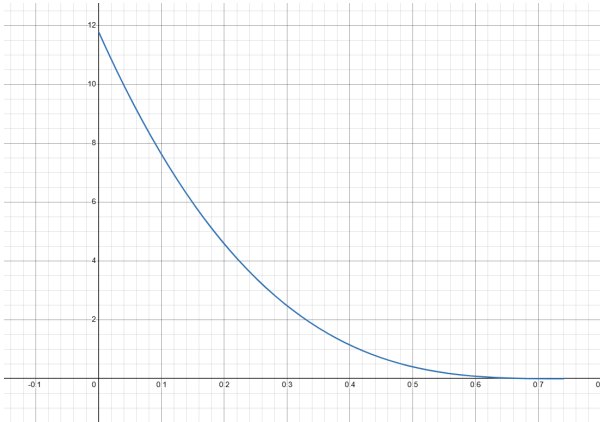


Figure 2: Spiky kernel

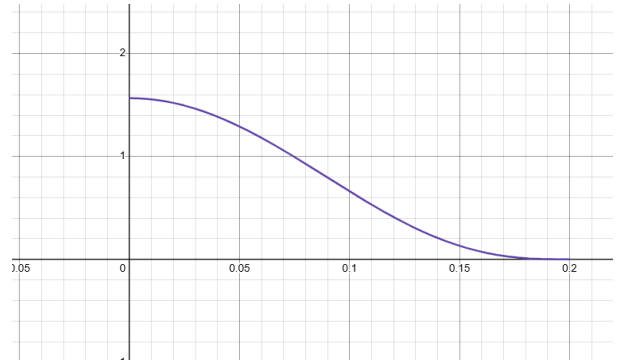


Figure 3: Poly6 kernel

4.1 Derivation of Kernel Functions

4.1.1 Poly6 Kernel Derivation

$$W(r, h) = \frac{315}{64\pi h^9} (h^2 - r^2)^3 \quad (15)$$

$$= \frac{315}{64\pi h^9} \left(h^2 \left(1 - \frac{r^2}{h^2} \right) \right)^3 \quad (16)$$

$$= \frac{315}{64\pi h^9} h^6 \left(1 - \frac{r^2}{h^2} \right)^3 \quad (17)$$

$$= \frac{315}{64\pi h^3} \left(1 - \frac{r^2}{h^2} \right)^3 \quad (18)$$

$$= \frac{315}{64\pi h^3} x^3, \quad \text{with } x = 1 - \frac{r^2}{h^2} \quad (19)$$

4.1.2 Spiky Kernel First Derivate

$$\frac{dW}{dr} = -\frac{45}{\pi h^6} (h - r)^2 \quad (20)$$

$$= -\frac{45}{\pi h^6} (h^2 (1 - r/h)^2) \quad (21)$$

$$= -\frac{45}{\pi h^4} (1 - r/h)^2 \quad (22)$$

$$= -\frac{45}{\pi h^4} x^2, \quad \text{with } x = 1 - r/h \quad (23)$$

4.1.3 Spiky Kernel Second Derivate

$$\frac{dW}{dr} = \frac{d}{dr} \left[-\frac{45}{\pi h^6} (h - r)^2 \right] \quad (24)$$

$$= -\frac{45}{\pi h^6} \cdot 2(h - r) \cdot \frac{d}{dr}(h - r) \quad (25)$$

$$= -\frac{45}{\pi h^6} \cdot 2(h - r) \cdot (-1) \quad (26)$$

$$= \frac{90}{\pi h^6} (h - r) \quad (27)$$

$$= \frac{90}{\pi h^6} (h(1 - r/h)) \quad (28)$$

$$= \frac{90}{\pi h^6} h x \quad \text{with } x = 1 - r/h \quad (29)$$

$$= \frac{90}{\pi h^5} x \quad (30)$$

5. Surface Rendering via Ray Marching

5.1 The Rendering Problem

The SPH produces a set of discrete particles, each representing a point within the fluid volume. A native rendering of these particles as individual spheres or points fails to convey the impression of continuous fluid with a coherent surface. Therefore, a method is required to reconstruct and render a visually plausible surface from this particle data in real-time.

5.2 The Different techniques of Rendering Methods

Two primary techniques exist for this task: polygonization and screen-space rendering.

- Polygonization methods, such as the popular Marching Cubes algorithm, first convert the particle data into a density field on a 3D grid (a process known as voxelization). The algorithm then traverses this grid to generate a triangle mesh representing the fluid’s surface, which can be rendered with standard techniques. While capable of producing high-quality meshes, this approach was deemed unsuitable for this project due to two main drawbacks: the high computational cost of voxelization and mesh generation, and the performance bottleneck associated with transferring a potentially large, dynamic mesh from the GPU (where the simulation runs) to the CPU for rendering in Unity.
- Screen-space methods, by contrast, operate directly on the GPU for each pixel on the screen. The chosen method for this project is Ray Marching an implicit surface, which avoids the creation of any intermediate geometry and is exceptionally well-suited for the parallel architecture of the GPU.

5.3 Theory of Ray Marching

The core of the rendering technique is to define the fluid surface not with triangles, but as an implicit surface. The surface is defined as the set of all points p in space where a function $F(p)$ equals zero. Specifically, we use a Signed Distance Field (SDF), a special type of implicit function that, for any point p , returns the shortest distance to the surface. The sign of the distance is positive outside the fluid and negative inside.

5.4 Constructing the Fluid SDF

The SDF for the entire fluid is built by combining the SDFs of the individual particles. A single is presented by a sphere, whose SDF is given by:

equation here

To combine the fields from all particles into a single, smooth “blobby” surface, a simple minimum operation is insufficient as it would create sharp creases. Instead, a polynomial smooth minimum(*smn*) function is used. This smoothly bends the distance fields of nearby particles.

5.5 The Ray Marching Algorithm

With the SDF defined, the surface can be rendered using a ray marching algorithm, also known as sphere tracing. For each pixel on the screen, a ray is cast from the camera. The algorithm proceeds iteratively:

1. From the ray's current position, the SDF is evaluated to find the distance d to the surface.
2. The SDF guarantees that we can safely “march” the ray forward along its direction by the distance d without passing through the surface.
3. This process is repeated. If d becomes smaller than a small threshold (epsilon), the ray has hit the surface. If the ray travels too far, it is considered a miss.

This process is highly efficient as it takes the largest possible safe steps through empty space.

6. Implementation and Methods

6.1 Project Setup

A simple object scene was prepared in order for the simulation to be tested. There is a simple Ground cube and a few test objects which are the sphere and cube here.

We then create a SPH.cs script that initialize the particles that we are going to use.

6.2 SPH.cs Script implementation

6.2.1 Particle Sturcture

The First step in the script is to define a data structure that represents a single particle in the simulation. Each particle needs to store its physical properties (pressure, density), its current motion (velocity, force), and its position in the world. To make sure this structure is compatible between C# and the compute shader, it is laid out in memory sequentially.

```
1 [System.Serializable]
2 [StructLayout(LayoutKind.Sequential, Size=44)]
3 public struct Particle {
4     public float pressure; // 4 bytes
5     public float density; // 8 bytes
6     public Vector3 currentForce; // 20 bytes
7     public Vector3 velocity; // 32 bytes
8     public Vector3 position; // 44 total bytes
9 }
```

Listing 1: Particle struct

This structure is only 44 bytes, which is small enough to handle thousands of particles efficiently on the GPU. Each particle is initialized with default values in the script, and later updated every frame by the compute shaders (for density, pressure, force, and integration).

6.2.2 Settings for SPH Class

We will then create a **SPH class** which will contain all the settings for the SPH Simulation:

- **General Settings**
 - `collisionSphere`: We can assign our test sphere which can interact with the fluid.
 - `showSpheres`: Toggle to show the particles in the scene (useful for debugging).
 - `numToSpawn`: Number of particles to spawn along each axis (X,Y,Z).
 - `totalParticles`: The number of particles to spawn (product of the per-axis count).
 - `boxSize`: The bounding box of the scene.
 - `spawnCenter`: The spawn center of the particle grid in the scene.
 - `particleRadius`: Radius of each particle.
 - `spawnJitter`: Adds randomness so the particle grid is not perfectly uniform.
- **Particle Rendering Settings**
 - `particleMesh`: Mesh of the particle.
 - `particleRenderSize`: Size in which the particle will render.
 - `material`: Material for the particles.
- **Compute Settings**
 - `shader`: Our compute shader.
 - `particles`: List that stores all the particles in the scene.
- **Fluid Constants**
 - `boundDamping`: Value used when particles collide with the boundary (reflects velocity and scales it down to simulate energy loss).
 - `viscosity`: Viscosity of the fluid.
 - `particleMass`: Mass of an individual particle.
 - `gasConstant`: The gas constant.
 - `restDensity`: Rest density of the fluid.
 - `timestep`: Simulation timestep.
- **Private Compute Shader Buffer Variables**
 - `_argsBuffer`: Arguments related to objects in the scene (sent to compute shader).
 - `_particlesBuffer`: Total amount of particles sent to the compute shader.
 - `integrateKernel`: The integrate function in the compute shader.
 - `computeKernel`: The compute function in the compute shader.
 - `densityKernel`: The density function in the compute shader.

```

1 public class SPH : MonoBehaviour
2 {
3     [Header("General")]
4     public Transform collisionSphere;
5     public bool showSpheres = true;
6     public Vector3Int numToSpawn = new Vector3Int(10,10,10);
7     private int totalParticles {
8         get {
9             return numToSpawn.x*numToSpawn.y*numToSpawn.z;
10        }
11    }
12    public Vector3 boxSize = new Vector3(4,10,3);
13    public Vector3 spawnCenter;
14    public float particleRadius = 0.1f;
15    public float spawnJitter = 0.2f;
16
17    [Header("Particle Rendering")]
18    public Mesh particleMesh;
19    public float particleRenderSize = 8f;
20    public Material material;
21
22    [Header("Compute")]
23    public ComputeShader shader;
24    public Particle[] particles;
25
26    [Header("Fluid Constants")]
27    public float boundDamping = -0.3f;
28    public float viscosity = -0.003f;
29    public float particleMass = 1f;
30    public float gasConstant = 2f;
31    public float restingDensity = 1f;
32    public float timestep = 0.007f;
33
34    // Private Variables
35    private ComputeBuffer _argsBuffer;
36    public ComputeBuffer _particlesBuffer;
37    private int integrateKernel;
38    private int computeKernel;
39    private int densityPressureKernel;
40
41 }

```

Listing 2: SPH Class and Settings

6.2.3 Gizmos Function to Draw the Boxes

I am using the `OnDrawGizmos` function to the boundary boxes and the `spawnCenter` (for debugging).

```
1 private void OnDrawGizmos() {  
2  
3  
4     // Draw simulation bounding box  
5     Gizmos.color = Color.blue;  
6     Gizmos.DrawWireCube(Vector3.zero, boxSize);  
7  
8     // Draw spawn center (only in editor, not while running)  
9     if (!Application.isPlaying) {  
10         Gizmos.color = Color.cyan;  
11         Gizmos.DrawWireSphere(spawnCenter, 0.1f);  
12     }  
13  
14 }
```

Listing 3: `OnDrawGizmos()` function

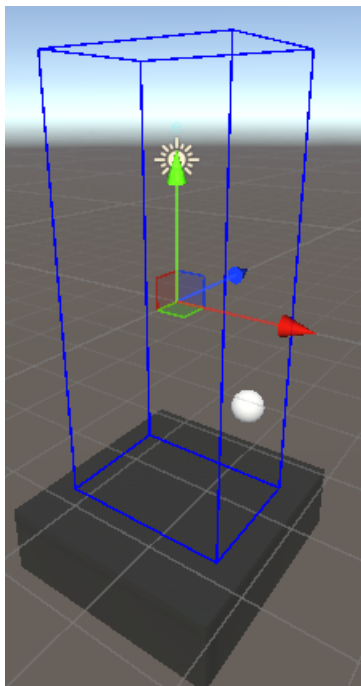


Figure 4: Gizmos Box

6.2.4 Spawning the Particles in a Grid

The `SpawnParticleInBox()` function takes the `spawnCenter` and stores it in the variable `spawnPoint` and creates a new List called `_particles`. It loops and goes in a grid like fashion across the three axis (x,y, and z), using `numToSpawn` to determine the number of particles per axis. Each particle is positioned relative to the `spawnCenter` with spacing determined by twice the particle radius.

To avoid the grid being a perfectly uniform grid which will lead to simulation accuracy, a small random offset is added to each position using `Random.onUnitSphere * particleRadius * spawnJitter`. This creates a slight offset in the particles that should give more accurate results.

```
1 private void SpawnParticlesInBox() {
2
3     Vector3 spawnPoint = spawnCenter;
4     List<Particle> _particles = new List<Particle>();
5
6     for (int x = 0; x < numToSpawn.x; x++) {
7         for (int y = 0; y < numToSpawn.y; y++) {
8             for (int z = 0; z < numToSpawn.z; z++) {
9
10                Vector3 spawnPos = spawnPoint + new Vector3(x*
11                    particleRadius*2, y*particleRadius*2, z*particleRadius
12                    *2);
13
14                // Randomize spawning position a little bit for more
15                // convincing simulation
16                spawnPos += Random.onUnitSphere * particleRadius *
17                    spawnJitter;
18
19                Particle p = new Particle {
20                    position = spawnPos
21                };
22                _particles.Add(p);
23            }
24        }
25    }
26
27    particles = _particles.ToArray();
28 }
```

Listing 4: `SpawnParticleInBox()` function

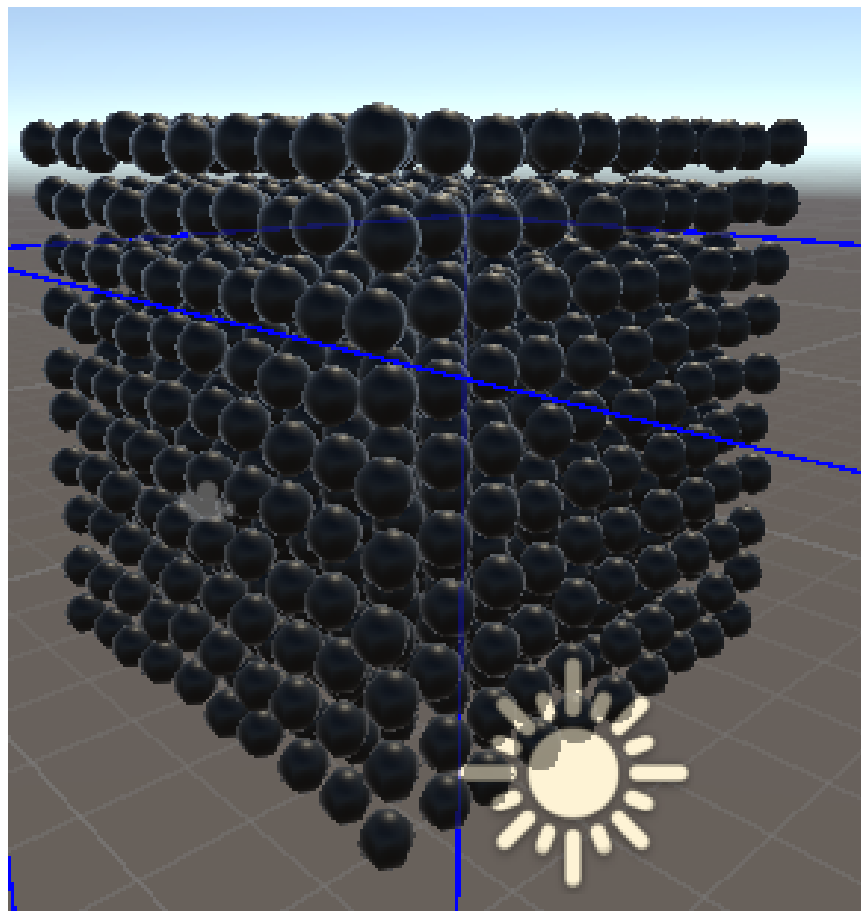


Figure 5: Particle in a grid box

6.2.5 Initalizing the Simulation

The Awake function is called when the simulation object is initialized, It first calls `SpawnParticlesInBox()` to generate the initial particle distribution. Afterwards, it sets up the data structures required for the GPU compute shaders.

And Finally it calls the `SetupComputeBuffers()`.

```
1 private void Awake() {
2
3     SpawnParticlesInBox(); // Spawn Particles
4
5     // Setup Args for Instanced Particle Rendering
6     uint[] args = {
7         particleMesh.GetIndexCount(0),
8         (uint)totalParticles,
9         particleMesh.GetIndexStart(0),
10        particleMesh.GetBaseVertex(0),
11        0
12    };
13
14    _argsBuffer = new ComputeBuffer(1,args.Length * sizeof(uint),
15        ComputeBufferType.IndirectArguments);
16    _argsBuffer.SetData(args);
17
18    // Setup Particle Buffer
19    _particlesBuffer = new ComputeBuffer(totalParticles,44);
20    _particlesBuffer.SetData(particles);
21
22    SetupComputeBuffers();
23 }
```


6.2.6 Setting up Compute Buffers

The function `SetupComputeBuffers` sets up all the Buffers from the compute shader and also passes the values which are calculated from the `SPH.cs` script to the compute shader.

```
1 private void SetupComputeBuffers() {
2
3     integrateKernel = shader.FindKernel("Integrate");
4     computeKernel = shader.FindKernel("ComputeForces");
5     densityPressureKernel = shader.FindKernel("ComputeDensityPressure");
6
7     shader.SetInt("particleLength", totalParticles);
8     shader.SetFloat("particleMass", particleMass);
9     shader.SetFloat("viscosity", viscosity);
10    shader.SetFloat("gasConstant", gasConstant);
11    shader.SetFloat("restDensity", restingDensity);
12    shader.SetFloat("boundDamping", boundDamping);
13    shader.SetFloat("pi", Mathf.PI);
14    shader.SetVector("boxSize", boxSize);
15
16    shader.SetFloat("radius", particleRadius);
17    shader.SetFloat("radius2", particleRadius * particleRadius);
18    shader.SetFloat("radius3", particleRadius * particleRadius *
19        particleRadius);
20    shader.SetFloat("radius4", particleRadius * particleRadius *
21        particleRadius * particleRadius);
22    shader.SetFloat("radius5", particleRadius * particleRadius *
23        particleRadius * particleRadius * particleRadius);
24
25    shader.SetBuffer(integrateKernel, "_particles", _particlesBuffer);
26    shader.SetBuffer(computeKernel, "_particles", _particlesBuffer);
27    shader.SetBuffer(densityPressureKernel, "_particles", _particlesBuffer
28        );
29 }
```

6.2.7 Rendering the particles

The `Update` function is responsible for just rendering the particles that we are initializing which are rendered with the `GridParticle.shader`

```
1 private static readonly int SizeProperty = Shader.PropertyToID("_size");
2 private static readonly int ParticlesBufferProperty = Shader.PropertyToID(
    _particlesBuffer");
3
4 private void Update() {
5
6     // Render the particles
7     material.SetFloat(SizeProperty, particleRenderSize);
8     material.SetBuffer(ParticlesBufferProperty, _particlesBuffer);
9
10    if (showSpheres)
11        Graphics.DrawMeshInstancedIndirect (
12            particleMesh,
13            0,
14            material,
15            new Bounds(Vector3.zero, boxSize),
16            _argsBuffer,
17            castShadows: UnityEngine.Rendering.ShadowCastingMode.Off
18        );
19
20 }
21
```

6.2.8 Calling the Compute Shader

The `FixedUpdate` is called every physics frame. This function passes all the parameters to the compute shader and dispatches the individual kernels and divides them by 100 because the kernel we are using uses 100 threads.

```
1 private void FixedUpdate() {
2
3     shader.SetVector("boxSize", boxSize);
4     shader.SetFloat("timestep", timestep);
5     shader.SetVector("spherePos", collisionSphere.transform.position);
6     shader.SetFloat("sphereRadius", collisionSphere.transform.localScale.x
7         /2);
8
9     // Total Particles has to be divisible by 100
10    shader.Dispatch(densityPressureKernel, totalParticles / 100, 1, 1);
11    shader.Dispatch(computeKernel, totalParticles / 100, 1, 1);
12    shader.Dispatch(integrateKernel, totalParticles / 100, 1, 1);
13 }
14
```

6.3 SPH Compute compute shader

The SPH Compute function is the function that computes the forces for each particles to neighbouring particles and sends the data to Unity to use.

6.3.1 Initialization of the Kernels

- **Kernels**

- **Integrate**: The **Integrate** kernel updates each particle's position and velocity based on the computed forces.
- **ComputeForces**: The **ComputeForces** kernel calculates forces between particles, such as pressure and viscosity interactions.
- **ComputeDensityPressure**: The **ComputeDensityPressure** kernel computes each particle's density and pressure.

We are implementing the respective kernels to Integrate the timestep which the **Integrate** kernel does, we compute the forces between the particles using **ComputeForces** kernel, and finally we are use the **ComputeDensityPressure** kernel to compute the density and pressure of each of the particle.

```
1 #pragma kernel Integrate // Use the force of each particle to move particle
2 #pragma kernel ComputeForces // Compute forces for each particle
3 #pragma kernel ComputeDensityPressure // Compute density/pressure for each
   particle
4
5 struct Particle
6 {
7     float pressure;
8     float density;
9     float3 currentForce;
10    float3 velocity;
11    float3 position;
12 };
```

Listing 5: Initilize block of the shader

In the particle struct, scalar properties (e.g., pressure, density) are represented by float types, whereas vector properties (e.g., position, velocity, currentForce) are represented by float3 types. The reason they are multiple different radius **radius2**, **radius3**, etc are for kernel optimizations

6.3.2 Setting up the variables for the Compute shader

We set a `RWStructuredBuffer` and also set all of the different variables which are passed in the `SPH.cs` script

```
1 RWStructuredBuffer<Particle> _particles;
2
3 float particleMass;
4 float viscosity;
5 float gasConstant;
6 float restDensity;
7 float boundDamping;
8 float radius;
9 float radius3;
10 float radius2;
11 float radius4;
12 float radius5;
13 float pi;
14 float timestep;
15 float3 boxSize;
16 float3 spherePos;
17 float sphereRadius;
18
19 int particleLength;
```

Listing 6: Block that contains variables of the shader

6.3.3 The Integrate Kernel Function

- The first two `float3` variables define the boundaries for the particles so that they do not move outside the simulation box.
- The `float3 vel` is updated according to Newton's law of motion: $F = m \cdot a$, where the acceleration is `currentForce / particleMass` for the given particle.
- The position is updated using the distance–speed–time formula: $v = \frac{d}{t}$.
- Boundary conditions are enforced by checking if a particle exceeds the domain along any axis. If it does, the velocity is damped by `boundDamping` and the position is corrected to remain inside the box.
- Below that, the boundary box checks are applied for all axes.

```

1 [numthreads(100,1,1)]
2 void Integrate (uint3 id: SV_DISPATCHTHREADID)
3 {
4     float3 topRight = boxSize / 2;
5     float3 bottomLeft = -boxSize /2;
6
7     float3 vel = _particles[id.x].velocity + ((_particles[id.x].currentForce/
8         particleMass) * timestep);
9     _particles[id.x].position += vel * timestep;
10
11     // Minimum Enforcements
12
13     if (_particles[id.x].position.x - radius < bottomLeft.x) {
14         vel.x *= boundDamping;
15         _particles[id.x].position.x = bottomLeft.x + radius;
16     }
17
18     if (_particles[id.x].position.y - radius < bottomLeft.y) {
19         vel.y *= boundDamping;
20         _particles[id.x].position.y = bottomLeft.y + radius;
21     }
22
23     if (_particles[id.x].position.z - radius < bottomLeft.z) {
24         vel.z *= boundDamping;
25         _particles[id.x].position.z = bottomLeft.z + radius;
26     }
27
28     // Maximum Enforcements
29
30     if (_particles[id.x].position.x + radius > topRight.x) {
31         vel.x *= boundDamping;
32         _particles[id.x].position.x = topRight.x - radius;
33     }
34
35     if (_particles[id.x].position.y + radius > topRight.y) {
36         vel.y *= boundDamping;
37         _particles[id.x].position.y = topRight.y - radius;
38     }
39
40     if (_particles[id.x].position.z + radius > topRight.z) {
41         vel.z *= boundDamping;
42         _particles[id.x].position.z = topRight.z - radius;
43     }
44
45
46     _particles[id.x].velocity = vel;
47 }

```

Listing 7: The Integrate kernel

6.3.4 Kernel Equations

These four functions are the kernel implementations in the compute shader.

- **StdKernel**
 - This is the Standard Kernel also called the Poly6 kernel.
 - It takes the distance which is called `distanceSquared` to be faithful to the formula.
 - The formula in the function is modified for optimization purposes from Eqn. (11)
- **SpikyKernelFirstDerivative**
 - This is the First Derivation of the Spiky Kernel.
 - We compute the first derivate of the Spiky kernel because we want to know how strongly each neighbouring particle exerts pressure. In mathematical terms we are seeing the vector between the two points which is distance and radius.
 - The formula in the function has also been modified for optimization purposes from Eqn. (12)
- **SpikyKernelSecondDerivative**
 - This is the Second Derivation of the Spiky Kernel.
 - We compute the second derivate of the Spiky kernel because we want to the viscosity which involves velocity of the particles. In mathematical terms we are measuring how curved the kernel function is around the particle, a larger curvature means stronger smoothing / diffusion effect.
 - Again this formula is also modified for optimization purposes from Eqn. (12)
- **SpikyKernelGradient**
 - This is the Gradient of the Spiky Kernel.
 - We need this because it gives us the magnitude of the vector of how strong the vector of the particles are is which we can use in the pressure computation.
 - This just returns the Spiky Kernels First Derivative and multiples that by the distance factor.

```
1 float StdKernel (float distanceSquared){
2     // 1 - r^2/h^2
3     float x = 1.0f - distanceSquared / radius2;
4     return 315.f/ (64.f * pi * radius3) * x * x * x;
5 }
6 // Smoothing Function for Compute Forces
7 float SpikyKernelFirstDerivative(float distance){
8     // 1 - r/h
9     float x = 1.0f - distance/radius;
10    return -45.f/(pi*radius4)*x*x;
11 }
12 float SpikyKernelSecondDerivative(float distance){
13     float x = 1.0f - distance/radius;
14     return 90.f / (pi*radius5) *x;
15 }
16 float3 SpikyKernelGradient(float distance, float3 direction){
17     return SpikyKernelFirstDerivative(distance) *direction;
18 }
```

Listing 8: The Integrate kernel

6.3.5 Calculating Pressure

- This `ComputeDensityPressure` kernel is calculating the pressure of each particle by taking the particles position as the origin and looping through all the particles in the simulation and calculating its difference and getting the distance from it.
- It will then check if the particle is within a certain radius then it will apply the smoothing kernel the sum, then it will multiply it by the mass which we will get the density from.
- Then to calculate pressure we can just multiply the difference of the densities with the `gasConstant` to get the pressure of the particle.

```
1 [numthreads(100,1,1)]
2 void ComputeDensityPressure(uint3 id: SV_DISPATCHTHREADID){
3
4     float3 origin = _particles[id.x].position;
5     float sum = 0;
6
7     for (int i = 0; i < particleLength; i++){
8         float3 diff = origin - _particles[i].position;
9         float distanceSquared = dot(diff, diff);
10
11         if (radius2*0.004 >= distanceSquared*0.004){
12             sum += StdKernel(distanceSquared*0.004); // Apply Smoothing kernel
13         }
14     }
15
16     _particles[id.x].density = sum * particleMass + 0.000001f;
17     _particles[id.x].pressure = gasConstant * (_particles[id.x].density -
18         restDensity);
19
20 }
```

Listing 9: Compute Kernel

6.3.6 Calculating the Force

- This `ComputeForces` kernel is then calculating the force of the particle by taking the `i` particle's position as the origin, then it loops through all the particles.
- We also do a check where we don't compute the force if the particle position is the same i.e we are checking ourselves.
- We then check the distance between the particles if the distance is twice of the radius which is the smoothing radius to remove computational overhead of calculating all the forces of the particles because we know that when the particle is far enough it's force to the other particle is non-existent.
- We then get the `_pressureGradientDirection` which is the pressure gradient direction by normalizing the vector between the particles.
- We then calculate the total pressure contribution which is stored in `_pressureContribution` which is twice the mass (the reason we are able to do this is because the mass of all the particles are same) which we multiply by the spiky kernel gradient, then we multiply that to the pressure formula
- For calculating viscosity we are able to use the formula and multiply with the viscosity of the fluid, we are also calculating the difference in the velocities of the particles and divide by the density which is what the formula says
- Then we finally multiply the viscosity to the Spiky Kernel Second Derivative.


```

1 [numthreads(100,1,1)]
2 void ComputeForces(uint3 id: SV_DISPATCHTHREADID){
3
4     float3 origin = _particles[id.x].position;
5     float density2 = _particles[id.x].density * _particles[id.x].density;
6     float mass2 = particleMass * particleMass;
7     float3 pressure = float3(0,0,0);
8     float3 visc = float3(0,0,0);
9
10    for (int i = 0; i < particleLength; i++){
11        if (origin.x == _particles[i].position.x && origin.y == _particles[i].
12            position.y && origin.z == _particles[i].position.z){
13            continue;
14        }
15
16        float dist = distance(_particles[i].position, origin);
17        if(dist < radius*2){
18            float3 pressureGradientDirection = normalize(_particles[id.x].
19                position - _particles[i].position);
20
21            float3 _pressureContribution = mass2 * SpikyKernelGradient(dist,
22                pressureGradientDirection);
23            _pressureContribution *= (_particles[id.x].pressure / density2 +
24                _particles[i].pressure / (_particles[i].density * _particles[i]
25                ].density));
26
27            float3 _viscosityContribution = viscosity * mass2 * (_particles[i]
28                ].velocity - _particles[id.x].velocity) / _particles[i].
29                density;
30            _viscosityContribution *= SpikyKernelSecondDerivative(dist);
31
32            pressure += _pressureContribution;
33            visc += _viscosityContribution;
34        }
35    }
36
37    _particles[id.x].currentForce = float3(0,-9.81*particleMass,0) - pressure
38        + visc;
39
40    float3 colDir = _particles[id.x].position - spherePos;
41    if (length(colDir) < sphereRadius){
42        _particles[id.x].currentForce += colDir * 300;
43    }
44 }

```

Listing 10: Compute Forces Kernel

6.4 Fluid Ray Marching

6.4.1 Initializing and Setting the Render Texture

The `FluidRayMarching` script serves as the central component responsible for managing the ray marching rendering effect. Its primary function is to perform a comprehensive initialization of all the necessary data, which includes configuring the shader parameters and setting up the required textures.

A critical part of this setup is handled by the `InitRenderTexture` method, which is dedicated specifically to initializing the main render texture that the camera will use as an output target. Once this entire initialization phase is complete and every parameter is correctly established, the script's final role is to send all of this configured information to the `Raymarching.compute` shader, which then utilizes the data to perform the fluid rendering calculations.

```
1 public class FluidRayMarching : MonoBehaviour
2 {
3     public ComputeShader raymarching;
4     public Camera cam;
5     List<ComputeBuffer> buffersToDispose = new List<ComputeBuffer>();
6     public SPH sph;
7     RenderTexture target;
8     [Header("Params")]
9     public float viewRadius;
10    public float blendStrength;
11    public Color waterColor;
12    public Color ambientLight;
13    public Light lightSource;
14
15    void InitRenderTexture()
16    {
17        if (target == null || target.width != cam.pixelWidth || target.height
18            != cam.pixelHeight)
19        {
20            if (target != null)
21            {
22                target.Release();
23            }
24
25            cam.depthTextureMode = DepthTextureMode.Depth;
26
27            target = new RenderTexture(cam.pixelWidth, cam.pixelHeight, 0,
28                RenderTextureFormat.ARGBFloat, RenderTextureReadWrite.Linear);
29            target.enableRandomWrite = true;
30            target.Create();
31        }
32    }
33    private bool render = false;
34    public ComputeBuffer _particlesBuffer;
```

6.4.2 Passing data to the GPU for the Ray Marching Compute Shader.

The `Begin` function it calls the `InitRenderTexture` function and then passes all the parameters to the `Raymarching` shader and sets its rendering to true.

The `OnRenderImage` function it checks if the render is false it calls the `Begin` method, when render is called it passes all the parameters to the group and combines divides the threads by 8 because that was how many threads we provided in the `Raymarching` shader and dispatches the shader.

```
1 public void Begin()
2 {
3     InitRenderTexture();
4     raymarching.SetBuffer(0, "particles", sph._particlesBuffer);
5     raymarching.SetInt("numParticles", sph.particles.Length);
6     raymarching.SetFloat("particleRadius", viewRadius);
7     raymarching.SetFloat("blendStrength", blendStrength);
8     raymarching.SetVector("waterColor", waterColor);
9     raymarching.SetVector("_AmbientLight", ambientLight);
10    raymarching.SetTextureFromGlobal(0, "_DepthTexture", "
        _CameraDepthTexture");
11    render = true;
12 }
13 void OnRenderImage(RenderTexture source, RenderTexture destination)
14 {
15
16     if (!render)
17     {
18         Begin();
19     }
20
21     if (render)
22     {
23
24         raymarching.SetVector("_Light", lightSource.transform.forward);
25
26         raymarching.SetTexture(0, "Source", source);
27         raymarching.SetTexture(0, "Destination", target);
28         raymarching.SetVector("_CameraPos", cam.transform.position);
29         raymarching.SetMatrix("_CameraToWorld", cam.cameraToWorldMatrix);
30         raymarching.SetMatrix("_CameraInverseProjection", cam.
            projectionMatrix.inverse);
31
32         int threadGroupsX = Mathf.CeilToInt(cam.pixelWidth / 8.0f);
33         int threadGroupsY = Mathf.CeilToInt(cam.pixelHeight / 8.0f);
34         raymarching.Dispatch(0, threadGroupsX, threadGroupsY, 1);
35
36         Graphics.Blit(target, destination);
37     }
38 }
```