

restart;

DEFINITION VARIABLES

$d := 2$: # DIMENSION, 2 POUR LES IMAGES

$m := 2d$: # NBRES DE FCTS EXTERNES -1

$\Delta := 10$: # BASE UTILISE, PLUS = MIEUX

$b := \frac{1}{\Delta(\Delta - 1)}$:

$\lambda_1 := 1$:

$\lambda_2 := \text{evalf}\left(\sum_{r=1}^{\infty} \frac{1}{\Delta^{(2^r - 1)}}\right)$;

0.1010001000

(1)

DONNE LA I EME DECIMAL EN BASE Δ DE K

$ieme := (\mathbf{k}, \mathbf{i}) \rightarrow \text{floor}\left(\Delta \cdot \left(\mathbf{k} \cdot \Delta^{i-1} - \text{floor}\left(\mathbf{k} \cdot \Delta^{i-1}\right)\right)\right)$:

TRONQUE LE REEL D AU K PREMIERE DECIMALS EN BASE Δ

$dk := (d, k) \rightarrow \text{floor}(ieme(d, w) \cdot \Delta)$:

AJOUTE 0.0ppppppp (K FOIS p) EN BASE Δ A D

$dkn := (d, k, p) \rightarrow \text{piecewise}\left(d + p \sum_{w=2}^k \Delta^{-w} < 1, d + p \sum_{w=2}^k \Delta^{-w}, \text{dkn}(0, k, \Delta - 1)\right)$:

DEFINITION DES FONCTIONS INTERNES

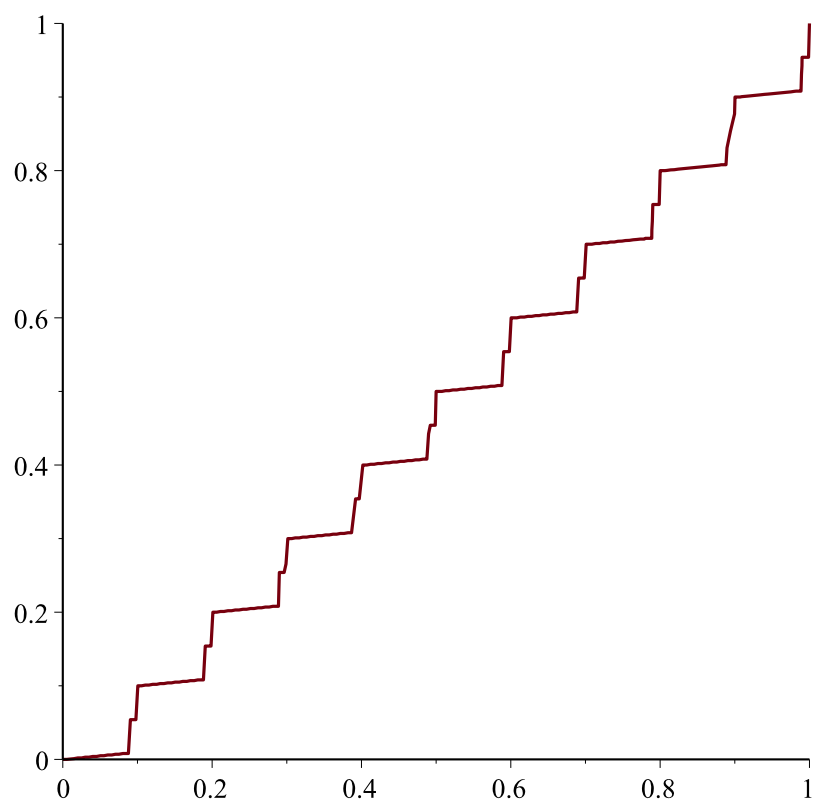
$\Psi := (d, k) \rightarrow \text{piecewise}\left(k = 1, d, ieme(d, k) < \Delta - 1, \Psi\left(d - \frac{ieme(d, k)}{\Delta^k}, k - 1\right) + \frac{ieme(d, k)}{\Delta^{2^k - 1}}, \frac{1}{2} \cdot \left(\Psi\left(d - \frac{1}{\Delta^k}, k\right) + \Psi\left(d + \frac{1}{\Delta^k}, k - 1\right)\right)\right)$:

$\text{plot}(x \rightarrow \Psi(x, 10), 0..1)$;

DEFINITION DE "LA" FCT INTERNE

$\xi := (x1, x2) \rightarrow \lambda_1 \Psi(x1, 5) + \lambda_2 \Psi(x2, 5)$:

$\text{plot3d}(\xi, 0..1, 0..1, \text{axes} = \text{BOXED}, \text{numpoints} = 600)$;



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Your operating system, graphics, or video driver may require updating.

See "gldriver" in the help system for more information.

IllegalArgumentException

Width (0) and height (0) must be > 0

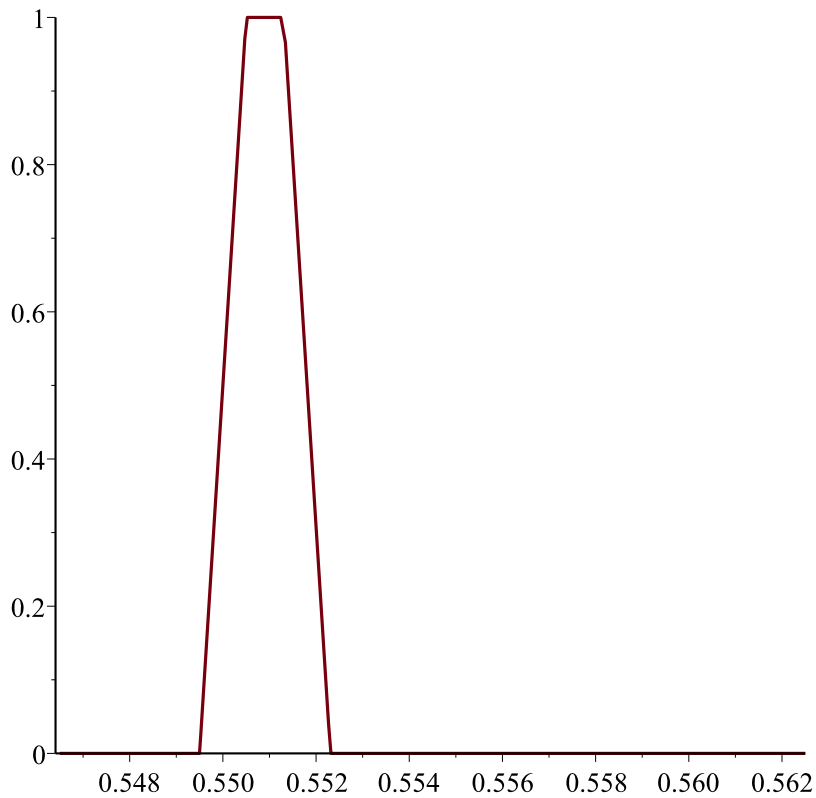
FCT NECESSAIRES AU CALCUL DES FONCTIONS EXTERNES

$\sigma := x \rightarrow \text{piecewise}(x \geq 1, 1, x \leq 0, 0, x) :$

$$c := x \rightarrow \lambda_2 \cdot \sum_{h=x+1}^{\infty} \left(\frac{1}{\Delta^{d^h - 1}} \right) :$$

$$\theta := (x1, x2, k, y) \rightarrow \text{evalf} \left(\sigma \left(\Delta^{d^{k+1} - 1} \cdot (y - \xi(x1, x2, 10)) + 1 \right) - \sigma \left(\Delta^{d^{k+1} - 1} \cdot (y - \xi(x1, x2, 10)) - (\Delta - 2) \cdot c(k) \right) \right) :$$

$\text{plot}(x \rightarrow \theta(.5, .5, 1, x), (\xi(.5, .5, 10) - .004) .. (\xi(.5, .5, 10) + .012), \text{resolution} = 20, \text{numpoints} = 20); \# \text{TEST}$



DEFINITION DE LA FCT A COMPRESSER

with(ImageTools) :

img := Read("lena.bmp") :

taille := Width(img) :

Preview(img);

val := (y1, y2, x) → y1 + (y2 − y1) · (x − floor(x)) :

*fimg := (x, y) → piecewise(x = 1 taille and y = taille, img[taille][taille], x = taille,
 val(img[floor(y)][taille], img[floor(y) + 1][taille], y), y = taille, val(img[taille][floor(x)],
 img[taille][floor(x) + 1], x)
 , val(val(img[floor(y)][floor(x)], img[floor(y)][floor(x) + 1], x), val(img[floor(y)
 + 1][floor(x)], img[floor(y) + 1][floor(x) + 1], x), y)) :*

fct := (x, y) → fimg(x · (taille − 1) + 1, y · (taille − 1) + 1) :

plot3d(fct, 0 ..1, 0 ..1, axes = BOXED, grid = [100, 100]);

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DEFINITION DES NORMES UTILISES

norminfderiv := **proc**(*f*) **local** *maxn*, *x*, *y* :

maxn := 0;

for *y* **from** 2 **to** *taille* **do**

for *x* **from** 2 **to** *taille* **do**

if *evalf*($|f(x-1, y) - f(x, y)|$) $> maxn$ **then** *maxn* := $f(x-1, y) - f(x, y)$ **fi** :

if *evalf*($|f(x, y-1) - f(x, y)|$) $> maxn$ **then** *maxn* := $f(x, y-1) - f(x, y)$ **fi** :

od;

od;

return *maxn*;

end proc;

norminf := **proc**(*f*) **local** *maxn*, *x*, *y* :

maxn := 0;

for *y* **from** 1 **to** *taille* **do**

for *x* **from** 1 **to** *taille* **do**

if $f(x, y) > maxn$ **then** *maxn* := $f(x, y)$ **fi** :

od;

od;

return *maxn*;

end proc:

PRECISION SOUHAITE

$\varepsilon := .01$: *# POUR LA FCT*

$r := 1$: *# NBRE DE FOIS QU'ON EXECUTE LA BOUCLE*

OBTENTION DES FCTS EXTERNES

$f[0] := fct$:

for t from 1 to r do

$$k := evalf \left(1 + \text{floor} \left(\frac{\log \left(\varepsilon \frac{\text{norminf}(fimg)}{\text{norminfderiv}(fimg)} \right)}{-\log(\Delta)} \right) \right);$$

for l from 0 to m do

$$g[t, l] := e \rightarrow \frac{1}{m+1} \left(add \left(add \left(f[evalf(t-1)] \left(dk \left(\frac{1}{\Delta^k}, k \right), dk \left(\frac{ay}{\Delta^k}, k \right) \right) \cdot \theta \left(dkn \left(\frac{1}{\Delta^k}, k, l \right), dkn \left(evalf \left(\frac{ay}{\Delta^k} \right), k, l \right), k, e \right), ay = 1 .. \Delta^k \right), ax = 1 .. \Delta^k \right) \right);$$

od;

$$f[t] := (x, y) \rightarrow f[0](x, y) - add \left(add \left(g[1, s] \left(\xi(x + s \cdot b, y + s \cdot b) \right), j = 1 .. t \right), s = 0 .. m \right);$$

od:

$\#f[1](.5, .5);$

$\#f[0](.5, .5);$

for t from 1 to r do

$$g[t] := x \rightarrow \sum_{j=1}^r g[j, t];$$

od:

[Warning. computation interrupted](#)

CREATION DE LA NOUVELLE FONCTION

$$newfct := (x, y) \rightarrow \sum_{i=0}^m g[i] \left(\xi(x + b \cdot i, y + b \cdot i) \right) :$$

AFFICHAGES DES FONCTIONS EXTERNES

$\#plot(x \rightarrow g[1, 0](x) + g[2, 0](x), 0 .. 1, numpoints = 20) :$

AFFICHAGE DE L'IMAGE OBTENU A PARTIR DES FCTS EXTERNES

$result := Create(taille, taille, channels = 1, (x, y) \rightarrow newfct(x, y)) :$

$Preview(result);$

[Warning. computation interrupted](#)

[Error, invalid input: Preview:-Preview expects its 1st argument, img. to be of type ImageTools:-Image, but received result](#)