NOTE: wherever i need k or k+1 or k-1 it is labeled to avoid too many wires

